

ARIMA Model – Complete Guide to Time Series Forecasting in Python

Using ARIMA model, you can forecast a time series using the series past values. In this post, we build an optimal ARIMA model from scratch and extend it to Seasonal ARIMA [SARIMA] and SARIMAX models. You will also see how to build autoarima models in python



ARIMA Model – Time Series Forecasting. Photo by Cerquiera

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1. Introduction to Time Series Forecasting

A time series is a sequence where a metric is recorded over regular time intervals.

Depending on the frequency, a time series can be of yearly (ex: annual budget), quarterly (ex: expenses), monthly (ex: air traffic), weekly (ex: sales qty), daily (ex: weather), hourly (ex: stocks price), minutes (ex: inbound calls in a call center) and even seconds wise (ex: web traffic).

We have already seen the steps involved in a previous post on ~~Time Series Analysis~~ (<https://www.machinelearningplus.com/time-series-analysis-python>). If you haven't read it, I highly encourage you to do so.

Forecasting is the next step where you want to predict the future values the series is going to take.

But why forecast?

Because, forecasting a time series (like demand and sales) is often of tremendous commercial value.

In most manufacturing companies, it drives the fundamental business planning, procurement and production activities. Any errors in the forecasts will ripple down throughout the supply chain or any business context for that matter. So it's important to get the forecasts accurate in order to save on costs and is critical to success.

Not just in manufacturing, the techniques and concepts behind time series forecasting are applicable in any business.

Now forecasting a time series can be broadly divided into two types.

If you use only the previous values of the time series to predict its future values, it is called **Univariate Time Series Forecasting**.

And if you use predictors other than the series [a.k.a exogenous variables] to forecast it is called **Multi Variate Time Series Forecasting**.

This post focuses on a particular type of forecasting method called **ARIMA** modeling.

ARIMA, short for 'AutoRegressive Integrated Moving Average', is a forecasting algorithm based on the idea that the information in the past values of the time series can alone be used to predict the future values.

2. Introduction to ARIMA Models

So what exactly is an ARIMA model?

ARIMA, short for 'Auto Regressive Integrated Moving Average' is actually a class of models that 'explains' a given time series based on its own past values, that is, its own lags and the lagged forecast errors, so that equation can be used to forecast future values.

Any 'non-seasonal' time series that exhibits patterns and is not a random white noise can be modeled with ARIMA models.

An ARIMA model is characterized by 3 terms: p , d , q

where,

p is the order of the AR term

q is the order of the MA term

d is the number of differencing required to make the time series stationary

If a time series, has seasonal patterns, then you need to add seasonal terms and it becomes SARIMA, short for 'Seasonal ARIMA'. More on that once we finish ARIMA.

So, what does the 'order of AR term' even mean? Before we go there, let's first look at the 'd' term.

3. What does the p, d and q in ARIMA model mean

The first step to build an ARIMA model is to ~~make the time series stationary~~ (<https://www.machinelearningplus.com/stationary-time-series>).

Why?

Because, term 'Auto Regressive' in ARIMA means it is a linear regression model (<https://www.machinelearningplus.com/machine-learning/complete-introduction-linear-regression-r/>), that uses its own lags as predictors. Linear regression models, as you know, work best when the predictors are not correlated and are independent of each other.

So how to make a series stationary?

The most common approach is to difference it. That is, subtract the previous value from the current value. Sometimes, depending on the complexity of the series, more than one differencing may be needed.

The value of d, therefore, is the minimum number of differencing needed to make the series stationary. And if the time series is already stationary, then $d = 0$.

Next, what are the 'p' and 'q' terms?

'p' is the order of the 'Auto Regressive' [AR] term. It refers to the number of lags of Y to be used as predictors. And 'q' is the order of the 'Moving Average' [MA] term. It refers to the number of lagged forecast errors that should go into the ARIMA Model.

4. What are AR and MA models

So what are AR and MA models? what is the actual mathematical formula for the AR and MA models?

A pure **Auto Regressive [AR only] model** is one where Y_t depends only on its own lags. That is, Y_t is a function of the 'lags of Y_t '.

$$Y_t = \alpha + \beta_1 Y_{t-1} + \beta_2 Y_{t-2} + \dots + \beta_p Y_{t-p} + \epsilon_t$$

(<https://www.machinelearningplus.com/wp-content/uploads/2019/02/Equation-1-min.png>).

where, Y_{t-1} is the lag1 of the series, β_1 is the coefficient of lag1 that the model estimates and α is the intercept term, also estimated by the model.

Likewise a pure **Moving Average [MA only] model** is one where Y_t depends only on the lagged forecast errors.

$$Y_t = \alpha + \epsilon_t + \phi_1 \epsilon_{t-1} + \phi_2 \epsilon_{t-2} + \dots + \phi_q \epsilon_{t-q}$$

(<https://www.machinelearningplus.com/wp-content/uploads/2019/02/Equation-2-min.png>).

where the error terms are the errors of the autoregressive models of the respective lags. The errors ϵ_t and ϵ_{t-1} are the errors from the following equations :

$$Y_t = \beta_1 Y_{t-1} + \beta_2 Y_{t-2} + \dots + \beta_0 Y_0 + \epsilon_t$$

$$Y_{t-1} = \beta_1 Y_{t-2} + \beta_2 Y_{t-3} + \dots + \beta_0 Y_0 + \epsilon_{t-1}$$

[<https://www.machinelearningplus.com/wp-content/uploads/2019/02/Equation-3-min.png>]

[Error: The beta coefficients in the second equation above is incorrect.]

That was AR and MA models respectively.

So what does the equation of an ARIMA model look like?

An ARIMA model is one where the time series was differenced at least once to make it stationary and you combine the AR and the MA terms. So the equation becomes:

$$Y_t = \alpha + \beta_1 Y_{t-1} + \beta_2 Y_{t-2} + \dots + \beta_p Y_{t-p} + \epsilon_t + \phi_1 \epsilon_{t-1} + \phi_2 \epsilon_{t-2} + \dots + \phi_q \epsilon_{t-q}$$

[<https://www.machinelearningplus.com/wp-content/uploads/2019/02/Equation-4-min.png>]

ARIMA model in words:

Predicted Y_t = Constant + Linear combination Lags of Y (upto p lags) + Linear Combination of Lagged forecast errors (upto q lags)

The objective, therefore, is to identify the values of p, d and q. But how?

Let's start with finding the 'd'.

5. How to find the order of differencing [d] in ARIMA model

The purpose of differencing it to make the time series stationary.

But you need to be careful to not over-difference the series. Because, an over differenced series may still be stationary, which in turn will affect the model parameters.

So how to determine the right order of differencing?

The right order of differencing is the minimum differencing required to get a near-stationary series which roams around a defined mean and the ACF plot reaches to zero fairly quick.

If the autocorrelations are positive for many number of lags [10 or more], then the series needs further differencing. On the other hand, if the lag 1 autocorrelation itself is too negative, then the series is probably over-differenced.

In the event, you can't really decide between two orders of differencing, then go with the order that gives the least standard deviation in the differenced series.

Let's see how to do it with an example.

First, I am going to check if the series is stationary using the Augmented Dickey Fuller test [`adfuller()`], from the statsmodels package.

Why?

Because, you need differencing only if the series is non-stationary. Else, no differencing is needed, that is, $d=0$.

The null hypothesis of the ADF test is that the time series is non-stationary. So, if the p-value of the test is less than the significance level [0.05] then you reject the null hypothesis and infer that the time series is indeed stationary.

So, in our case, if P Value > 0.05 we go ahead with finding the order of differencing.


```
from statsmodels.tsa.stattools import adfuller
from numpy import log
result = adfuller(df.value.dropna())
print('ADF Statistic: %f' % result[0])
print('p-value: %f' % result[1])
```

```
ADF Statistic: -2.464240
p-value: 0.124419
```

