

## RESEARCH NOTES AND COMMENTARIES

### THE USE OF LIMITED DEPENDENT VARIABLE TECHNIQUES IN STRATEGY RESEARCH: ISSUES AND METHODS

MARGARETHE F. WIERSEMA,<sup>1\*</sup> and HARRY P. BOWEN<sup>2</sup>

<sup>1</sup> *The Paul Merage School of Business, University of California, Irvine, California, U.S.A.*

<sup>2</sup> *McColl School of Business, Queens University of Charlotte, Charlotte, North Carolina, U.S.A.*

*Strategy researchers are increasingly turning their attention from examining the impact of strategic choices on firm performance to examining the factors that determine strategic choices at the firm level. This shift of research orientation has meant that researchers are increasingly faced with a limited dependent variable (LDV) that takes a limited number of usually discrete values, for which LDV methods such as logit or probit are required. Despite their growing popularity, there appears to be widespread problems in the use of LDV methods. This research note complements recent studies that offer general guidelines by presenting and illustrating the practical steps needed to implement the methods essential for analyzing and interpreting the results from LDV models.* Copyright © 2009 John Wiley & Sons, Ltd.

## INTRODUCTION

The statistical techniques used in strategic management research are becoming more sophisticated and more complex. While ordinary least squares (OLS) regression remains predominant,<sup>1</sup> an expanded array of statistical techniques is allowing researchers to explore new hypotheses as well as reevaluate past empirical studies that

have yielded contradictory or confounding results regarding key strategy research issues. Since many of the newer techniques involve less familiar methods of estimation, analysis, and interpretation, strategy researchers are being required to become increasingly sophisticated in terms of the breadth and depth of their understanding of alternative statistical methods (Shook *et al.*, 2003; Shook *et al.*, 2004). However, recent assessments of the use in strategy research of some of the newer analytical techniques have found major shortcomings in terms of implementation and interpretation of results. In response, general guidelines have been offered regarding key issues and problem areas in an effort to improve current practice in the use of newer and less familiar techniques (e.g., Bowen

---

Keywords: empirical methods; limited dependent variable; strategy research

\*Correspondence to: Margarethe F. Wiersema, The Paul Merage School of Business, University of California, Irvine, CA 92697-3125, U.S.A. E-mail: [mfwierse@uci.edu](mailto:mfwierse@uci.edu)

<sup>1</sup> Scandura and Williams (2000) report that 42 percent of recently published management articles used OLS.

and Wiersema, 2004; Hoetker, 2007; Shook *et al.*, 2004).<sup>2</sup>

In addition to studies that seek to improve current practice regarding specific techniques, another growing body of work addresses key methodological issues. These include the use of cross-sectional data (Bergh, 1995; Bowen and Wiersema, 1999), the issue of endogeneity (Hamilton and Nickerson, 2003), and the validity of measures (Chatterjee and Bloucher, 1992; Davis and Duhaime, 1992; Hoskisson *et al.*, 1993; Lubatkin, *et al.*, 1993; Robins and Wiersema, 2003). These studies all highlight systematic problems with prior empirical strategy research that may have led to biased results and invalid inferences and therefore uncertainty regarding the meaning of prior research findings. Growing recognition of a number of methodological failings means that, despite a multitude of empirical studies, the findings regarding many key theoretical linkages remain equivocal.

This study contributes to these streams of methodological inquiry by examining a set of statistical issues likely to occur in the analysis of firm-level data, the most common level of analysis in strategy research. In this regard, researchers often model strategic choices, such as acquisitions, market exit, and joint ventures, as a limited dependent variable (LDV); for example, as a binomial (yes/no) decision. Since OLS is an inappropriate estimation method in such cases, researchers have turned to LDV methods such as logit to estimate their models. However, many researchers may be less familiar with such specialized techniques and may feel uneasy about the appropriate methods for analyzing and interpreting the results from them.

Despite the growing use of LDV methods in strategy research (Shook *et al.*, 2003), only recently has attention been given to assessing whether LDV methods are being appropriately and consistently used in strategy research. Recent inquiries (e.g., Bowen and Wiersema, 2004; Hoetker, 2007) have indeed found widespread problems, and in response have offered general guidelines regarding key issues and problem areas. While general guidelines are imminently useful, they may be too broad to be fully understood and hence adopted by researchers who lack practical knowledge of LDV models. Given the growing

use of LDV models in strategy research and evidence of widespread problems regarding the analysis and interpretation of such models, it seems warranted to augment general guidelines with a more pragmatic approach.

Toward this goal, this study first considers the research design issue of when an LDV model is appropriate. It then presents and illustrates the essential methods for analyzing and interpreting the results from any LDV model via simple examples that use the binary logit model—the most common LDV model used in the strategy literature. The specific STATA commands used to conduct the analyses that we illustrate are presented in the Appendix. In taking a pragmatic approach, this study complements and contributes to the growing stream of articles in the strategy literature that highlight general methodological and statistical issues and, more specifically, recent studies that have raised awareness of key problems and offered general guidelines to foster the correct use of LDV methods.

## RESEARCH DESIGN

A study's research design refers to the systematic plan to be undertaken to arrive at an answer to a particular research question. This includes formulating the research question, operationalizing theoretical constructs, identifying and collecting data, selection of statistical method, analysis, interpretation, and reporting of results. An important part of a research design is the choice and operationalization of a model's dependent variable, which in general will depend on the phenomenon of interest and the unit of analysis. Historically, empirical strategy research has predominantly focused on organizational outcomes such as firm performance that could be operationalized by a continuous variable (e.g., return on assets) which permitted the use of OLS. However, strategy researchers are increasingly examining phenomena characterized by a discrete set of choices or organizational outcomes that cannot be operationalized by a continuous dependent variable. Examples include international expansion operationalized as either start-up or acquisition (Vermeulen and Barkema, 2002); strategic alliances categorized into various organizational forms (Colombo, 2003); the existence or absence of certain conditions, such as managerial turnover (Bloom and Michel, 2002; Shen and

<sup>2</sup> Bergh and Ketchen (2004), as well as articles in this journal, have addressed a host of specific research design and methodological issues.

