

## When to use regression?

If target variable is a continuous numeric variable (100–2000), then use a regression algorithm.

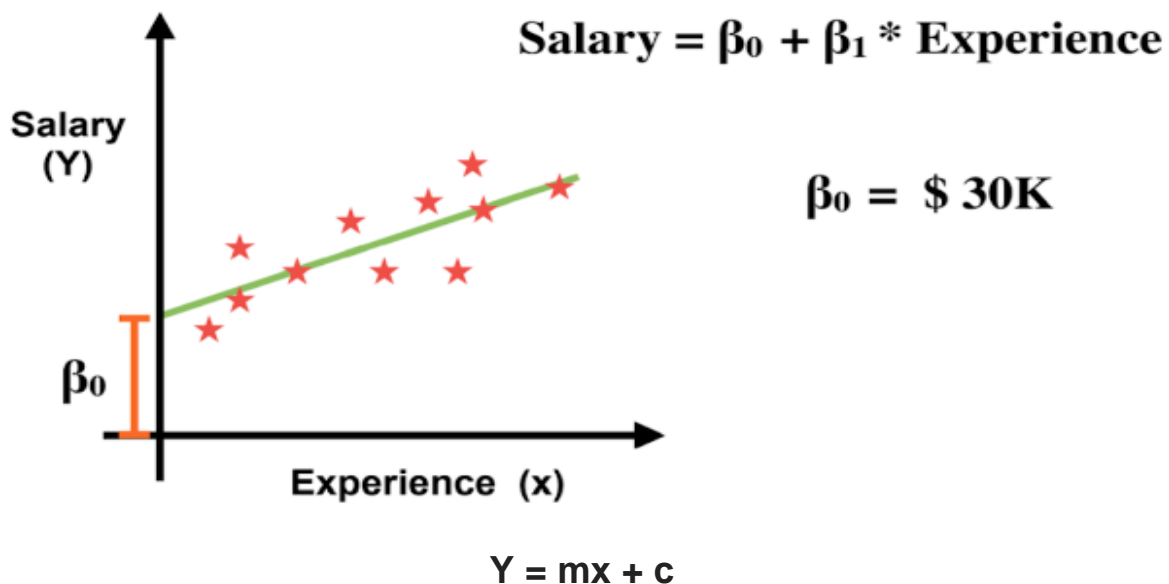
### Types of Regression Algorithms:

- Linear regression
- Multiple linear regression
- Polynomial regression
- Ridge regression
- Lasso regression
- ElasticNet regression

## Linear Regression

Linear Regression is a statistical model used to predict the relationship between independent and dependent variables denoted by  $x$  and  $y$  respectively

**Simple Linear Regression** is where only one independent variable is present and the model has to find the linear relationship of it with the dependent variable



## Performance Metrics for Regression Problem

**Error** = Y (actual) – Y (predicted)

### Mean Absolute Error (MAE)

$$\text{MAE} = \frac{1}{N} \sum_{i=1}^N |y_i - \hat{y}_i|$$

*Where,*

*N = total number of data points*

*Y<sub>i</sub> = actual value*

*Ŷ<sub>i</sub> = predicted value*

**the lower the MAE, the less error in your model.**

## Mean Squared Error (MSE)

$$\text{MSE} = \frac{1}{n} \sum_{i=1}^n (y_i - \hat{y}_i)^2$$

Where,

$n$  = total number of data points

$Y_i$  = actual value

$\hat{Y}_i$  = predicted value

Thus, as with MAE, the lower the MSE, the less error in the model.

## Root Mean Squared Error (RMSE)

$$\text{RMSE} = \sqrt{\sum_{i=1}^n \frac{(\hat{y}_i - y_i)^2}{n}}$$

Where,

$n$  = total number of data points

$Y_i$  = actual value

$\hat{Y}_i$  = predicted value

**lower RMSE → lower error.**

## R-Squared ( $R^2$ )

The  $R^2$  metric gives an indication of how well a model fits your data, but is unable to explain if your model is good or not.

