

CH 5120: Modern Control Theory

Project 2

Team project with 4 person per team

Implement MPC for various cases mentioned below to control the level of four tanks present in the quadruple tank process mentioned in project 1 (Kalman filter). Use the linearized discrete state space model used in project 1.

- h_1, h_2, h_3, h_4 are the levels of the respective tanks.
- K_c value is 1(V/cm).
- Assume the initial state values as $[12.4 \ 12.7 \ 1.8 \ 1.4]^T$ in the order h_1, h_2, h_3, h_4 respectively for the Kalman filter and the plant model.
- $T_s = 0.1s$.
- The constraints are
 - $DU_{min} = 5 * [-1 \ -1]^T$;
 - $DU_{max} = 5 * [1 \ 1]^T$;
 - $U_{min} = 0 * [-1 \ -1]^T$;
 - $U_{max} = 20 * [1 \ 1]^T$;
- Add appropriate integrated white noise as state noise and white noise as measurement noise in plant model and implement the Kalman filter from project 1 as estimator.
- Use only the commands mentioned in the lectures. Do not use any MATLAB Toolbox.
- Submit the MATLAB simulation file and a pdf of your report with necessary plots (max of 10 pages) before the deadline.

a) Implement Constraint MPC to control

- a. Case 1: h_1, h_2 when h_3, h_4 are measured; set-point for $[h_1 \ h_2]$ is $[13.4 \ 13.7]$
- b. Case 2: h_3, h_4 when h_1, h_2 are measured; set-point for $[h_3 \ h_4]$ is $[2.8 \ 2.4]$
- c. Case 3: h_1, h_2 when h_1, h_2 are measured; set-point for $[h_1 \ h_2]$ is $[13.4 \ 13.7]$
- d. Case 4: h_3, h_4 when h_3, h_4 are measured; set-point for $[h_3 \ h_4]$ is $[2.8 \ 2.4]$

- i) Comment on the MPC performance when used to control the above four cases.
 - ii) Do you see good control performance in all these cases?
 - iii) If there are performance deteriorations between cases, is it due to Kalman filter performance or MPC performance?
 - iv) Experiment few ways you improve the overall performance and report the same
- b) Report the effect of changes in control horizon and prediction horizon on the MPC performance for Case 3 and Case 4.
 - c) Implement Constraint MPC such that it can be used to control
 - a. h_2, h_3 when h_1, h_4 are measured with set-point for $[h_2 \ h_3]$ is $[13.7 \ 2.8]$
 - b. h_1, h_3 when h_2, h_4 are measured with set-point for $[h_1 \ h_3]$ is $[13.7 \ 2.4]$

Comment if the MPC is able to achieve set point tracking along with reason if required.

Note: if any assumptions made, mention them clearly along with the reason.