Since P-value is greater than the significance level, let's difference the series and see how the autocorrelation plot looks like.

```
import numpy as np, pandas as pd
from statsmodels.graphics.tsaplots import plot_acf, plot_pacf
import matplotlib.pyplot as plt
plt.rcParams.update({'figure.figsize':(9,7), 'figure.dpi':120})

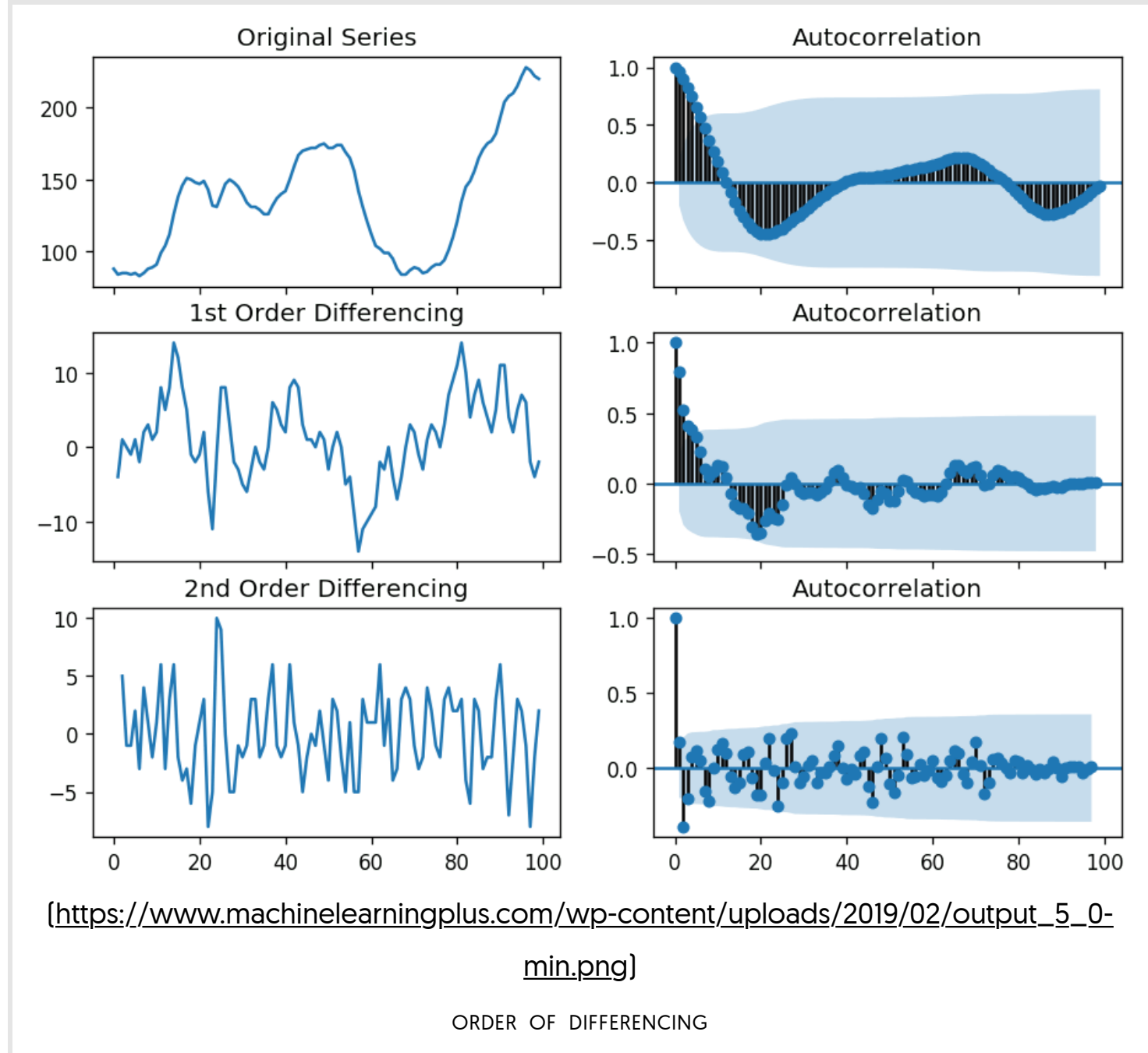
# Import data
df = pd.read_csv('https://raw.githubusercontent.com/selva86/datasets/master/wwwusage.csv')
df = df.rename(columns={'value': 'usage'})

# Original Series
fig, axes = plt.subplots(3, 2, sharex=True)
axes[0, 0].plot(df.value); axes[0, 0].set_title('Original Series')
plot_acf(df.value, ax=axes[0, 1])

# 1st Differencing
axes[1, 0].plot(df.value.diff()); axes[1, 0].set_title('1st Order Differencing')
plot_acf(df.value.diff().dropna(), ax=axes[1, 1])

# 2nd Differencing
axes[2, 0].plot(df.value.diff().diff()); axes[2, 0].set_title('2nd Order Differencing')
plot_acf(df.value.diff().diff().dropna(), ax=axes[2, 1])

plt.show()
```



For the above series, the time series reaches stationarity with two orders of differencing. But on looking at the autocorrelation plot for the 2nd differencing the lag goes into the far negative zone fairly quick, which indicates, the series might have been over differenced.

So, I am going to tentatively fix the order of differencing as 1 even though the series is not perfectly stationary (weak stationarity).

```

from pmdarima.arima.utils import ndiffs
df = pd.read_csv('https://raw.githubusercontent.com/selva86/datasets/master/www
usage.csv
(https://raw.githubusercontent.com/selva86/datasets/master/wwwusage.csv)',
names=['value'], header=0)
y = df.value

## Adf Test
ndiffs(y, test='adf') # 2

# KPSS test
ndiffs(y, test='kpss') # 0

# PP test:
ndiffs(y, test='pp') # 2

```

```
2 0 2
```

6. How to find the order of the AR term [p]

The next step is to identify if the model needs any AR terms. You can find out the required number of AR terms by inspecting the Partial Autocorrelation [PACF] plot.

But what is PACF?

Partial autocorrelation can be imagined as the correlation between the series and its lag, after excluding the contributions from the intermediate lags. So, PACF sort of conveys the pure correlation between a lag and the series. That way, you will know if that lag is needed in the AR term or not.

So what is the formula for PACF mathematically?

Partial autocorrelation of lag [k] of a series is the coefficient of that lag in the autoregression equation of Y.

$$Y_t = \alpha_0 + \alpha_1 Y_{t-1} + \alpha_2 Y_{t-2} + \alpha_3 Y_{t-3}$$

That is, suppose, if Y_t is the current series and Y_{t-1} is the lag 1 of Y , then the partial autocorrelation of lag 3 [Y_{t-3}] is the coefficient α_3 of Y_{t-3} in the above equation.

Good. Now, how to find the number of AR terms?

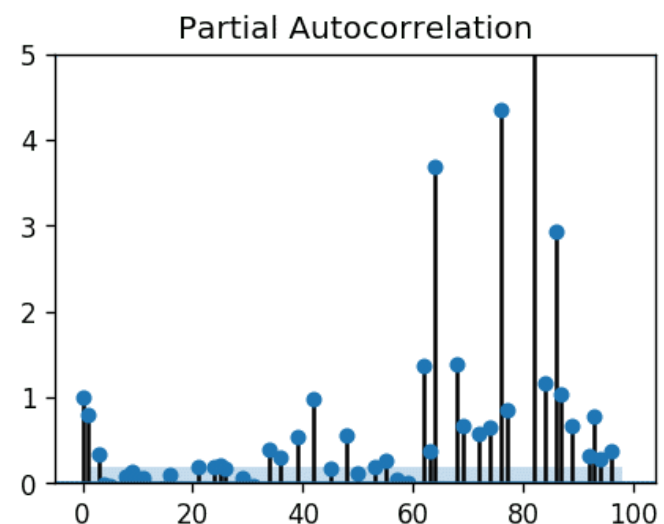
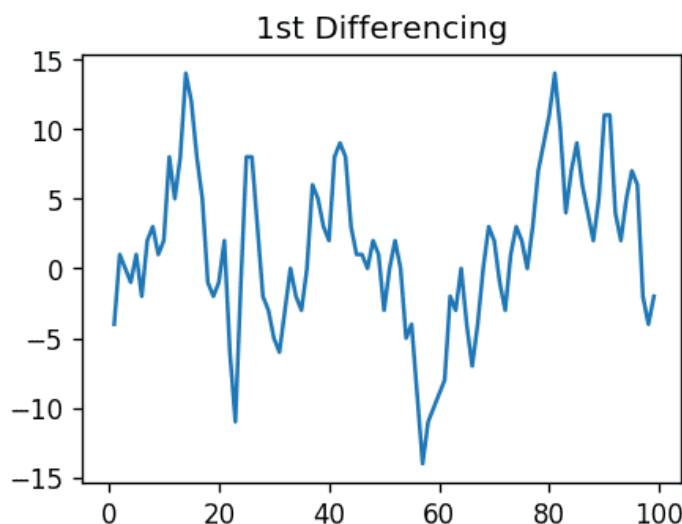
Any autocorrelation in a stationarized series can be rectified by adding enough AR terms. So, we initially take the order of AR term to be equal to as many lags that crosses the significance limit in the PACF plot.

```
# PACF plot of 1st differenced series
plt.rcParams.update({'figure.figsize':(9,3), 'figure.dpi':120})

fig, axes = plt.subplots(1, 2, sharex=True)
axes[0].plot(df.value.diff()); axes[0].set_title('1st Differencing')
axes[1].set(ylim=(0,5))
plot_pacf(df.value.diff().dropna(), ax=axes[1])

plt.show()
```

```
/Library/Frameworks/Python.framework/Versions/3.7/lib/python3.7/site-packages/statsmodels/regression/linear_model.py:1283: RuntimeWarning: invalid value encountered in sqrt
    return rho, np.sqrt(sigmasq)
```



You can observe that the PACF lag 1 is quite significant since is well above the significance line. Lag 2 turns out to be significant as well, slightly managing to cross the significance limit (blue region). But I am going to be conservative and tentatively fix the p as 1.

7. How to find the order of the MA term (q)

Just like how we looked at the PACF plot for the number of AR terms, you can look at the ACF plot for the number of MA terms. An MA term is technically, the error of the lagged forecast.

The ACF tells how many MA terms are required to remove any autocorrelation in the stationarized series.

