

$tnvar, x, y, f, m, n$	variables
$covar, c$	coercion variables
$datacon, K$	
$const, T, F$	
$index, i$	indices

$relflag, \rho$	$::=$ $ $ $+$ $ $ $-$ $ $ $app_rho \nu$ S $ $ (ρ) S	relevance flag
$appflag, \nu$	$::=$ $ $ R $ $ ρ	applicative flag
$role, R$	$::=$ $ $ Nom $ $ Rep $ $ $R_1 \cap R_2$ S $ $ param $R_1 R_2$ S $ $ $app_role \nu$ S $ $ (R) S	Role
$constraint, \phi$	$::=$ $ $ $a \sim_{A/R} b$ $ $ (ϕ) S $ $ $\phi\{b/x\}$ S $ $ $ \phi $ S $ $ $a \sim_R b$ S	props
$tm, a, b, p, v, w, A, B, C$	$::=$ $ $ \star $ $ x $ $ $\lambda^\rho x:A. b$ bind x in b $ $ $\lambda^\rho x. b$ bind x in b $ $ $a \ b^\nu$ $ $ $\Pi^\rho x:A \rightarrow B$ bind x in B $ $ $\Lambda c:\phi. b$ bind c in b $ $ $\Lambda c. b$ bind c in b $ $ $a[\gamma]$ $ $ $\forall c:\phi. B$ bind c in B $ $ $a \triangleright_R \gamma$ $ $ F $ $ \square $ $ $\text{case}_R a \text{ of } F \rightarrow b_1 \parallel - \rightarrow b_2$ $ $ K $ $ match a with brs $ $ sub $R a$ $ $ $a\{b/x\}$ S $ $ $a\{\gamma/c\}$ S $ $ a S $ $ a S	types and kinds

		(a)	S	
		a	S	parsing precedence is hard
		$ a _R$	S	
		Int	S	
		Bool	S	
		Nat	S	
		Vec	S	
		0	S	
		S	S	
		True	S	
		Fix	S	
		Age	S	
		$a \rightarrow b$	S	
		$\phi \Rightarrow A$	S	
		$a \ b$	S	
		$\lambda x. a$	S	
		$\lambda x : A. a$	S	
		$\forall x : A \rightarrow B$	S	
		if ϕ then a else b	S	
brs	$::=$			case branches
		none		
		$K \Rightarrow a; brs$		
		$brs\{a/x\}$	S	
		$brs\{\gamma/c\}$	S	
		(brs)	S	
co, γ	$::=$			explicit coercions
		\bullet		
		c		
		red $a \ b$		
		refl a		
		$(a \models_\gamma b)$		
		sym γ		
		$\gamma_1; \gamma_2$		
		sub γ		
		$\Pi^{R,\rho} x : \gamma_1. \gamma_2$	bind x in γ_2	
		$\lambda^{R,\rho} x : \gamma_1. \gamma_2$	bind x in γ_2	
		$\gamma_1 \ \gamma_2^{R,\rho}$		
		piFst γ		
		cpiFst γ		
		isoSnd γ		
		$\gamma_1 @ \gamma_2$		
		$\forall c : \gamma_1. \gamma_3$	bind c in γ_3	
		$\lambda c : \gamma_1. \gamma_3 @ \gamma_4$	bind c in γ_3	
		$\gamma(\gamma_1, \gamma_2)$		

		$\gamma @ (\gamma_1 \sim \gamma_2)$	
		$\gamma_1 \triangleright_R \gamma_2$	
		$\gamma_1 \sim_A \gamma_2$	
		conv $\phi_1 \sim_\gamma \phi_2$	
		eta a	
		left $\gamma \gamma'$	
		right $\gamma \gamma'$	
		(γ)	S
		γ	S
		$\gamma\{a/x\}$	S
$role_context, \Omega$	$::=$		$role_contexts$
		\emptyset	
		$x : R$	
		$\Omega, x : R$	
		Ω, Ω'	M
		Γ_{Nom}	
		(Ω)	M
		Ω	M
$roles, Rs$	$::=$		
		nilR	
		R, Rs	
		$range(W)$	S
sig_sort	$::=$		signature classifier
		$A @ Rs$	
		$p \sim a : A / R @ Rs$	
$sort$	$::=$		binding classifier
		Tm A	
		Co ϕ	
$context, \Gamma$	$::=$		contexts
		\emptyset	
		$\Gamma, x : A$	
		$\Gamma, c : \phi$	
		$\Gamma\{b/x\}$	M
		$\Gamma\{\gamma/c\}$	M
		Γ, Γ'	M
		$ \Gamma $	M
		(Γ)	M
		Γ	M
sig, Σ	$::=$		signatures
		\emptyset	
		$\Sigma \cup \{F sig_sort\}$	

		Σ_0	M
		Σ_1	M
		$ \Sigma $	M
$available_props, \Delta$	$::=$		
		\emptyset	
		Δ, c	
		$\tilde{\Gamma}$	M
		(Δ)	M
$terminals$	$::=$		
		\leftrightarrow	
		\Leftrightarrow	
		\longrightarrow	
		min	
		\equiv	
		\forall	
		\in	
		\notin	
		\Leftarrow	
		\Rightarrow	
		\Rightarrow^*	
		\rightarrow	
		Λ	
		\square	
		\vdash	
		\dashv	
		\models	
		\models	
		\neq	
		\triangleright	
		ok	
		$-$	
		\rightsquigarrow	
		\rightsquigarrow^*	
		\rightsquigarrow	
		\emptyset	
		\circ	
		fv	
		dom	
		\sim	
		\succ	
		$ $	
		\bullet	
		fst	

