

# Software Testing

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## Lecture 21

# Overview

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A common application of graph criteria is to **program source**

**Graph** : Usually the control flow graph (CFG)

**Node coverage** : Execute every statement

**Edge coverage** : Execute every branch

**Loops** : Looping structures such as for loops, while loops, etc.

**Data flow coverage** : Augment the CFG

- **defs** are statements that assign values to variables
- **uses** are statements that use variables

# Control Flow Graphs

A CFG **models** all executions of a method by describing control structures

**Nodes** : Statements or sequences of statements (basic blocks)

**Edges** : Transfers of control

**Basic Block** : A sequence of statements such that if the first statement is executed, all statements will be (no branches)

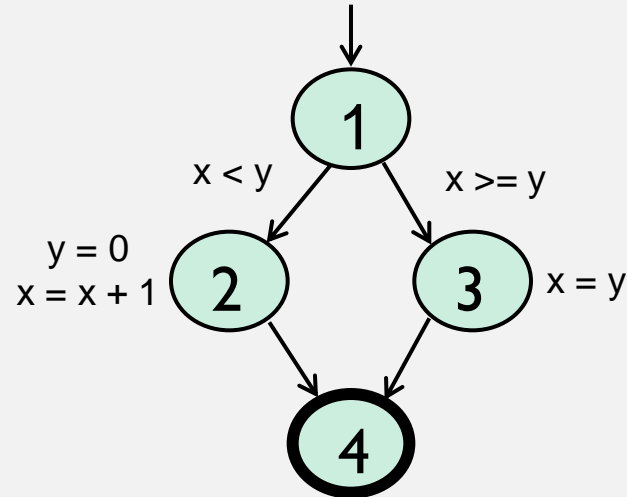
CFGs are sometimes annotated with extra information  
branch predicates

- **defs**
- **uses**

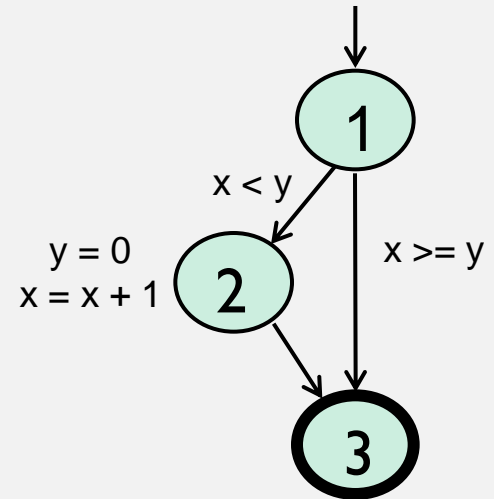
Rules for translating statements into graphs ...

# CFG : The if Statement

```
if (x < y)
{
  y = 0;
  x = x + 1;
}
else
{
  x = y;
}
```

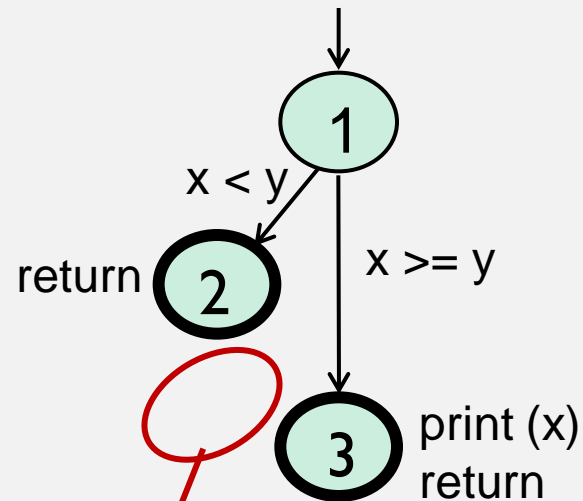


```
if (x < y)
{
  y = 0;
  x = x + 1;
}
```



# CFG : The if-Return Statement

```
if (x < y)
{
    return;
}
print (x);
return;
```



No edge from node 2 to 3.  
The return nodes must be distinct.

# Loops

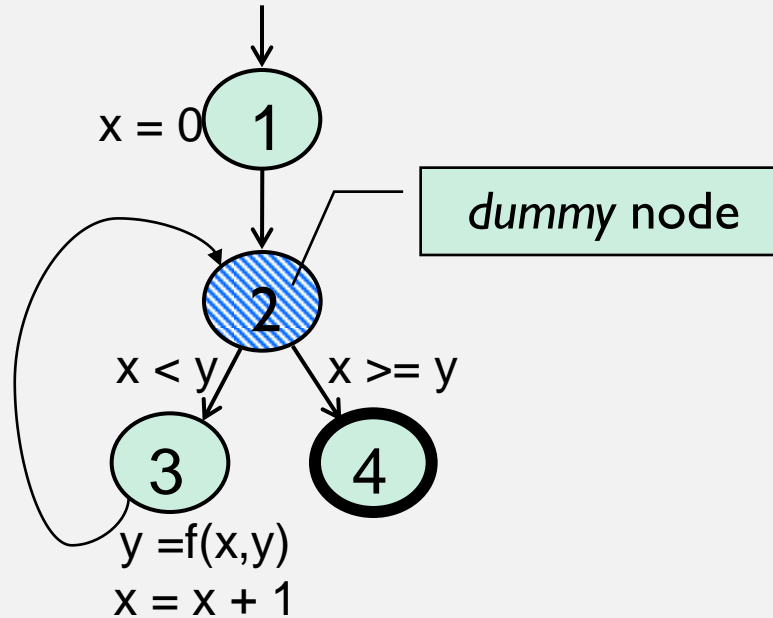
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Loops require “*extra*” nodes to be added

