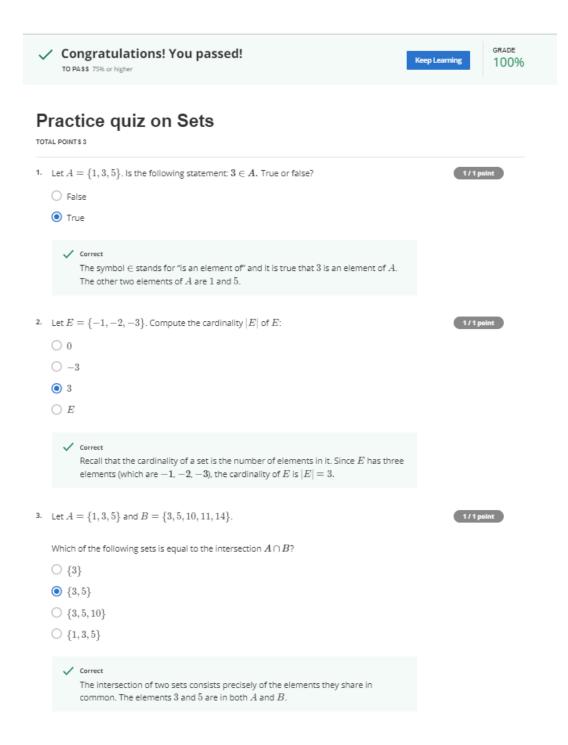
Building Blocks for Problem Solving - Practice quiz on Sets (3 questions)



 The infinite World of Real Numbers - Practice quiz on the Number Line, including Inequalities (8 questions) TO PASS 75% or higher

Practice quiz on the Number Line, including Inequalities

TOTAL POINTS 8

1.	Which	of the	following	real	numbers	ÌS	not	an	integer	?
----	-------	--------	-----------	------	---------	----	-----	----	---------	---

1/1 point

- 4.3
- 0
- \bigcirc -3
- O 7

4.3 is a decimal that is between two consecutive integers (4 and 5).

2. Which of the following is the absolute value |-7| of the number -7?

0 / 1 point

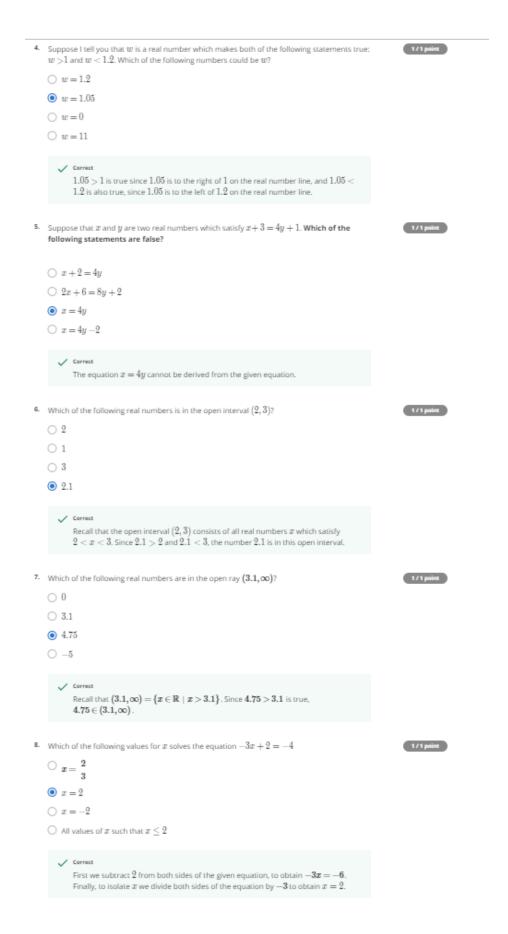
- \bigcirc -7
- \bigcirc 0
- 1
- 0.7

If you chose this one, you were being creative! Note that the cardinality of the set -7 is indeed 1, so perhaps this is what you were thinking. If so, math owes you an apology for using similar notation for two very different concepts!

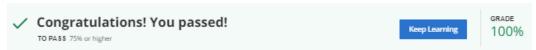
3. Suppose I tell you that x and y are two real numbers which make the statement x < y true. Which pair of numbers \underline{cannot} be values for x and y?

1/1 point

- \bigcirc x = 5 and y = 3.3
- $\bigcirc x = 1$ and y = 7.3
- $\bigcirc x = -1$ and y = 0
- \bigcirc x=-17.3 and y=-17.1



• That Jagged S Symbol - Practice quiz on Simplification Rules and Sigma Notation (6 questions)



Practice quiz on Simplification Rules and Sigma Notation

TOTAL	2001	10.00	~	~
TOTAL	. PUI	NI	ð	ь

1.	Which of the numbers below is equal to the following summation:
	$\sum_{i=1}^{3} i^2$?

1/1 point

O 30

14

 \bigcirc 1

O 9

 \checkmark correct We compute $\Sigma_{i=1}^3 i^2 = 1^2 + 2^3 + 3^2 = 14$

^{2.} Suppose that $A = \sum_{k=1}^{100} k^4$ and $B = \sum_{j=1}^{100} j^4$

1/1 point

Which of the following statements is true?

- $\bigcirc B > A$
- \bigcirc A = B
- O There is not enough information to do the problem
- $\bigcirc A > B$

✓ Correct

 ${\rm A}={\rm B}.$ Both summations evaluate to the same number, since k and j are just dummy indices.

3. Which of the numbers below is equal to the summation $\sum_{i=1}^{10} 7$?

1/1 point

- 70
- 07
- O 55
- \bigcirc 0

✓ Correc

According to one of our Sigma notation simplification rules, this summation is just equal to 10 copies of the number 7 all added together, and so we get $10\times 7=70.$

4. Suppose that $X\!=\!\sum_{t=1}^5\!i^3$ and $Y\!=\!\sum_{t=1}^5\!i^4$.

1/1 point

Which of the following expressions is equal to the summation $\Sigma_{i=1}^5(2i^3+5i^4)$?