$$R^2 = 1 - \frac{\sum (y_i - \hat{y}_i)^2}{\sum (y_i - \bar{y}_i)^2}$$

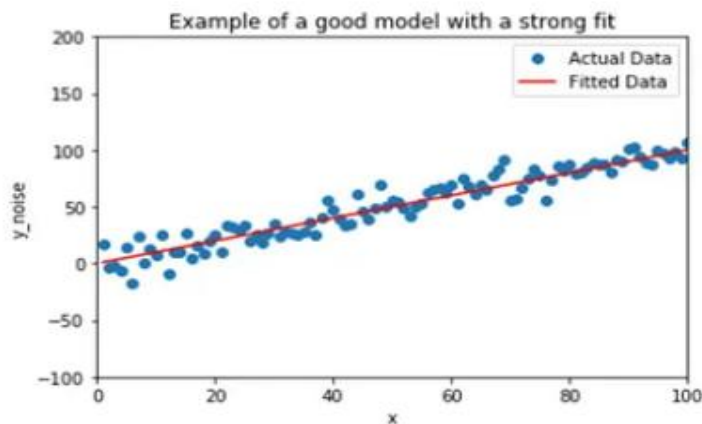
$y$  = dependent variable values,  $\hat{y}$  = predicted values from model,  $\bar{y}$  = the mean of  $y$

The  $R^2$  value ranges from 0 to 1, with higher values denoting a strong fit, and lower values denoting a weak fit. Typically, it's agreed that:

$R^2 < 0.5 \rightarrow$  Weak fit

$0.5 \leq R^2 \leq 0.8 \rightarrow$  Moderate fit

$R^2 > 0.8 \rightarrow$  Strong fit



$R^2 = 0.9186211060937284$

## Multiple Linear Regression:

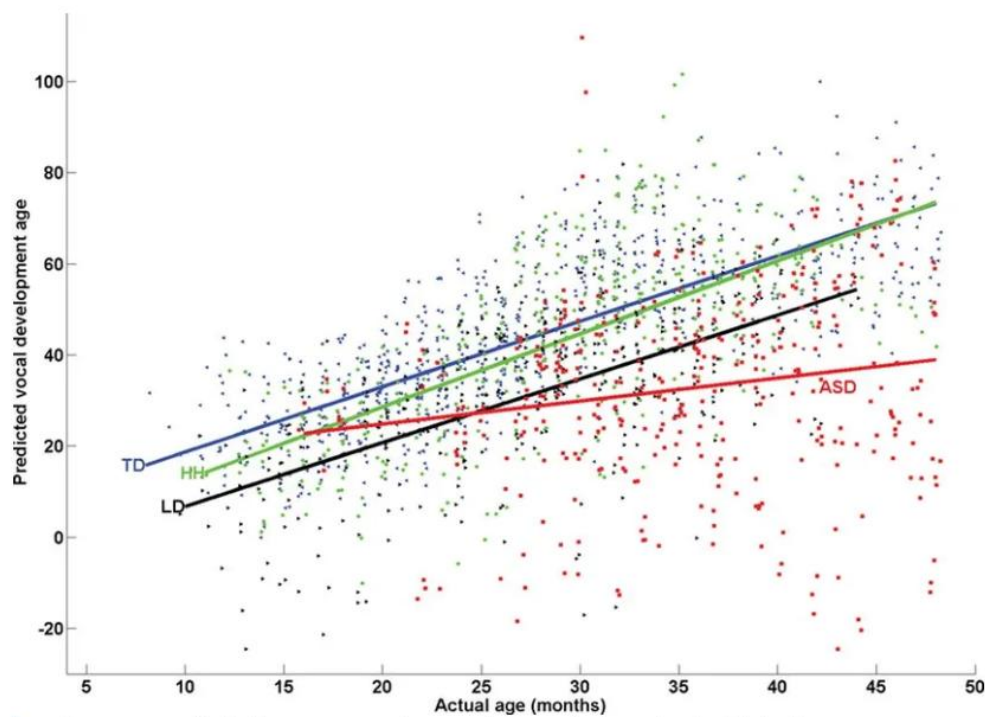
Multiple Linear Regression is one of the important regression algorithms, which models the linear relationship between a single dependent continuous variable and more than one independent variable.