Nodes that do not represent statements or basic blocks

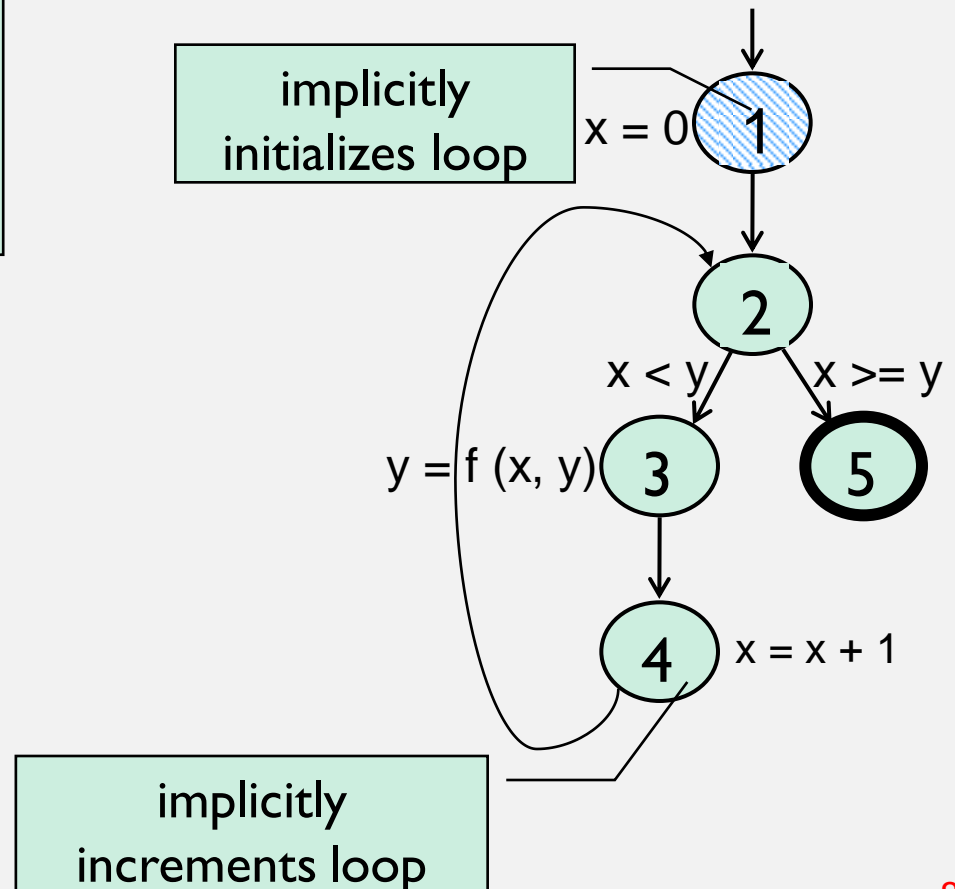
# CFG : while and for Loops

```
x = 0;  
while (x < y)  
{  
    y = f (x, y);  
    x = x + 1;  
}  
return (x);
```



# CFG : while and for Loops

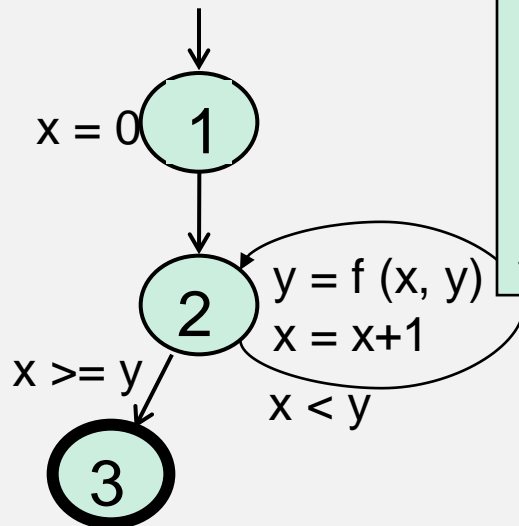
```
for (x = 0; x < y; x++)  
{  
    y = f (x, y) ;  
}  
return (x) ;
```



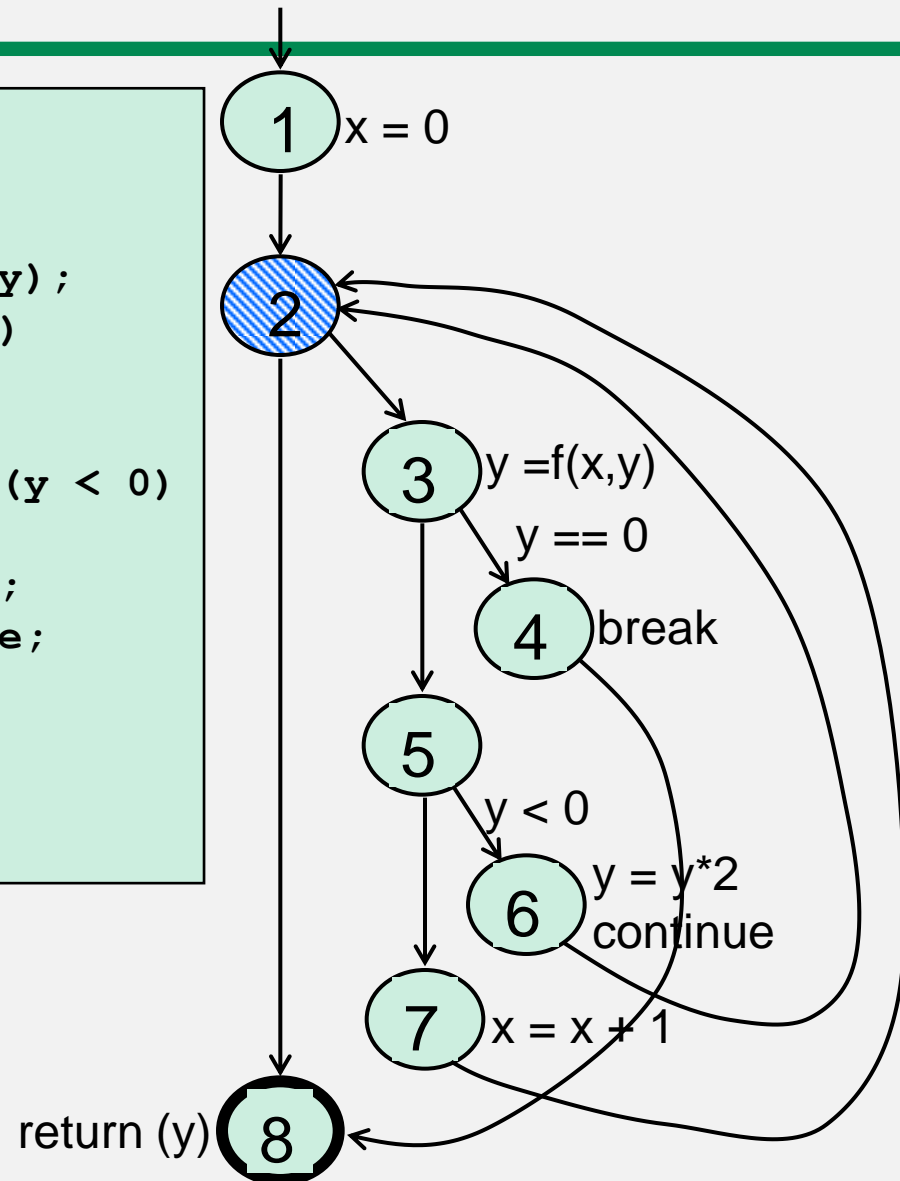


# CFG : do Loop, break and continue

```
x = 0;  
do  
{  
    y = f (x, y);  
    x = x + 1;  
} while (x < y);  
return (y);
```