- X + Y
- O 3375
- \bigcirc 7
- 2X + 5Y

✓ Correct

To get here, you apply two of our Sigma notation simplification rules

$$\Sigma_{i=1}^{5} 2i^{3} + 5i^{4} = 2(\Sigma_{i=1}^{5}i^{3}) + 5(\Sigma_{i=1}^{5}i^{4}) = 2X + 5Y.$$

5. Which of the following numbers is the mean μ_Z of the set $Z=\{-2,4,7\}$?

1/1 poin

- O 4
- 3
- 9
- $\bigcirc \frac{13}{3}$

✓ Correct

To get the mean of a set of numbers, you need to perform two steps: first add them all up (in this case getting -2+4+7=9), and then divide by the number of elements in the set (in this case that number is 3).

So you should obtain $\mu_Z=rac{9}{3}=3$, which you did!

6. Suppose the set X has five numbers in it: X = {x1, x2, x3, x4, x5}. Which of the following expression represents the mean of the set X?

1/1 point

$$\frac{1}{5} \left[\sum_{i=1}^{5} x_i \right]$$

$$\frac{1}{5} \left[\sum_{i=1}^{5} (x_i - \mu_X)^2 \right]$$

$$\bigcirc \sum_{i=1}^{5} x_i$$

$$\bigcirc \frac{1}{N} [\sum_{i=1}^{N} x_i]$$

✓ Correc

To obtain the mean of a set of numbers, you first add them all up (which is expressed here by the sigma operation inside the square brackets) and then you divide by the number of numbers in the set (which is expressed here by the $\frac{1}{5}$ outside the square brackets).

 That Jagged S Symbol - Graded quiz on Sets, Number Line, Inequalities, Simplification, and Sigma Notation (13 questions)



5.	Suppose that ${\it z}$ and ${\it w}$ are two positive numbers with ${\it z} < {\it w}$. Which of the following
	inequalities is false?

1/1 point

- $\bigcirc z + 3 < w + 3$
- $\bigcirc w-7 > z-7$
- $\bigcirc -z > -w$
- \bigcirc -5z < -5w

✓ Correct

If we start with z < w and multiply both sides by $-\mathbf{5}$, we need to flip the less-than sign, which would give $-\mathbf{5}z > -\mathbf{5}w$. For an example, try z=1 and y=2 and see what happens!

6. Find the set of all x which solve the inequality $-2x+5\leq 7$

1/1 point

- $\bigcirc x \le -1$
- $\bigcirc x \ge -6$
- $x \ge -1$
- $\bigcirc x = -1$

✓ Correct

Subtracting 5 from both sides of the given inequality gives $-2x \leq 2$. Then we divide both sides by -2, remembering to flip the inequality sign, and we obtain this answer

7. Which of the following real numbers is not in the closed interval $\left[2,3\right]$

1/1 point

- ① 1
- O 2.1
- O 2
- 3

✓ Correct

Recall that the closed interval [2,3] consists of all real numbers x which satisfy $2 \le x \le 3$. Since $2 \le 1$ is false, $1 \notin [2,3]$

8. Which of the following intervals represents the set of all solutions to:

0/1 point

$$-5 \le x + 2 < 10$$
?

- O [-7,8)
- (7,8)
- \bigcirc [-5, 10)
- O [-7,8]

Incorrec

Every single real number in (7,8) does satisfy the requirements. However, the number -7 also satisfies the requirements (check this!) and is not in this open interval.

9.	Which of the numbers below is equal to the following summation: $\Sigma_{k=2}^52k$?	1/1 point
	○ 14	
	○ 4	
	O 10	
	✓ Correct	
	We compute $\Sigma_{k=2}^5 2k = 4+6+8+10=28$.	
10.	Suppose we already know that $\Sigma_{k=1}^{20} k = 210$. Which of the numbers below is equal to $\Sigma_{k=1}^{20} 2k$?	1/1 point
	O 210	
	2 • 420	
	0 40	
	\checkmark correct By applying one of our Sigma notation simplification rules, we can rewrite the summation in question as $2\left(\Sigma_{k-1}^{20}k\right)=2\times210=420$.	
44	710 -	
	Which of the numbers below is equal to the summation $\Sigma^{10}_{t-2} 7$?	1/1 point
	○ 7 ○ 48	
	0 70	
	63	
	\checkmark correct According to one of our Sigma notation simplification rules, this summation is just equal to 9 copies of the number 7 all added together, and so we get $9\cdot 7=63$.	
12.	Which of the following numbers is the variance of the set $Z=\{-2,4,7\}$?	0/1 point
	O 69	
	 ◆√14 → 42 	
	0 14	
	! Incorrect You were almost there if you got this one. If you got here, you probably calculated the standard deviation of Z, which is just the square root of the variance.	
13.	Which of the following sets does not have zero variance? (hint: don't do any calculation here, just think!)	1/1 point
	○ {5,5,5,5,5,5,5,5,5,5,5,5,5}	
	○ {0,0,0,0,0,0,0}	
	○ {1,1,1,1} • {2,5,9,13}	
	\(\begin{align*} \partial \par	
	✓ Correct	
	Intuitively, the numbers in this set are spread out.	

WEEK 2

Descartes Was Really Smart - Practice quiz on the Cartesian Plane (5 questions)

✓ Congratulations! You passed! 10 1988 75% or higher	Keep Learning	100%
Practice quiz on the Cartesian Plane		
 Which of the following points in the Cartesian Plane is on the y-axis? (5,0) (-5,0) (1,1) (0,-5) ✓ Correct The y-axis is defined to be all points in the Cartesian plane with zero as x-	1/1;	oint
coordinate. The point $(0,-5)$ meets that requirement. 2. Find the distance between the points $A=(2,2)$ and $C=(3,3)$: 0 ① $\sqrt{2}$ 1 2	1/19	
Correct Recall that the distance between points (a,b) and (c,d) is $\sqrt{(c-a)^2+(d-b)^2}$. In this case $(a,b)=(2,2)$ and $(c,d)=(3,3)$, so the distance is $\sqrt{(3-2)^2+(3-2)^2}=\sqrt{2}.$		
3. Find the point-slope form of the equation of the line that goes between $A=(1,1)$ and $B=(5,3)$ $0 y=\frac{1}{2}x$ $0 y-1=\frac{1}{2}(x-5)$ $0 y-3=\frac{1}{2}(x-1)$ $0 y-1=\frac{1}{2}(x-1)$	1): 1/16	oint

The point-slope form for the equation of a line with slope m that goes through the point (x_0,y_0) is $y-y_0=m(x-x_0)$

We can choose either \boldsymbol{A} or \boldsymbol{B} for the point on the line, but in neither case do we get

In this case, the slope $m\!=\!rac{3-1}{5-1}\!=\!rac{1}{2}$

this chosen answer.



