

Homework3 q3

Please use [Substitution method](#) to find Big-O of this recursion . .

$$\begin{aligned} T(n) &= 0 && \text{if } n = 1 \\ T(n) &= T(n-1) + n - 1 && \text{if } n \geq 2 \end{aligned}$$

$$T(n) = T(n-1) + n - 1$$

$$= [T(n-2) + (n-1) - 1] + (n-1) - 1$$

$$= T(n-2) + 2(n-1) - 2$$

$$= T(n-3) + 3(n-1) - 3$$

$$= T(n-4) + 4(n-1) - 4$$

$$= T(n-5) + 5(n-1) - 5$$

$$= ..$$

$$= T(1) + n(n-1) - (1 + 2 + 3 + \dots + (n-1))$$

$$T(1) + n(n-1) - (1 + 2 + 3 + \dots + (n-1))$$

$$= 0 + n(n-1) - (n(n-1))/2$$

$$= n(n-1) - (n(n-1))/2$$

$$= (2n(n-1) - n(n-1))/2$$

$$= (n^2 - n)/2$$

$$\text{Big O} = O(n^2)$$