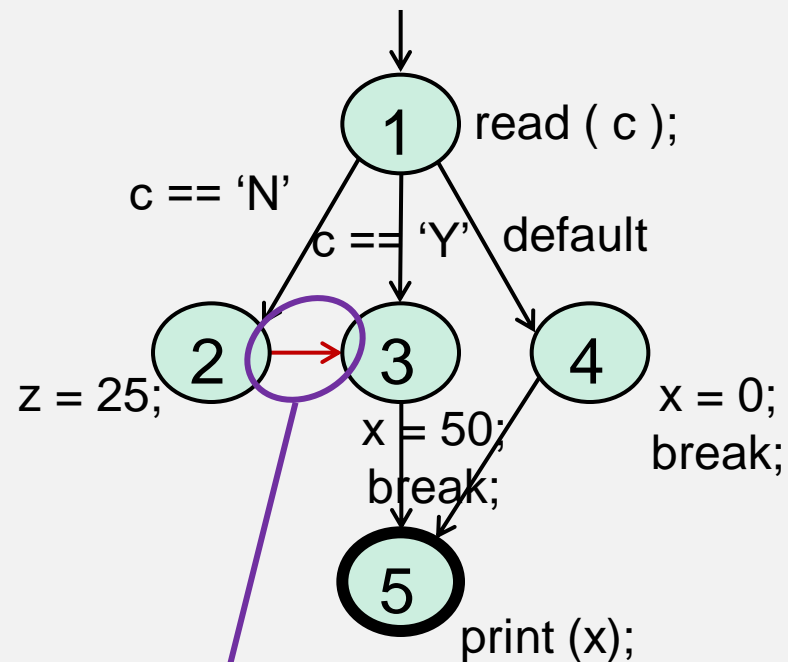


```
x = 0;  
while (x < y)  
{  
    y = f (x, y);  
    if (y == 0)  
    {  
        break;  
    } else if (y < 0)  
    {  
        y = y*2;  
        continue;  
    }  
    x = x + 1;  
}  
return (y);
```



# CFG : The case (switch) Structure

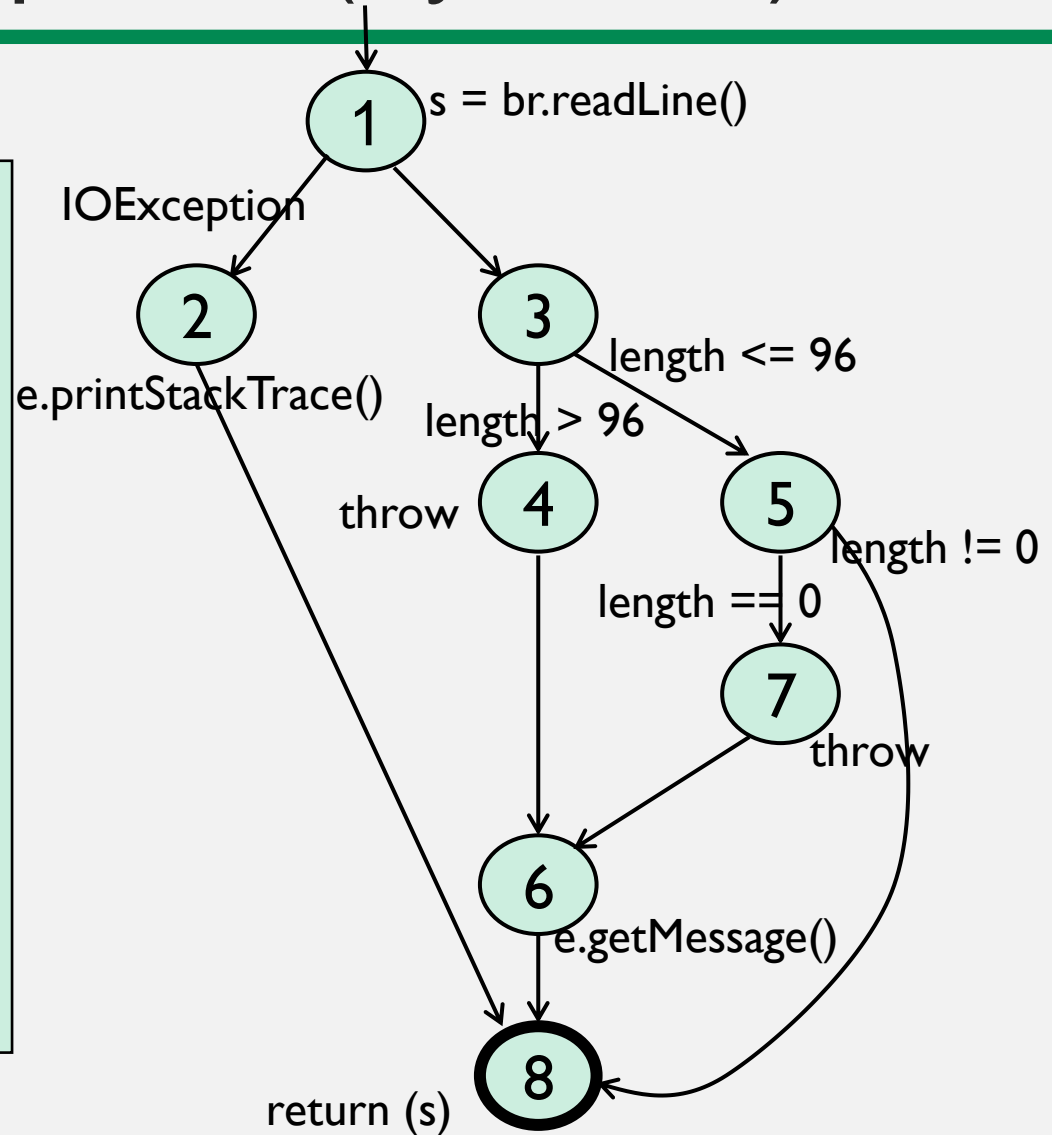
```
read ( c ) ;  
switch ( c )  
{  
    case 'N' :  
        z = 25;  
    case 'Y' :  
        x = 50;  
        break;  
    default:  
        x = 0;  
        break;  
}  
print (x) ;
```