- (3,2)
- (2, 1)
- \bigcirc (0,0)
- O (2, 3)

✓ Correct

If we plug in 1 for y and 2 for x in the equation of the line, we make a true statement, 0 = 0, so this point lies on the line.

Suppose that a line ℓ has slope 2 and goes through the point (-1,0). What is the y-intercept
of ℓ?

1/1 point

- \bigcirc -1
- \bigcirc 1
- \bigcirc 0
- 2

✓ Correct

Recall that the y-intercept of ℓ is the y-coordinate of where ℓ hits the y-axis.

Since $(-1,0)\in \ell$, the point on ℓ with x=0 is obtained by running one unit from (-1,0) while rising two units.

This gives y=2 as the y-intercept.

• Input-Output Machines - Practice quiz on Types of Functions (6 questions)

Congratulations! You passed! 10 PASS 75% or higher

Keep Learning

CKADE 100%

Practice quiz on Types of Functions

TOTAL POINTS 6

 Suppose that A = {1, 2, 10} and B = {4, 8, 40}. Which of the following formulae do not define a function f: A → B?

1/1 point

- f(1) = 4, f(2) = 40, and f(10) = 8.
- f(1) = 5, f(2) = 8, and f(10) = 40.
- \bigcirc f(1) = 4, f(2) = 4, and f(10) = 4.
- $\bigcap f(a) = 4a$, for each $a \in A$

✓ Correct

A function $f:A\to B$ is a rule which assigns an element $f(a)\in B$ to each $a\in A$. In this case, unfortunately, $f(1)=5\notin B$.

 Suppose that A contains every person in the VBS study (see the second video in the course if you're confused here!). Suppose that Y = {+,-} and Z = {H,S} 1/1 point

Suppose that $T: A \to Y$ is the function which gives T(a) = + if person a tests positive and T(a) = - if they test negative.

Suppose that $D: A \to Z$ is the function which gives D(a) = H does not actually have VBS and D(a) = S if the person actually has VBS.

Which of the following must be true of person a if we have a false positive?

- $\bigcirc T(a) = \text{ and } D(a) = H$
- \bullet T(a) = + and D(a) = H
- $\bigcap T(a) = \text{ and } D(a) = S$
- $\bigcap T(a) = + \operatorname{and} D(a) = S$

✓ Correct

Recall that a false positive is a positive test result (so T(a)=+) which is misleading because the person actually does not have the disease (D(a)=H)

Consider the function g: R → R defined by g(x) = x² - 1. Which of the following points are not on the graph of g?

1/1 point

- (0,-1)
- \bigcirc (1,0)
- (2, −1)
- (-1,0)

✓ Correct

Recall that the graph of g consists of all points (x,y) such that y=g(x). Here $g(2)=3 \not= -1$, so the point (2,-1) is \temphinot\) on the graph of g.

4.	Let the point $A = (2, 4)$. Which of the following graphs does not contain the point A ?	1/1 point
	O The graph of $s(x) = x^2$	
	(a) The graph of $h(x) = x - 1$	
	\bigcirc The graph of $f(x) = 2x$	
	\bigcirc The graph of $g(x) = x + 2$	
	\checkmark Correct The graph of h consists of all points (x,y) such that $y=h(x)$. Here $h(2)=1\neq 4$, so the point $(2,4)$ is not on the graph of h .	
5.	Suppose that $h(x) = -3x + 4$. Which of the following statements is true?	1/1 point
	All statements are correct	
	 h is neither a strictly increasing function nor a strictly decreasing function. 	
	h is a strictly decreasing function	
	h is a strictly increasing function	
	\checkmark Correct A function h is called strictly decreasing if whenever $a < b$, then $h(a) > h(b)$	
	Since the graph of h is a line with negative slope, this is in fact true!	
á.	Suppose that $f: \mathbb{R} \to \mathbb{R}$ is a strictly increasing function, with $f(3) = 15$	1/1 point
	Which of the following is a possible value for $f(3.7)$?	
	17	
	○ -3	
	O 3	
	O 14.7	
	\checkmark Correct A function f is called strictly increasing if whenever $a < b$, then $f(a) < f(b)$.	
	Since $f(3)=15$ is given and $3<3.7$, it must be that $15< f(3.7)$, and this answer satisfies that.	

• Input-Output Machines - Graded quiz on Cartesian Plane and Types of Function (13 questions)

✓ Congratulations! You passed! 10 1933 75% or higher	p Learning 100%
Graded quiz on Cartesian Plane and Types of	Function
Which of the following points in the Cartesian Plane have positive <i>x</i> -coordinate and negative <i>y</i> -coordinate? (7, -1) (5, 7) (-4, 5) (0, 0) Correct The <i>x</i> -coordinate, 7, is positive, and the <i>y</i> -coordinate, -1, is negative.	1/1 point
 Which of the following points is in the first quadrant of the Cartesian Plane? (-4, -7) (7, 11) (5, -1) (-5, 1) ✓ Correct The first quadrant is defined to be all points in the Cartesian plane whose coordinates are both positive. 	1/1 point
 3. Let A, B, C, D be points in the Cartesian Plane, and let the set S = {B, C, D} Suppose that the distances from A to B, C, D are 5.3, 2.1, and 11.75, respectively. Which of the following points is the nearest neighbor to the point A in the set S? ⊕ C ○ A ○ B ○ D ✓ Correct The distance from A to C is 2.1 and that is smaller than the distance from A to any other element of S. 	1/1 point
4. Find the distance between the points $A=(2,2)$ and $B=(-1,-2)$. 1 -25 26 5 Correct Recall that the distance between points (a,b) and (c,d) is $\sqrt{(c-a)^2+(d-b)^2}$. In this case we have: $\sqrt{(-1-2)^2+(-2-2)^2}=\sqrt{(-3)^2+(-4)^2}=\sqrt{25}=5$	1/1 point

5.	Find the slope	of the line	e seament l	setween the	e points A =	-(0.1)	and $R =$	(1.00)

1/1 point

O 1

 $\bigcirc \sqrt{2}$

0 0

✓ Correct

The slope of this line segment is $egin{array}{c} 0-1 \\ 1-0 \end{array} = -1$

6. Find the point-slope form of the equation of the line with slope -2 that goes through the point (5,4).

1/1 point

O (5,4)

y - 4 = -2(x - 5)

y - 4 = 2(x - 5)

y - 5 = -2(x - 4)

✓ Correct

The point-slope form for the equation of a line with slope m that goes through the point (x_0,y_0) is $y-y_0=m(x-x_0)$.