Cannella, 2002); the existence of a COO position (Hambrick and Canella, 2004); CEO/Chair duality (Nelson, 2003); and whether or not a new CEO differs from his/her predecessor (Zajac and Westphal, 1996). As researchers increasingly examine phenomena that cannot be operationalized by a continuous variable, they have come to rely on LDV methods to model the relationship of interest. But while the use of LDV models is growing, there has been scant discussion of whether and when such models are appropriate.

The choice of measure (and therefore model) should be dictated first and foremost by the research question of interest. For example, if one's interest is to understand whether a firm's research and development (R&D) activity influences its decision to expand abroad, then a discrete variable indicating whether or not the firm is international is appropriate. If one's interest is instead to understand how a firm's R&D activity impacts the geographic diversity of its activities, then the phenomenon of interest is instead the extent of a firm's international operations, and a continuous measure of a firm's foreign activities is appropriate. Utilizing a discrete measure, such as a count of the number of countries in which a firm operates, will fail to capture the extent of a firm's foreign presence; a firm with sales offices in multiple countries would appear highly internationally diversified, but in reality may have minimal foreign presence. In this example, the country count measure not only fails to capture the full range of variation of the phenomenon of interest, it also fails to adequately reflect the real meaning of the construct under consideration, that is, it lacks content validity. One should not impose a discrete categorization on a strategic phenomenon if it fails to represent the actual set of managerial choices or organizational outcomes, since information on the full range of variation in the dependent measure is then ignored. Generally, a continuous measure is appropriate if the phenomenon is the extent of something; a discrete measure is appropriate if the phenomenon is instead a set of discrete choices or outcomes. Recent studies note that strategy researchers rarely articulate a rationale for their choice of measures, and that measures are often adopted without systematic consideration of their content validity (Acar and Sankaran, 1999; Robins and Wiersema, 2003). The result is a research design that fails to fully explain the research question of interest.

## ANALYZING AND INTERPRETING LDV MODELS

If the phenomenon of interest is best operationalized by a discrete measure, then the use of an LDV model becomes appropriate.<sup>3</sup> Recent reviews (Bowen and Wiersema, 2004; Hoetker, 2007) of the use of LDV models in the strategy literature indicate considerable variation in the accuracy with which the results from LDV models are analyzed and interpreted. To a large extent, this variation arises because many researchers are not aware that supplementary analysis is required to correctly analyze the results from an LDV model. This need for additional effort—and often a lack of understanding of the special characteristics of LDV models—undermines the ability of many researchers to interpret their findings and to therefore make a research contribution.

Hoetker (2007) recently echoed such concerns, and in response offered general guidelines regarding the analysis and interpretation of the most commonly used LDV models in strategy research. Although general guidelines are imminently useful, for many researchers they may be too broad to provide sufficient understanding of how to implement the recommendations. This study therefore provides a practical contribution in understanding LDV models by providing straightforward examples that illustrate the essential methods for analyzing and interpreting hypotheses.

### Why LDV models are different

To correctly analyze and interpret any LDV model, it is important to understand two fundamental differences between LDV and OLS type models. First, LDV models are *intrinsically nonlinear*, which means the relationship to be estimated cannot be written as a summation of terms, where each term is a model coefficient times a model variable.<sup>4</sup> The intrinsic nonlinearity of LDV models has two major methodological ramifications. First, an explanatory variable's *marginal effect*—the effect

<sup>3</sup> Such models include all forms of the logit (e.g., binary, multinomial, ordered) and probit models, as well as models such as the TOBIT.

<sup>4</sup> For an intrinsically linear model, a variable can be a function of itself (e.g., the square or logarithm of its value) or a function that includes other model variables (e.g., an interaction variable). Key is that the relationship to be estimated is linear in model coefficients (e.g., see Greene, 2003: 122).

of a unit change in an explanatory variable on the dependent variable—does not equal the variable's model coefficient. Second, the value of this *marginal effect* varies with the value of all model variables. These facts imply that, in an LDV model, *an explanatory variable's estimated coefficient can rarely be used to infer the true nature of the relationship between the explanatory variable and the dependent variable.*

The second fundamental difference is that most LDV models are estimated using the method of maximum likelihood, which, unlike the method of least squares, is not based on minimizing error variance. This means there is no measure of model 'fit' directly comparable to the r-square in OLS, and, as a result, model assessment is largely restricted to testing the joint significance of all model variables (as is done in OLS using an F-test of overall model significance).

These differences imply that it is potentially misleading, and often not correct, to analyze and interpret the results from LDV models using the methods commonly used for OLS type models. In particular, information presented in the output of most statistical packages regarding the sign, magnitude, and statistical significance of a variable's estimated coefficient is rarely sufficient to detect the nature of the true relationship between an explanatory variable and the dependent variable, and hence also to test a hypothesis about the nature of their relationship. Instead, for LDV models the focus of analysis is on the value and statistical significance of an explanatory variable's marginal effect, which requires analysis beyond simply estimating one's model. The following sections present examples that illustrate this additional analysis and provide recommendations for writing up results; the specific STATA commands used to conduct this analysis are presented in the Appendix.