Cases without breaks fall through to the next case

# CFG : Exceptions (try-catch)

```
try
{
    s = br.readLine();
    if (s.length() > 96)
        throw new Exception
            ("too long");
    if (s.length() == 0)
        throw new Exception
            ("too short");
} (catch IOException e) {
    e.printStackTrace();
} (catch Exception e) {
    e.getMessage();
}
return (s);
```



# Example Control Flow – Stats

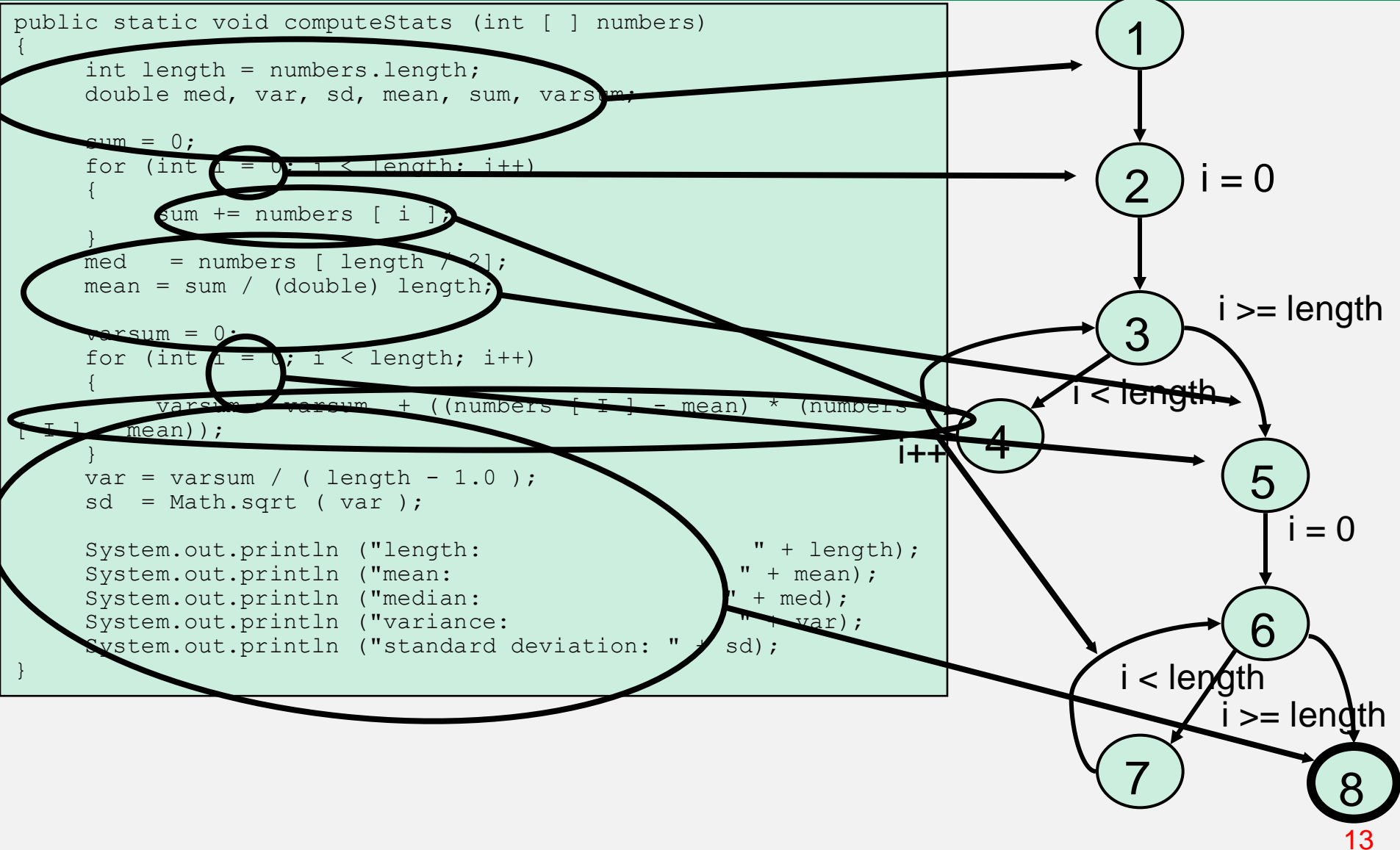
```
public static void computeStats (int [ ] numbers)
{
    int length = numbers.length;
    double med, var, sd, mean, sum, varsum;

    sum = 0;
    for (int i = 0; i < length; i++)
    {
        sum += numbers [ i ];
    }
    med    = numbers [ length / 2];
    mean = sum / (double) length;

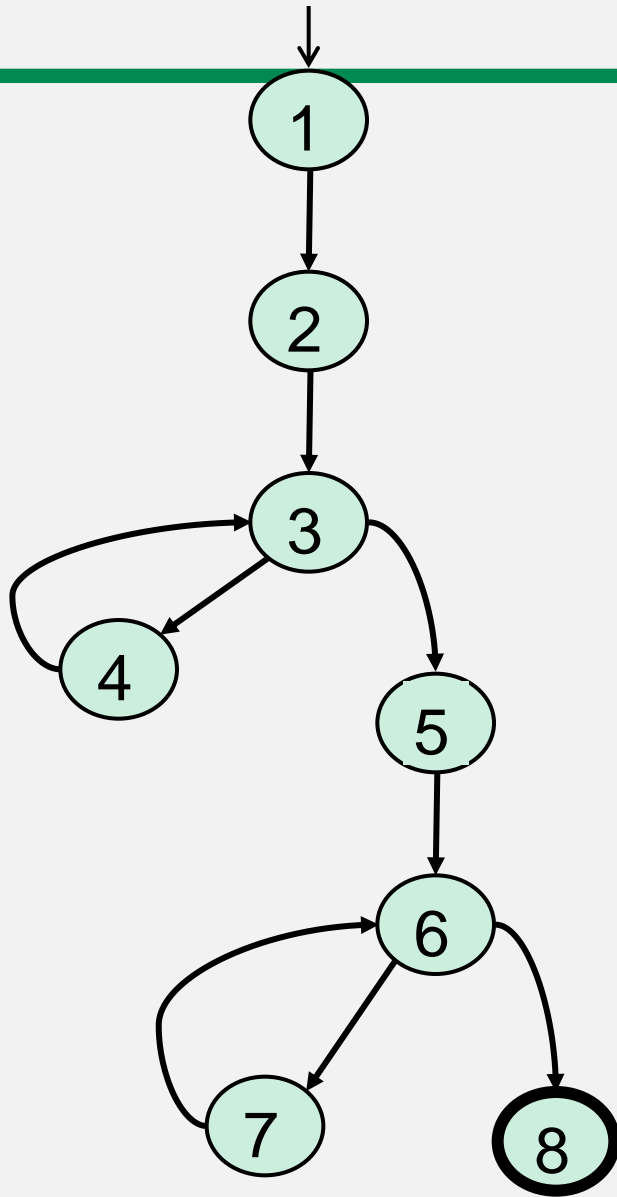
    varsum = 0;
    for (int i = 0; i < length; i++)
    {
        varsum = varsum + ((numbers [ i ] - mean) * (numbers [ i ] - mean));
    }
    var = varsum / ( length - 1.0 );
    sd  = Math.sqrt ( var );

    System.out.println ("length:           " + length);
    System.out.println ("mean:           " + mean);
    System.out.println ("median:         " + med);
    System.out.println ("variance:       " + var);
    System.out.println ("standard deviation: " + sd);
}
```