	$ \begin{array}{ l} \mathbf{snd} \\ \mathbf{as} \\ \Rightarrow \\ \vdash_{=} \\ \mathbf{refl_2} \\ ++ \\ \end{array} $	
$formula, \psi$	$ \begin{array}{ l} ::= \\ judgement \\ x : A \in \Gamma \\ x : R \in \Omega \\ c : \phi \in \Gamma \\ F : sig_sort \in \Sigma \\ x \in \Delta \\ c \in \Delta \\ c \mathbf{not\ relevant} \in \gamma \\ x \notin fva \\ x \notin \mathbf{dom} \Gamma \\ uniqu \Gamma \\ uniqu(\Omega) \\ c \notin \mathbf{dom} \Gamma \\ T \notin \mathbf{dom} \Sigma \\ F \notin \mathbf{dom} \Sigma \\ R_1 = R_2 \\ a = b \\ \phi_1 = \phi_2 \\ \Gamma_1 = \Gamma_2 \\ \gamma_1 = \gamma_2 \\ \neg \psi \\ \psi_1 \wedge \psi_2 \\ \psi_1 \vee \psi_2 \\ \psi_1 \Rightarrow \psi_2 \\ (\psi) \\ \psi \\ c : (a : A \sim b : B) \in \Gamma \\ \end{array} $	<p>suppress lc hypothesis generated by Ott</p>
$JSubRole$	$ \begin{array}{ l} ::= \\ R_1 \leq R_2 \\ \end{array} $	<p>Subroling judgement</p>
$JPath$	$ \begin{array}{ l} ::= \\ \mathbf{Path} \ a = F@Rs \\ \end{array} $	<p>Type headed by constant (partial function)</p>
$JRoledPath$	$ \begin{array}{ l} ::= \\ \mathbf{Path}_R \ a = F@Rs \\ \end{array} $	<p>Type headed by constant (role-sensitive partial function)</p>
$JPatCtx$	$::= $	

	$\Omega; \Gamma \models p : A$	Contexts generated by a pattern (variables h
$JMatchSubst$	$::=$ $\text{match } a_1 \text{ with } p \rightarrow b_1 = b_2$	match and substitute
$JApplyArgs$	$::=$ $\text{apply args } a \text{ to } b \mapsto b'$	apply arguments of a (headed by a constant
$JValue$	$::=$ $\text{Value}_R A$	values
$JValueType$	$::=$ $\text{ValueType}_R A$	Types with head forms (erased language)
$Jconsistent$	$::=$ $\text{consistent}_R a \ b$	(erased) types do not differ in their heads
$Jroleing$	$::=$ $\Omega \models a : R$	Roleing judgment
$JChk$	$::=$ $(\rho = +) \vee (x \notin \text{fv } A)$	irrelevant argument check
$Jpar$	$::=$ $\Omega \models a \Rightarrow_R b$ $\Omega \models a \Rightarrow_R^* b$ $\Omega \models a \Leftrightarrow_R b$	parallel reduction (implicit language) multistep parallel reduction parallel reduction to a common term
$Jbeta$	$::=$ $\models a > b/R$ $\models a \rightsquigarrow b/R$ $\models a \rightsquigarrow^* b/R$	primitive reductions on erased terms single-step head reduction for implicit langua multistep reduction
$JBranchTyping$	$::=$ $\Gamma \models \text{case}_R a : A \text{ of } b : B \Rightarrow C \mid C'$	Branch Typing (aligning the types of case)
$JFoldCtxType$	$::=$ $\Gamma \text{ CtxType } p : A = B$	Fold Context to Type
$Jett$	$::=$ $\Gamma \models \phi \text{ ok}$ $\Gamma \models a : A$ $\Gamma; \Delta \models \phi_1 \equiv \phi_2$ $\Gamma; \Delta \models a \equiv b : A/R$ $\models \Gamma$	Prop wellformedness typing prop equality definitional equality context wellformedness
$Jsig$	$::=$	

		$\models \Sigma$	signature wellformedness
<i>judgement</i>	$::=$	<ul style="list-style-type: none"> <i>JSubRole</i> <i>JPath</i> <i>JRoledPath</i> <i>JPatCtx</i> <i>JMatchSubst</i> <i>JApplyArgs</i> <i>JValue</i> <i>JValueType</i> <i>Jconsistent</i> <i>Jroleing</i> <i>JChk</i> <i>Jpar</i> <i>Jbeta</i> <i>JBranchTyping</i> <i>JFoldCtxType</i> <i>Jett</i> <i>Jsig</i> 	
<i>user_syntax</i>	$::=$	<ul style="list-style-type: none"> <i>tmvar</i> <i>covar</i> <i>datacon</i> <i>const</i> <i>index</i> <i>relflag</i> <i>appflag</i> <i>role</i> <i>constraint</i> <i>tm</i> <i>brs</i> <i>co</i> <i>role_context</i> <i>roles</i> <i>sig_sort</i> <i>sort</i> <i>context</i> <i>sig</i> <i>available_props</i> <i>terminals</i> <i>formula</i> 	

$\boxed{R_1 \leq R_2}$ Subroling judgement

$\overline{\mathbf{Nom} \leq R}$ NOMBOT

$\overline{R \leq \mathbf{Rep}}$ REPTOP

$\overline{R \leq R}$ REFL

$$\frac{R_1 \leq R_2 \quad R_2 \leq R_3}{R_1 \leq R_3} \text{TRANS}$$

$\boxed{\text{Path } a = F@Rs}$ Type headed by constant (partial function)

$$\frac{F : A@Rs \in \Sigma_0}{\text{Path } F = F@Rs} \text{PATH_ABSCONST}$$

$$\frac{F : p \sim a : A/R_1@Rs \in \Sigma_0}{\text{Path } F = F@Rs} \text{PATH_CONST}$$

$$\frac{\text{Path } a = F@R_1, Rs \quad app_role\nu = R_1}{\text{Path } (a \ b'^\nu) = F@Rs} \text{PATH_APP}$$

$$\frac{\text{Path } a = F@Rs}{\text{Path } (a[\bullet]) = F@Rs} \text{PATH_CAPP}$$

$\boxed{\text{Path}_R a = F@Rs}$ Type headed by constant (role-sensitive partial function)

$$\frac{F : A@Rs \in \Sigma_0}{\text{Path}_R F = F@Rs} \text{ROLEDPATH_ABSCONST}$$

$$\frac{F : p \sim a : A/R_1@Rs \in \Sigma_0 \quad \neg(R_1 \leq R)}{\text{Path}_R F = F@Rs} \text{ROLEDPATH_CONST}$$

$$\frac{\text{Path}_R a = F@R_1, Rs \quad app_role\nu = R_1}{\text{Path}_R (a \ b'^\nu) = F@Rs} \text{ROLEDPATH_APP}$$

$$\frac{\text{Path}_R a = F@Rs}{\text{Path}_R (a[\bullet]) = F@Rs} \text{ROLEDPATH_CAPP}$$