Table 1. Results from Stata's *logit* command estimating probability of CEO dismissal  
Logistic regression

Number of obs = 199  
LR chi2(2) = 49.03  
Prob > chi2 = 0.0000  
Pseudo R2 = 0.1853

Log likelihood = -107.81781

Dismissal	Coefficient	Std. Err.	z	P> z	[95% Conf. Interval]
X	-4.196446	.7772556	-5.40	0.000	-5.719839 -2.673053
Z	1.106789	.3815787	2.90	0.004	.3589082 1.854669
_cons	-3.145352	.8648826	-3.64	0.000	-4.840491 -1.450213

## Model estimation and assessment

For our illustrations, we model the probability that a CEO's succession is either a dismissal or a routine succession using a binary logit specification. While the binary logit model is in some respects a special case, the methods illustrated are general and applicable to any LDV model. Our dependent variable, 'dismissal,' is coded as a binary variable; it equals one if the CEO was dismissed and zero for routine succession. Our dataset comprises 199 large public firms that have undergone a CEO succession over a specific period of time; for 76 (38%) of the observations the CEO was dismissed. For simplicity, there are two 'generic' explanatory variables  $X$  and  $Z$ . Given this, our logit model of CEO dismissal can, for a given observation, be written:

$$\begin{aligned} \Pr(\text{dismissal} = 1 | X, Z; \beta_0, \beta_X, \beta_Z) \\ = \frac{e^{\beta_0 + \beta_X X + \beta_Z Z}}{1 + e^{\beta_0 + \beta_X X + \beta_Z Z}} = \frac{e^{\mathbf{V}\boldsymbol{\beta}'}}{1 + e^{\mathbf{V}\boldsymbol{\beta}'}} \\ = \Pi(\mathbf{V}\boldsymbol{\beta}') \end{aligned} \quad (1)$$

In the above,  $\Pi(\mathbf{V}\boldsymbol{\beta}')$  is the probability that a CEO succession will be a dismissal,  $\boldsymbol{\beta}$  is the (row) vector of model coefficients  $\beta_0$ ,  $\beta_X$ , and  $\beta_Z$ , and  $\mathbf{V}$  is the (row) vector of model variables (including a '1' for the intercept).

Our model is estimated using STATA's *logit* command. As shown in Table 1, variables  $X$  and  $Z$  are each significant ( $p < 0.004$ ), where significance is based on the value of a normal z-statistic rather than a t-statistic, since the statistical theory underlying maximum likelihood estimation refers to large sample (asymptotic) properties of the estimates (Greene, 2003). Model significance is indicated by the significance ( $p < 0.001$ ) of the likelihood ratio chi-square statistic, which tests our model against an intercept-only model; this

test is analogous to the overall F-test of model significance in OLS estimation. The McFadden pseudo r-square reported in Table 1 is one of the many ‘goodness-of-fit’ measures proposed for LDV models (e.g., see Hoetker, 2007).

### Hypothesis testing: direct effect

Testing a hypothesis about the nature of the direct relationship between an explanatory variable and the dependent variable requires the researcher to estimate their relationship and assess its statistical significance. In strategy research, such a hypothesis most often concerns the sign (e.g., positive or negative) of the relationship. For OLS type models estimated using the method of least squares, such a directional hypothesis is tested by observing the sign and statistical significance of the explanatory variable’s estimated model coefficient. However, in LDV models, the direct relationship between an explanatory variable and the dependent variable is not given by the explanatory variable’s model coefficient but instead by the variable’s marginal effect, which will vary with the value of all model variables. Hence, a directional hypothesis in LDV models is tested by examining the sign (positive or negative) and statistical significance of the values of an explanatory variable’s marginal effect over all values of the model variables.<sup>5</sup>

Consider then testing the hypothesis that the relationship between variable  $X$  and CEO dismissal is negative. This will require analysis of  $X$ ’s marginal effect which, since  $X$  is a continuous variable, is found by differentiating Equation 1

with respect to  $X$ .<sup>6</sup> The result is:

$$\begin{aligned} \text{Marginal effect of } X \\ = \frac{\partial \Pr(\text{dismissal} = 1 | \mathbf{V}, \boldsymbol{\beta})}{\partial X} \\ = \frac{\partial \Pi(\mathbf{V}\boldsymbol{\beta}')}{\partial X} = \pi(\mathbf{V}\boldsymbol{\beta}')\beta_X \end{aligned} \quad (2)$$

This indicates that the marginal effect of  $X$  is proportional to its model coefficient  $\beta_X$ . Since  $\pi(\mathbf{V}\boldsymbol{\beta}')$  is always positive,<sup>7</sup>  $X$ ’s marginal effect has the same sign as its model coefficient ( $\beta_X$ ). Hence, in this model, the nature of the true relationship between  $X$  and CEO dismissal can be directly inferred from the sign of the estimated model coefficient (in this case negative).<sup>8</sup>

We now need to determine if this negative relationship is statistically significant. Due to the presence of the term  $\pi(\mathbf{V}\boldsymbol{\beta}')$  in Equation 2, the value and significance of  $X$ ’s marginal effect is not given by the value and significance of its estimated model coefficient. Instead, there are many values of the marginal effect, and each has its own standard error. We must therefore compute, at each observation, the value of the marginal effect, its standard error, and implied z-statistic value (ratio of the marginal effect value to its standard error) to test the significance of each value. Since computation of the marginal effect value at each observation means that the values of all model variables are being varied, assessment of the marginal effect and associated z-statistic values is best done graphically by plotting these values against the predicted value of the dependent outcome (i.e., probability of CEO dismissal). The STATA commands that performed these calculations and generated the graphical analysis for our logit model of CEO dismissal are presented in the Appendix.

<sup>5</sup> Analysis of the individual values of a marginal effect is the most general approach (for additional approaches see Long, 1997). Less general are ‘representative value’ methods, of which two are common. The first computes the value of the marginal effect using the sample mean of all variables and assesses its significance; the second method computes the average of the individual marginal effect values at each observation and assesses its significance. In STATA, the *mfx* command performs the first method, while the *margeff* command performs the second method. However, we caution that these commands assume a conventional model, that is, one where all model variables are measured in natural units (e.g., not logarithms), and each variable appears only once in the model and in level form. This excludes models that, for example, include the square of a variable or an interaction variable.