# Control Flow Graph for Stats

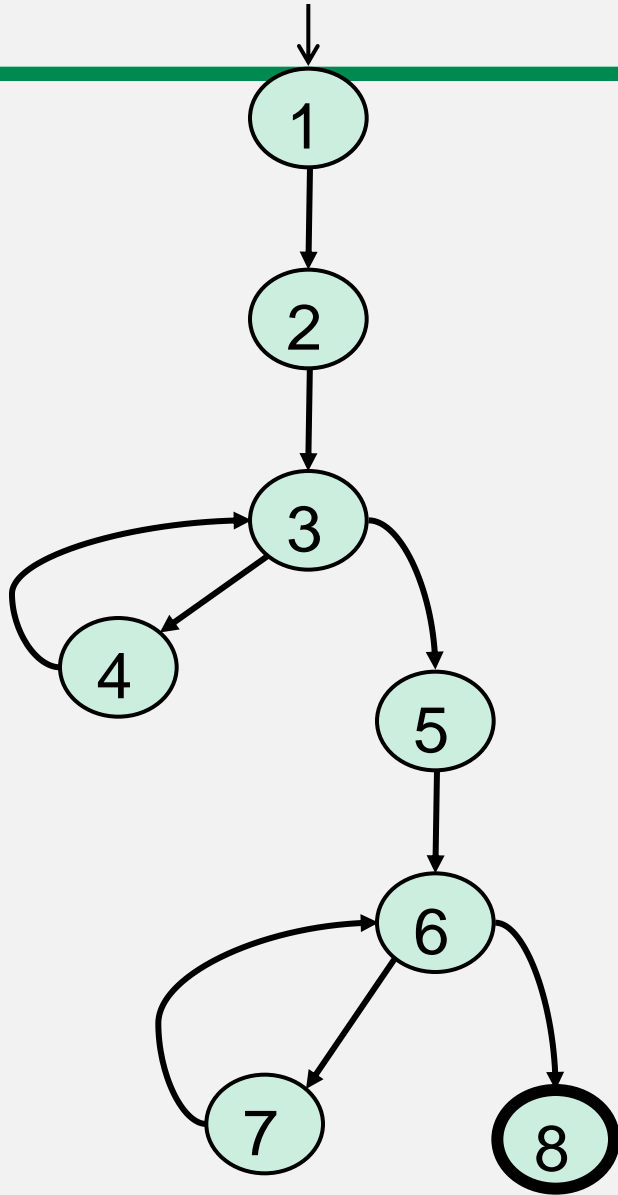


# Control Flow TRs and Test Paths—EC



| Edge Coverage |                                  |
|---------------|----------------------------------|
| TR            | Test Path                        |
| A. [ 1, 2 ]   | [ 1, 2, 3, 4, 3, 5, 6, 7, 6, 8 ] |
| B. [ 2, 3 ]   |                                  |
| C. [ 3, 4 ]   |                                  |
| D. [ 3, 5 ]   |                                  |
| E. [ 4, 3 ]   |                                  |
| F. [ 5, 6 ]   |                                  |
| G. [ 6, 7 ]   |                                  |
| H. [ 6, 8 ]   |                                  |
| I. [ 7, 6 ]   |                                  |

# Control Flow TRs and Test Paths—EPC



## Edge-Pair Coverage

### TR

A. [ 1, 2, 3 ]  
 B. [ 2, 3, 4 ]  
 C. [ 2, 3, 5 ]  
 D. [ 3, 4, 3 ]  
 E. [ 3, 5, 6 ]  
 F. [ 4, 3, 5 ]  
 G. [ 5, 6, 7 ]  
 H. [ 5, 6, 8 ]  
 I. [ 6, 7, 6 ]  
 J. [ 7, 6, 8 ]  
 K. [ 4, 3, 4 ]  
 L. [ 7, 6, 7 ]