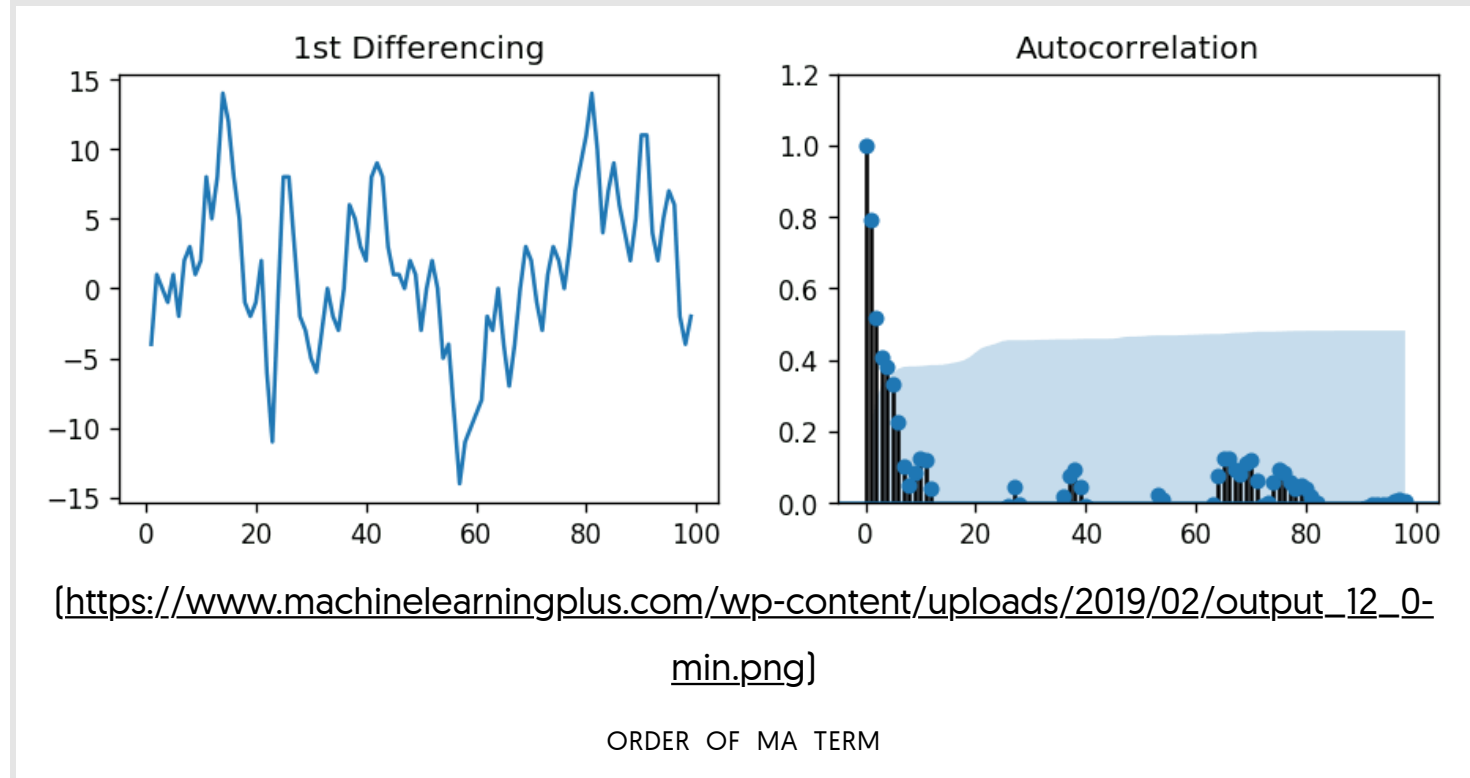
Let's see the autocorrelation plot of the differenced series.

```
import pandas as pd
from statsmodels.graphics.tsaplots import plot_acf, plot_pacf
import matplotlib.pyplot as plt
plt.rcParams.update({'figure.figsize':(9,3), 'figure.dpi':120})

# Import data
df = pd.read_csv('https://raw.githubusercontent.com/selva86/datasets/master/austa.csv')

fig, axes = plt.subplots(1, 2, sharex=True)
axes[0].plot(df.value.diff()); axes[0].set_title('1st Differencing')
axes[1].set(ylim=(0,1.2))
plot_acf(df.value.diff().dropna(), ax=axes[1])

plt.show()
```



Couple of lags are well above the significance line. So, let's tentatively fix q as 2. When in doubt, go with the simpler model that sufficiently explains the Y .

8. How to handle if a time series is slightly under or over differenced

It may so happen that your series is slightly under differenced, that differencing it one more time makes it slightly over-differenced.

How to handle this case?

If your series is slightly under differenced, adding one or more additional AR terms usually makes it up. Likewise, if it is slightly over-differenced, try adding an additional MA term.

9. How to build the ARIMA Model

Now that you've determined the values of p , d and q , you have everything needed to fit the ARIMA model. Let's use the `ARIMA()` implementation in `statsmodels` package.

```
from statsmodels.tsa.arima_model import ARIMA
```

```
# 1,1,2 ARIMA Model
```

```
model = ARIMA(df.value, order=(1,1,2))
```

```
model_fit = model.fit(dispatch=0)
```

```
print(model_fit.summary())
```


ARIMA Model Results

```

=====
Dep. Variable:          D.value    No. Observations:
99
Model:                  ARIMA(1, 1, 2)    Log Likelihood          -253.7
90
Method:                  css-mle    S.D. of innovations          3.119
Date:                    Wed, 06 Feb 2019    AIC          517.57
9
Time:                    23:32:56    BIC          530.555
Sample:                  1    HQIC          522.829

```

```

=====
==
coef      std err          z      P>|z|      [0.025      0.97
5]
-----
--
const      1.1202      1.290      0.868      0.387      -1.409      3.
649
ar.L1.D.value      0.6351      0.257      2.469      0.015      0.131      1.
139
ma.L1.D.value      0.5287      0.355      1.489      0.140      -0.167      1.
224
ma.L2.D.value     -0.0010      0.321     -0.003      0.998      -0.631      0.
629

```

Roots

```

=====
Real      Imaginary      Modulus      Frequen
cy
-----
AR.1      1.5746      +0.0000j      1.5746      0.0000
MA.1      -1.8850      +0.0000j      1.8850      0.5000
MA.2      545.3515      +0.0000j      545.3515      0.0000
-----

```

The model summary reveals a lot of information. The table in the middle is the coefficients table where the values under 'coef' are the weights of the respective terms.

Notice here the coefficient of the MA2 term is close to zero and the P-Value in 'P>|z|' column is highly insignificant. It should ideally be less than 0.05 for the respective X to be significant.

So, let's rebuild the model without the MA2 term.

```
# 1,1,1 ARIMA Model  
model = ARIMA(df.value, order=(1,1,1))  
model_fit = model.fit(dis=0)  
print(model_fit.summary())
```

ARIMA Model Results

```

=====
Dep. Variable:          D.value    No. Observations:
99
Model:                  ARIMA(1, 1, 1)    Log Likelihood          -253.7
90
Method:                  css-mle    S.D. of innovations          3.119
Date:                    Sat, 09 Feb 2019    AIC          515.57
9
Time:                    12:16:06    BIC          525.960
Sample:                  1    HQIC          519.779

```

```

=====
==
              coef    std err          z      P>|z|      [0.025    0.97
5]
-----
--
const          1.1205      1.286      0.871      0.386     -1.400      3.
641
ar.L1.D.value   0.6344      0.087      7.317      0.000      0.464      0.
804
ma.L1.D.value   0.5297      0.089      5.932      0.000      0.355      0.
705

```

Roots

```

=====
              Real          Imaginary      Modulus      Frequen
cy
-----
AR.1          1.5764          +0.0000j      1.5764      0.0000
MA.1          -1.8879          +0.0000j      1.8879      0.5000
-----

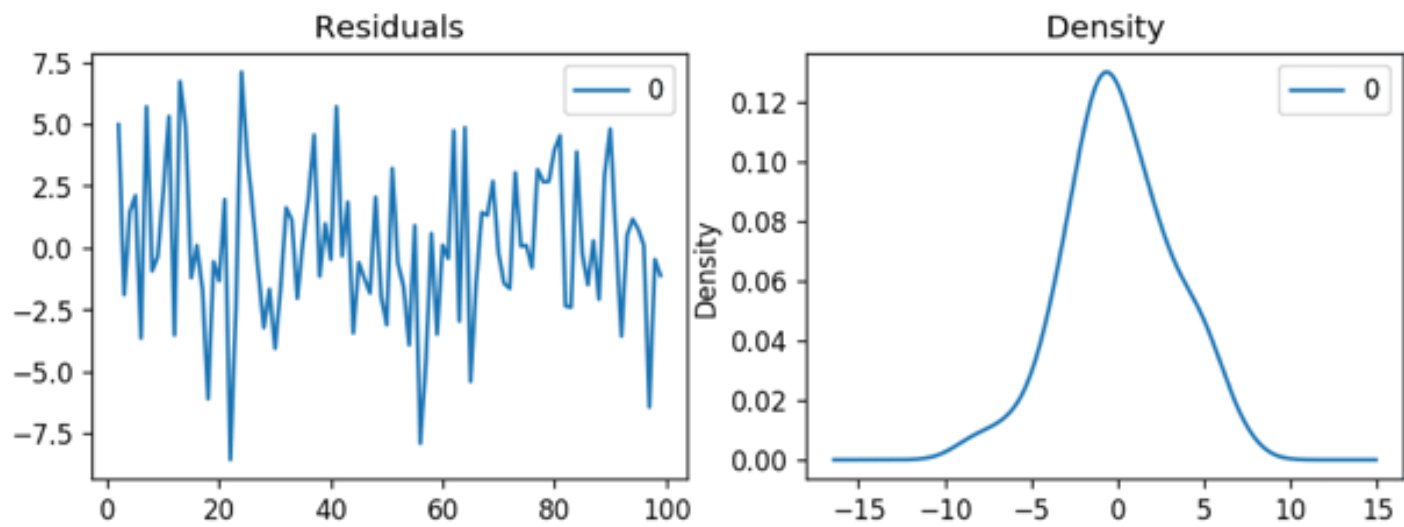
```

The model AIC has reduced, which is good. The P Values of the AR1 and MA1 terms have improved and are highly significant [< 0.05].

