

Digital Image Processing (CSE/ECE 478)

Lecture # 16: Image morphing and Chamfer Matching

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Today's Lecture

- Image Morphing
- Chamfer Matching



500 years of female portrait



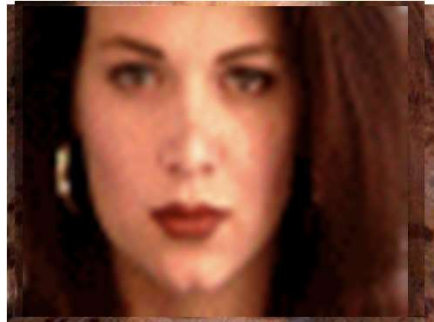
https://www.youtube.com/watch?v=nUDIoN-_Hxs

0 to 65 and back in a minute



<https://www.youtube.com/watch?v=LOGKp-uvjO0>

Averaging vs Morphing



- The aim is to find “an average” between two objects
 - Not an average of two images of objects...
 - ...but an image of the average object!
 - How can we make a smooth transition in time?
 - Do a “weighted average” over time t



Averaging points

What's the average
of P and Q?

Linear Interpolation

New point: $(1-t)P + tQ$

$0 < t < 1$

$$\mathbf{v} = Q - P$$

$$\begin{aligned} P + 0.5\mathbf{v} \\ &= P + 0.5(Q - P) \\ &= 0.5P + 0.5Q \end{aligned}$$

Extrapolation: $t < 0$ or $t > 1$

$$\begin{aligned} P + 1.5\mathbf{v} \\ &= P + 1.5(Q - P) \\ &= -0.5P + 1.5Q \quad (t=1.5) \end{aligned}$$

- P and Q can be anything:
 - points on a plane (2D) or in space (3D)
 - Colors in RGB (3D)
 - Whole images (m-by-n D)... etc.

Idea-1: cross dissolve



- Interpolate whole images:
 - $\text{Image}_{\text{halfway}} = (1-t) \cdot \text{Image}_1 + t \cdot \text{Image}_2$
 - This is called **cross-dissolve** in film industry
 - But what if the images are not aligned?
-

Idea-2: align, then cross dissolve

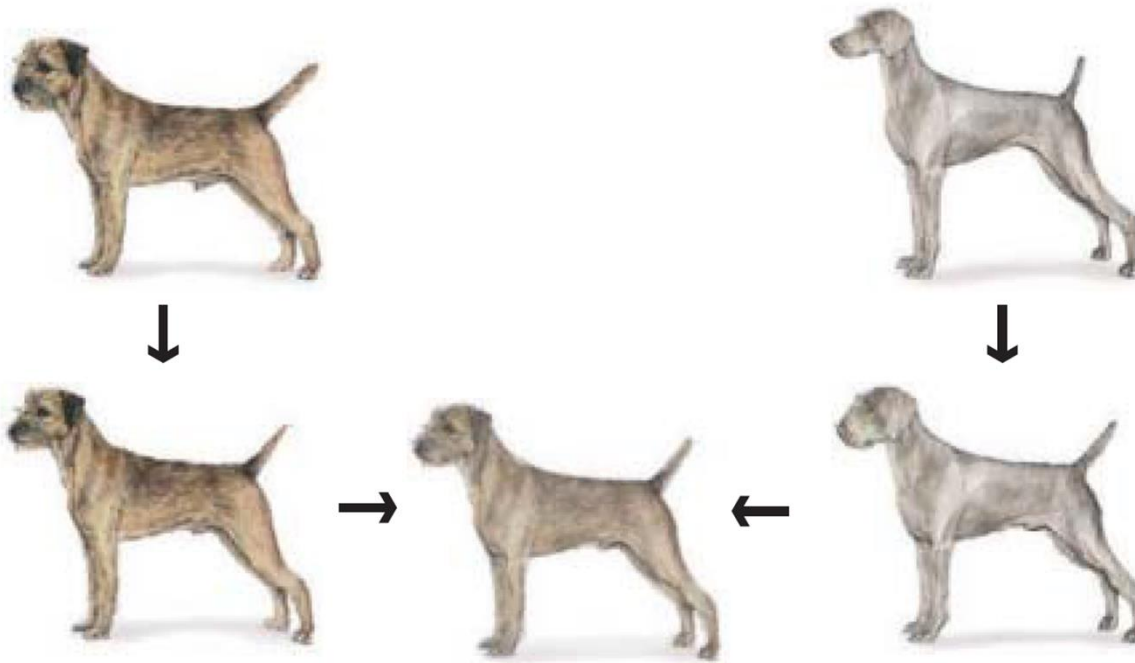


Dog averaging



- What to do?
 - Cross-dissolve doesn't work
 - Global alignment doesn't work
 - Cannot be done with a global transformation (e.g. affine)
 - Any ideas?
 - Feature matching!
 - Nose to nose, tail to tail, etc.
 - This is a local (non-parametric) warp
-

Idea-3: Local warp, then cross-dissolve



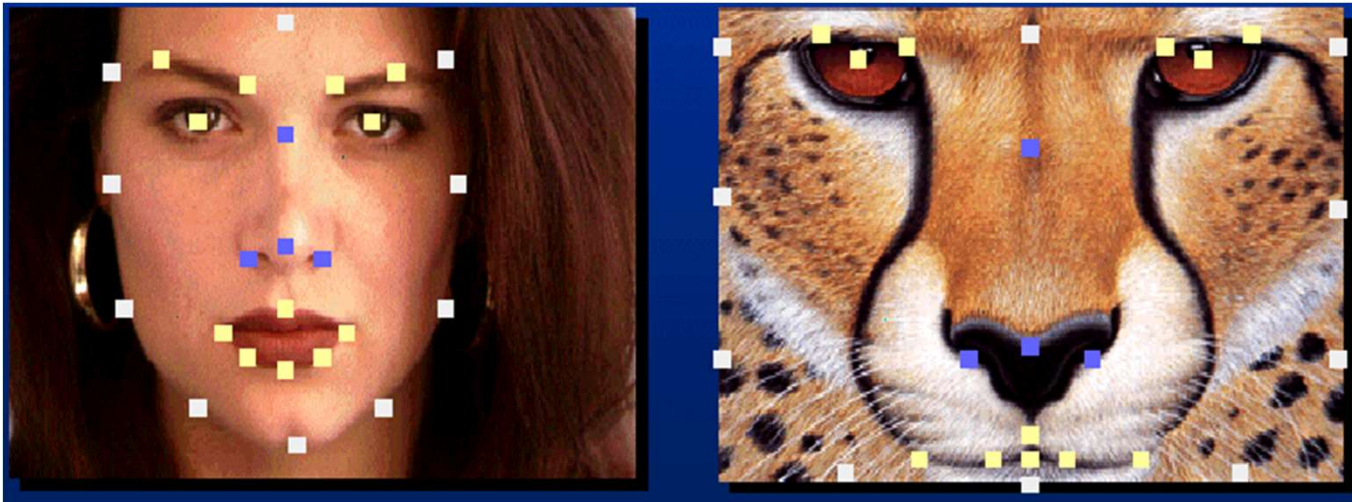
- *For every frame t ,*
 1. Find the average shape (the “mean dog” 😊)
 - local warping
 2. Find the average color
 - Cross-dissolve the warped images

Warp specification

- How can we specify the warp?