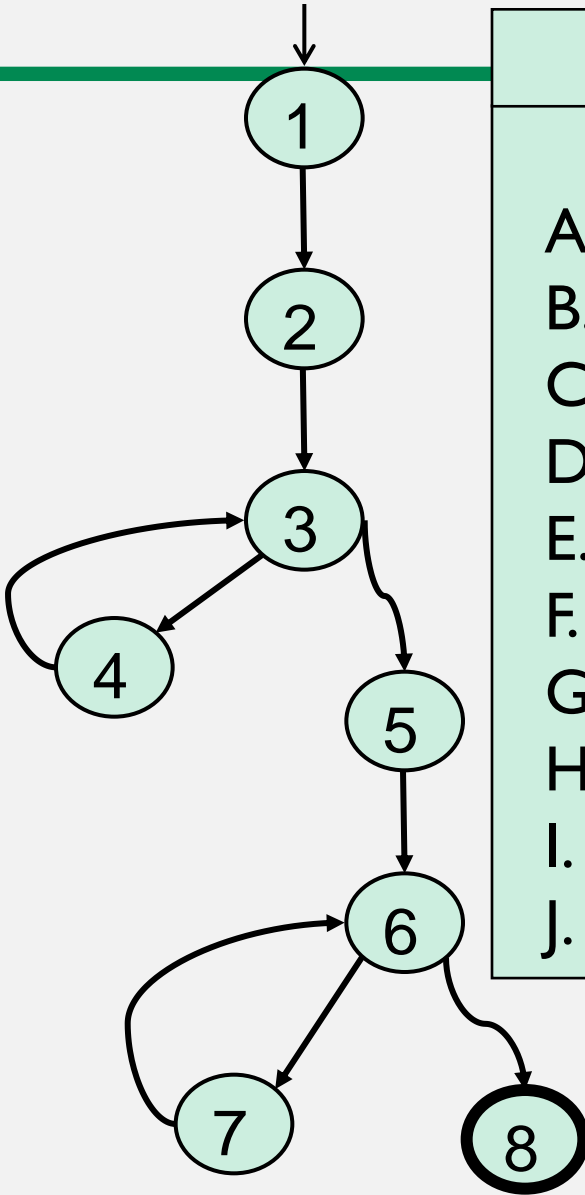
### Test Paths

i. [ 1, 2, 3, 4, 3, 5, 6, 7, 6, 8 ]  
 ii. [ 1, 2, 3, 5, 6, 8 ]  
 iii. [ 1, 2, 3, 4, 3, 4, 3, 5, 6, 7, 6, 7, 6, 8 ]

| TP  | TRs toured                   | <i>sidetrips</i> |
|-----|------------------------------|------------------|
| i   | A, B, D, E, F, G, I, J       | C, H             |
| ii  | A, C, E, H                   |                  |
| iii | A, B, D, E, F, G, I, J, K, L | C, H             |

TP iii makes TP i redundant. A *minimal* set of TPs is cheaper.

# Control Flow TRs and Test Paths—PPC



## Prime Path Coverage

### TR

- A. [ 3, 4, 3 ]
- B. [ 4, 3, 4 ]
- C. [ 7, 6, 7 ]
- D. [ 7, 6, 8 ]
- E. [ 6, 7, 6 ]
- F. [ 1, 2, 3, 4 ]
- G. [ 4, 3, 5, 6, 7 ]
- H. [ 4, 3, 5, 6, 8 ]
- I. [ 1, 2, 3, 5, 6, 7 ]
- J. [ 1, 2, 3, 5, 6, 8 ]

### Test Paths

- i. [ 1, 2, 3, 4, 3, 5, 6, 7, 6, 8 ]
- ii. [ 1, 2, 3, 4, 3, 4, 3, 5, 6, 7, 6, 7, 6, 8 ]
- iii. [ 1, 2, 3, 4, 3, 5, 6, 8 ]
- iv. [ 1, 2, 3, 5, 6, 7, 6, 8 ]
- v. [ 1, 2, 3, 5, 6, 8 ]

TP ii makes  
TP i redundant.

| TP  | TRs toured           | <i>sidetrips</i> |
|-----|----------------------|------------------|
| i   | A, D, E, F, G        | H, I, J          |
| ii  | A, B, C, D, E, F, G, | H, I, J          |
| iii | A, F, H              | J                |
| iv  | D, E, F, I           | J                |
| v   | J                    |                  |



# Data Flow Coverage for Source

**def** : a location where a value is stored into memory

- x appears on the left side of an assignment (`x = 44;`)

- x is an actual parameter in a call and the method changes its value

- x is a formal parameter of a method (implicit def when method starts)

- x is an input to a program

**use** : a location where variable's value is accessed

- x appears on the right side of an assignment

- x appears in a conditional test

- x is an actual parameter to a method

- x is an output of the program

- x is an output of a method in a return statement

If a def and a use appear on the same node, then it is only a DU-pair if the def occurs after the use and the node is in a loop