Let's plot the residuals to ensure there are no patterns [that is, look for constant mean and variance].

```
# Plot residual errors
```

```
residuals = pd.DataFrame(model_fit.resid)  
fig, ax = plt.subplots(1,2)  
residuals.plot(title="Residuals", ax=ax[0])  
residuals.plot(kind='kde', title='Density', ax=ax[1])  
plt.show()
```



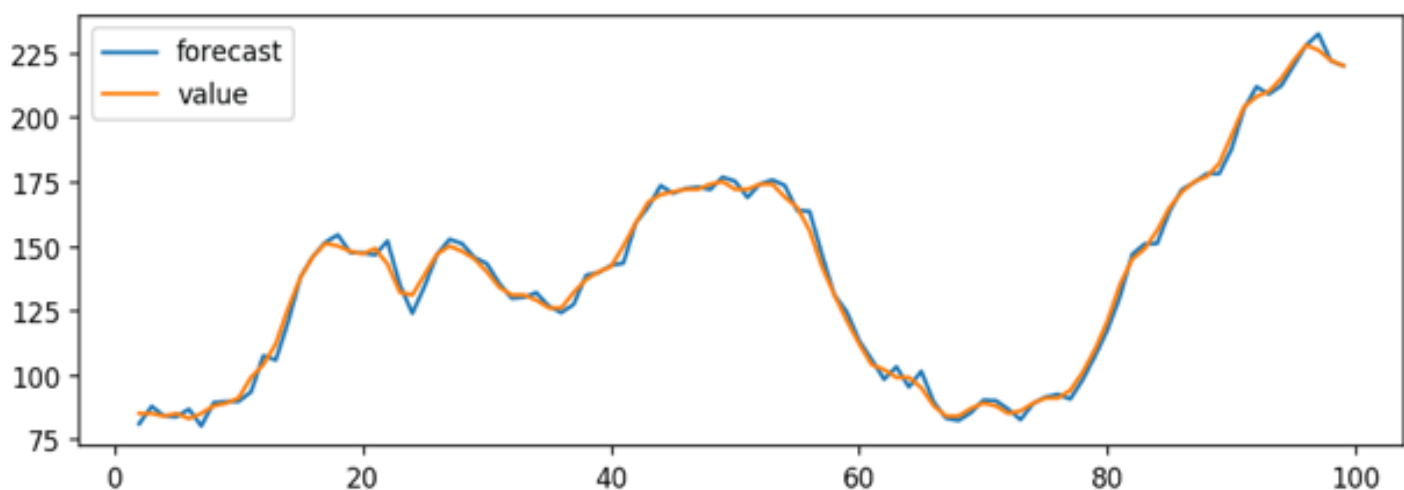
(https://www.machinelearningplus.com/wp-content/uploads/2019/02/output_20_0-min.png)

RESIDUALS DENSITY

The residual errors seem fine with near zero mean and uniform variance. Let's plot the actuals against the fitted values using `plot_predict()`.

```
# Actual vs Fitted
```

```
model_fit.plot_predict(dynamic=False)  
plt.show()
```



(https://www.machinelearningplus.com/wp-content/uploads/2019/02/output_22_0-min.png)

When you set `dynamic=False` the in-sample lagged values are used for prediction.

That is, the model gets trained up until the previous value to make the next prediction. This can make the fitted forecast and actuals look artificially good.

So, we seem to have a decent ARIMA model. But is that the best?

Can't say that at this point because we haven't actually forecasted into the future and compared the forecast with the actual performance.

So, the real validation you need now is the Out-of-Time cross-validation.

10. How to do find the optimal ARIMA model manually using Out-of-Time Cross validation

In Out-of-Time cross-validation, you take few steps back in time and forecast into the future to as many steps you took back. Then you compare the forecast against the actuals.

To do out-of-time cross-validation, you need to create the training and testing dataset by splitting the time series into 2 contiguous parts in approximately 75:25 ratio or a reasonable proportion based on time frequency of series.

Why am I not sampling the training data randomly you ask?

That's because the order sequence of the time series should be intact in order to use it for forecasting.

```
from statsmodels.tsa.stattools import acf
```

```
# Create Training and Test
```

```
train = df.value[:85]
```

```
test = df.value[85:]
```

You can now build the ARIMA model on training dataset, forecast and plot it.

```

# Build Model
# model = ARIMA(train, order=(3,2,1))
model = ARIMA(train, order=(1, 1, 1))
fitted = model.fit(dispatch=-1)

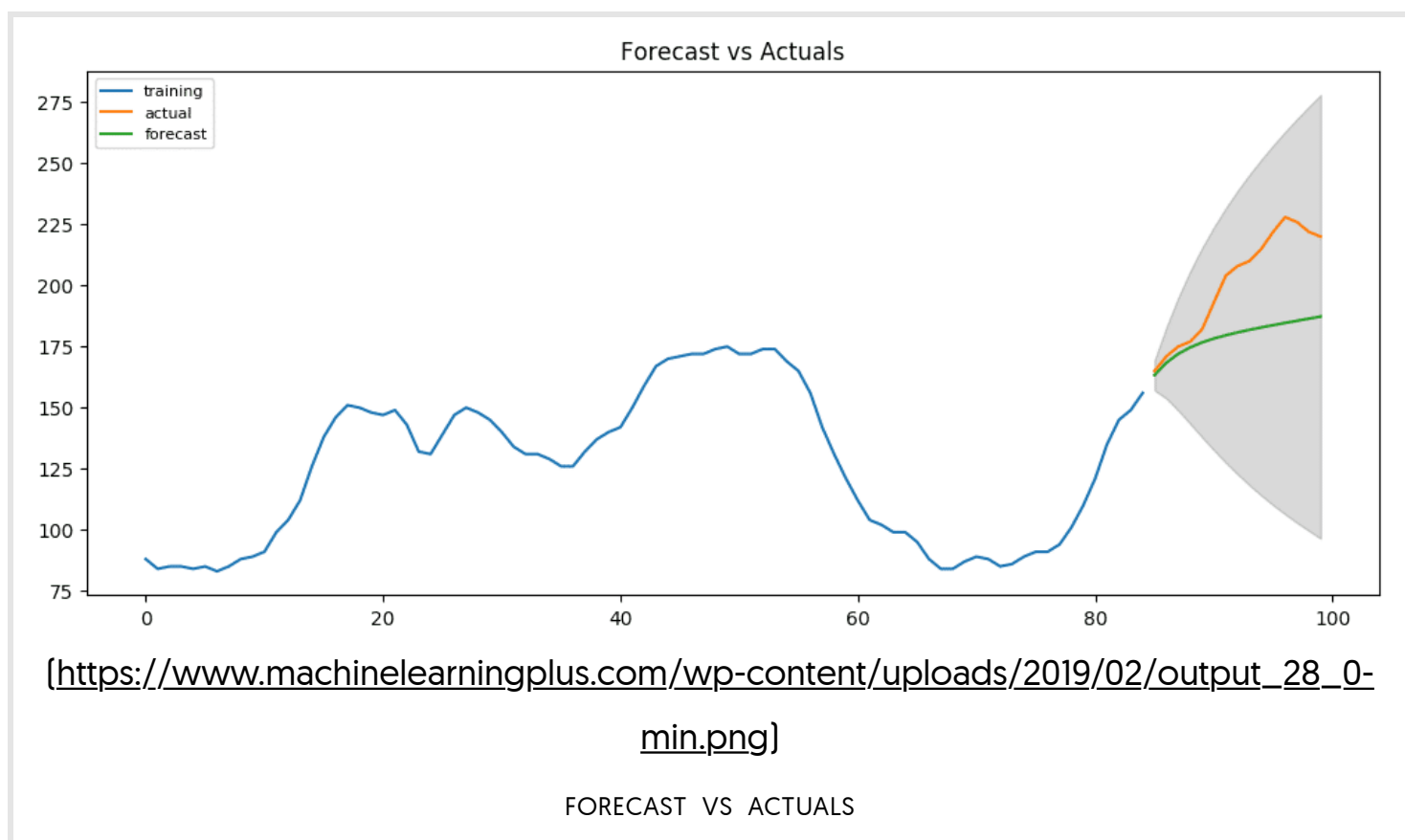
# Forecast
fc, se, conf = fitted.forecast(15, alpha=0.05) # 95% conf

# Make as pandas series
fc_series = pd.Series(fc, index=test.index)
lower_series = pd.Series(conf[:, 0], index=test.index)
upper_series = pd.Series(conf[:, 1], index=test.index)

# Plot
plt.figure(figsize=(12,5), dpi=100)
plt.plot(train, label='training')
plt.plot(test, label='actual')
plt.plot(fc_series, label='forecast')
plt.fill_between(lower_series.index, lower_series, upper_series,
                 color='k', alpha=.15)

plt.title('Forecast vs Actuals')
plt.legend(loc='upper left', fontsize=8)
plt.show()

```



From the chart, the ARIMA[1,1,1] model seems to give a directionally correct forecast. And the actual observed values lie within the 95% confidence band. That seems fine.

But each of the predicted forecasts is consistently below the actuals. That means, by adding a small constant to our forecast, the accuracy will certainly improve. So, there is definitely scope for improvement.

So, what I am going to do is to increase the order of differencing to two, that is set $d=2$ and iteratively increase p to up to 5 and then q up to 5 to see which model gives least AIC and also look for a chart that gives closer actuals and forecasts.