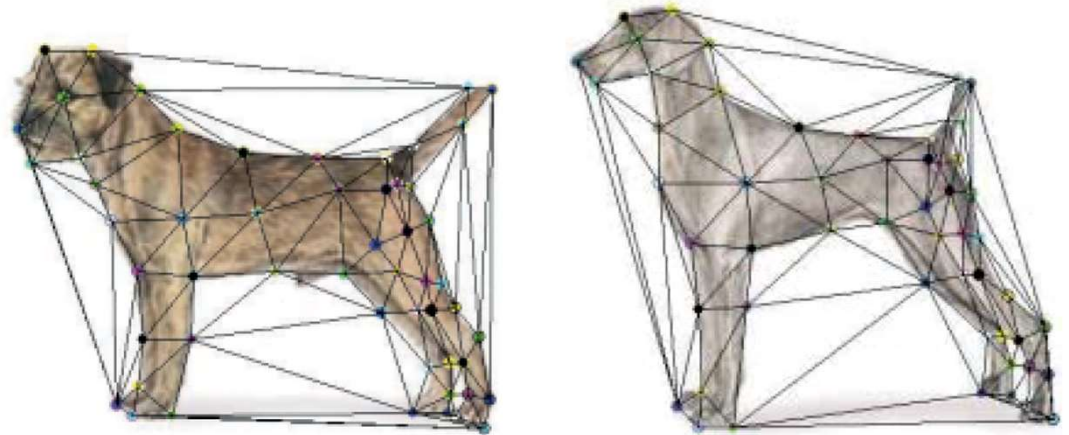
Specify corresponding *points*

- *interpolate* to a complete warping function
- How do we do it?

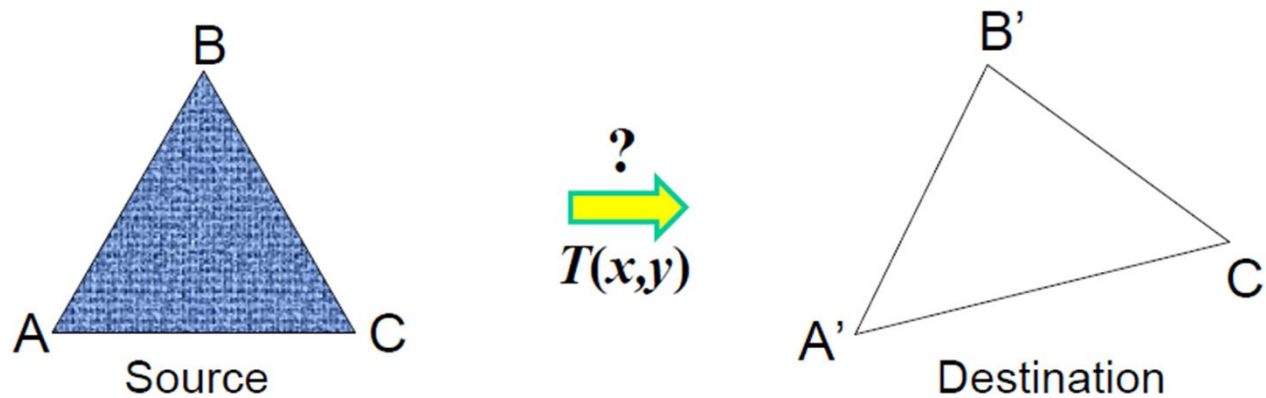


Triangular Mesh

1. Input correspondences at key feature points
2. Define a triangular mesh over the points
 - Same mesh (triangulation) in both images!
 - Now we have triangle-to-triangle correspondences
3. Warp each triangle separately from source to destination
 - Affine warp with three corresponding points



Warping Triangles



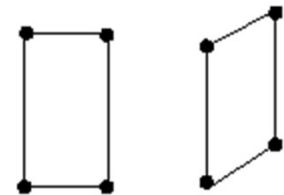
Given two triangles: ABC and A'B'C' in 2D (12 numbers)
Need to find transform T to transfer all pixels from one to the other.
What kind of transformation is T?

Affine transformation

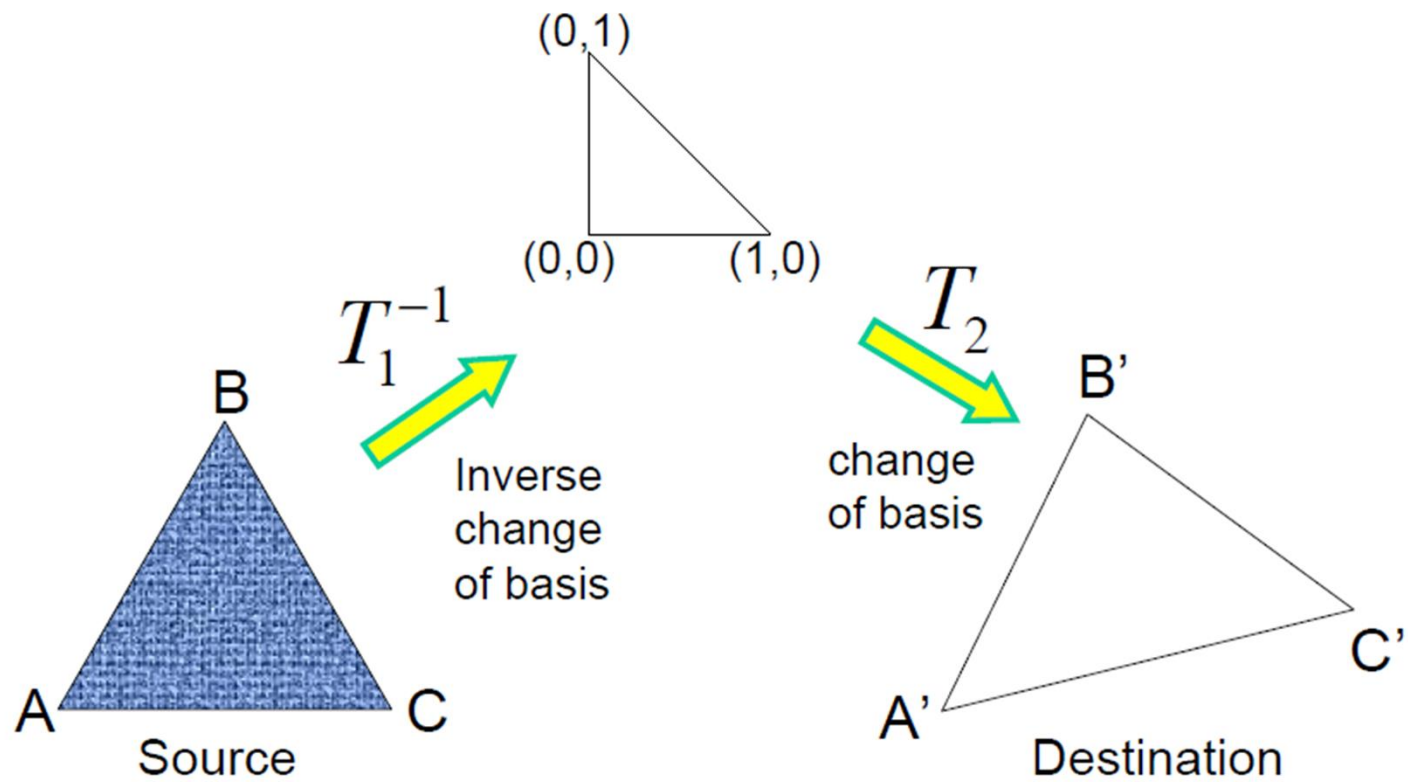
- Preserves collinearity (all points on a line, remain on a line)
 - Parallel lines remain parallel
 - Does not necessarily preserve angles between lines or distances between points (**any triangle can be transformed into another using affine transformation**)
 - Preserve ratios of distances between points lying on a straight line
- Desired transformation as combination of simpler ones