In this case, the slope m=-2 is given and the point (5,4) on the line is given.

7. Which of the following equations is for a line with the same slope as y=-3x+2?

1/1 point

$$\bigcirc \ y=5x+2$$

$$y = -3x − 8$$

$$\bigcirc y = 5x$$

$$\bigcirc \ y = 8x - 3$$

✓ Correct

The slope-intercept formula for a line is y=mx+b, where m is the slope and b is the y-coordinate of the point where the line hits the y-axis.

This line has slope m=-3 which is the same slope as the given line.

8. Which of the following equations is for a line with the same y-intercept as y = -3x + 2?

1/1 point

$$\bigcirc \ y = -3x - 8$$

(i)
$$y = 5x + 2$$

$$\bigcirc y = 8x - 3$$

$$\bigcirc y = 5x$$

✓ Correct

The the slope-intercept formula for a line is y = mx + b, where m is the slope and b is the y-coordinate of the point where the line hits the y-axis. This line has a y-intercept of 2 which is the same as the given line.

9.	How many	lines contain	both the point	A = (1.1)) and the point	$B = (2, 2)^2$

1/1 point

O infinitely many

 \bigcirc 2

O None

✓ Correct

The line with equation y=x is the one and only line that meets the stated requirements.

10. Suppose that we have two sets, $A=\{a,b\}$ and $Z=\{x,y\}$. How many different functions $F:A\to Z$ are possible?

1 / 1 point

() There are infinitely many

⊕ 4

() I

○ There are none

✓ Correct

A function $F:A \to Z$ is a rule which assigns an element $F(a) \in Z$ to each element $a \in A$.

There are two elements in A; namely, α and δ . For each of these elements, there are two assignment choices we could make: x and y.

Here are the four possible functions:

$$F(a) = x, F(b) = y, OR$$

$$F(a) = y, F(b) = x, OR$$

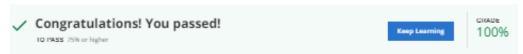
$$F(a) = x, F(b) = x, OR$$

$$F(a) = y, F(b) = y.$$

11. How many graphs contain both the point $A=(0,0)$ and the point $B=(1,1)$	1/1 point
1 2 None Infinitely marry	
\checkmark Correct The graphs of $f(x)=x, g(x)=x^2, h(x)=x^3, s(x)=x^4, \ldots$ all contain both A and B	
 12. Suppose that g: R → R is a continuous function whose graph intersects the x-axis more than once. Which of the following statements is true? g is neither strictly increasing nor strictly decreasing. g is strictly decreasing. All of the above. g is strictly increasing. 	1/1 point
Correct The function g fails the horizontal line test, so it can neither be strictly increasing nor strictly decreasing.	
13. Find the slope of the line segment between the points $A=(1,1)$ and $B=(5,3)$.	1/1 point
\checkmark Correct The slope of this line segment is $\frac{3-1}{5-1}=\frac{1}{2}$, where $3-1$ is the rise and $5-1$ is the run.	

WEEK 3

This is about that derivative stuff - Practice quiz on Tangent Lines to Functions (2 questions)



Practice quiz on Tangent Lines to Functions

TOTAL POINTS 2

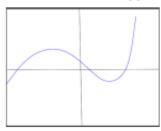
 Suppose that f: R→R is a function. Which of the following expressions corresponds to f'(2), the slope of the tangent line to the graph of f(x) at x = 2? 1/1 point

- $\bigcirc f'(2) = mx + b$
- f'(2) = 2
- $f'(2) = \lim_{h \to 0} \frac{f(a+h) f(a)}{h}$
- © $f'(2) = \lim_{h \to 0} \frac{f(2+h) f(2)}{h}$

 \checkmark Correct This expression can be obtained from the first screen of our video by plugging in 2 for α .

Suppose that h: R→R is a function whose graph is shown as the blue curve in the figure.
 For how many values of a is h'(a) = 0?

1/1 point



- 3
- O Never
- O Always
- ② 2

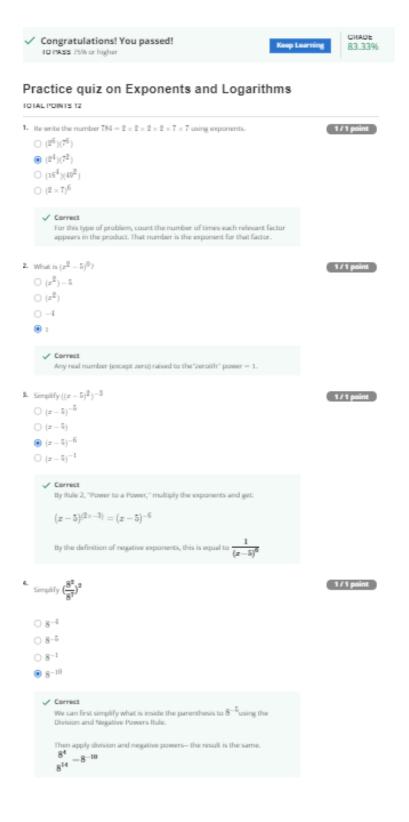
✓ Correct

h'(a) gives the slope of the tangent line to the graph of h at the point x=a.

When h'(a) = 0, this means that the tangent line is horizontal.

There are two places (one on each side of the y-axis) where this tangent line is horizontal, so this answer is correct.