$\boxed{\Omega; \Gamma \models p : A}$ Contexts generated by a pattern (variables bound by the pattern)

$$\frac{}{\emptyset; \emptyset \models F : A} \text{PATCTX_CONST}$$

$$\frac{\Omega; \Gamma \models p : \Pi^+ x : A' \rightarrow A}{\Omega, x : R; \Gamma, x : A' \models p \ x^+ : A} \text{PATCTX_PIREL}$$

$$\frac{\Omega; \Gamma \models p : \Pi^- x : A' \rightarrow A}{\Omega; \Gamma, x : A' \models p \ \Box^- : A} \text{PATCTX_PIIRR}$$

$$\frac{\Omega; \Gamma \models p : \forall c : \phi. A}{\Omega; \Gamma, c : \phi \models p[\bullet] : A} \text{PATCTX_CPI}$$

$\boxed{\text{match } a_1 \text{ with } p \rightarrow b_1 = b_2}$ match and substitute

$$\frac{}{\text{match } F \text{ with } F \rightarrow b = b} \text{MATCHSUBST_CONST}$$

$$\frac{\text{match } a_1 \text{ with } a_2 \rightarrow b_1 = b_2}{\text{match } (a_1 \ a^{R'}) \text{ with } (a_2 \ x^+) \rightarrow b_1 = (b_2\{a/x\})} \text{MATCHSUBST_APPRELR}$$

$$\frac{\text{match } a_1 \text{ with } a_2 \rightarrow b_1 = b_2}{\text{match } (a_1 \ a^+) \text{ with } (a_2 \ x^+) \rightarrow b_1 = (b_2\{a/x\})} \text{MATCHSUBST_APPREL}$$

$$\frac{\text{match } a_1 \text{ with } a_2 \rightarrow b_1 = b_2}{\text{match } (a_1 \square^-) \text{ with } (a_2 \square^-) \rightarrow b_1 = b_2} \quad \text{MATCHSUBST_APP_IRREL}$$

$$\frac{\text{match } a_1 \text{ with } a_2 \rightarrow b_1 = b_2}{\text{match } (a_1[\bullet]) \text{ with } (a_2[\bullet]) \rightarrow b_1 = b_2} \quad \text{MATCHSUBST_CAPP}$$

$\boxed{\text{apply args } a \text{ to } b \mapsto b'}$ apply arguments of a (headed by a constant) to b

$$\frac{}{\text{apply args } F \text{ to } b \mapsto b} \quad \text{APPLYARGS_CONST}$$

$$\frac{\text{apply args } a \text{ to } b \mapsto b'}{\text{apply args } a \ a'^{\nu} \text{ to } b \mapsto b' \ a'^{(app.rhov)}} \quad \text{APPLYARGS_APP}$$

$$\frac{\text{apply args } a \text{ to } b \mapsto b'}{\text{apply args } a[\gamma] \text{ to } b \mapsto b'[\gamma]} \quad \text{APPLYARGS_CAPP}$$

$\boxed{\text{Value}_R \ A}$ values

$$\frac{}{\text{Value}_R \ \star} \quad \text{VALUE_STAR}$$

$$\frac{}{\text{Value}_R \ \Pi^{\rho} x : A \rightarrow B} \quad \text{VALUE_PI}$$

$$\frac{}{\text{Value}_R \ \forall c : \phi. B} \quad \text{VALUE_CPI}$$

$$\frac{}{\text{Value}_R \ \lambda^+ x : A. a} \quad \text{VALUE_ABSREL}$$

$$\frac{}{\text{Value}_R \ \lambda^+ x. a} \quad \text{VALUE_UABSREL}$$

$$\frac{\text{Value}_R \ a}{\text{Value}_R \ \lambda^- x. a} \quad \text{VALUE_UABSIRREL}$$

$$\frac{}{\text{Value}_R \ \Lambda c : \phi. a} \quad \text{VALUE_CABS}$$

$$\frac{}{\text{Value}_R \ \Lambda c. a} \quad \text{VALUE_UCABS}$$

$$\frac{\text{Path}_R \ a = F @ R s}{\text{Value}_R \ a} \quad \text{VALUE_ROLEPATH}$$

$$\frac{\neg(\text{Path}_R \ a = F @ R s) \quad \text{Path} \ a = F @ R', R s'}{\text{Value}_R \ a} \quad \text{VALUE_PATH}$$

$\boxed{\text{ValueType}_R \ A}$ Types with head forms (erased language)

$$\frac{}{\text{ValueType}_R \ \star} \quad \text{VALUE_TYPE_STAR}$$

$$\frac{}{\text{ValueType}_R \ \Pi^{\rho} x : A \rightarrow B} \quad \text{VALUE_TYPE_PI}$$

$$\frac{}{\text{ValueType}_R \ \forall c : \phi. B} \quad \text{VALUE_TYPE_CPI}$$

$$\frac{\text{Path}_R \ a = F @ R s}{\text{ValueType}_R \ a} \quad \text{VALUE_TYPE_ROLEDPATH}$$

$$\frac{\neg(\text{Path}_R \ a = F @ R s) \quad \text{Path} \ a = F @ R', R s'}{\text{ValueType}_R \ a} \quad \text{VALUE_TYPE_PATH}$$

$\boxed{\text{consistent}_R a b}$ (erased) types do not differ in their heads

$$\begin{array}{c}
\frac{}{\text{consistent}_R \star \star} \text{CONSISTENT_A_STAR} \\
\frac{}{\text{consistent}_{R'} (\Pi^\rho x_1 : A_1 \rightarrow B_1) (\Pi^\rho x_2 : A_2 \rightarrow B_2)} \text{CONSISTENT_A_PI} \\
\frac{}{\text{consistent}_R (\forall c_1 : \phi_1. A_1) (\forall c_2 : \phi_2. A_2)} \text{CONSISTENT_A_CPI} \\
\frac{\text{Path}_R a_1 = F @ R s \quad \text{Path}_R a_2 = F @ R s}{\text{consistent}_R a_1 a_2} \text{CONSISTENT_A_ROLEDPATH} \\
\frac{\neg \text{ValueType}_R b}{\text{consistent}_R a b} \text{CONSISTENT_A_STEP_R} \\
\frac{\neg \text{ValueType}_R a}{\text{consistent}_R a b} \text{CONSISTENT_A_STEP_L}
\end{array}$$