$$\begin{pmatrix} x' \\ y' \\ 1 \end{pmatrix} = \begin{pmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ 0 & 0 & 1 \end{pmatrix} \cdot \begin{pmatrix} x \\ y \\ 1 \end{pmatrix}$$

T

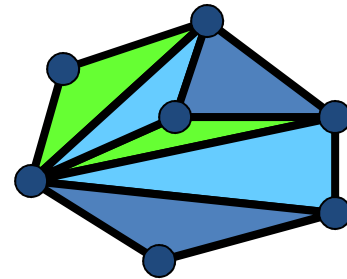
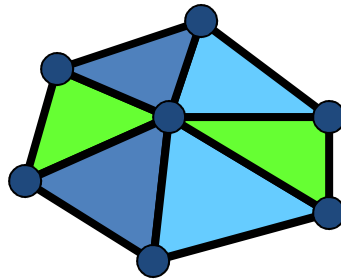
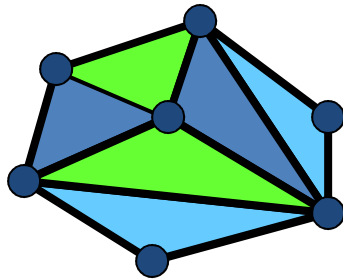


Warping Triangles



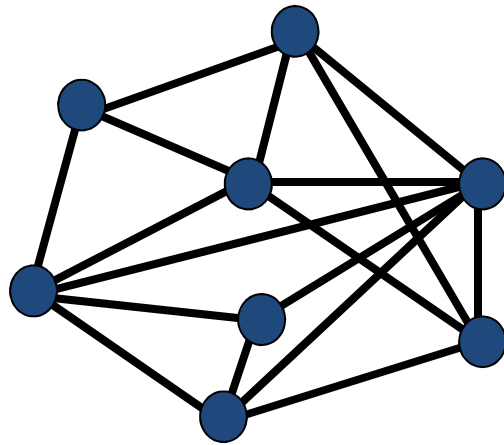
Triangulations

- A *triangulation* of set of points in the plane is a *partition* of the convex hull to triangles whose vertices are the points, and do not contain other points.
- There are an exponential number of triangulations of a point set.



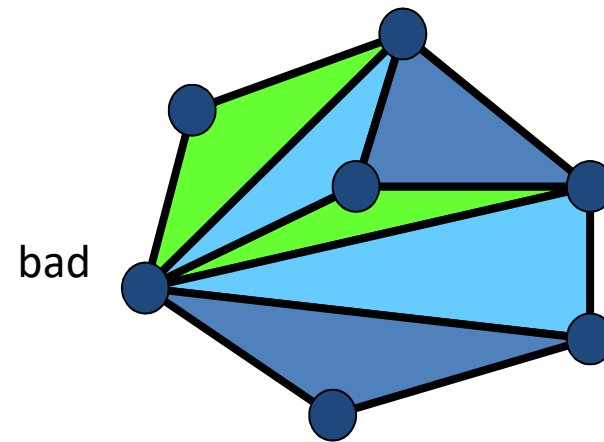
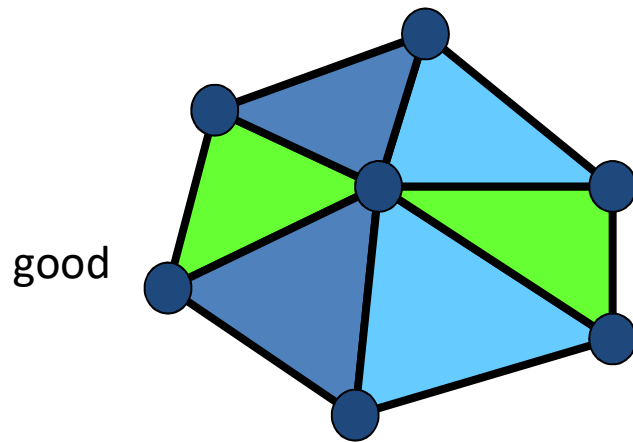
An $O(n^3)$ Triangulation Algorithm

- Repeat until impossible:
 - Select two sites.
 - If the edge connecting them does not intersect previous edges, keep it.



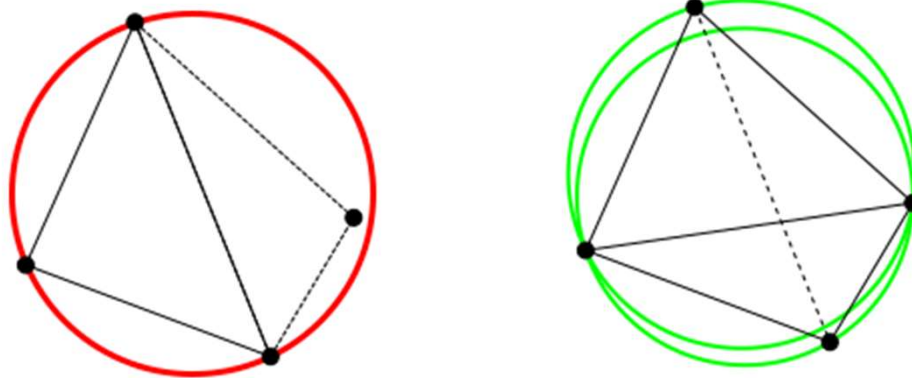
“Quality” Triangulations

- Let $\alpha(T_i) = (\alpha_{i1}, \alpha_{i2}, \dots, \alpha_{i3})$ be the vector of angles in the triangulation T in increasing order:
- A triangulation T_1 is “better” than T_2 if the smallest angle of T_1 is larger than the smallest angle of T_2
- Delaunay triangulation is the “best” (maximizes the smallest angles)



Delaunay triangulation

A Delaunay triangulation for a given set P of discrete points in a plane is a triangulation $DT(P)$ such that no point in P is inside the circumcircle of any triangle in $DT(P)$.