<sup>6</sup> For a discrete explanatory variable, its marginal effect is the change in the dependent variable when the explanatory variable is incremented by one unit. For example, for a dummy 0/1 explanatory variable  $X$ , its marginal effect is Equation 1 when  $X = 1$  minus Equation 1 when  $X = 0$  (e.g., see Long, 1997).

<sup>7</sup> The term  $\pi(\mathbf{V}\boldsymbol{\beta}') = d\Pi(\mathbf{V}\boldsymbol{\beta}')/d\mathbf{V}\boldsymbol{\beta}' = e^{\beta_0 + \beta_X X + \beta_Z Z} / (1 + e^{\beta_0 + \beta_X X + \beta_Z Z})^2 = \Pi(\mathbf{V}\boldsymbol{\beta}')(1 - \Pi(\mathbf{V}\boldsymbol{\beta}'))$  is the derivative of the logit cumulative distribution function. By definition,  $\pi(\mathbf{V}\boldsymbol{\beta}')$  is the logit probability density function whose values are always positive.

<sup>8</sup> More generally, the sign of a variable’s marginal effect is the same as the sign of its model coefficient in both the binary logit and binary probit models. However, this result may not hold for other LDV models, so the marginal effect of a variable should always be computed to assess its relationship to model coefficients.

Since our sample comprises 199 observations, there are 199 values of the marginal effect given by Equation 2. Each value and its associated z-statistic value are plotted in Figure 1; the solid symbols indicate values of the marginal effect (recorded on the left axis) while the diamond shaped symbols indicate z-statistic values (recorded on the right axis). As expected from Equation 2, all values of the marginal effect are negative;<sup>9</sup> the values range from -1.0491 to -0.0397. The z-statistic values range from -10.7551 to -1.2981, but as indicated in Figure 1, the z-statistic value associated with any given marginal effect value exceeds 1.96 in absolute value except at very high and low probabilities of CEO dismissal.<sup>10</sup> A summary measure of these results computes the value of the marginal effect and its significance at the means of all model variables. This computations yields a marginal effect value of -0.9618 with standard error 0.1791 and hence a z-statistic value of -5.37 ( $p < 0.001$ ). We conclude from this analysis that, as hypothesized, the relationship between  $X$  and CEO dismissal is negative and statistically significant ( $p < 0.05$ ).

To summarize, testing a hypothesis about the nature of the relationship between an explanatory variable and the dependent variable in an LDV model requires a supplementary analysis that

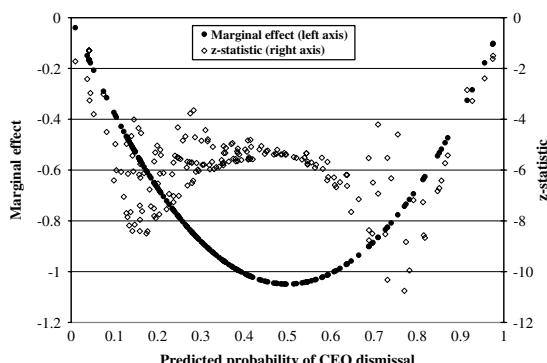


Figure 1. Analysis of  $X$ 's marginal effect on the probability of CEO dismissal

<sup>9</sup> The values of the marginal effect follow a U-shape since the term  $\pi(V\beta')$  in Equation 2 is simply the 'bell-shaped' logit probability density function (cf. Footnote 7). In Figure 1, this function is inverted since the estimated model coefficient for  $X$  is negative.

<sup>10</sup> That values of the marginal effect at extreme probability values are not significant is to be expected. It simply reflects that the slope of the logit cumulative distribution function approaches zero at the extreme ends of the distribution.

examines the value and significance of the explanatory variable's marginal effect. The researcher should graphically examine, as in Figure 1, the sign (positive or negative) and statistical significance of the value of the marginal effect at each observation to determine if the hypothesized relationship between the explanatory and dependent variable is accepted or rejected. If space limitations preclude a graphical presentation, then the write-up of results should include a discussion of the value and significance of the explanatory variable's marginal effect over its range of variation. This discussion can include reporting the minimum and maximum of the marginal effect and z-statistic values. For presentation of estimation results, a column showing the value and significance of the marginal effect for each model variable computed at the sample mean of all model variables should be added next to the column showing the estimated model coefficients;<sup>11</sup> the marginal effect values computed at variable means can also be referenced in the discussion of results. Table 1a gives an example of this recommended presentation format based on the results in Table 1.

### Hypothesis testing: moderating effect

In the strategy literature, it is common for researchers to postulate that one or more variables

Table 1a. Recommended presentation format for estimation results

Variable	Coefficient	Marginal effect at variable means
X	-4.1965*	-0.9618*
Z	1.1068*	0.2537*
Intercept	-3.1454*	—
Log-likelihood	-107.818	
Chi-square	49.03*	
Pseudo R-square	0.1853	

$n = 199$ ; \*  $p < 0.01$

Source: Table 1 and author's calculations.

<sup>11</sup> One could alternatively report the average of the marginal effect values and its significance (cf. Footnote 5). There is no consensus as to which 'average' is most representative, and they are in any event the same asymptotically (Greene, 2003: 668). The key obstacle to using the average of the marginal effect values is determining its significance, since deriving the expression needed to compute (using the delta method) the standard error of this value can be daunting. Ai and Norton (2003) and Greene (2003: 174) present formulas for the standard binary logit and probit models.

moderate the relationship between an explanatory variable and the dependent variable. The methods for analysis and testing of moderating (interaction) hypotheses in the OLS framework are both well documented (e.g., Jaccard, Wan, and Turrisi, 1990) and familiar to most researchers. It is therefore not surprising that researchers have often adopted OLS procedures to guide them in interpreting an interaction hypothesis (Hoetker, 2007) in an LDV model, despite the fact that these procedures are not correct for nonlinear LDV models. In particular, in an LDV model, the influence of a moderator variable on the relationship between an explanatory variable and the dependent variable is rarely indicated by the sign and statistical significance of the estimated coefficient on the interaction variable in the model. Instead, a moderating effect is itself a marginal effect, and hence all the issues regarding a marginal effect discussed in the previous section apply. In particular, the equation for the moderating effect will be nonlinear, its value will depend on the values taken by all model variables and, as noted, it will not equal the coefficient on the model's interaction variable. Hence, a moderator hypothesis in an LDV model is tested by examining the sign (positive or negative) and statistical significance of the values of the moderator variable's marginal effect on the relationship between the explanatory variable and the dependent variable over all sample values of the model variables.