• Fast Growth, Slow Growth - Practice quiz on Exponents and Logarithms (12 questions)



5. $\log 35 = \log 7 + \log x$ 1/1 point Salve for z O 4 O 28 ⊕ 5 0.7 \checkmark Correct $\log(x) = \log 35 - \log 7$ $log(x) = log(\frac{35}{7})$ By the Quotient Rule $\log x = \log 5$ 6. $\log_2(x^2 + 5x + 7) = 0$ 1/1 point Salve for x ⓐ x = -2 or x = -3 $\bigcirc x = 3$ $\bigcirc x = 2$ $\bigcirc \ x = 2 \text{ or } x = 3$ ✓ Correct We use the property that $b^{\log_2 a} - a$ Use both sides as exponent for 2. $2^{\log 2} x^2 + 5x + 7 = 2^0$ $x^2 + 5x + 7 = 1$ $x^2+5x+6=0$ (x+3)(x+2)=0 $x=-3\,\mathrm{or}$ x = -27. Simplify $\log_2 72 - \log_2 9$ 1/1 point \bigcirc $\log 2$ 63 ⊕ 3 \bigcirc 4 O log2 4 ✓ Correct By the quotient rule, this is $\log_2 \frac{72}{9} - \log_2 2^3 - 3$ 8. Simplify $\log 3.9 - \log 3.3 + \log 3.5$ 1/1 point O 15 log3 15 0.8 O log3 8 By the Quotient and Product Rules, this is $\log_3 \frac{9 \times 5}{3} = \log_3 15$

9. Simplify $\log_2(3^8 \times 5^7)$

- \bigcirc $(5 \times \log_2 3) + (8 \times \log_2 5)$
- $\bigcirc \ 15 \times \log 2 \ 56$
- 56 × logg 15
- \odot $(8 \times \log_2 3) + (7 \times \log_2 5)$

✓ Correct

We first apply the Product Rule to convert to the sum: $\log 2 \left(\frac{5^2}{2} \right) + \log 2 \left(\frac{5^2}{2} \right)$. Then apply the power and root rule.

10. If $log_{10} y = 100$, what is $log_{2} y = ?$

- ② 20
- O 301.63
- O 332.19
- O 500

! Incorrect

Use the change of base formula, $\log_{\alpha}b = \frac{\log_{\alpha}b}{\log_{\alpha}a}$

Where the "old" base is z and the "new" base is a.

$$50 \frac{100}{\log_{10}(2)} = \frac{100}{0.30103} = 332.19$$

11. A tree is growing taller at a continuous rate. In the past 12 years it has grown from 3 meters to 15 meters. What is its rate of growth per year? 0/1 point

1/1 point

0/1 point

- 10.41%
- O 12.41%
- O 18.41%
- O 11.41%

Incorrect ln 15/3 -0.1341

12. Bacteria can reproduce exponentially if not constrained. Assume a colony grows at a continually compounded rate of 460% per day. How many days before a colony with initial mass of 6.25 X 10⁻²⁰ grams weights 1000 Kilograms?

1/1 point

- 8.75 days
- 0.875 days
- O 87.5 days
- 875 days

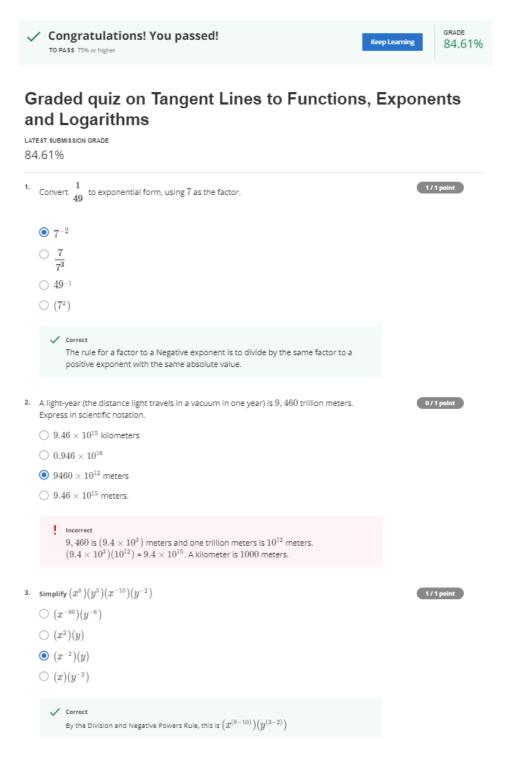
✓ Correct

$$6.25 \times 10^{-10} \times e^{4l} = 10^6$$

$$4t\!-\!\ln{(\frac{10^6}{(6.25\!\times\!10^{-10})})}\!-\!35.00878$$

$$t\!-\!\ln\!\frac{10^6}{6.25\!\times\!10^{-10}}\!-\!8.752195$$

• Fast Growth, Slow Growth - Graded quiz on Tangent Lines to Functions, Exponents and Logarithms (13 questions)



4. Simplify $[(x^4)(y^{-5})]^{-1}$ $\bigcirc \frac{(x^{-4})}{(y^0)}$ **③** $(x^{-4})(y^6)$

(y⁻⁰)

 $\bigcirc (x^3)(y^{-7})$

✓ Correct

By the Power to a Power Rule, each of the exponents is multiplied by (-1)

5. Solve for x:

 $\log_2(39x) - \log_2(x - 5) = 4$

○ 23 80

⊕ -80 23

O 39 23

○ 80 38

 \checkmark Correct $\frac{39x}{\log_2{(x-5)}}{=}4$ by the Quotient Rule.

Since both sides are equal, we can use them as exponents in an equation.

$$2^{\log 2} \frac{39x}{(x-5)} = 2^4$$

 $\frac{30x}{(x-5)} = 16$

 $39x = 16 \times (x - 5)$

39x = 16x - 80

23x=-80

 $x = \frac{-80}{23}$

6. Simplify this expression:

 $(x^{\frac{1}{2}})^{\frac{-3}{2}}$

 $O_{x^{\frac{1}{3}}}$

0 2 4

⊕ _x =³

 $\bigcirc \ x^{-1}$

✓ Correct We use the Power to a Power Rule — multiply exponents:

 $x^{\frac{1}{2} \times \frac{-3}{2}} = x^{\frac{-3}{4}}$

7- Simplify $\log_{10} 1000 + \log_{10} \frac{1}{10000}$

⊕ -1

 $\bigcirc \, \log_{10} -10$

0.1

01

By the Product Rule, this is:

 $\log_{10}(\frac{1000}{10000}) = \log_{10}(\frac{1}{10}) = -1$

1/1 point

1/1 point

1/1 point

1/1 point

- 0 5.216
- 0.4347
- 0.8934
- 1.304

. / Come

To convert from \log_3 to \log_9 , divide by $\log_3 9.$ Which is equal to 2 , so the answer is 1.34