# Example Data Flow – Stats

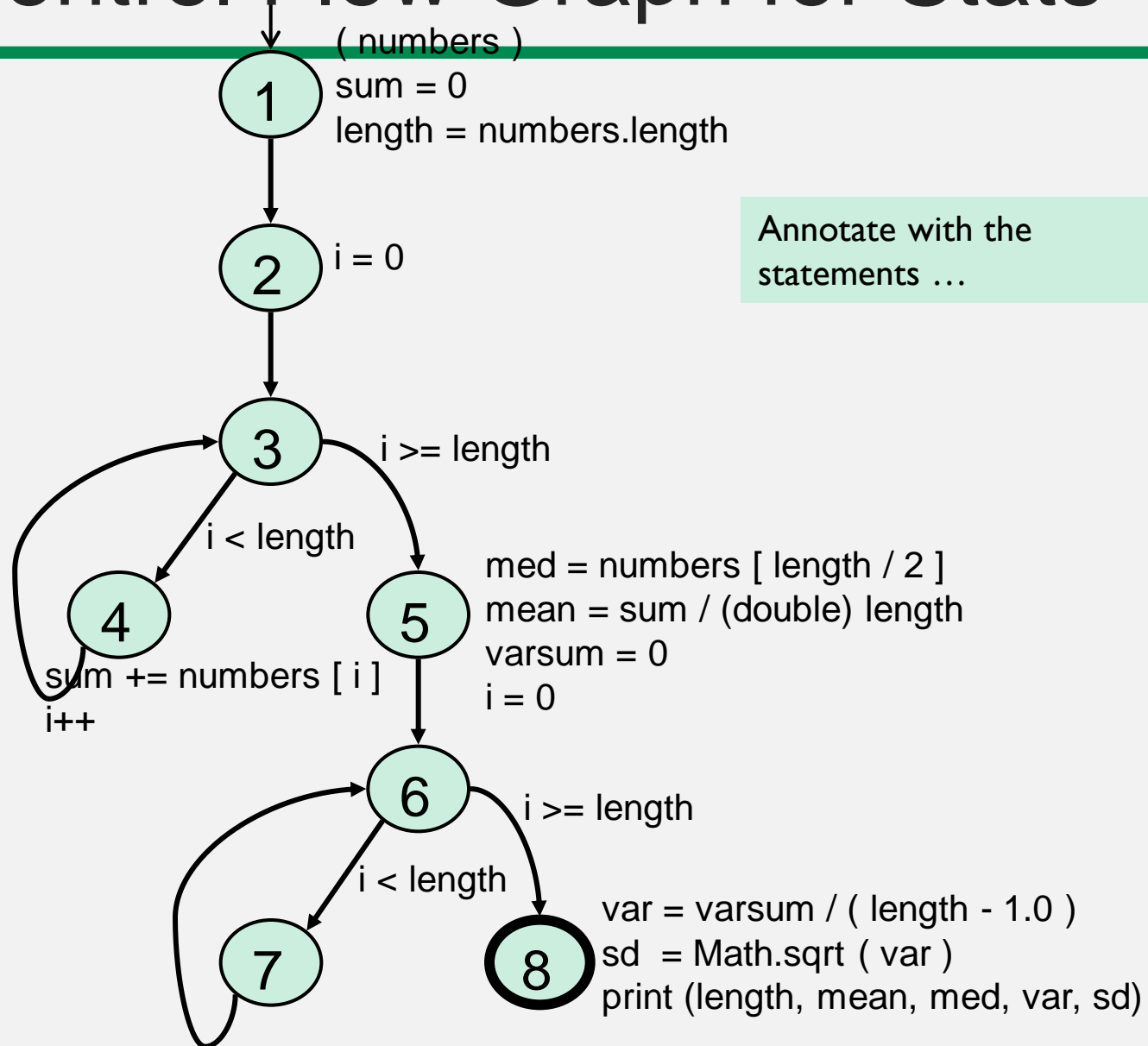
```
public static void computeStats (int [ ] numbers)
{
    int length = numbers.length;
    double med, var, sd, mean, sum, varsum;

    sum = 0.0;
    for (int i = 0; i < length; i++)
    {
        sum += numbers [ i ];
    }
    med    = numbers [ length / 2 ];
    mean = sum / (double) length;

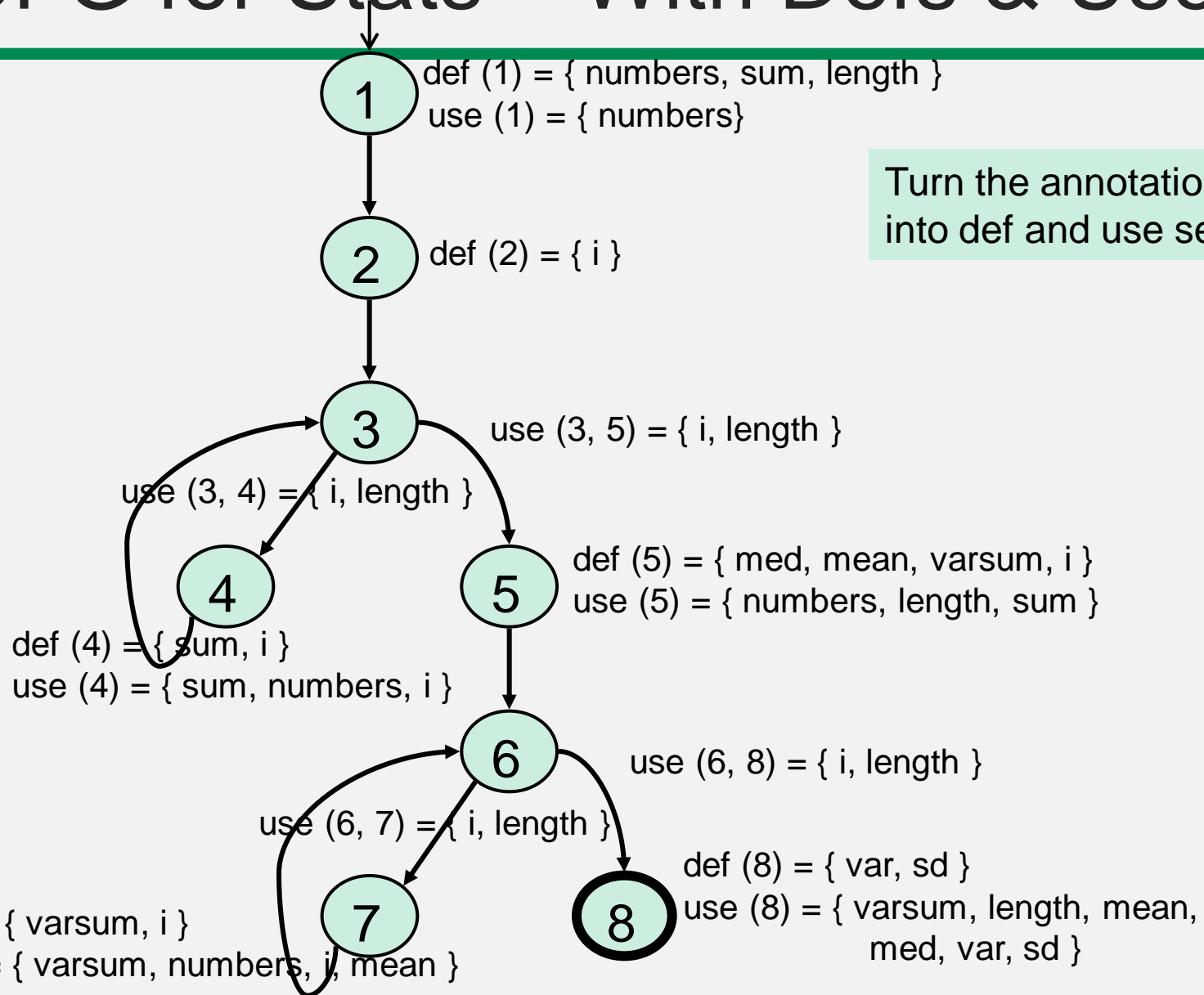
    varsum = 0.0;
    for (int i = 0; i < length; i++)
    {
        varsum = varsum + ((numbers [ i ] - mean) * (numbers [ i ] - mean));
    }
    var = varsum / ( length - 1 );
    sd  = Math.sqrt ( var );

    System.out.println ("length:           " + length);
    System.out.println ("mean:           " + mean);
    System.out.println ("median:        " + med);
    System.out.println ("variance:      " + var);
    System.out.println ("standard deviation: " + sd);
}
```

# Control Flow Graph for Stats



# CFG for Stats – With Defs & Uses



# Defs and Uses Tables for Stats

| Node | Def                      | Use   |
|------|--------------------------|---|
| 1    | { numbers, sum, length } | { numbers }                                 |
| 2    | { i }                    |   |
| 3    |                          |   |
| 4    | { sum, i }               | { numbers, i, sum }                         |
| 5    | { med, mean, varsum, i } | { numbers, length, sum }                    |
| 6    |                          |   |
| 7    | { varsum, i }            | { varsum, numbers, i, mean }                |
| 8    | { var, sd }              | { varsum, length, var, mean, med, var, sd } |

| Edge   | Use           |
|--------|---------------|
| (1, 2) |               |
| (2, 3) |               |
| (3, 4) | { i, length } |
| (4, 3) |               |
| (3, 5) | { i, length } |
| (5, 6) |               |
| (6, 7) | { i, length } |
| (7, 6) |               |
| (6, 8) | { i, length } |