To illustrate, we examine the hypothesis that the relationship between variable  $X$  and CEO dismissal is positively moderated by variable  $Z$ . Since the relationship between  $X$  and CEO dismissal is expected to be negative, this moderating hypothesis means that the relationship between  $X$  and CEO dismissal is expected to become less negative at higher values of  $Z$ . To test this hypothesis we add to our logit model (Equation 1) the interaction variable ( $XZ$ ). For a given observation, this

expanded model can be written:

$$\begin{aligned} \Pr(dismissal = 1 | \mathbf{V}, \boldsymbol{\beta}) \\ = \frac{e^{\beta_0 + \beta_X X + \beta_Z Z + \beta_{XZ}(XZ)}}{1 + e^{\beta_0 + \beta_X X + \beta_Z Z + \beta_{XZ}(XZ)}} \\ = \Pi(\mathbf{V}\boldsymbol{\beta}') \end{aligned} \quad (3)$$

Table 2 presents the output from estimating this model using STATA's *logit* command.

To test our moderator hypothesis, we first determine if the coefficient on the interaction variable ( $\beta_{XZ}$ ) is statistically significant.<sup>12</sup> Since this is indeed the case (see Table 2), the next step is to determine the equation for the marginal effect of the moderator variable on the relationship between the explanatory variable and dependent variable; what Ai and Norton (2003) labeled the *true interaction effect*. Since  $X$  and  $Z$  are continuous variables, the equation for the true interaction effect is given by the cross-partial derivative of Equation 3, first with respect to  $X$  and then with respect to  $Z$ . Taking first the derivative of Equation 3 with respect to  $X$  yields the following equation for the marginal effect of  $X$  in this expanded model:

$$\begin{aligned} \text{Marginal effect of } X &= \frac{\partial \Pi(\mathbf{V}\boldsymbol{\beta}')}{\partial X} \\ &= \pi(\mathbf{V}\boldsymbol{\beta}')(\beta_X + \beta_{XZ}Z) \end{aligned} \quad (4)$$

Differentiating Equation 4 with respect to  $Z$  then yields the equation for the true interaction

<sup>12</sup> As suggested by Equation 5 below, significance of the interaction variable does not necessarily imply a significant moderating effect.

Table 2. Results from Stata's *logit* command estimating probability of CEO dismissal  
Logistic regression

		Number of obs = 199
		LR chi2(3) = 55.17
		Prob > chi2 = 0.0000
		Pseudo R2 = 0.2085
Log likelihood = -104.74792		
Dismissal	Coefficient	Std. Err.
X	-16.57889	5.298664
Z	1.319382	0.410072
XZ	5.502511	2.264677
_cons	-3.736800	0.961833
		[95% Conf. Interval]

effect of moderator variable  $Z$ :<sup>13</sup>

$$\begin{aligned} \text{True interaction effect} &= \frac{\partial(\text{Marginal effect of } X)}{\partial Z} \\ &= \frac{\partial \Pi(\mathbf{V}\beta')}{\partial X \partial Z} \\ &= \Pi(\mathbf{V}\beta')(1 - \Pi(\mathbf{V}\beta'))[\beta_{xz} + (1 - 2\Pi(\mathbf{V}\beta')) \\ &\quad (\beta_x + \beta_{xz}Z)(\beta_z + \beta_{xz}X)] \end{aligned} \quad (5)$$

In the above, the term  $\Pi(\mathbf{V}\beta')$  is now given by Equation 3. Clearly, the value and significance of the true interaction effect is not given by the value and statistical significance of the coefficient ( $\beta_{xz}$ ) on the interaction variable. Instead, there are many values of the true interaction effect, and each has its own standard error. As in the previous section, to assess the nature and significance of the marginal effect given by Equation 5, we must compute its value, and the implied z-statistic value at each observation, and then examine these values graphically as presented in Figure 2. The STATA commands that performed this analysis are given in the Appendix.

In Figure 2, the solid symbols indicate values of the true interaction effect (recorded on the left axis), while the diamond shaped symbols indicate z-statistic values (recorded on the right axis). As seen, the value, sign, and significance of the true interaction effect differs over the range of the predicted values of CEO dismissal. The values of the true interaction effect range from  $-0.5116$

to  $1.3819$ , with a mean value of  $0.5309$ . The z-statistic values range from  $-6.0614$  to  $4.3106$ , so some values of the true interaction effect are not significant. As seen in Figure 2, the true interaction effect is positive and significant only when the probability of CEO dismissal is in the range from about  $0.45$  to  $0.65$ , and its value is negative and significant when the probability of CEO dismissal is less than about  $0.1$ . These findings indicate the complexity of analyzing the results from nonlinear LDV models, and that clear-cut results are not always to be expected. The results also underscore that examining only the sign and statistical significance of the average of the values of the interaction effect, or the sign and significance of the interaction effect computed at variable means, may not provide an accurate assessment of the moderating effect. However, if the graphical analysis indicates no change in the sign of the true interaction effect over its range of variation, then the value of the true interaction effect (Equation 5) at each variable's mean can be reported as a summary measure. For our model, the value of the true interaction effect computed at the variable means is  $0.901$  with standard error  $0.5321$ , and hence has a z-statistic value of  $1.69$  ( $p = 0.09$ ). This result, but more importantly the graphical analysis in Figure 2, indicates virtually no support for the hypothesis that the relationship between  $X$  and CEO dismissal is positively moderated by variable  $Z$ .