$\boxed{\Omega \models a : R}$ Roleing judgment

$$\begin{array}{c}
\frac{\text{uniq}(\Omega)}{\Omega \models \square : R} \text{ROLE_A_BULLET} \\
\frac{\text{uniq}(\Omega)}{\Omega \models \star : R} \text{ROLE_A_STAR} \\
\frac{\text{uniq}(\Omega) \quad x : R \in \Omega \quad R \leq R_1}{\Omega \models x : R_1} \text{ROLE_A_VAR} \\
\frac{\Omega, x : \mathbf{Nom} \models a : R}{\Omega \models (\lambda^\rho x. a) : R} \text{ROLE_A_ABS} \\
\frac{\Omega \models a : R \quad \Omega \models b : \mathbf{Nom}}{\Omega \models (a \ b^+) : R} \text{ROLE_A_APP} \\
\frac{\Omega \models a : R}{\Omega \models a \ \square^- : R} \text{ROLE_A_IAPP} \\
\frac{\Omega \models a : R \quad \text{Path } a = F @ R_1, R s \quad \Omega \models b : R_1}{\Omega \models a \ b^{R_1} : R} \text{ROLE_A_TAPP} \\
\frac{\Omega \models A : R \quad \Omega, x : \mathbf{Nom} \models B : R}{\Omega \models (\Pi^\rho x : A \rightarrow B) : R} \text{ROLE_A_PI} \\
\frac{\Omega \models a : R_1 \quad \Omega \models b : R_1 \quad \Omega \models A : R_0 \quad \Omega \models B : R}{\Omega \models (\forall c : a \sim_{A/R_1} b. B) : R} \text{ROLE_A_CPI} \\
\frac{\Omega \models b : R}{\Omega \models (\Lambda c. b) : R} \text{ROLE_A_CAbs}
\end{array}$$

$$\begin{array}{c}
\frac{\Omega \models a : R}{\Omega \models (a[\bullet]) : R} \quad \text{ROLE_A_CAPP} \\
\\
\frac{\text{uniq}(\Omega) \quad F : A @ R s \in \Sigma_0}{\Omega \models F : R} \quad \text{ROLE_A_CONST} \\
\\
\frac{\text{uniq}(\Omega) \quad F : p \sim a : A / R @ R s \in \Sigma_0}{\Omega \models F : R_1} \quad \text{ROLE_A_FAM} \\
\\
\frac{\Omega \models a : R \quad \Omega \models b_1 : R_1 \quad \Omega \models b_2 : R_1}{\Omega \models \text{case}_R a \text{ of } F \rightarrow b_1 \parallel_- \rightarrow b_2 : R_1} \quad \text{ROLE_A_PATTERN} \\
\\
\boxed{(\rho = +) \vee (x \notin \text{fv } A)} \quad \text{irrelevant argument check} \\
\\
\frac{}{(+ = +) \vee (x \notin \text{fv } A)} \quad \text{RHO_REL} \\
\\
\frac{x \notin \text{fv } A}{(- = +) \vee (x \notin \text{fv } A)} \quad \text{RHO_IRRREL} \\
\\
\boxed{\Omega \models a \Rightarrow_R b} \quad \text{parallel reduction (implicit language)} \\
\\
\frac{\Omega \models a : R}{\Omega \models a \Rightarrow_R a} \quad \text{PAR_REFL} \\
\\
\frac{\Omega \models a \Rightarrow_R (\lambda^\rho x. a') \quad \Omega \models b \Rightarrow_{\text{app_role}\nu} b'}{\Omega \models a \ b^\nu \Rightarrow_R a' \{b'/x\}} \quad \text{PAR_BETA} \\
\\
\frac{\Omega \models a \Rightarrow_R a' \quad \Omega \models b \Rightarrow_{\text{app_role}\nu} b'}{\Omega \models a \ b^\nu \Rightarrow_R a' \ b'^\nu} \quad \text{PAR_APP} \\
\\
\frac{\Omega \models a \Rightarrow_R (\Lambda c. a')}{\Omega \models a[\bullet] \Rightarrow_R a' \{\bullet/c\}} \quad \text{PAR_CBETA} \\
\\
\frac{\Omega \models a \Rightarrow_R a'}{\Omega \models a[\bullet] \Rightarrow_R a'[\bullet]} \quad \text{PAR_CAPP} \\
\\
\frac{\Omega, x : \mathbf{Nom} \models a \Rightarrow_R a'}{\Omega \models \lambda^\rho x. a \Rightarrow_R \lambda^\rho x. a'} \quad \text{PAR_ABS} \\
\\
\frac{\Omega \models A \Rightarrow_R A' \quad \Omega, x : \mathbf{Nom} \models B \Rightarrow_R B'}{\Omega \models \Pi^\rho x : A \rightarrow B \Rightarrow_R \Pi^\rho x : A' \rightarrow B'} \quad \text{PAR_PI} \\
\\
\frac{\Omega \models a \Rightarrow_R a'}{\Omega \models \Lambda c. a \Rightarrow_R \Lambda c. a'} \quad \text{PAR_CABS} \\
\\
\frac{\Omega \models A \Rightarrow_{R_0} A' \quad \Omega \models a \Rightarrow_{R_1} a' \quad \Omega \models b \Rightarrow_{R_1} b' \quad \Omega \models B \Rightarrow_R B'}{\Omega \models \forall c : a \sim_{A/R_1} b. B \Rightarrow_R \forall c : a' \sim_{A'/R_1} b'. B'} \quad \text{PAR_CPI}
\end{array}$$

$$\begin{array}{c}
F : p \sim b : A/R_1 @ Rs \in \Sigma_0 \\
\text{match } a' \text{ with } p \rightarrow b = b' \\
R_1 \leq R \\
\text{uniq}(\Omega) \\
\hline
\Omega \models a \Rightarrow_R b' \quad \text{PAR_AXIOM}
\end{array}$$

$$\begin{array}{c}
\Omega \models a \Rightarrow_R a' \\
\Omega \models b_1 \Rightarrow_{R_0} b'_1 \\
\Omega \models b_2 \Rightarrow_{R_0} b'_2 \\
\hline
\Omega \models (\text{case}_R a \text{ of } F \rightarrow b_1 \parallel_- \rightarrow b_2) \Rightarrow_{R_0} (\text{case}_R a' \text{ of } F \rightarrow b'_1 \parallel_- \rightarrow b'_2) \quad \text{PAR_PATTERN}
\end{array}$$