- 9. If $\log_{10} b = 1.8$ and $\log_a b = 2.5752$, what is a?
 - \bigcirc 4
 - 06
 - 03
 - 5

✓ Correct

To solve for a in the formula;

$$\log_a b = \frac{\log_x b}{\log_x a}$$

 $\log_a b = 2.5752$ and $\log_{10} b = 1.8$

Therefore, $\log_{10} a$ must equal to $\dfrac{1.8}{2.5752} = 0.69897$

Treating both sides of equation $\log_{10}a=0.69897$ as exponents of 10 gives $a=10^{0.69897}=5$

- $^{10.}$ An investment of 1,600 is worth 7,400 after 8.5 years. What is the continuously compounded rate of return of this investment?
 - 18.02%
 - 0 20.01
 - O 19.01%
 - 0 17.01%

1/1 point

1/1 point

0.0002478

- $\bigcirc 0.02478$
- 0.2478
- 0.002478

Incorrect
$$e^{(0.24\times25)}=rac{1}{x}$$
 $x=rac{1}{(e^{0.24 imes25})}$ $x=rac{1}{403.4288}$ $x=?$ Try to rework the problem.

^{12.} $\log_2 z = 6.754$. What is $\log_{10}(z)$?

- 0.49185
- 0 1.3508
- ② 2.03316
- 0.82956

$$\begin{array}{l} \checkmark \text{ } \frac{\text{Correct}}{\log_2 z} \\ \log_2 10 = \\ \\ (\log_{10} z) \times (\log_2 10) = 3.321928 \\ \\ \text{Therefore, } \log_{10} z = \frac{6.754}{3.321928} = 2.03316 \end{array}$$

 Suppose that g: R→R is a function, and that g(1) = 10. Suppose that g'(a) is negative for every single value of a.Which of the following could possibly be g(1.5)? 1/1 point

1/1 point

$$(0.5) = 9.7$$

$$\bigcirc$$
 g(1.5) = 103.4

$$\bigcirc$$
 g(1.5) = 10.1

$$\bigcirc g(1.5) = 11$$

✓ Correc

Since the slope of the tangent line to the graph of g is negative everywhere on the graph, we know that g is *decreasing* function! And therefore we must have g(1.5) < g(1). That is the case here, so this value is at least possible.

WEEK 4

• Basic Probability Definitions - Practice quiz on Probability Concepts (9 questions)



5.	I don't know what it means to be "ingenuous." What probability would I assign to the statement, "I am ingenuous OR I am not ingenuous"?	1/1 point
	O -1	
	O .5	
	O 0	
	\checkmark correct It is always the case, regardless of the content of the statement x, that $p(x$ or $\sim x) = 1$	
6.	A friend of mine circumscribes a circle inside a square, so that the diameter of the circle and the edge of the square are the same length. He asks me to close my eyes and pick a point at random inside the square. He says the probability that my point will also be inside the circle is $\frac{\pi}{4}$	1/1 point
	Is this correct?	
	Yes No	
	Correct Probabilities can be any real number between 0 and 1. They do not need to be rational numbers – a numerator that is a transcendental number like Pi is acceptable.	
	Note that the correct probability does not depend on the length r of the circle's radius. For a circle with any radius r to be circumscribed inside a square, the square must have sides each of length 2r. The area of the circle is Pi*r^2 and the area of the square is (2r)^2 = 4*r^2 = The probability of landing in a circle of area Pi*r^2 when it is known that one is in the area of the square is equal to the ratio of the area of the circle to the area of the square in which it is circumscribed, or Pi*r^2/4*r^2, which equals Pi/4.	
7.	The probability of drawing a straight flush (including a Royal Flush) in a five-card poker hand is 0.0000153908	1/1 point
	What is the probability of not drawing a straight flush?	
	○ .9996582672	
	○ .9999745688	
	.9999846092	
	○ .9967253809	
	\checkmark Correct $p(\sim x) = 1 - p(x)$	

8.	What is the probability that a fair, six-sided die will come up with a prime number? (Recall that prime numbers are positive integers other than 1 that are divisible only by themselves and 1) $\begin{array}{c} 1 \\ 3 \\ \hline \\ \frac{1}{2} \\ \hline \\ \\ \frac{1}{6} \\ \hline \\ \\ 2 \\ \\ \\ 3 \\ \end{array}$	1/1 point
	Correct $ \begin{tabular}{ll} \begin{tabular}{ll} \checkmark Correct \\ The faces with 2, 3 and 5 satisfy the condition – which makes 3 relevant outcomes \\ out of the "universe" of 6 outcomes = \begin{tabular}{ll} $\frac{3}{6}$ = $\frac{1}{2}$ \\ \end{tabular} $	
9.	The joint probability p (the die will come up 5, the next card will be a heart) Is equal to the joint probability: p (the next card will be a heart, the die will not come up 5) p (the next card will not come up 5, the next card will be a heart) p (the die will not come up 5, the next card will not be a heart) p (the next card will be a heart, the die will come up 5) $correct$ In joint probabilities, the order does not change the probability: $p(A, B) = p(B, A)$	1/1 point

• Problem Solving Methods - Practice quiz on Problem Solving (9 questions)



4	I have two coins. One is fair, and has a probability of coming up heads of .5. The
	second is bent, and has a probability of coming up heads of .75. If I toss each coin
	once, what is the probability that at least one of the coins will come up heads?

1/1 point

- 875
- O 1.8
- O .375
- O .625

✓ Correct

We apply the rule p(A or B or both)

- = 1 (p(-A)p(-B))
- -1-((1-.5)(1-.75))
- = 1 .125
- -.875

- O 110,000
- O 554,480
- \bigcirc 4,435,200
- ① 110

✓ Correct 11! g(-11 × 10 - 110

6. What is the probability that, in six throws of a die, there will be exactly one each of "I" "Z" "3" "4" "5" and "0"?

- O .00187220
- .01432110
- .01543210
- 0.01176210

Connect

There are 65-720 permutations where each face occurs exactly once.

There are $6 \times 6 \times 6 \times 6 \times 6 \times 6 = 46656$ total permutations of 6 throws.