Equation for MLR

$$Y = m_1 * x_1 + m_2 * x_2 + m_3 * x_3 + \dots + m_n * x_n + c$$

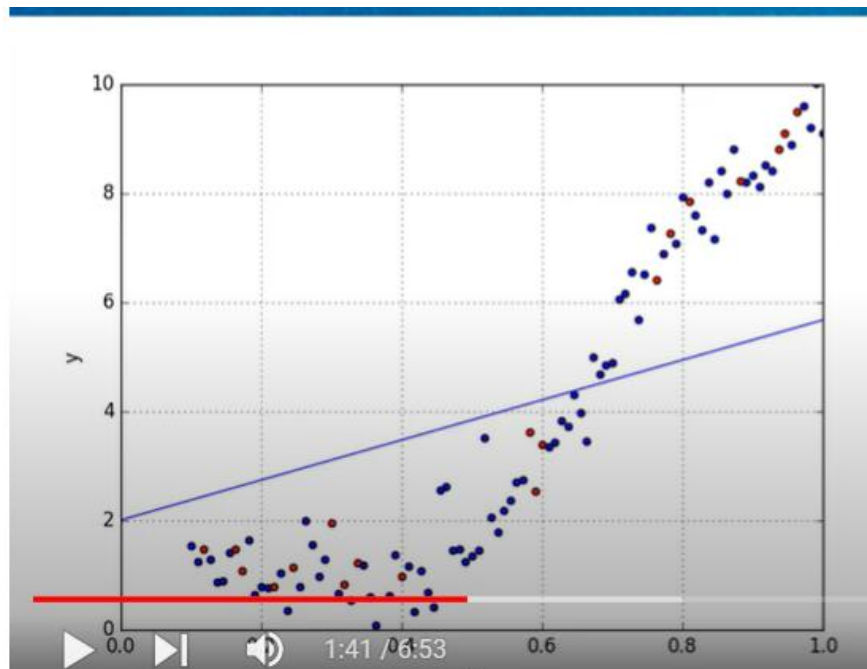
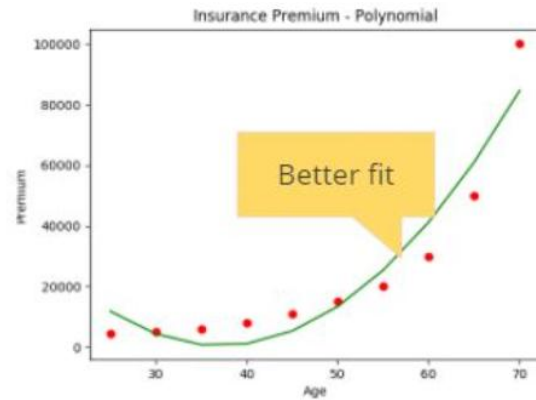
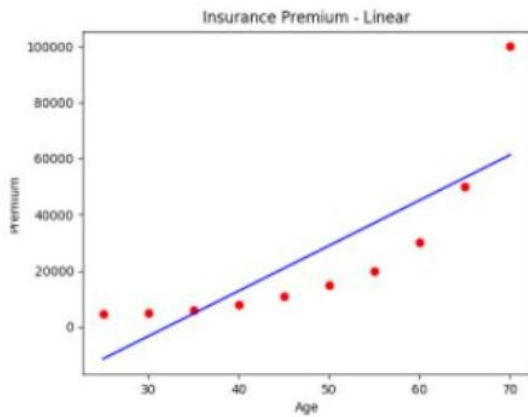
Diagram illustrating the components of the Multiple Linear Regression equation:

- $Y$ : Dependent Variable
- $m_1, m_2, m_3, \dots, m_n$ : Slopes
- $c$ : Coefficient



### ***Polynomial Regression:***

It is a form of regression analysis in which the relationship between the independent variables and dependent variables are modeled in the **nth degree polynomial**.



Simple  
Linear  
Regression

$$y = b_0 + b_1x_1$$

Multiple  
Linear  
Regression

$$y = b_0 + b_1x_1 + b_2x_2 + \dots + b_nx_n$$

Polynomial  
Linear  
Regression

$$y = b_0 + b_1x_1 + b_2x_1^2 + \dots + b_nx_1^n$$

Polynomials	Form	Degree	Examples
Linear Polynomial	$p(x): ax+b, a \neq 0$	Polynomial with Degree 1	$x + 8$
Quadratic Polynomial	$p(x): ax^2+b+c, a \neq 0$	Polynomial with Degree 2	$3x^2-4x+7$
Cubic Polynomial	$p(x): ax^3+bx^2+cx, a \neq 0$	Polynomial with Degree 3	$2x^3+3x^2+4x+6$

It does not require the relationship between the independent and dependent variables to be linear in the data set.