$$\begin{array}{c}
\Omega \models a \Rightarrow_R a' \\
\Omega \models b_1 \Rightarrow_{R_0} b'_1 \\
\text{Path}_R a' = F @ Rs \\
\text{apply args } a' \text{ to } b'_1 \mapsto b \\
\hline
\Omega \models (\text{case}_R a \text{ of } F \rightarrow b_1 \parallel_- \rightarrow b_2) \Rightarrow_{R_0} b[\bullet] \quad \text{PAR_PATTERNTRUE}
\end{array}$$

$$\begin{array}{c}
\Omega \models a \Rightarrow_R a' \\
\Omega \models b_2 \Rightarrow_{R_0} b'_2 \\
\text{Value}_R a' \\
\neg(\text{Path}_R a' = F @ Rs) \\
\hline
\Omega \models (\text{case}_R a \text{ of } F \rightarrow b_1 \parallel_- \rightarrow b_2) \Rightarrow_{R_0} b'_2 \quad \text{PAR_PATTERNFALSE}
\end{array}$$

$$\boxed{\Omega \models a \Rightarrow_R^* b} \quad \text{multistep parallel reduction}$$

$$\frac{}{\Omega \models a \Rightarrow_R^* a} \quad \text{MP_REFL}$$

$$\frac{\Omega \models a \Rightarrow_R b \quad \Omega \models b \Rightarrow_R^* a'}{\Omega \models a \Rightarrow_R^* a'} \quad \text{MP_STEP}$$

$$\boxed{\Omega \models a \Leftrightarrow_R b} \quad \text{parallel reduction to a common term}$$

$$\frac{\Omega \models a_1 \Rightarrow_R^* b \quad \Omega \models a_2 \Rightarrow_R^* b}{\Omega \models a_1 \Leftrightarrow_R a_2} \quad \text{JOIN}$$

$$\boxed{\models a > b/R} \quad \text{primitive reductions on erased terms}$$

$$\frac{\text{Value}_{R_1} (\lambda^\rho x.v)}{\models (\lambda^\rho x.v) \ b^\nu > v\{b/x\}/R_1} \quad \text{BETA_APPABS}$$

$$\frac{}{\models (\Lambda c.a')[\bullet] > a'\{\bullet/c\}/R} \quad \text{BETA_CAPPCABS}$$

$$\begin{array}{c}
F : p \sim b : A/R_1 @ Rs \in \Sigma_0 \\
\text{match } a \text{ with } p \rightarrow b = b' \\
R_1 \leq R \\
\hline
\models a > b'/R \quad \text{BETA_AXIOM}
\end{array}$$

$$\begin{array}{c}
\text{Path}_R a = F @ Rs \\
\text{apply args } a \text{ to } b_1 \mapsto b'_1 \\
\hline
\models \text{case}_R a \text{ of } F \rightarrow b_1 \parallel_- \rightarrow b_2 > b'_1[\bullet]/R_0 \quad \text{BETA_PATTERNTRUE}
\end{array}$$

$$\begin{array}{c}
\text{Value}_R a \\
\neg(\text{Path}_R a = F @ Rs) \\
\hline
\models \text{case}_R a \text{ of } F \rightarrow b_1 \parallel_- \rightarrow b_2 > b_2/R_0 \quad \text{BETA_PATTERNFALSE}
\end{array}$$

$\boxed{\models a \rightsquigarrow b/R}$ single-step head reduction for implicit language

$$\begin{array}{c}
\frac{\models a \rightsquigarrow a'/R_1}{\models \lambda^-x.a \rightsquigarrow \lambda^-x.a'/R_1} \quad \text{E_ABSTERM} \\
\frac{\models a \rightsquigarrow a'/R_1}{\models a \ b^\nu \rightsquigarrow a' \ b^\nu/R_1} \quad \text{E_APPLEFT} \\
\frac{\models a \rightsquigarrow a'/R}{\models a[\bullet] \rightsquigarrow a'[\bullet]/R} \quad \text{E_CAPPLEFT} \\
\frac{\models a \rightsquigarrow a'/R}{\models \text{case}_R a \text{ of } F \rightarrow b_1 \parallel_- \rightarrow b_2 \rightsquigarrow \text{case}_R a' \text{ of } F \rightarrow b_1 \parallel_- \rightarrow b_2/R_0} \quad \text{E_PATTERN} \\
\frac{\models a > b/R}{\models a \rightsquigarrow b/R} \quad \text{E_PRIM}
\end{array}$$

$\boxed{\models a \rightsquigarrow^* b/R}$ multistep reduction

$$\begin{array}{c}
\overline{\models a \rightsquigarrow^* a/R} \quad \text{EQUAL} \\
\frac{\models a \rightsquigarrow b/R \quad \models b \rightsquigarrow^* a'/R}{\models a \rightsquigarrow^* a'/R} \quad \text{STEP}
\end{array}$$

$\boxed{\Gamma \models \text{case}_R a : A \text{ of } b : B \Rightarrow C \mid C'}$ Branch Typing (aligning the types of case)

$$\begin{array}{c}
\frac{\text{uniq } \Gamma}{\Gamma \models \text{case}_R a : A \text{ of } b : A \Rightarrow \forall c : (a \sim_{A/R} b). C \mid C'} \quad \text{BRANCH_TYPING_BASE} \\
\frac{\Gamma, x : A \models \text{case}_R a : A_1 \text{ of } b \ x^+ : B \Rightarrow C \mid C'}{\Gamma \models \text{case}_R a : A_1 \text{ of } b : \Pi^+ x : A \rightarrow B \Rightarrow \Pi^+ x : A \rightarrow C \mid C'} \quad \text{BRANCH_TYPING_PIREL} \\
\frac{\Gamma, x : A \models \text{case}_R a : A_1 \text{ of } b \ \square^- : B \Rightarrow C \mid C'}{\Gamma \models \text{case}_R a : A_1 \text{ of } b : \Pi^- x : A \rightarrow B \Rightarrow \Pi^- x : A \rightarrow C \mid C'} \quad \text{BRANCH_TYPING_PIIRREL} \\
\frac{\Gamma, c : \phi \models \text{case}_R a : A \text{ of } b[\bullet] : B \Rightarrow C \mid C'}{\Gamma \models \text{case}_R a : A \text{ of } b : \forall c : \phi. B \Rightarrow \forall c : \phi. C \mid C'} \quad \text{BRANCH_TYPING_CPI}
\end{array}$$