The probability is therefore $\frac{720}{40056}$ = 0.01543210

1/1 point

1/1 point

7- On 1 day in 1898, there is a fire and the fire alarm rings.	1/1 point
On 1 day in 100, there is no fire and the fire alarm rings (false alarm)	
On 1 day in 10,000, there is a fire and the fire alarm does not ring (defective alarm).	
On 9,889 days out of 10,000, there is no fire and the fire alarm does not ring.	
If the fire alarm rings, what is the (conditional) probability that there is a fire?	
Written p(there is a fire fire alarm rings)	
○ 1.1%	
@ 9.09%	
○ 1.12% ○ 90.9%	
✓ Correct 10 days out of every 10,000 there is fire and the fire alarm rings.	
100 days out of every 10,000 there is no fire and the fire alarm rings.	
110 days out of every 10,000 the fire alarm rings.	
The probability that there is a fire, given that the fire alarm rings, is	
10 - 2.09%	
 On 1 day in 1000, there is a fire and the fire alarm rings. 	1/1 point
On 1 day in 100, there is no fire and the fire alarm rings (false alarm)	
On 1 day in 10,000, there is a fire and the fire alarm does not ring (defective alarm).	
On 9,889 days out of 10,000, there is no fire and the fire alarm does not ring.	
If the fine alarm does not ring, what is the (conditional) probability that there is a fine?	
p(there is a fire fire alarm does not ring)	
O 1.0001%	
⊕ 0.01011%	
O. 01000%	
O.18011%	
✓ Correct On (1 + 9,889) = 9,890 days out of every 10,000 the fire alarm does not ring.	
On 1 of those 10,000 days there is a fire.	
1 -0.01011%	
9890	
9. A group of 45 civil servents at the State Department are newly qualified to serve as Ambassadors to foreign governments. There are 22 countries that currently need Ambassadors. How many distinct groups of 22 people can the President promote to fill these jobs?	0/1 point
O \$\$4.1167 \times (10^12)	
8.2334 Virnes (10*12) 0 =1.06*(10*35)	
O =2.429*(10*-13)	
Incorrect	
(22)	
-45!/(22!)(22!)	
= 45! 23! × 22!	

• Applying Bayes Theorem and the Binomial Theorem - Practice quiz on Bayes Theorem and the Binomial Theorem (9 questions)

Practice quiz on Bayes Theorem and the Binomial Theorem

TOTAL POINTS 9

 A jewelry store that serves just one customer at a time is concerned about the safety of its isolated customers. 1/1 point

The store does some research and learns that:

- 10% of the times that a jewelry store is robbed, a customer is in the store.
- A jewelry store has a customer on average 20% of each 24-hour day.
- . The probability that a jewelry store is being robbed (anywhere in the world) is 1 in 2 million.

What is the probability that a robbery will occur while a customer is in the store?

- O 1 500000
- \bigcirc $\frac{1}{2000000}$
- $\frac{1}{5000000}$

✓ Correct

What is known is:

A: "a customer is in the store," P(A)=0.2

B: "a robbery is occurring," $P(B) = \frac{1}{2.000,000}$

 $P(a \text{ customer is in the store} \mid a \text{ robbery occurs}) = P(A \mid B)$

$$P(A \mid B) = 10\%$$

What is wanted:

 $P(a \text{ robbery occurs} \mid a \text{ customer is in the store}) = P(B \mid A)$

By the product rule:

$$P(B \mid A) = \frac{P(A, B)}{P(A)}$$

and
$$P(A,B) = P(A \mid B)P(B)$$

Therefore:

$$P(B \mid A) = \frac{P(A \mid B)P(B)}{P(A)} = \frac{(0.1) \binom{1}{200000}}{0.2} = \frac{1}{4000000}$$

ex.	act	ly:	Six	h	ea	ds:	ľ

1/1 point

- 0.021
- 0.187
- 0.2051
- 0.305

✓ Correct

By Binomial Theorem, equals

$$\binom{10}{6}\Big(0.5^{10}\Big)$$

$$= \left(\frac{10!}{4! \times 6!}\right) \left(\frac{1}{1024}\right) \\ = 0.2051$$

3. If a coin is bent so that it has a 40% probability of coming up heads, what is the probability of getting exactly 6 heads in 10 throws?

2. If I flip a fair coin, with heads and tails, ten times in a row, what is the probability that I will get

1/1 point

- 0.0974
- 0.1045
- 0.1115
- 0.1219

$$\binom{10}{6} \times 0.4^6 \times 0.6^4 = 0.1115$$

4. A bent coin has 40% probability of coming up heads on each independent toss. If I toss the coin ten times, what is the probability that I get at least 8 heads?

0 / 1 point

- 0.0123
- 0.0312
- 0.0213
- 0.0132

Incorrect

The answer is the sum of three binomial probabilities:

$$(\binom{10}{8} \times (0.4^8) \times (.6^2)) + (\binom{10}{9} \times (0.4^9) \times (0.6^1)) +$$

$$(\binom{10}{10}) \times (0.4^{10}) \times (0.6^{0})$$

5. Suppose I have a bent coin with a 60% probability of coming up heads. I throw the coin ten times and it comes up heads 8 times. What is the value of the "likelihood" term in Bayes' Theorem -- the conditional probability of the data given the parameter. 0.122885 0.043945 0.168835 0.120932 Bayesian "likelihood" --- the p(observed data | parameter) is p(8 of 10 heads | coin has p = .6 of coming up heads) $\binom{10}{8} \times (0.6^8) \times (0.4^2) = 0.120932$ 6. We have the following information about a new medical test for diagnosing cancer. Before any data are observed, we know that 5% of the population to be tested actually have Cancer. Of those tested who do have cancer, 90% of them get an accurate test result of "Positive" for cancer. The other 10% get a false test result of "Negative" for Cancer. Of the people who do not have cancer, 90% of them get an accurate test result of "Negative" for cancer. The other 10% get a false test result of "Positive" for cancer. What is the conditional probability that I have Cancer, if I get a "Positive" test result for Cancer? **Formulas in the feedback section are very long, and do not fit within the standard viewing window. Therefore, the font is a bit smaller and the word "positive test" has been abbreviated as PT. 0 9.5% O 67.9% 32.1% probability that I have cancer O 4.5% I still have a more than $\frac{2}{3}$ probability of not having cancer Posterior probability: p() actually have cancer [receive a "positive" Test) By Bayes Theorem: = (chance of observing a PT if I have cancer)(prior probability of having cancer)
(marginal likelihood of the observation of a PT)

= p(receiving positive test) has cancer p(has cancer before data is observed))
p(positive) has cancer p(has cancer) = p(positive) an cancer [s(no cancer)

- (90%)(5%) / ((90%)(5%) + (10%)(95%)

-32.1%

Before any data are observed, we know that 8% of the population to be tested actually have Cancer.