A graphical analysis, such as that presented in Figure 2, provides for the most complete assessment of the nature of an interaction effect and should therefore always be conducted and reported in the discussion of results. If space limitations prevent including a graphical analysis, one should indicate the maximum and minimum of the true interaction effect and z-statistic values together with an indication of whether, over the range of values of the predicted dependent outcome, the true interaction effect changes sign or is not statistically significant. Finally, as Figure 2 makes clear, reporting only the value and significance of the true interaction effect computed at variable means is (in this example) not a reliable indicator of the sign or significance of the true interaction effect over its range of variation. However, this measure can be mentioned in the discussion of results once full consideration has been given to discussing the behavior of the values of the true interaction effect

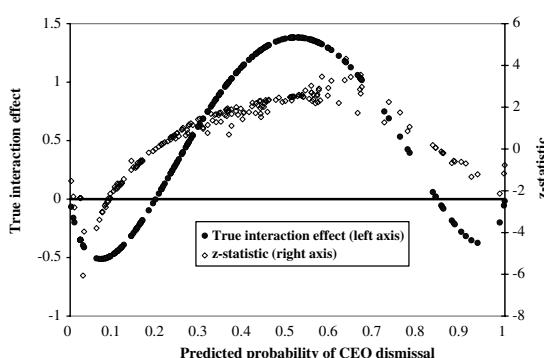


Figure 2. True interaction effect of  $Z$  on the relationship between  $X$  and the probability of CEO dismissal

<sup>13</sup> cf. Footnote 6. If  $Z$  were a dummy 0/1 variable, the true interaction effect is Equation 4 with  $Z = 1$  minus Equation 4 with  $Z = 0$ . The value of this difference equation would then be computed at each observation.

values and their significance as indicated by the graphical analysis.

Given a significant interaction effect, it is common in an OLS analysis to graphically illustrate the influence of a moderating variable by a pair of straight lines, where the slope of each line is the marginal effect of the explanatory variable at a low and high value of the moderator variable. Visual comparison of the slopes of the two lines then indicates how the explanatory variable's marginal effect differs at the two values of the moderator. Although this type of graphical analysis can be done in the context of an LDV model, we believe it is seriously misleading, not least because it assumes that the value of the explanatory variable's marginal effect is constant over values of the explanatory variable, which directly contradicts that a variable's marginal effect in an LDV model is not a constant value. At best, this type of graphical analysis is only suggestive of the moderating influence of a moderating variable, and cannot be used for statistical inference.<sup>14</sup>

Instead of a graphical approach to illustrate the directional effect of moderator  $Z$  on the marginal effect of  $X$ , we instead recommend that the write-up of results include a table showing the value and significance of  $X$ 's marginal effect at selected values of the moderator  $Z$ . For this analysis, the value of all model variables except  $Z$  (i.e.,  $X$  in the present model) must be held fixed. Such analysis illustrates not only the influence of moderator  $Z$  on the value of  $X$ 's marginal effect, it also serves to indicate how values of moderator  $Z$  influence the significance of  $X$ 's marginal effect.

While in our example our moderator hypothesis was not supported, we can nonetheless indicate how one would conduct and present the results of this analysis by computing the value of Equation 4 at a low, mean, and high value of  $Z$  while always keeping all other model variables at their sample mean value.<sup>15</sup> By convention, the low and high value of variable  $Z$  is one standard deviation

<sup>14</sup> If such a graphical analysis is desired, we recommend graphing, for each specific value of the moderator (e.g., low, mean, and high), the values of Equation 3 against the values of the explanatory variable (i.e.,  $X$ ), with all other model variables always set equal to their sample mean value.

<sup>15</sup> A more general analysis would compute Equation 4 at each sample value of  $Z$  while keeping all other model variables (i.e.,  $X$ ) equal to their sample mean value. The values of Equation 4 and associated z-statistic values can then be plotted against the values of variable  $Z$  to observe the entire range of variation in the value and significance of Equation 4.

below and above its mean. Each calculated value of Equation 4 has a standard error and implied z-statistic value. The STATA commands that performed this analysis are given in the Appendix. Table 3 shows the recommended presentation format based on the results from this analysis.

As shown in Table 3, the relationship between  $X$  and the probability of CEO dismissal is less negative at higher values of  $Z$ , suggestive of a generally positive moderating effect of  $Z$ . At the high value of  $Z$  this positive effect is sufficient to render the (negative) marginal effect of  $X$  statistically insignificant ( $p = 0.0784$ ). These results indicate that, holding fixed the value of all model variables (except  $Z$ ) at their sample mean value, higher values of  $Z$  reduce the impact that  $X$  has on the probability of CEO dismissal. While this analysis suggests variable  $Z$  has a positive moderating effect on the relationship between  $X$  and the probability of CEO dismissal, we caution that this analysis is not a test for the existence of a moderating effect of  $Z$ , nor does it indicate the sign or significance of such an effect; that analysis instead requires analysis of the true interaction effect as presented above. However, if the significance of a moderator effect is established then the suggested presentation format (Table 3) offers a convenient way to summarize this effect.