While doing this, I keep an eye on the P values of the AR and MA terms in the model summary. They should be as close to zero, ideally, less than 0.05.

```
# Build Model
model = ARIMA(train, order=(3, 2, 1))
fitted = model.fit(dis=-1)
print(fitted.summary())

# Forecast
fc, se, conf = fitted.forecast(15, alpha=0.05) # 95% conf

# Make as pandas series
fc_series = pd.Series(fc, index=test.index)
lower_series = pd.Series(conf[:, 0], index=test.index)
upper_series = pd.Series(conf[:, 1], index=test.index)

# Plot
plt.figure(figsize=(12,5), dpi=100)
plt.plot(train, label='training')
plt.plot(test, label='actual')
plt.plot(fc_series, label='forecast')
plt.fill_between(lower_series.index, lower_series, upper_series,
                 color='k', alpha=.15)
plt.title('Forecast vs Actuals')
plt.legend(loc='upper left', fontsize=8)
plt.show()
```

ARIMA Model Results

```

=====
Dep. Variable:          D2.value    No. Observations:
83
Model:                  ARIMA(3, 2, 1)    Log Likelihood          -214.2
48
Method:                  css-mle    S.D. of innovations          3.153
Date:                    Sat, 09 Feb 2019    AIC          440.49
7
Time:                    12:49:01    BIC          455.010
Sample:                  2    HQIC          446.327

```

```

=====
===
              coef      std err          z      P>|z|      [0.025      0.9
75]
-----
---
const          0.0483      0.084      0.577      0.565      -0.116      0
.212
ar.L1.D2.value  1.1386      0.109     10.399      0.000      0.924      1
.353
ar.L2.D2.value -0.5923      0.155     -3.827      0.000      -0.896     -0
.289
ar.L3.D2.value  0.3079      0.111      2.778      0.007      0.091      0
.525
ma.L1.D2.value -1.0000      0.035    -28.799      0.000      -1.068     -0
.932

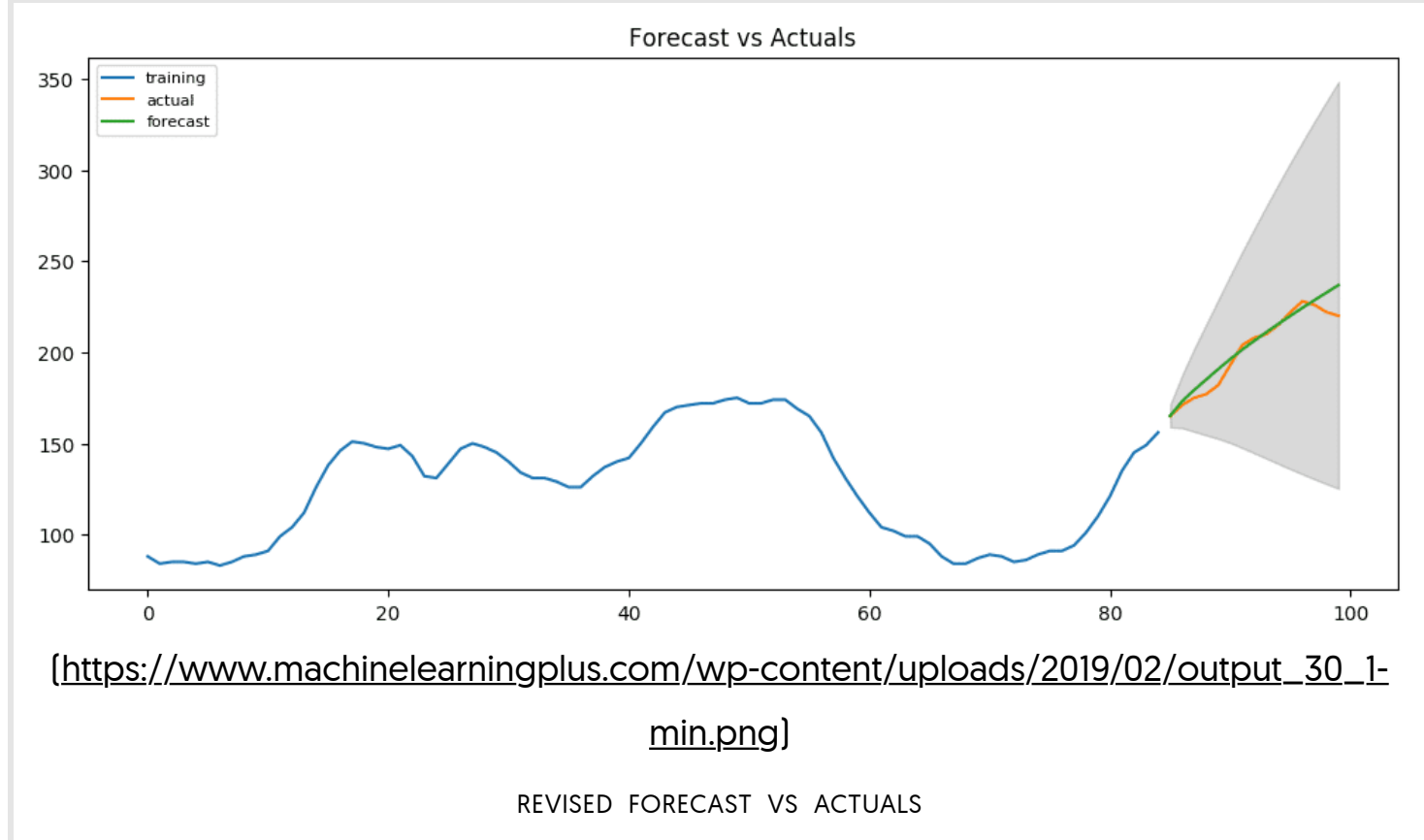
```

Roots

```

=====
              Real      Imaginary      Modulus      Frequen
cy
-----
AR.1          1.1557      -0.0000j      1.1557      -0.0000
AR.2          0.3839      -1.6318j      1.6763      -0.2132
AR.3          0.3839      +1.6318j      1.6763      0.2132
MA.1          1.0000      +0.0000j      1.0000      0.0000
-----

```

The AIC has reduced to 440 from 515. Good. The P-values of the X terms are less than 0.05, which is great.

So overall it's much better.

Ideally, you should go back multiple points in time, like, go back 1, 2, 3 and 4 quarters and see how your forecasts are performing at various points in the year.

Here's a great practice exercise: Try to go back 27, 30, 33, 36 data points and see how the forecasts perform. The forecast performance can be judged using various accuracy metrics discussed next.

11. Accuracy Metrics for Time Series Forecast

The commonly used accuracy metrics to judge forecasts are:

1. Mean Absolute Percentage Error (MAPE)
2. Mean Error (ME)
3. Mean Absolute Error (MAE)
4. Mean Percentage Error (MPE)
5. Root Mean Squared Error (RMSE)

6. Lag 1 Autocorrelation of Error [ACF1]
7. Correlation between the Actual and the Forecast [corr]
8. Min-Max Error [minmax]

Typically, if you are comparing forecasts of two different series, the MAPE, Correlation and Min-Max Error can be used.

Why not use the other metrics?

Because only the above three are percentage errors that vary between 0 and 1. That way, you can judge how good is the forecast irrespective of the scale of the series.

The other error metrics are quantities. That implies, an RMSE of 100 for a series whose mean is in 1000's is better than an RMSE of 5 for series in 10's. So, you can't really use them to compare the forecasts of two different scaled time series.

Accuracy metrics

```
def forecast_accuracy(forecast, actual):
    mape = np.mean(np.abs(forecast - actual)/np.abs(actual))  # MAPE
    me = np.mean(forecast - actual)                          # ME
    mae = np.mean(np.abs(forecast - actual))                 # MAE
    mpe = np.mean((forecast - actual)/actual)                # MPE
    rmse = np.mean((forecast - actual)**2)**.5               # RMSE
    corr = np.corrcoef(forecast, actual)[0,1]                # corr
    mins = np.amin(np.hstack([forecast[:,None],
                              actual[:,None]]), axis=1)
    maxs = np.amax(np.hstack([forecast[:,None],
                              actual[:,None]]), axis=1)
    minmax = 1 - np.mean(mins/maxs)                          # minmax
    acf1 = acf(fc-test)[1]                                    # ACF1
    return({'mape':mape, 'me':me, 'mae': mae,
            'mpe': mpe, 'rmse':rmse, 'acf1':acf1,
            'corr':corr, 'minmax':minmax})
```

```
forecast_accuracy(fc, test.values)
```

```
#> {'mape': 0.02250131357314834,
#>  'me': 3.230783108990054,
#>  'mae': 4.548322194530069,
#>  'mpe': 0.016421001932706705,
#>  'rmse': 6.373238534601827,
#>  'acf1': 0.5105506325288692,
#>  'corr': 0.9674576513924394,
#>  'minmax': 0.02163154777672227}
```

Around 2.2% MAPE implies the model is about 97.8% accurate in predicting the next 15 observations.

Now you know how to build an ARIMA model manually.

But in industrial situations, you will be given a lot of time series to be forecasted and the forecasting exercise be repeated regularly.

So we need a way to automate the best model selection process.

12. How to do Auto Arima Forecast in Python

Like R's popular `auto.arima()` function, the `pmdarima` package provides `auto_arima()` with similar functionality.