Delaunay triangulation

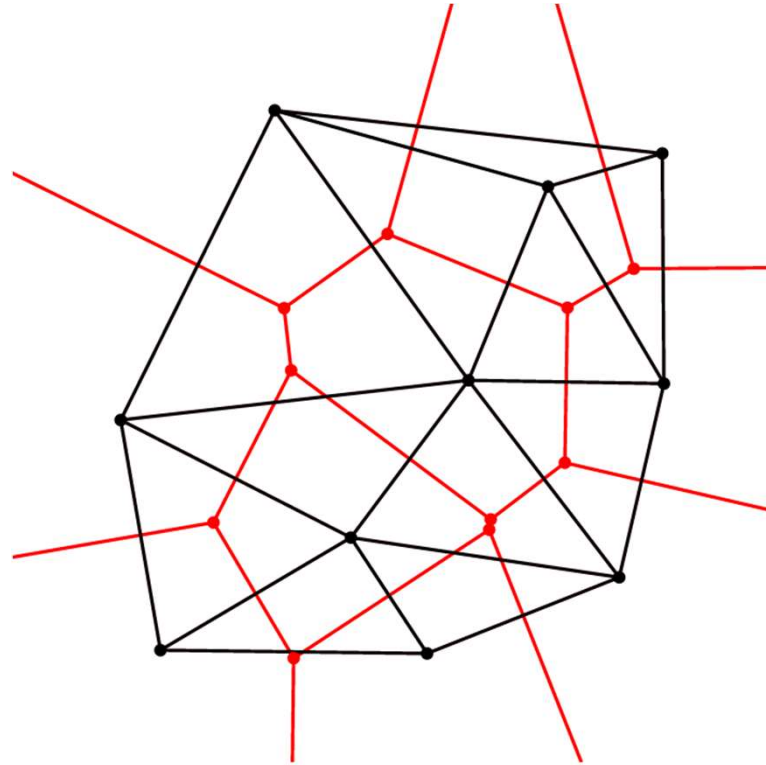
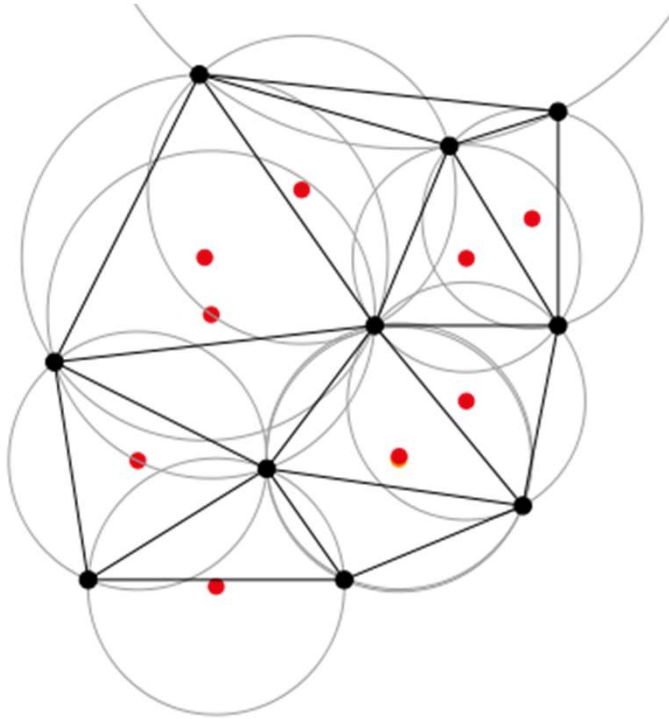
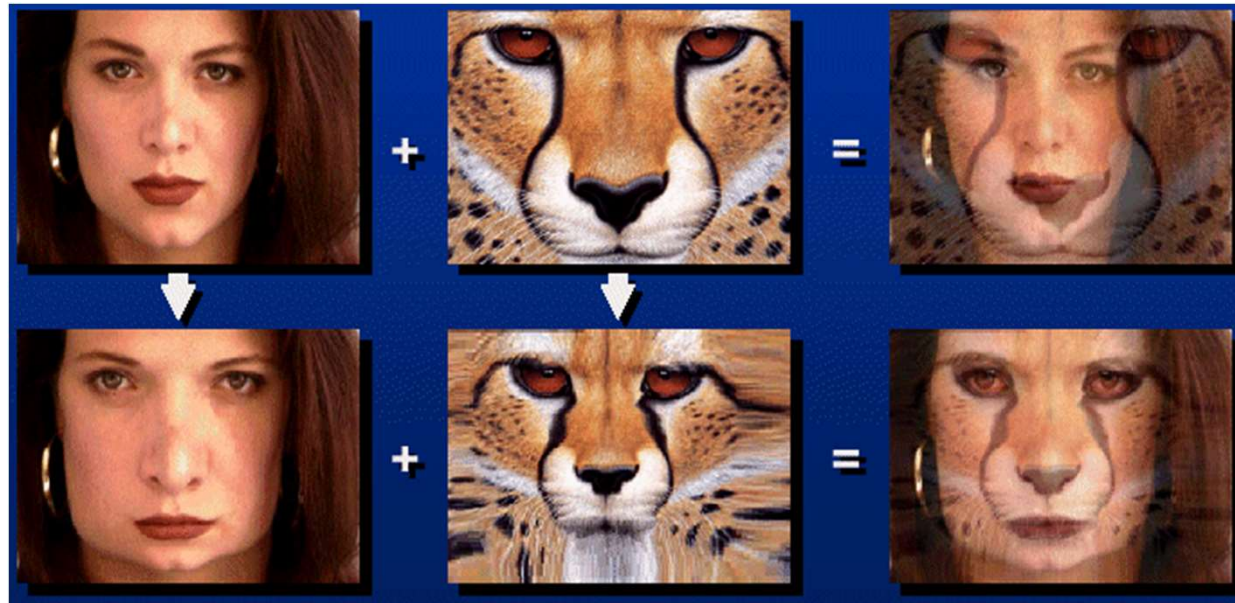


Image Morphing

How do we create a morphing sequence?

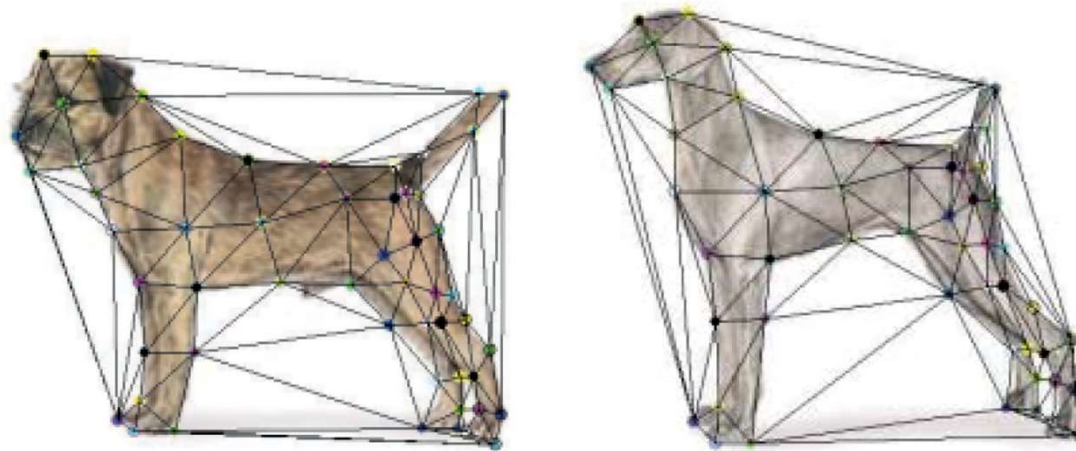
1. Create an intermediate shape (by interpolation)
2. Warp both images towards it
3. Cross-dissolve the colors in the newly warped images



Warp interpolation

How do we create an intermediate shape at time t ?