# DU Pairs for Stats

| variable | DU Pairs   |
|----------|--|
| numbers  | (1, 4) (1, 5) (1, 7)   |
| length   | (1, 5) (1, 8) (1, (3,4)) (1, (3,5)) (1, (6,7)) (1, (6,8))  |
| med      | (5, 8)   |
| var      | (8, 8)   |
| sd       | (8, 8)   |
| mean     | (5, 7) (5, 8)  |
| sum      | (1, 4) (1, 5) (4, 4) (4, 5)  |
| varsum   | (5, 7) (5, 8) (7, 7) (7, 8)  |
| i        | <del>(2, 4) (2, (3,4)) (2, (3,5)) (2, 7) (2, (6,7)) (2, (6,8))</del><br><del>(4, 4) (4, (3,4)) (4, (3,5)) (4, 7) (4, (6,7)) (4, (6,8))</del><br>(5, 7) (5, (6,7)) (5, (6,8))<br>(7, 7) (7, (6,7)) (7, (6,8)) |

defs come before uses, do not count as DU pairs

defs after use in loop, these are valid DU pairs

No def-clear path ... different scope for i

No path through graph from nodes 5 and 7 to 4 or 3

# DU Paths for Stats

| variable | DU Pairs   | DU Paths   |
|----------|--|--|
| numbers  | (1, 4)<br>(1, 5)<br>(1, 7)   | [ 1, 2, 3, 4 ]<br>[ 1, 2, 3, 5 ]<br>[ 1, 2, 3, 5, 6, 7 ]   |
| length   | (1, 5)<br>(1, 8)<br>(1, (3,4))<br>(1, (3,5))<br>(1, (6,7))<br>(1, (6,8)) | [ 1, 2, 3, 5 ]<br>[ 1, 2, 3, 5, 6, 8 ]<br>[ 1, 2, 3, 4 ]<br>[ 1, 2, 3, 5 ]<br>[ 1, 2, 3, 5, 6, 7 ]<br>[ 1, 2, 3, 5, 6, 8 ] |
| med      | (5, 8)   | [ 5, 6, 8 ]  |
| var      | (8, 8)   | <i>No path needed</i>  |
| sd       | (8, 8)   | <i>No path needed</i>  |
| sum      | (1, 4)<br>(1, 5)<br>(4, 4)<br>(4, 5)                                     | [ 1, 2, 3, 4 ]<br>[ 1, 2, 3, 5 ]<br>[ 4, 3, 4 ]<br>[ 4, 3, 5 ]   |

| variable | DU Pairs   | DU Paths   |
|----------|--|--|
| mean     | (5, 7)<br>(5, 8)   | [ 5, 6, 7 ]<br>[ 5, 6, 8 ]   |
| varsum   | (5, 7)<br>(5, 8)<br>(7, 7)<br>(7, 8)   | [ 5, 6, 7 ]<br>[ 5, 6, 8 ]<br>[ 7, 6, 7 ]<br>[ 7, 6, 8 ]   |
| i        | (2, 4)<br>(2, (3,4))<br>(2, (3,5))<br>(4, 4)<br>(4, (3,4))<br>(4, (3,5))<br>(5, 7)<br>(5, (6,7))<br>(5, (6,8))<br>(7, 7)<br>(7, (6,7))<br>(7, (6,8)) | [ 2, 3, 4 ]<br>[ 2, 3, 4 ]<br>[ 2, 3, 5 ]<br>[ 4, 3, 4 ]<br>[ 4, 3, 4 ]<br>[ 4, 3, 5 ]<br>[ 5, 6, 7 ]<br>[ 5, 6, 7 ]<br>[ 5, 6, 8 ]<br>[ 7, 6, 7 ]<br>[ 7, 6, 7 ]<br>[ 7, 6, 8 ] |

# DU Paths for Stats—No Duplicates

There are 38 DU paths for Stats, but only 12 unique

|                        |               |
|------------------------|---------------|
| ★ [ 1, 2, 3, 4 ]       | [ 4, 3, 4 ] ★ |
| ★ [ 1, 2, 3, 5 ]       | [ 4, 3, 5 ] ★ |
| ★ [ 1, 2, 3, 5, 6, 7 ] | [ 5, 6, 7 ] ★ |
| ★ [ 1, 2, 3, 5, 6, 8 ] | [ 5, 6, 8 ] ★ |
| ★ [ 2, 3, 4 ]          | [ 7, 6, 7 ] ★ |
| ★ [ 2, 3, 5 ]          | [ 7, 6, 8 ] ★ |

★ 4 expect a loop not to be “entered”

★ 6 require at least one iteration of a loop

★ 2 require at least two iterations of a loop



# Test Cases and Test Paths

Test Case : numbers = (44) ; length = 1

Test Path : [ 1, 2, 3, 4, 3, 5, 6, 7, 6, 8 ]

Additional DU Paths covered (no sidetrips)

[ 1, 2, 3, 4 ] [ 2, 3, 4 ] [ 4, 3, 5 ] [ 5, 6, 7 ] [ 7, 6, 8 ]

*The five stars ✨ that require at least one iteration of a loop*

Test Case : numbers = (2, 10, 15) ; length = 3

Test Path : [ 1, 2, 3, 4, 3, 4, 3, 4, 3, 5, 6, 7, 6, 7, 6, 7, 6, 8 ]

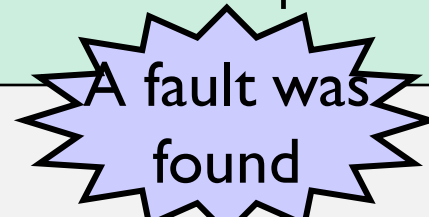
DU Paths covered (no sidetrips)

[ 4, 3, 4 ] [ 7, 6, 7 ]

*The two stars ✨ that require at least two iterations of a loop*

Other DU paths require arrays with length 0 to skip loops  
But the method fails with index out of bounds exception...

med = numbers [length / 2];



# Summary

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- Applying the graph test criteria to control flow graphs is relatively straightforward
  - Most of the developmental research work was done with CFGs
- A few subtle decisions must be made to translate control structures into the graph
- Some tools will assign each statement to a unique node
  - These slides and the book uses basic blocks
  - Coverage is the same, although the bookkeeping will differ

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Thank You