`auto_arima()` uses a stepwise approach to search multiple combinations of p, d, q parameters and chooses the best model that has the least AIC.

```
from statsmodels.tsa.arima_model import ARIMA
import pmdarima as pm

df = pd.read_csv('https://raw.githubusercontent.com/selva86/datasets/master/wwwusage.csv')
df = pd.read_csv('https://raw.githubusercontent.com/selva86/datasets/master/wwwusage.csv',
names=['value'], header=0)

model = pm.auto_arima(df.value, start_p=1, start_q=1,
                      test='adf',          # use adftest to find optimal 'd'
                      max_p=3, max_q=3,    # maximum p and q
                      m=1,                 # frequency of series
                      d=None,               # let model determine 'd'
                      seasonal=False,      # No Seasonality
                      start_P=0,
                      D=0,
                      trace=True,
                      error_action='ignore',
                      suppress_warnings=True,
                      stepwise=True)

print(model.summary())
```

```
#> Fit ARIMA: order=(1, 2, 1); AIC=525.586, BIC=535.926, Fit time=0.060 seconds
#> Fit ARIMA: order=(0, 2, 0); AIC=533.474, BIC=538.644, Fit time=0.005 seconds
#> Fit ARIMA: order=(1, 2, 0); AIC=532.437, BIC=540.192, Fit time=0.035 seconds
#> Fit ARIMA: order=(0, 2, 1); AIC=525.893, BIC=533.648, Fit time=0.040 seconds
#> Fit ARIMA: order=(2, 2, 1); AIC=515.248, BIC=528.173, Fit time=0.105 seconds
#> Fit ARIMA: order=(2, 2, 0); AIC=513.459, BIC=523.798, Fit time=0.063 seconds
#> Fit ARIMA: order=(3, 2, 1); AIC=512.552, BIC=528.062, Fit time=0.272 seconds
#> Fit ARIMA: order=(3, 2, 0); AIC=515.284, BIC=528.209, Fit time=0.042 seconds
```

```

#> Fit ARIMA: order=(3, 2, 2); AIC=514.514, BIC=532.609, Fit time=0.234 seconds
#> Total fit time: 0.865 seconds
#>
#> ARIMA Model Results
#> =====
==
#> Dep. Variable:          D2.y    No. Observations:
98
#> Model:                ARIMA(3, 2, 1)    Log Likelihood          -250.2
76
#> Method:                css-mle    S.D. of innovations          3.0
69
#> Date:                  Sat, 09 Feb 2019    AIC          512.5
52
#> Time:                  12:57:22    BIC          528.0
62
#> Sample:                2    HQIC          518.8
25
#>
#> =====
==
#>          coef    std err          z      P>|z|      [0.025    0.97
5]
#> -----
--
#> const          0.0234    0.058      0.404    0.687    -0.090    0.1
37
#> ar.L1.D2.y      1.1586    0.097     11.965    0.000     0.969    1.3
48
#> ar.L2.D2.y     -0.6640    0.136     -4.890    0.000    -0.930   -0.3
98
#> ar.L3.D2.y      0.3453    0.096      3.588    0.001     0.157    0.5
34
#> ma.L1.D2.y     -1.0000    0.028    -36.302    0.000    -1.054   -0.9
46
#>
#> Roots
#> =====
=
#>          Real          Imaginary          Modulus          Frequenc
y

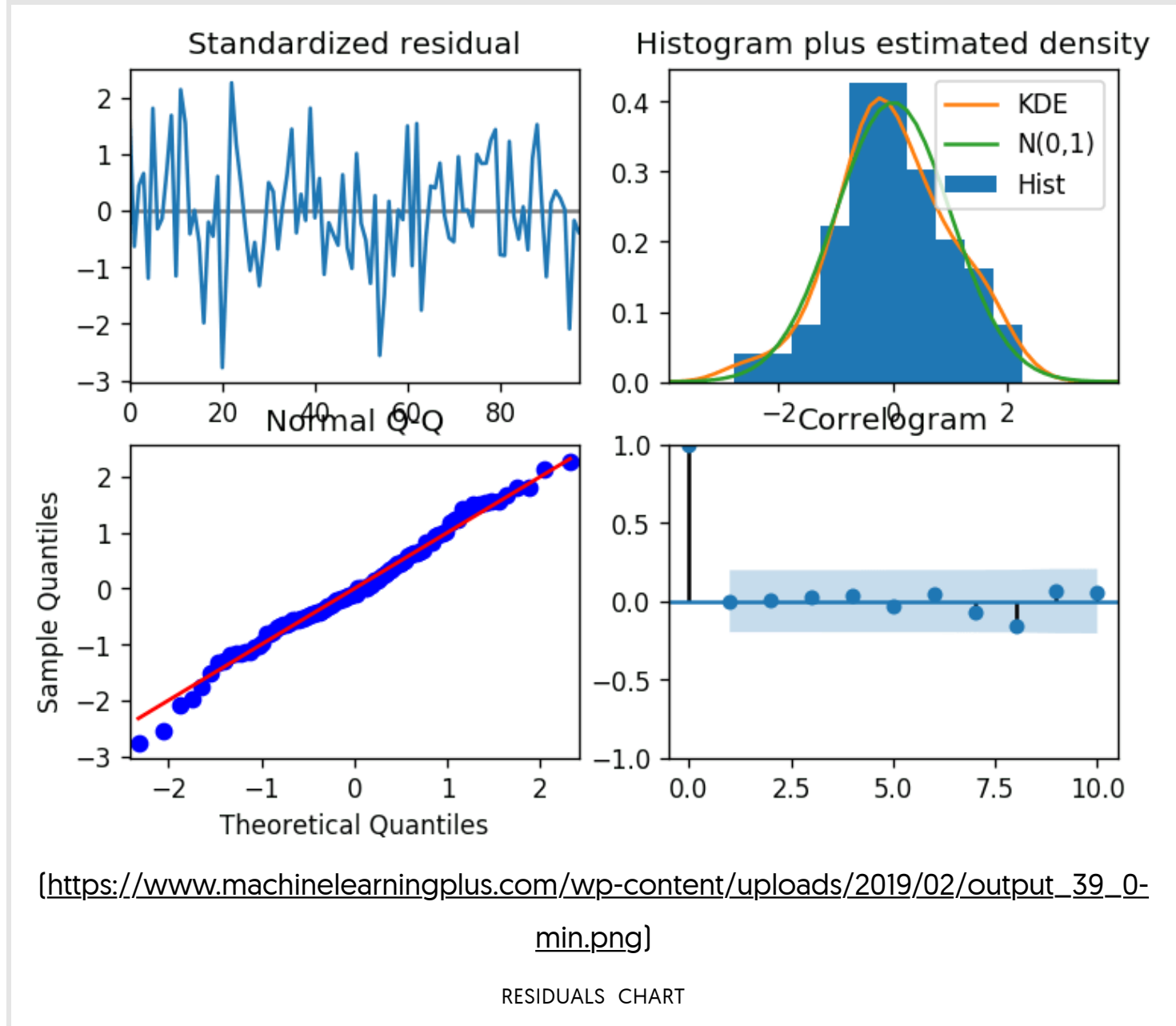
```

```
#> -----
-
#> AR.1          1.1703          -0.0000j          1.1703          -0.000
0
#> AR.2          0.3763          -1.5274j          1.5731          -0.211
6
#> AR.3          0.3763          +1.5274j          1.5731          0.211
6
#> MA.1          1.0000          +0.0000j          1.0000          0.000
0
#> -----
-
```

13. How to interpret the residual plots in ARIMA model

Let's review the residual plots using `stepwise_fit`.

```
model.plot_diagnostics(figsize=(7,5))
plt.show()
```



So how to interpret the plot diagnostics?

Top left: The residual errors seem to fluctuate around a mean of zero and have a uniform variance.

Top Right: The density plot suggest normal distribution with mean zero.

Bottom left: All the dots should fall perfectly in line with the red line. Any significant deviations would imply the distribution is skewed.

Bottom Right: The Correlogram, aka, ACF plot shows the residual errors are not autocorrelated. Any autocorrelation would imply that there is some pattern in the residual errors which are not explained in the model. So you will need to look for more X's [predictors] to the model.