$\boxed{\Gamma \text{ CtxType } p : A = B}$ Fold Context to Type

$$\begin{array}{c}
\overline{\emptyset \text{ CtxType } F : A = A} \quad \text{FOLDCTXTYPE_BASE} \\
\frac{\Gamma \text{ CtxType } p : A = B}{\Gamma, x : A_1 \text{ CtxType } p \ x^+ : A = \Pi^+ x : A_1 \rightarrow B} \quad \text{FOLDCTXTYPE_PIREL} \\
\frac{\Gamma \text{ CtxType } p : A = B}{\Gamma, x : A_1 \text{ CtxType } p \ \square^- : A = \Pi^- x : A_1 \rightarrow B} \quad \text{FOLDCTXTYPE_PIIRREL} \\
\frac{\Gamma \text{ CtxType } p : A = B}{\Gamma, c : \phi \text{ CtxType } p[\bullet] : A = \forall c : \phi. B} \quad \text{FOLDCTXTYPE_CPI}
\end{array}$$

$\boxed{\Gamma \models \phi \text{ ok}}$ Prop wellformedness

$$\frac{\Gamma \models a : A \quad \Gamma \models b : A \quad \Gamma \models A : \star}{\Gamma \models a \sim_{A/R} b \text{ ok}} \quad \text{E_WFF}$$

$\boxed{\Gamma \models a : A}$ typing

$$\begin{array}{c}
\frac{\vdash \Gamma}{\Gamma \models \star : \star} \quad \text{E_STAR} \\
\\
\frac{\vdash \Gamma \quad x : A \in \Gamma}{\Gamma \models x : A} \quad \text{E_VAR} \\
\\
\frac{\Gamma, x : A \models B : \star \quad \Gamma \models A : \star}{\Gamma \models \Pi^\rho x : A \rightarrow B : \star} \quad \text{E_PI} \\
\\
\frac{\Gamma, x : A \models a : B \quad \Gamma \models A : \star \quad (\rho = +) \vee (x \notin \text{fv } a)}{\Gamma \models \lambda^\rho x. a : (\Pi^\rho x : A \rightarrow B)} \quad \text{E_ABS} \\
\\
\frac{\Gamma \models b : \Pi^+ x : A \rightarrow B \quad \Gamma \models a : A}{\Gamma \models b \ a^+ : B\{a/x\}} \quad \text{E_APP} \\
\\
\frac{\Gamma \models b : \Pi^+ x : A \rightarrow B \quad \Gamma \models a : A}{\Gamma \models b \ a^R : B\{a/x\}} \quad \text{E_TAPP} \\
\\
\frac{\Gamma \models b : \Pi^- x : A \rightarrow B \quad \Gamma \models a : A}{\Gamma \models b \ \Box^- : B\{a/x\}} \quad \text{E_IAPP} \\
\\
\frac{\Gamma \models a : A \quad \Gamma; \tilde{\Gamma} \models A \equiv B : \star / \mathbf{Rep} \quad \Gamma \models B : \star}{\Gamma \models a : B} \quad \text{E_CONV} \\
\\
\frac{\Gamma, c : \phi \models B : \star \quad \Gamma \models \phi \text{ ok}}{\Gamma \models \forall c : \phi. B : \star} \quad \text{E_CPI} \\
\\
\frac{\Gamma, c : \phi \models a : B \quad \Gamma \models \phi \text{ ok}}{\Gamma \models \Lambda c. a : \forall c : \phi. B} \quad \text{E_CABS} \\
\\
\frac{\Gamma \models a_1 : \forall c : (a \sim_{A/R} b). B_1 \quad \Gamma; \tilde{\Gamma} \models a \equiv b : A/R}{\Gamma \models a_1[\bullet] : B_1\{\bullet/c\}} \quad \text{E_CAPP} \\
\\
\frac{\vdash \Gamma \quad F : A @ Rs \in \Sigma_0 \quad \emptyset \models A : \star}{\Gamma \models F : A} \quad \text{E_CONST} \\
\\
\frac{\vdash \Gamma \quad F : p \sim a : A/R_1 @ Rs \in \Sigma_0 \quad \emptyset \models A : \star \quad \Omega; \Gamma' \models p : A \quad \Gamma' \text{CtxType } p : A = A'}{\Gamma \models F : A'} \quad \text{E_FAM}
\end{array}$$

$$\begin{array}{c}
\Gamma \models a : A \\
\Gamma \models F : A_1 \\
\Gamma \models b_1 : B \\
\Gamma \models b_2 : C \\
\Gamma \models \text{case}_R a : A \text{ of } F : A_1 \Rightarrow B \mid C \\
\hline
\Gamma \models \text{case}_R a \text{ of } F \rightarrow b_1 \parallel - \rightarrow b_2 : C
\end{array} \quad \text{E_CASE}$$

$$\boxed{\Gamma; \Delta \models \phi_1 \equiv \phi_2} \quad \text{prop equality}$$

$$\begin{array}{c}
\Gamma; \Delta \models A_1 \equiv A_2 : A/R \\
\Gamma; \Delta \models B_1 \equiv B_2 : A/R \\
\hline
\Gamma; \Delta \models A_1 \sim_{A/R} B_1 \equiv A_2 \sim_{A/R} B_2
\end{array} \quad \text{E_PROP_CONG}$$

$$\begin{array}{c}
\Gamma; \Delta \models A \equiv B : \star/R_0 \\
\Gamma \models A_1 \sim_{A/R} A_2 \text{ ok} \\
\Gamma \models A_1 \sim_{B/R} A_2 \text{ ok} \\
\hline
\Gamma; \Delta \models A_1 \sim_{A/R} A_2 \equiv A_1 \sim_{B/R} A_2
\end{array} \quad \text{E_ISO_CONV}$$

$$\begin{array}{c}
\Gamma; \Delta \models \forall c : (a_1 \sim_{A/R_1} a_2). B_1 \equiv \forall c : (b_1 \sim_{B/R_2} b_2). B_2 : \star/R' \\
\hline
\Gamma; \Delta \models a_1 \sim_{A/R_1} a_2 \equiv b_1 \sim_{B/R_2} b_2
\end{array} \quad \text{E_CPI_FST}$$

$$\boxed{\Gamma; \Delta \models a \equiv b : A/R} \quad \text{definitional equality}$$

$$\begin{array}{c}
\vdash \Gamma \\
c : (a \sim_{A/R} b) \in \Gamma \\
c \in \Delta \\
\hline
\Gamma; \Delta \models a \equiv b : A/R
\end{array} \quad \text{E_ASSN}$$