- Assume $t = [0,1]$
- Simple linear interpolation of each feature pair
 - $(1-t)*p_1+t*p_0$ for corresponding features p_0 and p_1



Summary of Morphing

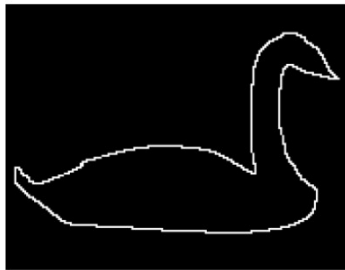
1. Define corresponding points
 2. Define triangulation on points
 - Use same triangulation for both images
 3. For each t in $0:\text{step}:1$
 - a. Compute the average shape (weighted average of points)
 - b. For each triangle in the average shape
 - Get the affine projection to the corresponding triangles in each image
 - For each pixel in the triangle, find the corresponding points in each image and set value to weighted average (optionally use interpolation)
 - c. Save the image as the next frame of the sequence
-

Today's Lecture

- Image Morphing
- Chamfer Matching



Contour based shape matching



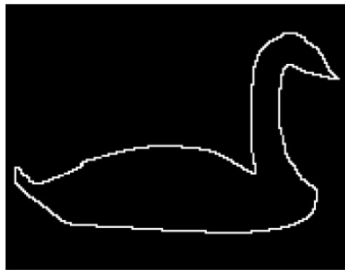
Template shape



Query Image



Contour based shape matching



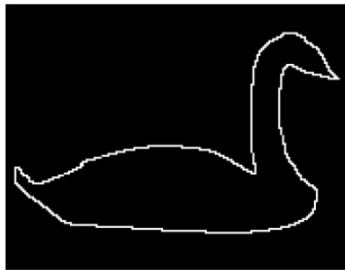
Template shape



Query Image



Contour based shape matching



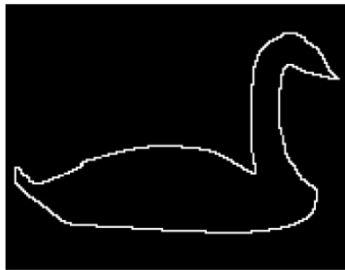