To summarize, the method for testing a moderator hypothesis in an LDV model differs substantially from that used in OLS. If the estimated model coefficient on the interaction variable is significant, the values of the true interaction effect are then computed and analyzed to assess the sign (positive or negative) and statistical significance of a moderating effect. For presenting results, a plot of the true interaction effect and z-statistic values computed at each observation against the predicted values of the dependent variable, as done in Figure 2, is crucial. The write-up of results should

Table 3. Recommended format for presenting effect of  $Z$  on the marginal effect of  $X$  on the probability of CEO dismissal

Value of moderator $Z$	Marginal effect of $X$ <sup>a</sup>	z-statistic
Low	-1.3707*	-3.78
Mean	-1.1029*	-5.51
High	-0.4897	-1.76

\*  $p < 0.05$

<sup>a</sup> Computed at sample mean value of  $X$ .

summarize the values and significance of the true interaction effect over its range of variation. If the values of the true interaction effect do not change sign, then the value and significance of this effect computed at variable means can be reported as a summary measure. Finally, if the true interaction effect is statistically significant, analysis of the value and statistical significance of the explanatory variable's marginal effect at different values of the moderator variable, as shown in Table 3, can be undertaken and reported in lieu of a graphical analysis to illustrate the influence of the moderator variable for the value and significance of the explanatory variable's marginal effect.

## CONCLUSION

This study has provided and illustrated the most general methods for analyzing and interpreting the results from LDV models. In taking a pragmatic approach, it is hoped that our detailed presentation of the essential methods for making statistical inferences in LDV models will enable strategy researchers to feel more confident when using LDV models, and can help prevent them from perpetuating past mistakes when analyzing and reporting the results from such models. In this respect, this study has contributed to the ongoing stream of methodological inquiry in strategy research by providing greater clarity on an important set of statistical issues that can arise in the analysis of firm-level data.

## REFERENCES

- Acar W, Sankaran K. 1999. The myth of the unique decomposability: specializing the Herfindahl and entropy measures? *Strategic Management Journal* **20**(10): 969–975.
- Ai C, Norton EC. 2003. Interaction terms in logit and probit models. *Economics Letters* **80**(1): 123–129.
- Bergh DD. 1995. Problems with repeated measures analysis: demonstration with a study of the diversification and performance relationship. *Academy of Management Journal* **38**(6): 1692–708.
- Bergh D, Ketchen DJ Jr (eds). 2004. *Research Methodology in Strategy and Management (Volume 1)*. JAI/Elsevier Press: Oxford, UK.
- Bloom M, Michel JG. 2002. The relationships among organizational context, pay dispersion, and among managerial turnover. *Academy of Management Journal* **45**(1): 33–42.
- Bowen HP, Wiersema MF. 1999. Matching method to paradigm in strategy research: limitations of cross-sectional analysis and some methodological alternatives. *Strategic Management Journal* **20**(7): 625–636.
- Bowen HP, Wiersema MF. 2004. Modeling limited dependent variables: guidelines for researchers of strategic management. In *Research Methodology in Strategy and Management (Volume 1)*, Ketchen DJ Jr, Bergh D (eds). JAI/Elsevier Press: Oxford, UK; 87–134.
- Chatterjee S, Bloucher JD. 1992. Measurement of firm diversification: is it robust? *Academy of Management Journal* **35**(4): 874–888.
- Colombo MG. 2003. Alliance form: a test of the contractual and competence perspectives. *Strategic Management Journal* **24**(12): 1209–1229.
- Davis R, Duhaime IM. 1992. Diversification, vertical integration, and industry analysis: new perspectives and measurement. *Strategic Management Journal* **13**(7): 511–524.
- Greene WH. 2003. *Econometric Analysis* (5th edn). Prentice Hall: Upper Saddle River, NJ.
- Hambrick A, Cannella AA Jr. 2004. CEOs who have COOs: contingency analysis of an unexplored structural form. *Strategic Management Journal* **25**(10): 959–979.
- Hamilton BH, Nickerson JA. 2003. Correcting for endogeneity bias in strategic management research. *Strategic Organization* **1**(1): 51–78.
- Hoetker G. 2007. The use of logit and probit models in strategic management research: critical issues. *Strategic Management Journal* **28**(4): 331–343.
- Hoskisson RE, Hitt MA, Johnson RA, Moesel DD. 1993. Construct validity of an objective (entropy) categorical measure of diversification strategy. *Strategic Management Journal* **14**(3): 215–235.
- Jaccard J, Wan CK, Turrisi R. 1990. The detection and interpretation of interaction effects between continuous variables in multiple regression. *Multivariate Behavioral Research* **25**(4): 467–479.
- Long JS. 1997. *Regression Models for Categorical and Limited Dependent Variables (Advanced Quantitative Techniques in the Social Sciences)*. Sage: Thousand Oaks, CA.
- Lubatkin MH, Merchant H, Srinivasan N. 1993. Construct validity of some unweighted product-count diversification measures. *Strategic Management Journal* **14**(6): 433–449.
- Nelson T. 2003. The persistence of founder influence: management, ownership, and performance effects at initial public offering. *Strategic Management Journal* **24**(8): 707–724.
- Robins JA, Wiersema MF. 2003. The measurement of corporate portfolio strategy: analysis of the content validity of related diversification indexes. *Strategic Management Journal* **24**(1): 39–59.
- Scandura TA, Williams EA. 2000. Research methodology in management: current practices, trends, and implications of future research. *Academy of Management Journal* **43**(6): 1248–1264.

- Shen W, Cannella AA Jr. 2002. Power dynamics within top management and their impacts on CEO dismissal followed by inside succession. *Academy of Management Journal* **45**(6): 1195–1206.
- Shook CL, Ketchen DJ Jr, Cycyota CS, Crockett D. 2003. Data analytic trends and training in Strategic Management. *Strategic Management Journal* **24**(12): 1231–1237.
- Shook CL, Ketchen DJ Jr, Hult GTM, Kacmar KM. 2004. An assessment of the use of structural equation modeling in strategic management research. *Strategic Management Journal* **25**(4): 397–404.
- Vermeulen F, Barkema H. 2002. Pace, rhythm, and scope: process dependence in building a profitable multinational corporation. *Strategic Management Journal* **23**(7): 637–653.
- Zajac EJ, Westphal JD. 1996. Director reputation, CEO/board power, and the dynamics of board interlocks. *Administrative Science Quarterly* **41**: 507–529.