Overall, it seems to be a good fit. Let's forecast.

```

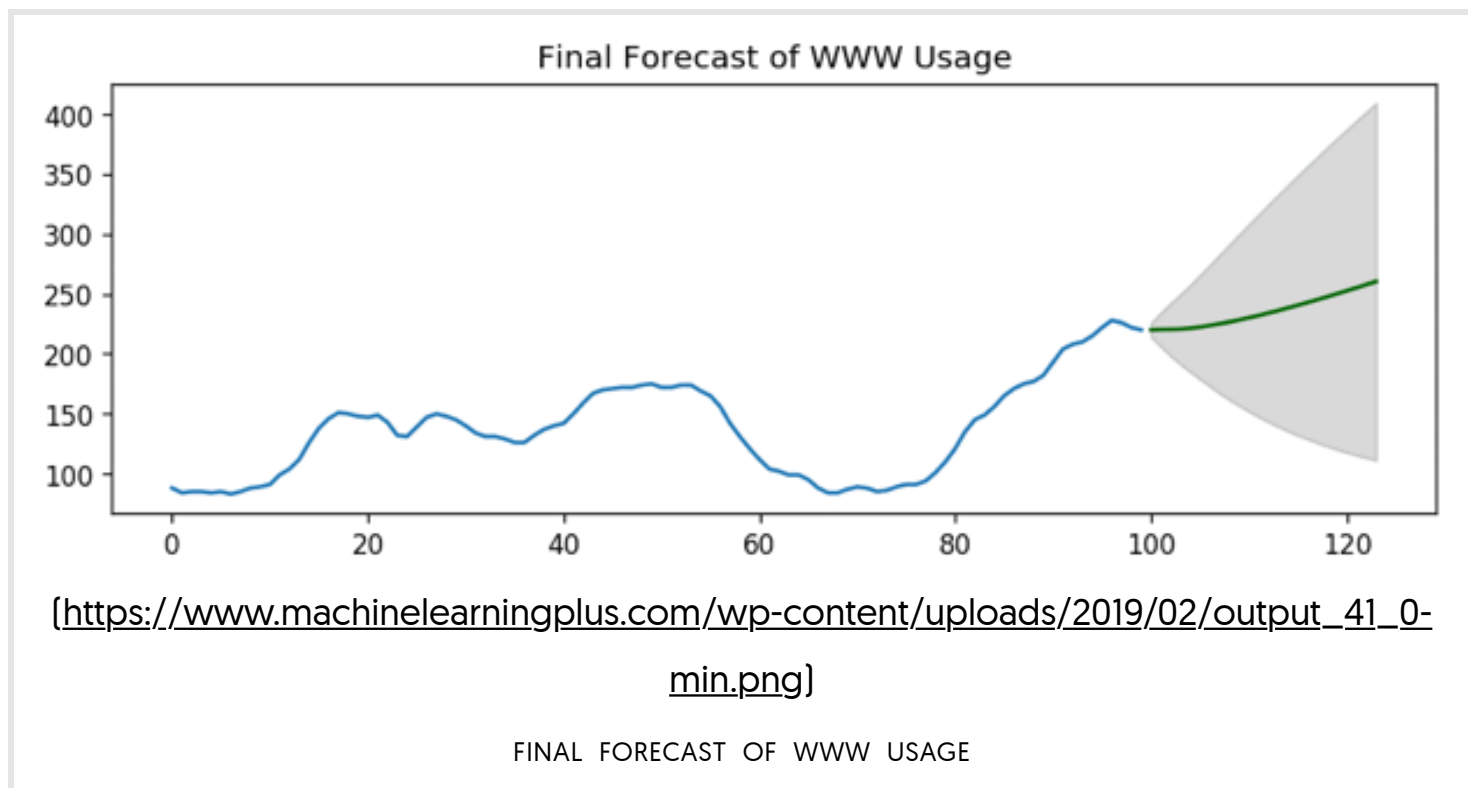
# Forecast
n_periods = 24
fc, confint = model.predict(n_periods=n_periods, return_conf_int=True)
index_of_fc = np.arange(len(df.value), len(df.value)+n_periods)

# make series for plotting purpose
fc_series = pd.Series(fc, index=index_of_fc)
lower_series = pd.Series(confint[:, 0], index=index_of_fc)
upper_series = pd.Series(confint[:, 1], index=index_of_fc)

# Plot
plt.plot(df.value)
plt.plot(fc_series, color='darkgreen')
plt.fill_between(lower_series.index,
                 lower_series,
                 upper_series,
                 color='k', alpha=.15)

plt.title("Final Forecast of WWW Usage")
plt.show()

```



14. How to automatically build SARIMA model in python

The problem with plain ARIMA model is it does not support seasonality.

If your time series has defined seasonality, then, go for SARIMA which uses seasonal differencing.

Seasonal differencing is similar to regular differencing, but, instead of subtracting consecutive terms, you subtract the value from previous season.

So, the model will be represented as $SARIMA(p,d,q) \times (P,D,Q)$, where, P, D and Q are SAR, order of seasonal differencing and SMA terms respectively and 'x' is the frequency of the time series.

If your model has well defined seasonal patterns, then enforce $D=1$ for a given frequency 'x'.

Here's some practical advice on building SARIMA model:

As a general rule, set the model parameters such that D never exceeds one. And the total differencing ' $d + D$ ' never exceeds 2. Try to keep only either SAR or SMA terms if your model has seasonal components.

Let's build an SARIMA model on 'a10' – the drug sales dataset.

```
# Import
```

```
data = pd.read_csv('https://raw.githubusercontent.com/selva86/datasets/master/a10.csv (https://raw.githubusercontent.com/selva86/datasets/master/a10.csv)',  
parse_dates=['date'], index_col='date')
```

```
# Plot
```

```
fig, axes = plt.subplots(2, 1, figsize=(10,5), dpi=100, sharex=True)
```

```
# Usual Differencing
```

```
axes[0].plot(data[:,], label='Original Series')
```

```
axes[0].plot(data[:,].diff(1), label='Usual Differencing')
```

```
axes[0].set_title('Usual Differencing')
```

```
axes[0].legend(loc='upper left', fontsize=10)
```

```
# Seasonal Dei
```

```
axes[1].plot(data[:,], label='Original Series')
```

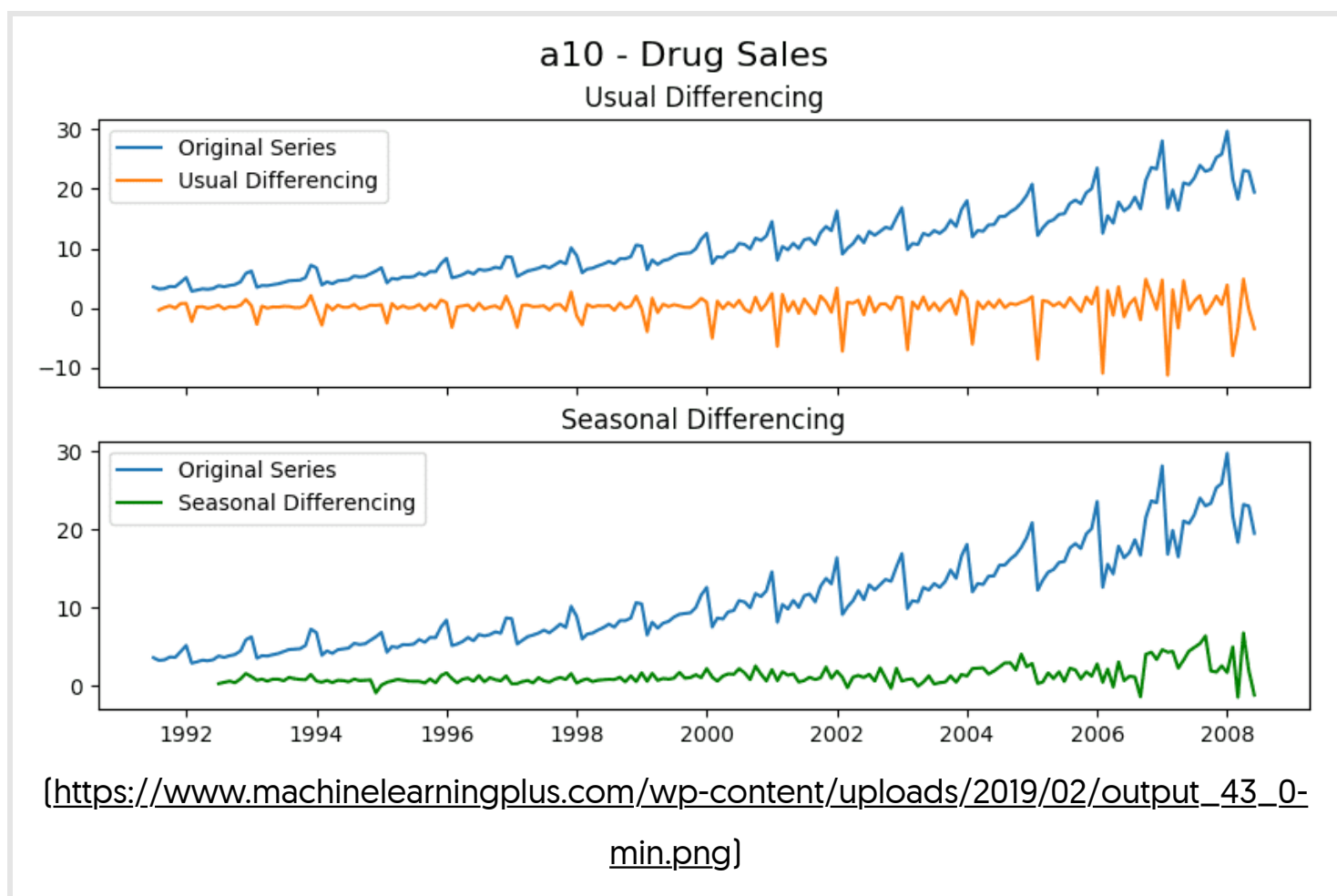
```
axes[1].plot(data[:,].diff(12), label='Seasonal Differencing', color='green')
```

```
axes[1].set_title('Seasonal Differencing')
```

```
plt.legend(loc='upper left', fontsize=10)
```

```
plt.suptitle('a10 - Drug Sales', fontsize=16)
```

```
plt.show()
```



Fit ARIMA: order=(1, 0, 1) seasonal_order=(0, 1, 1, 12); AIC=534.818, BIC=551.105, **Fit** time=1.742 seconds
Fit ARIMA: order=(0, 0, 0) seasonal_order=(0, 1, 0, 12); AIC=624.061, BIC=630.576, **Fit** time=0.028 seconds
Fit ARIMA: order=(1, 0, 0) seasonal_order=(1, 1, 0, 12); AIC=596.004, BIC=609.034, **Fit** time=0.683 seconds
Fit ARIMA: order=(0, 0, 1) seasonal_order=(0, 1, 1, 12); AIC=611.475, BIC=624.505, **Fit** time=0.709 seconds
Fit ARIMA: order=(1, 0, 1) seasonal_order=(1, 1, 1, 12); AIC=557.501, BIC=577.046, **Fit** time=3.687 seconds
(...TRUNCATED...)
Fit ARIMA: order=(3, 0, 0) seasonal_order=(1, 1, 1, 12); AIC=554.570, BIC=577.372, **Fit** time=2.431 seconds
Fit ARIMA: order=(3, 0, 0) seasonal_order=(0, 1, 0, 12); AIC=554.094, BIC=570.381, **Fit** time=0.220 seconds
Fit ARIMA: order=(3, 0, 0) seasonal_order=(0, 1, 2, 12); AIC=529.502, BIC=552.305, **Fit** time=2.120 seconds
Fit ARIMA: order=(3, 0, 0) seasonal_order=(1, 1, 2, 12); AIC=nan, BIC=nan, **Fit** time=nan seconds
Total fit time: 31.613 seconds