$$\begin{array}{c}
\Gamma \models a : A \\
\hline
\Gamma; \Delta \models a \equiv a : A/\mathbf{Nom}
\end{array} \quad \text{E_REFL}$$

$$\begin{array}{c}
\Gamma; \Delta \models b \equiv a : A/R \\
\hline
\Gamma; \Delta \models a \equiv b : A/R
\end{array} \quad \text{E_SYM}$$

$$\begin{array}{c}
\Gamma; \Delta \models a \equiv a_1 : A/R \\
\Gamma; \Delta \models a_1 \equiv b : A/R \\
\hline
\Gamma; \Delta \models a \equiv b : A/R
\end{array} \quad \text{E_TRANS}$$

$$\begin{array}{c}
\Gamma; \Delta \models a \equiv b : A/R_1 \\
R_1 \leq R_2 \\
\hline
\Gamma; \Delta \models a \equiv b : A/R_2
\end{array} \quad \text{E_SUB}$$

$$\begin{array}{c}
\Gamma \models a_1 : B \\
\Gamma \models a_2 : B \\
\vdash a_1 > a_2/R \\
\hline
\Gamma; \Delta \models a_1 \equiv a_2 : B/R
\end{array} \quad \text{E_BETA}$$

$$\begin{array}{c}
\Gamma; \Delta \models A_1 \equiv A_2 : \star/R' \\
\Gamma, x : A_1; \Delta \models B_1 \equiv B_2 : \star/R' \\
\Gamma \models A_1 : \star \\
\Gamma \models \Pi^\rho x : A_1 \rightarrow B_1 : \star \\
\Gamma \models \Pi^\rho x : A_2 \rightarrow B_2 : \star \\
\hline
\Gamma; \Delta \models (\Pi^\rho x : A_1 \rightarrow B_1) \equiv (\Pi^\rho x : A_2 \rightarrow B_2) : \star/R'
\end{array} \quad \text{E_PI_CONG}$$

$$\begin{array}{c}
\frac{\Gamma, x : A_1; \Delta \models b_1 \equiv b_2 : B/R' \quad \Gamma \models A_1 : \star \quad (\rho = +) \vee (x \notin \text{fv } b_1) \quad (\rho = +) \vee (x \notin \text{fv } b_2)}{\Gamma; \Delta \models (\lambda^\rho x. b_1) \equiv (\lambda^\rho x. b_2) : (\Pi^\rho x : A_1 \rightarrow B)/R'} \quad \text{E_AbsCong} \\
\\
\frac{\Gamma; \Delta \models a_1 \equiv b_1 : (\Pi^+ x : A \rightarrow B)/R' \quad \Gamma; \Delta \models a_2 \equiv b_2 : A/\mathbf{Nom}}{\Gamma; \Delta \models a_1 \ a_2^+ \equiv b_1 \ b_2^+ : (B\{a_2/x\})/R'} \quad \text{E_AppCong} \\
\\
\frac{\Gamma; \Delta \models a_1 \equiv b_1 : (\Pi^+ x : A \rightarrow B)/R' \quad \text{Path}_{R'} \ a_1 = F @ R, Rs \quad \Gamma; \Delta \models a_2 \equiv b_2 : A/\mathbf{param} \ R \ R'}{\Gamma; \Delta \models a_1 \ a_2^R \equiv b_1 \ b_2^R : (B\{a_2/x\})/R'} \quad \text{E_TAppCong} \\
\\
\frac{\Gamma; \Delta \models a_1 \equiv b_1 : (\Pi^- x : A \rightarrow B)/R' \quad \Gamma \models a : A}{\Gamma; \Delta \models a_1 \ \Box^- \equiv b_1 \ \Box^- : (B\{a/x\})/R'} \quad \text{E_IApCong} \\
\\
\frac{\Gamma; \Delta \models \Pi^\rho x : A_1 \rightarrow B_1 \equiv \Pi^\rho x : A_2 \rightarrow B_2 : \star/R'}{\Gamma; \Delta \models A_1 \equiv A_2 : \star/R'} \quad \text{E_PiFst} \\
\\
\frac{\Gamma; \Delta \models \Pi^\rho x : A_1 \rightarrow B_1 \equiv \Pi^\rho x : A_2 \rightarrow B_2 : \star/R' \quad \Gamma; \Delta \models a_1 \equiv a_2 : A_1/R'}{\Gamma; \Delta \models B_1\{a_1/x\} \equiv B_2\{a_2/x\} : \star/R'} \quad \text{E_PiSnd} \\
\\
\frac{\Gamma; \Delta \models a_1 \sim_{A_1/R} b_1 \equiv a_2 \sim_{A_2/R} b_2 \quad \Gamma, c : a_1 \sim_{A_1/R} b_1; \Delta \models A \equiv B : \star/R' \quad \Gamma \models a_1 \sim_{A_1/R} b_1 \ \text{ok} \quad \Gamma \models \forall c : a_1 \sim_{A_1/R} b_1. A : \star \quad \Gamma \models \forall c : a_2 \sim_{A_2/R} b_2. B : \star}{\Gamma; \Delta \models \forall c : a_1 \sim_{A_1/R} b_1. A \equiv \forall c : a_2 \sim_{A_2/R} b_2. B : \star/R'} \quad \text{E_CPiCong} \\
\\
\frac{\Gamma, c : \phi_1; \Delta \models a \equiv b : B/R \quad \Gamma \models \phi_1 \ \text{ok}}{\Gamma; \Delta \models (\Lambda c. a) \equiv (\Lambda c. b) : \forall c : \phi_1. B/R} \quad \text{E_CAbsCong} \\
\\
\frac{\Gamma; \Delta \models a_1 \equiv b_1 : (\forall c : (a \sim_{A/R} b). B)/R' \quad \Gamma; \tilde{\Gamma} \models a \equiv b : A/\mathbf{param} \ R \ R'}{\Gamma; \Delta \models a_1[\bullet] \equiv b_1[\bullet] : (B\{\bullet/c\})/R'} \quad \text{E_CApCong} \\
\\
\frac{\Gamma; \Delta \models \forall c : (a_1 \sim_{A/R} a_2). B_1 \equiv \forall c : (a'_1 \sim_{A'/R'} a'_2). B_2 : \star/R_0 \quad \Gamma; \tilde{\Gamma} \models a_1 \equiv a_2 : A/\mathbf{param} \ R \ R_0 \quad \Gamma; \tilde{\Gamma} \models a'_1 \equiv a'_2 : A'/\mathbf{param} \ R' \ R_0}{\Gamma; \Delta \models B_1\{\bullet/c\} \equiv B_2\{\bullet/c\} : \star/R_0} \quad \text{E_CPiSnd} \\
\\
\frac{\Gamma; \Delta \models a \equiv b : A/R \quad \Gamma; \Delta \models a \sim_{A/R} b \equiv a' \sim_{A'/R'} b'}{\Gamma; \Delta \models a' \equiv b' : A'/R'} \quad \text{E_Cast} \\
\\
\frac{\Gamma; \Delta \models a \equiv b : A/R \quad \Gamma; \tilde{\Gamma} \models A \equiv B : \star/\mathbf{Rep} \quad \Gamma \models B : \star}{\Gamma; \Delta \models a \equiv b : B/R} \quad \text{E_EqConv}
\end{array}$$