Template shape



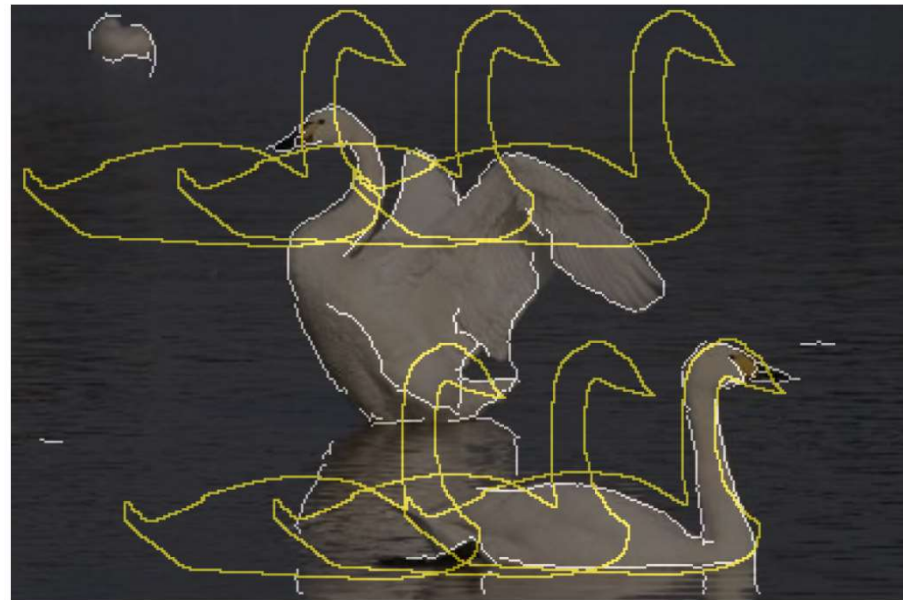
Query Image



Contour based shape matching



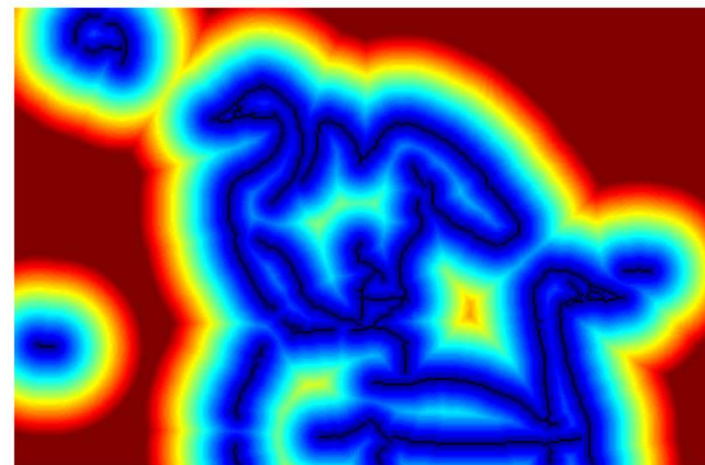
Template shape



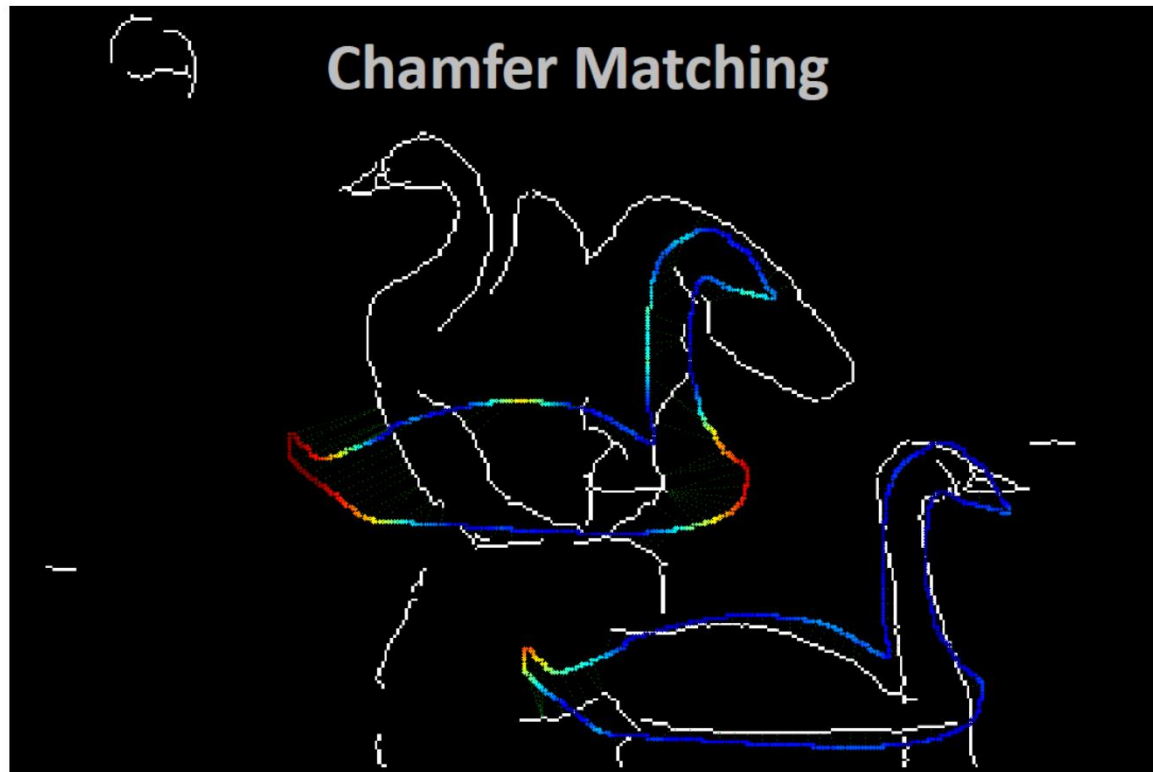
Query Image



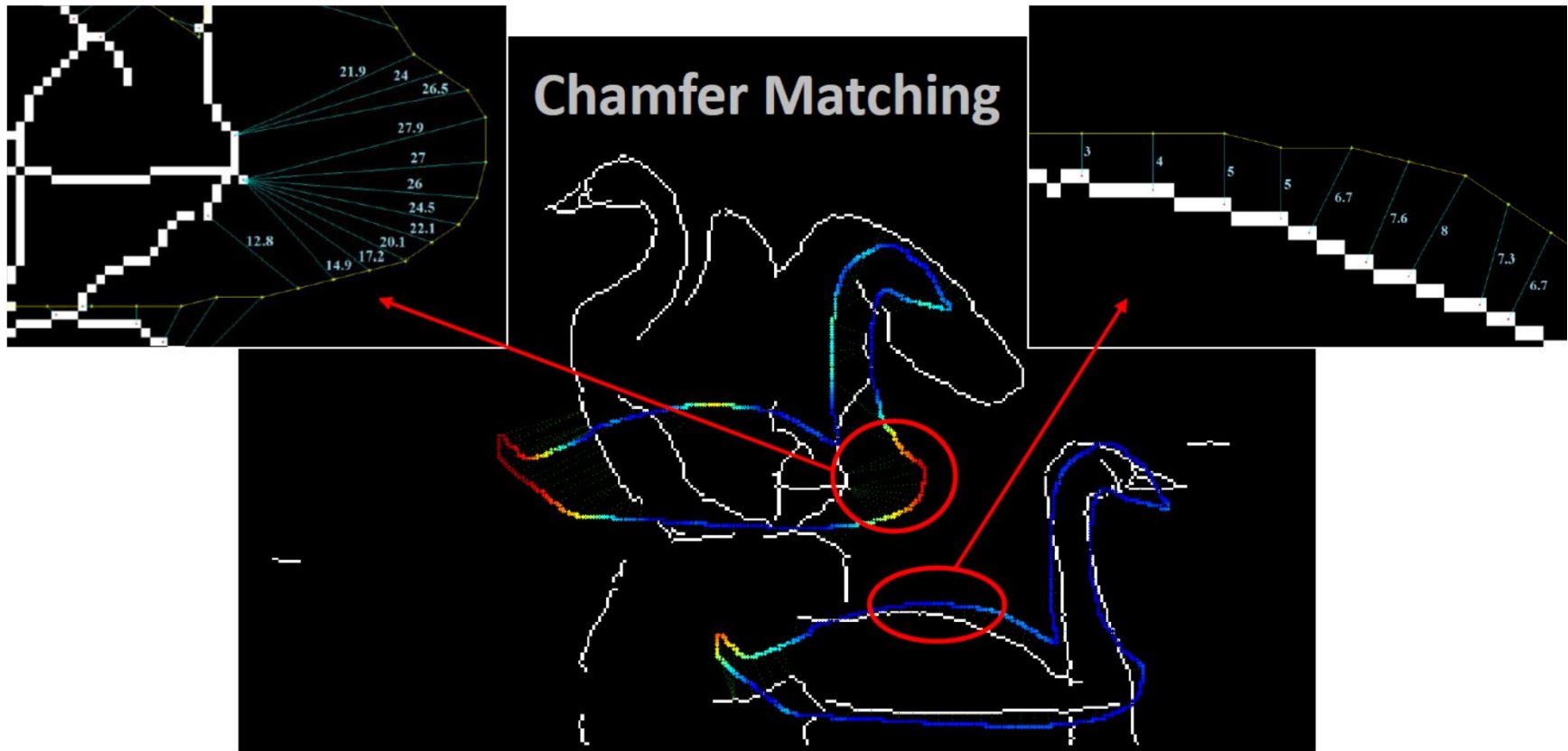
Distance Transform



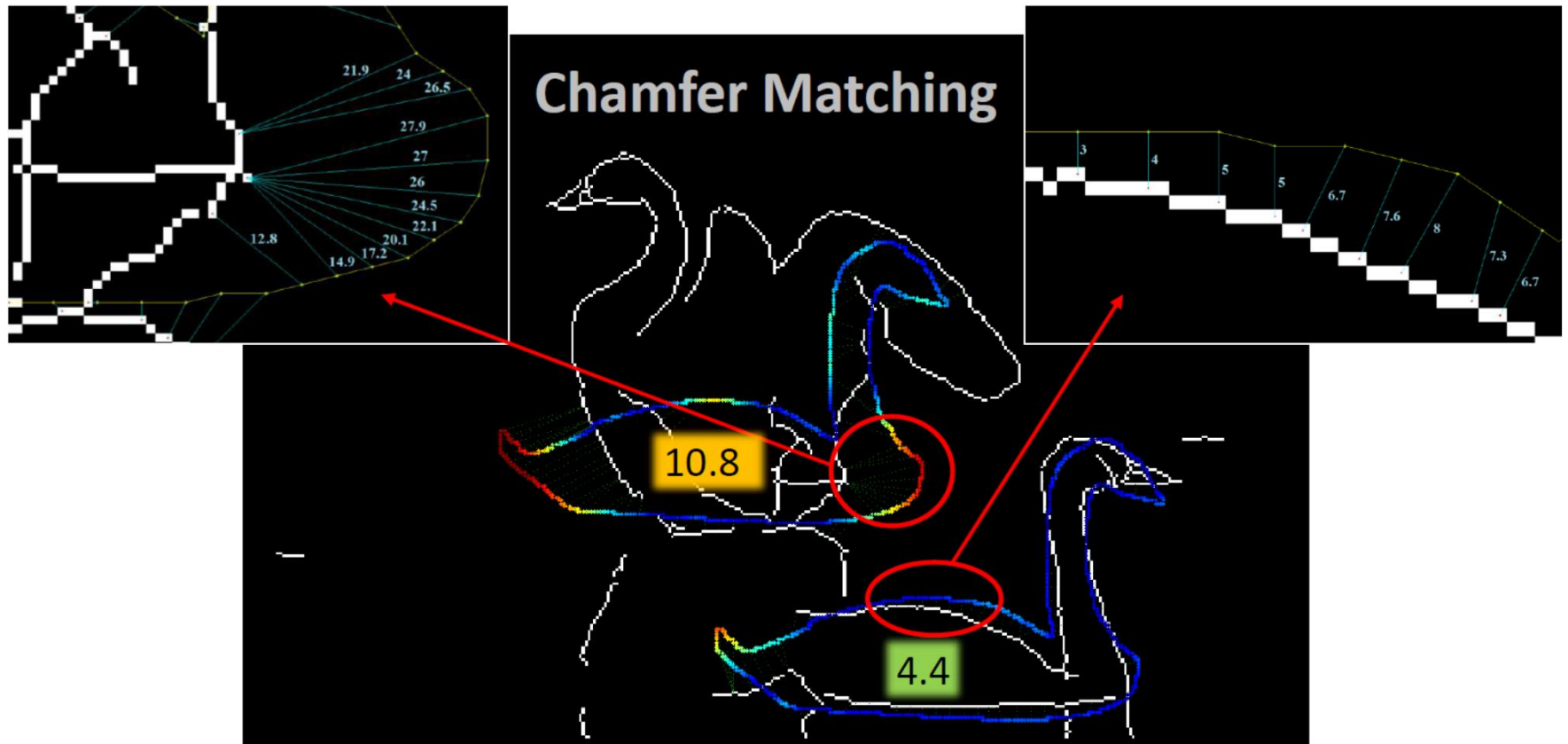
Chamfer Matching



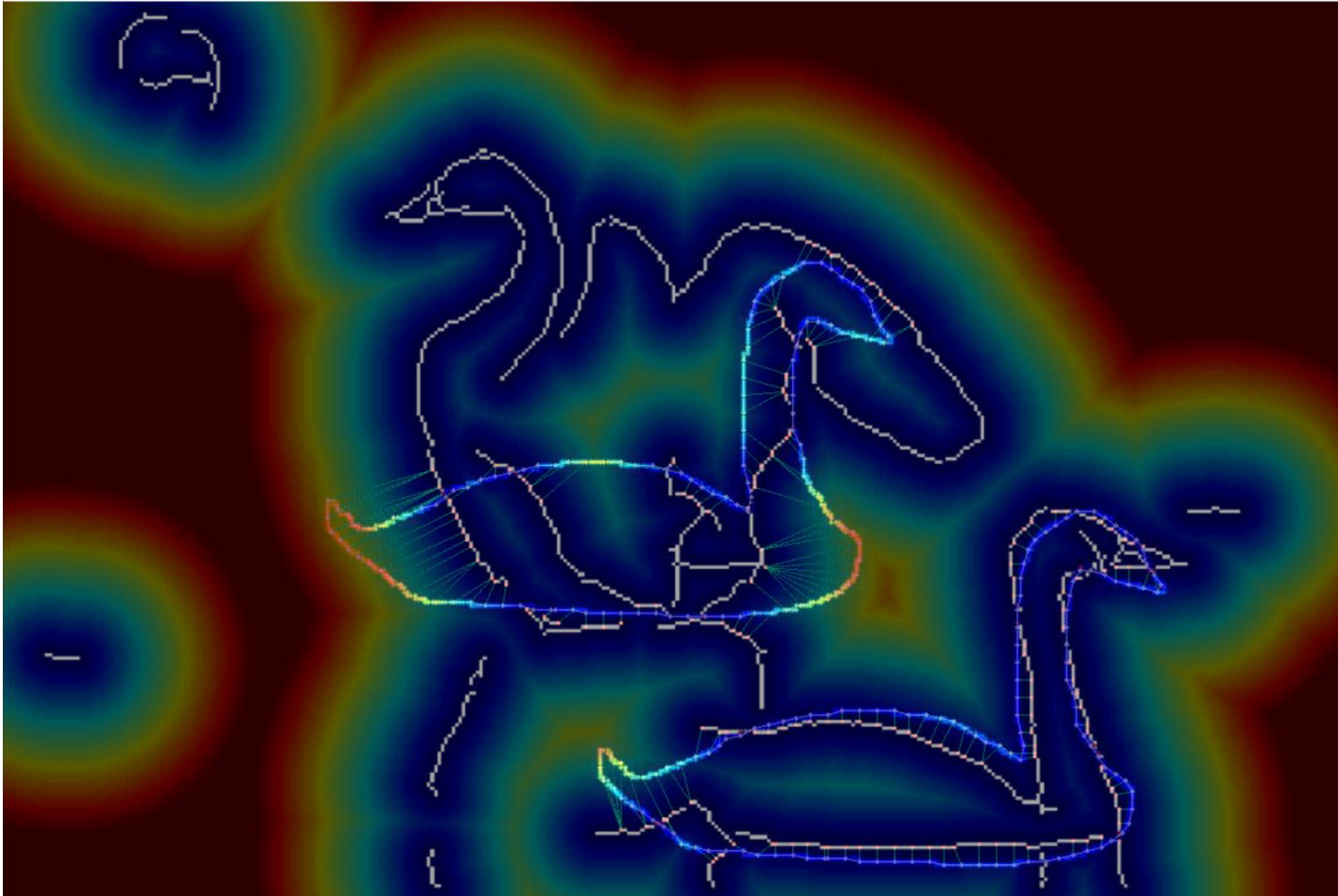
Chamfer Matching



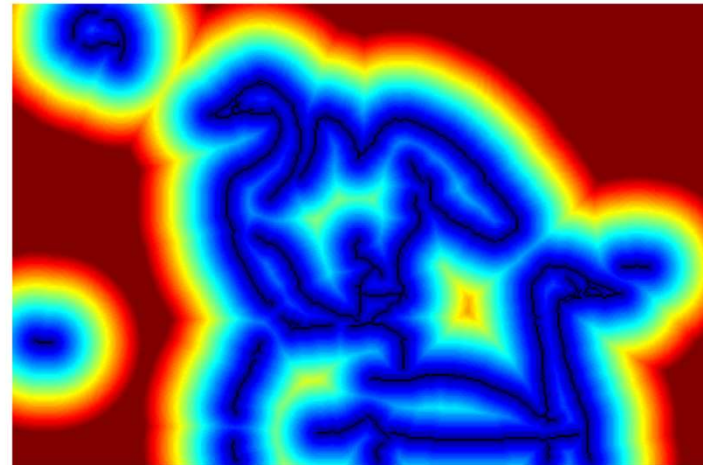
Chamfer Matching



Chamfer Matching



How to efficiently compute DT?