Of those tested who do have cancer, 90% of them get an accurate test result of "Positive" for cancer.

The other 10% get a false test result of "Negative" for Cancer.

Of the people who do not have cancer, 95% of them get an accurate test result of "Negative" for cancer.

The other 5% get a false test result of "Positive" for cancer.

What is the conditional probability that I have cancer, if I get a "Negative" test result for Cancer?

- O 99.1%
- .80%
- 88.2%
- 0.9%

```
Correct p(\operatorname{cancer} \mid \operatorname{negative test}) =
p(\operatorname{negative test} \mid \operatorname{Cancer}) p(\operatorname{Cancer})
p(\operatorname{negative test} \mid \operatorname{cancer}) p(\operatorname{negative test} \mid \operatorname{no cancer}) p(\operatorname{no cancer})
\frac{(10\%)(8\%)}{(10\%)(8\%) + (95\%)(92\%)}
\frac{0.8\%}{0.8\% + 87.4\%}
0.8\%
88.2\%
= 0.9\%
```

 An urn contains 50 marbles – 40 blue and 10 white. After 50 draws, exactly 40 blue and 10 white are observed.

You are not told whether the draw was done "with replacement" or "without replacement."

What is the probability that the draw was done with replacement?

- 0 1
- O 87.73%
- 12.27%
- O 13.98%



p(40 blue and 10 white | draws without replacement) = 1 [this is the only possible outcome when 50 draws are made without replacement]

p(40 blue and 10 white | draws with replacement)

$$S = 40$$

N = 50

P = .8 [for draws with replacement] because 40 blue of 50 total means p(blue) = 40/50 = .8

$$\binom{50}{40}$$
 $\binom{50}{10}$ $\binom{50}{10}$ $\binom{50}{10}$

$$= 13.98\%$$

By Bayes' Theorem:

p(draws with replacement | observed data) =

$$\frac{13.98\%(.5)}{(13.98\%)(.5)+(1)(.5)}$$

$$=\frac{0.1398}{1.1398}$$

$$=12.27\%$$

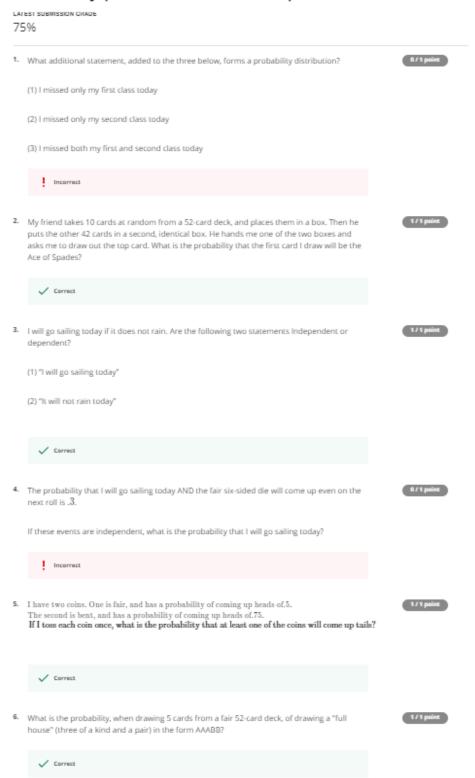
9.	According to Department of Customs Enforcement Research: 99% of people crossing into the United States are not smugglers.
	The majority of all Smugglers at the border (65%) appear nervous and sweaty.
	Only 8% of innocent people at the border appear nervous and sweaty.
	If someone at the border appears nervous and sweaty, what is the probability that they are a Smuggler?
	○ 8.57%
	● 7.58%
	○ 92.42%
	○ 7.92%
	✓ Correct
	By Bayes' Theorem, the answer is
	$\frac{(.65)(.01)}{((.65)(.01) + (.08)(.99))}$

=7.58%

1/1 point

 Applying Bayes Theorem and the Binomial Theorem - Probability (basic and Intermediate) Graded Quiz (12 questions)

Probability (basic and Intermediate) Graded Quiz



7.	If it rains, I do not go sailing. It rains 10% of days; I go sailing 3% of days.	1/1 point
	If it does not rain, what is the (conditional) probability that I go sailing?	
	Written *p(I go sailing it does not rain)*?	
	✓ Correct	
8.	I am at my office AND not working 2% of the time. I am at my office 10% of the time. What is the conditional probability that I am not working, if I am at my office?	1/1 point
	✓ Correct	
9.	The factory quality control department discovers that the conditional probability of making a manufacturing mistake in its precision ball bearing production is 4% on Tuesday, 4% on Wednesday, 4% on Thursday, 8% on Monday, and 12% on Friday.	1/1 point
	The Company manufactures an equal amount of ball bearings (20%) on each weekday. What is the probability that a defective ball bearing was manufactured on a Friday?	
	✓ Correct	
10.	An Urn contains two white marbles and one black marble. A marble is drawn from the Urn without replacement and put aside without my seeing it. Then a second marble is drawn, and it is white.	1/1 point
	What is the probability that the unknown removed marble is white, and what is the probability that it is black?	
	✓ Correct	
11.	What is the probability, if I flip a fair coin with heads and tails ten times in a row, that I get at least 8 heads?	0/1 point
	Incorrect	
12.	Suppose I have either a fair coin or a bent coin, and I don't know which. The bent coin has a 60% probability of coming up heads.	1/1 point
	I throw the coin ten times and it comes up heads 8 times. What is the probability I have the fair coin vs. the probability I have the bent coin?	
	Assume at the outset there is an equal $(.5,.5)$ prior probability of either coin. *Please note that in order to fit the entire formula in the feedback, probability has been abbreviated to "prob."	
	✓ Correct	