$$\begin{array}{c}
\frac{\Gamma; \Delta \models a \sim_{A/R_1} b \equiv a' \sim_{A'/R_1} b'}{\Gamma; \Delta \models A \equiv A' : \star / \mathbf{Rep}} \quad \text{E_ISO_SND} \\
\\
\frac{\begin{array}{c} \Gamma; \Delta \models a \equiv a' : A/R \\ \Gamma; \Delta \models b_1 \equiv b'_1 : B/R_0 \\ \Gamma; \Delta \models b_2 \equiv b'_2 : B/R_0 \end{array}}{\Gamma; \Delta \models \text{case}_R a \text{ of } F \rightarrow b_1 \parallel - \rightarrow b_2 \equiv \text{case}_R a' \text{ of } F \rightarrow b'_1 \parallel - \rightarrow b'_2 : B/R_0} \quad \text{E_PAT_CONG} \\
\\
\frac{\begin{array}{c} \text{Path}_{R'} a = F @ R, Rs \\ \text{Path}_{R'} a' = F @ R, Rs \\ \Gamma \models a : \Pi^+ x : A \rightarrow B \\ \Gamma \models b : A \\ \Gamma \models a' : \Pi^+ x : A \rightarrow B \\ \Gamma \models b' : A \\ \Gamma; \Delta \models a \ b^{R_1} \equiv a' \ b'^{R_1} : B\{b/x\}/R' \\ \Gamma; \tilde{\Gamma} \models B\{b/x\} \equiv B\{b'/x\} : \star / R' \end{array}}{\Gamma; \Delta \models a \equiv a' : \Pi^+ x : A \rightarrow B/R'} \quad \text{E_LEFT_REL} \\
\\
\frac{\begin{array}{c} \text{Path}_{R'} a = F @ R, Rs \\ \text{Path}_{R'} a' = F @ R, Rs \\ \Gamma \models a : \Pi^- x : A \rightarrow B \\ \Gamma \models b : A \\ \Gamma \models a' : \Pi^- x : A \rightarrow B \\ \Gamma \models b' : A \\ \Gamma; \Delta \models a \ \square^- \equiv a' \ \square^- : B\{b/x\}/R' \\ \Gamma; \tilde{\Gamma} \models B\{b/x\} \equiv B\{b'/x\} : \star / R_0 \end{array}}{\Gamma; \Delta \models a \equiv a' : \Pi^- x : A \rightarrow B/R'} \quad \text{E_LEFT_IRREL} \\
\\
\frac{\begin{array}{c} \text{Path}_{R'} a = F @ R, Rs \\ \text{Path}_{R'} a' = F @ R, Rs \\ \Gamma \models a : \Pi^+ x : A \rightarrow B \\ \Gamma \models b : A \\ \Gamma \models a' : \Pi^+ x : A \rightarrow B \\ \Gamma \models b' : A \\ \Gamma; \Delta \models a \ b^+ \equiv a' \ b'^+ : B\{b/x\}/R' \\ \Gamma; \tilde{\Gamma} \models B\{b/x\} \equiv B\{b'/x\} : \star / R_0 \end{array}}{\Gamma; \Delta \models b \equiv b' : A / \mathbf{param} \ R_1 \ R'} \quad \text{E_RIGHT} \\
\\
\frac{\begin{array}{c} \text{Path}_{R'} a = F @ R, Rs \\ \text{Path}_{R'} a' = F @ R, Rs \\ \Gamma \models a : \forall c : (a_1 \sim_{A/R_1} a_2). B \\ \Gamma \models a' : \forall c : (a_1 \sim_{A/R_1} a_2). B \\ \Gamma; \tilde{\Gamma} \models a_1 \equiv a_2 : A/R' \\ \Gamma; \Delta \models a[\bullet] \equiv a'[\bullet] : B\{\bullet/c\}/R' \end{array}}{\Gamma; \Delta \models a \equiv a' : \forall c : (a_1 \sim_{A/R_1} a_2). B/R'} \quad \text{E_CLEFT}
\end{array}$$

$\boxed{\models \Gamma}$ context wellformedness

$$\begin{array}{c}
\frac{}{\models \emptyset} \quad \text{E_EMPTY} \\
\\
\frac{\begin{array}{c} \models \Gamma \\ \Gamma \models A : \star \\ x \notin \text{dom } \Gamma \end{array}}{\models \Gamma, x : A} \quad \text{E_CONSTM}
\end{array}$$

$$\frac{\begin{array}{l} \models \Gamma \\ \Gamma \models \phi \text{ ok} \\ c \notin \text{dom } \Gamma \end{array}}{\models \Gamma, c : \phi} \quad \text{E_CONSCo}$$

$\boxed{\models \Sigma}$ signature wellformedness

$$\frac{}{\models \emptyset} \quad \text{SIG_EMPTY}$$

$$\frac{\begin{array}{l} \models \Sigma \\ \emptyset \models A : \star \\ F \notin \text{dom } \Sigma \end{array}}{\models \Sigma \cup \{FA@Rs\}} \quad \text{SIG_CONSCONST}$$

$$\frac{\begin{array}{l} \models \Sigma \\ F \notin \text{dom } \Sigma \\ \Omega; \Gamma \models p : A \\ \Gamma \models a : A \\ \Omega \models a : \mathbf{Rep} \end{array}}{\models \Sigma \cup \{F p \sim a : A / R@range(W)\}} \quad \text{SIG_CONSAx}$$

Definition rules: 146 good 0 bad
 Definition rule clauses: 405 good 0 bad