Distance Transform – 1D case

- 1D case, L1 norm: $|x_1 - y_1| + |x_2 - y_2|$
 - Two passes:
 - Find closest point on left
 - Find closest on right if closer than one on left
 - $O(n)$ algorithm

1. Initialize

$$j = \begin{matrix} 0 & 1 & & & & & & & n-1 \end{matrix}$$

∞	0	∞	0	∞	∞	∞	0	∞
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2. Forward pass ($j=1$ to $n-1$) $D[j] \leftarrow \min(D[j], D[j-1]+1)$

∞	0	1	0	1	2	3	0	1
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3. Backward pass ($j=n-2$ to 0) $D[j] \leftarrow \min(D[j], D[j+1]+1)$

1	0	1	0	1	2	1	0	1
---	---	---	---	---	---	---	---	---



Distance Transform – 2D

- 2D case similar to 1D
 - Initialize
 - Forward Pass (left and top)
 - Backward Pass (right and below)

∞	∞	∞	∞
∞	0	∞	∞
∞	0	∞	∞
∞	∞	∞	∞

∞	∞	∞	∞
∞	0	1	∞
∞	0	∞	∞
∞	∞	∞	∞

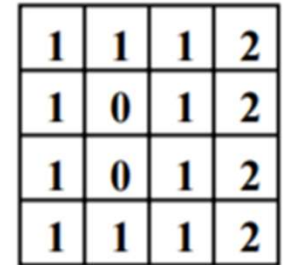
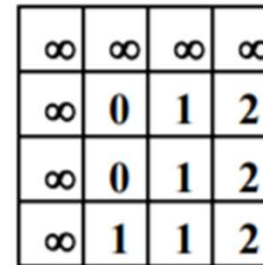
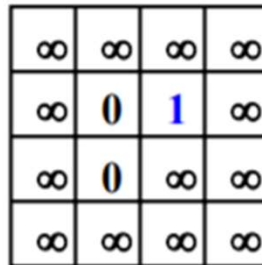
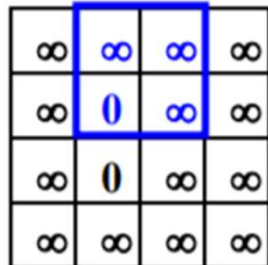
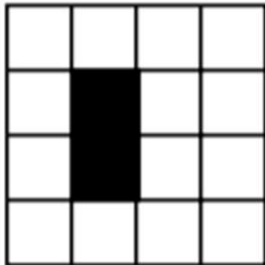
∞	∞	∞	∞
∞	0	1	2
∞	0	1	2
∞	1	2	3

2	1	2	3
1	0	1	2
1	0	1	2
2	1	2	3



Distance Transform – 2D

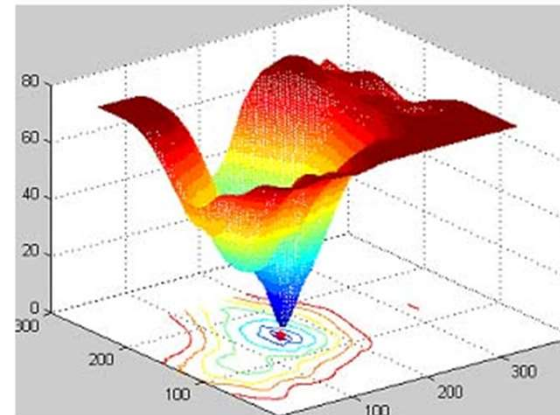
- Similar extension to 8 neighbours (Chessboard distance)
 - Initialize
 - Forward Pass (left, top, top-left)
 - Backward Pass (right, below, right-below)



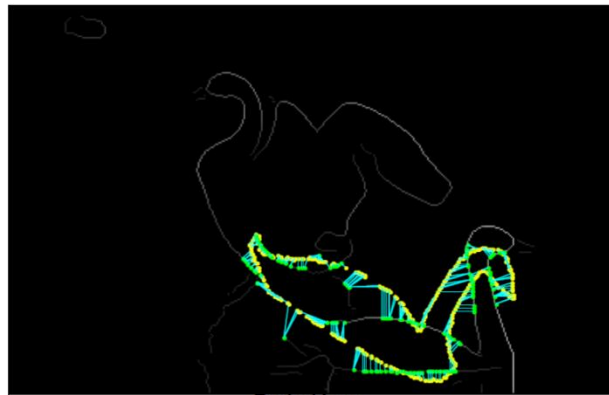
What about Euclidian Distance??

Chamfer Matching Overview

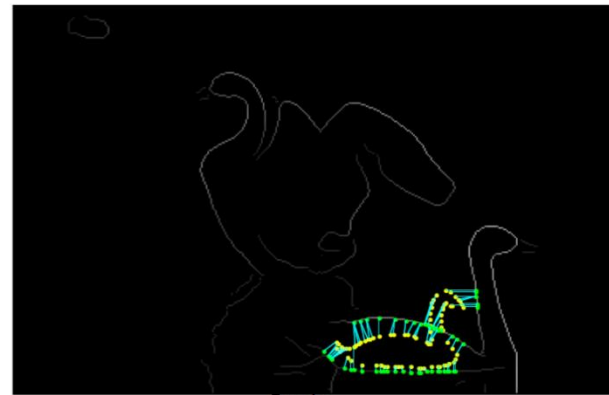
- Detect edges in query image
- Slide template over query image edge map
- Find closest edge pixel in image for each shifted template pixel
- At each location, compute average distance from each pixel in template to closest edge in image
- Lowest cost is the best match



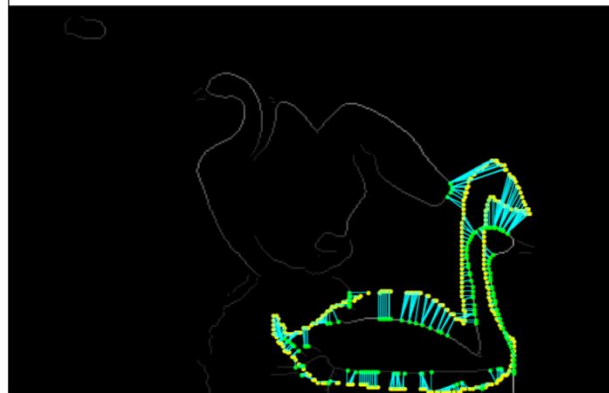
Limitations



Rotation



Scale

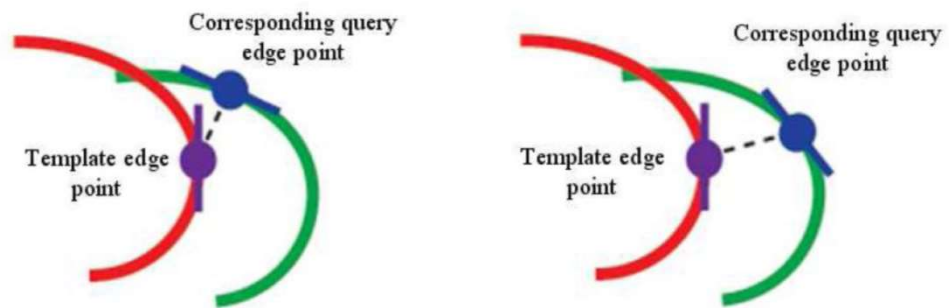


Aspect ratio



Bad edge map threshold / Clutter

Possible improvement



THANK YOU