## APPENDIX

### Hypothesis testing: direct effect

The following STATA commands compute, at each observation, the value of the marginal effect given by Equation 2, its standard error, and implied z-statistic value. Summary statistics for the marginal effect and z-statistic values are computed, the marginal effect and z-statistic values are plotted as in Figure 1, and the marginal effect at the variable means and its associated z-statistic are computed for each model variable.

```
* Estimate Logit model
logit dismissal X Z
* Predict probability of CEO dismissal, store values in variable pprob
predict pprob
* Define expression for X's marginal effect to use in predictnl command
* Save marginal effect values in meX; standard error values in meX_se
local vb_b[_cons] +_b[X]*X +_b[Z]*Z
local phat (exp('vb')/(1+exp('vb')))
predictnl meX = 'phat'*(1-'phat')*_b[X], se(meX_se)
* Compute z-statistic values and store in variable z_stat
gen z_stat = meX/meX_se
* print summary statistics for marginal effect and z-statistic values
tabstat meX z_stat, stats(mean min max)
* Graph marginal effect and z-statistic values (Figure 1)
graph twoway (scatter meX pprob) || ///
(scatter z_stat pprob, yaxis(2)yline
(-1.96 1.96, axis(2)))
* Compute and save sample means of variables X and Z
egen meanX = mean(X)
egen meanZ = mean(Z)
* Determine value and significance of marginal effect at data means
local vb_b[_cons] +_b[X]*meanX +_b[Z]*meanZ
local phat (exp('vb')/(1+exp('vb')))
nlcom meX_means: 'phat'*(1-'phat')*_b[X]
nlcom meZ_means: 'phat'*(1-'phat')*_b[Z]
```

### Hypothesis testing: moderating effect

The following STATA commands compute at each observation the value of the true interaction effect given by Equation 5, its standard error, and implied z-statistic value. Summary statistics for the interaction effect and z-statistic values are computed and the interaction effect and z-statistic values are then plotted as in Figure 2.

```
* Create interaction variable
gen XZ = X*Z
* Estimate Logit model
logit dismissal X Z XZ
* Predict probability of CEO dismissal, store values in variable pprob
predict pprob
```

```

* Define expression for interaction effect to use in predictnl command
* Store interaction effect values in new variable ie
* Store standard errors values in new variable ie_se
    local vb _b[X]*X+_b[Z]*Z+_b[XZ]*XZ+_b[_cons]
    local phat (exp(`vb')/(1+exp(`vb')))
    local term1 ('phat'*(1-'phat'))
    local term2 (1-2*'phat')
    local coef1 (_b[X]+_b[XZ]*Z)
    local coef2 (_b[Z]+_b[XZ]*X)
    predictnl ie = `term1'*(_b[XZ]+`term2'*`coef1'*`coef2'), se(ie_se)
* Compute z-statistic values and store in new variable z_stat;
    gen z_stat = ie/ie_se
* Print mean, minimum and maximum of interaction effect and z-statistic values
    tabstat ie z_stat, stats(mean min max)
* Graph marginal effect and z-statistic values (Figure 2)
    graph twoway (scatter ie pprob) || ///
        (scatter z_stat pprob, yaxis(2) yline (-1.96 1.96, axis(2)))
* Compute and save sample means of model variables
    egen meanX = mean(X)
    egen meanZ = mean(Z)
    egen meanXZ = mean(XZ)
* Determine value and significance of interaction effect at data means
    local vb _b[X]*meanX+_b[Z]* meanZ+_b[XZ] *meanXZ+_b[_cons]
    local phat (exp(`vb')/(1+exp(`vb')))
    local term1 ('phat'*(1-'phat'))
    local term2 (1-2*'phat')
    local coef1 (_b[X]+_b[XZ]*meanZ)
    local coef2 (_b[Z]+_b[XZ]*meanX)
    nlcom ie_means: `term1'*(_b[XZ]+`term2'*`coef1'*`coef2')

```

### **Effect of moderator Z on marginal effect of X in interaction model**

The following STATA commands compute and report significance of the value of the marginal effect of  $X$  given by Equation 4 and at a low, mean and high value of variable  $Z$  while holding fixed the value of all other model variables (i.e.,  $X$ ) equal at their sample mean value.

```

* Compute and save variable means and standard deviation of moderator Z
    egen meanX = mean(X)
    egen meanZ = mean(Z)
    egen sdZ = sd(Z)
* Compute and save high and low values of moderator variable Z
    gen Zhig = meanZ + sdZ
    gen Zlow = meanZ - sdZ
* Estimate Logit model (Equation 3)
    logit dismissal X Z XZ
* Compute and test significance of marginal effect (Equation 4)
* Z at its low value; X at its mean value

```

```
local vb (_b[_cons] +_b[X]*meanX +_b[Z] *Zlow +_b[XZ]*meanX*Zlow)
nlcom meanX_lowZ: ((exp(`vb'))/(1+exp(`vb'))^ 2)*(_b[X]+_b[XZ]*Zlow)
* Z at its mean value; X at its mean value
local vb (_b[_cons]+_b[X]*meanX+_b[Z]*meanZ+_b[XZ]*meanX*meanZ)
nlcom meanX_meanZ: ((exp(`vb'))/(1+exp(`vb'))^ 2)*(_b[X]+_b[XZ]*meanZ)
* Z at its high value; X at its mean value
local vb (_b[_cons]+_b[X]*meanX+_b[Z] *Zhigh+_b[XZ]*meanX*Zhigh)
nlcom meanZ_highZ: ((exp(`vb'))/(1+exp(`vb'))^ 2)*(_b[X]+_b[XZ]*Zhigh)
```