Statespace Model Results

Dep. Variable:	y	No. Observations:	204
Model:	SARIMAX(3, 0, 0)x(0, 1, 1, 12)	Log Likelihood	-258.300
Date:	Sat, 09 Feb 2019	AIC	528.601
Time:	21:07:16	BIC	548.146
Sample:	0	HQIC	536.517
	- 204		

Covariance Type: opg

	coef	std err	z	P> z	[0.025	0.975]
intercept	0.1649	0.097	1.705	0.088	-0.025	0.354
ar.L1	0.0949	0.043	2.205	0.027	0.011	0.179
ar.L2	0.4145	0.035	11.907	0.000	0.346	0.483
ar.L3	0.3531	0.053	6.601	0.000	0.248	0.458
ma.S.L12	-0.4635	0.058	-8.008	0.000	-0.577	-0.350
sigma2	0.8461	0.057	14.925	0.000	0.735	0.957

Ljung-Box (Q): 59.80 **Jarque-Bera (JB):** 124.59

Prob(Q):	0.02	Prob(JB):	0.00
Heteroskedasticity (H):	12.75	Skew:	0.29
Prob(H) (two-sided):	0.00	Kurtosis:	6.90

(<https://www.machinelearningplus.com/wp-content/uploads/2019/02/Model-Summary-1-min.png>)

The model has estimated the AIC and the P values of the coefficients look significant. Let's look at the residual diagnostics plot.

The best model SARIMAX(3, 0, 0)x(0, 1, 1, 12) has an AIC of 528.6 and the P Values are significant.

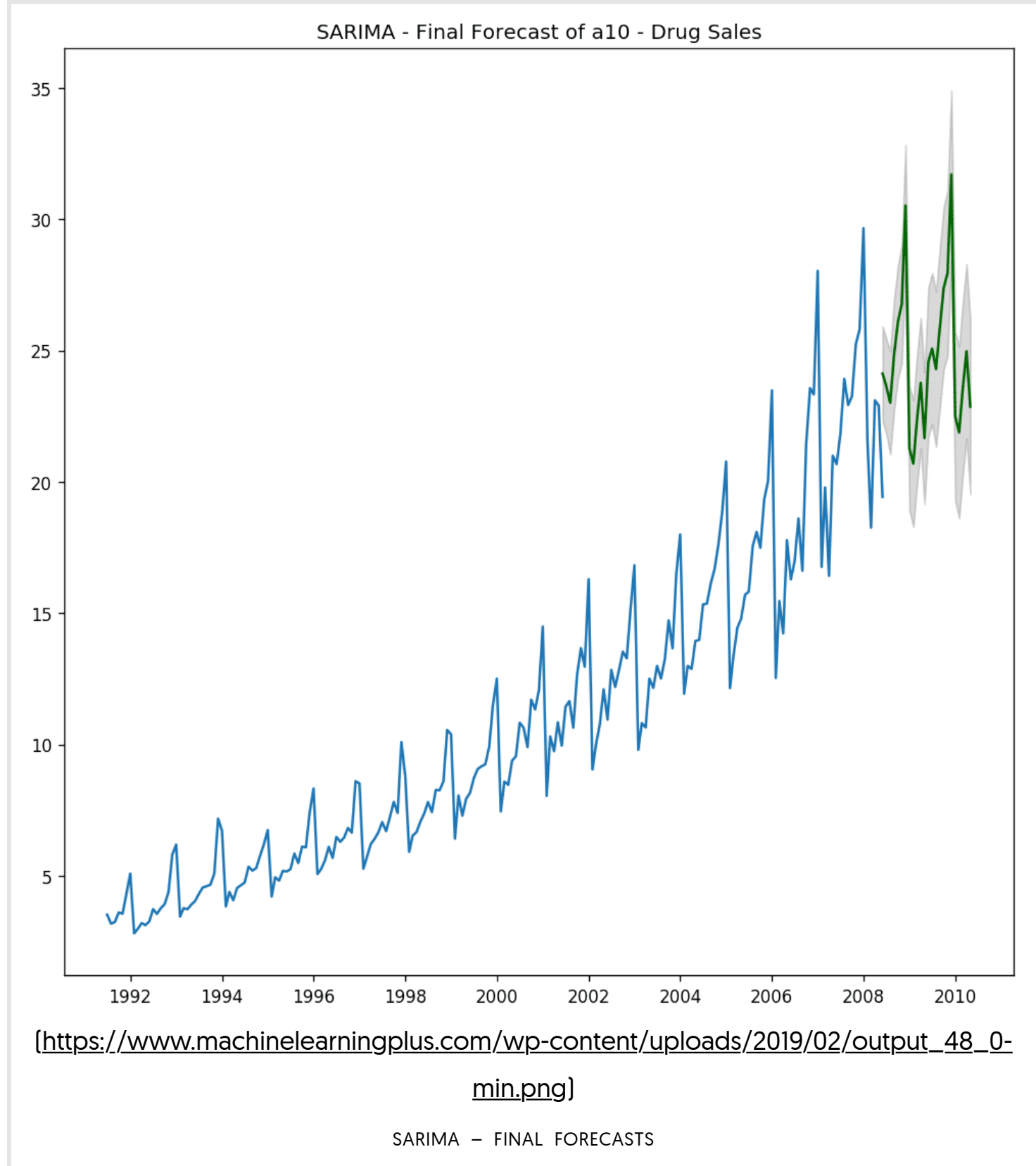
Let's forecast for the next 24 months.

```
# Forecast
n_periods = 24
fitted, confint = smodel.predict(n_periods=n_periods, return_conf_int=True)
index_of_fc = pd.date_range(data.index[-1], periods = n_periods, freq='MS')

# make series for plotting purpose
fitted_series = pd.Series(fitted, index=index_of_fc)
lower_series = pd.Series(confint[:, 0], index=index_of_fc)
upper_series = pd.Series(confint[:, 1], index=index_of_fc)

# Plot
plt.plot(data)
plt.plot(fitted_series, color='darkgreen')
plt.fill_between(lower_series.index,
                 lower_series,
                 upper_series,
                 color='k', alpha=.15)

plt.title("SARIMA - Final Forecast of a10 - Drug Sales")
plt.show()
```



There you have a nice forecast that captures the expected seasonal demand pattern.

15. How to build SARIMAX Model with exogenous variable

The SARIMA model we built is good. I would stop here typically.

But for the sake of completeness, let's try and force an external predictor, also called, 'exogenous variable' into the model. This model is called the SARIMAX model.

The only requirement to use an exogenous variable is you need to know the value of the variable during the forecast period as well.

For the sake of demonstration, I am going to use the seasonal index from the [classical seasonal decomposition](https://www.machinelearningplus.com/time-series/time-series-analysis-python/) [\[https://www.machinelearningplus.com/time-series/time-series-analysis-python/\]](https://www.machinelearningplus.com/time-series/time-series-analysis-python/) on the latest 36 months of data.

Why the seasonal index? Isn't SARIMA already modeling the seasonality, you ask?

You are correct.

But also, I want to see how the model looks if we force the recent seasonality pattern into the training and forecast.

Secondly, this is a good variable for demo purpose. So you can use this as a template and plug in any of your variables into the code. The seasonal index is a good exogenous variable because it repeats every frequency cycle, 12 months in this case.

So, you will always know what values the seasonal index will hold for the future forecasts.

```
# Import Data  
data = pd.read_csv('https://raw.githubusercontent.com/selva86/datasets/master/a10.csv (https://raw.githubusercontent.com/selva86/datasets/master/a10.csv)',  
parse_dates=['date'], index_col='date')
```

Let's compute the seasonal index so that it can be forced as a [exogenous] predictor to the SARIMAX model.

Fit ARIMA: order=(1, 0, 1) seasonal_order=(0, 1, 1, 12); AIC=536.818, BIC=556.362, **Fit** time=2.083 seconds

Fit ARIMA: order=(0, 0, 0) seasonal_order=(0, 1, 0, 12); AIC=626.061, BIC=635.834, **Fit** time=0.033 seconds

Fit ARIMA: order=(1, 0, 0) seasonal_order=(1, 1, 0, 12); AIC=598.004, BIC=614.292, **Fit** time=0.682 seconds

Fit ARIMA: order=(0, 0, 1) seasonal_order=(0, 1, 1, 12); AIC=613.475, BIC=629.762, **Fit** time=0.510 seconds

Fit ARIMA: order=(1, 0, 1) seasonal_order=(1, 1, 1, 12); AIC=559.530, BIC=582.332, **Fit** time=3.129 seconds

(...Truncated...)

Fit ARIMA: order=(3, 0, 0) seasonal_order=(0, 1, 0, 12); AIC=556.094, BIC=575.639, **Fit** time=0.260 seconds

Fit ARIMA: order=(3, 0, 0) seasonal_order=(0, 1, 2, 12); AIC=531.502, BIC=557.562, **Fit** time=2.375 seconds

Fit ARIMA: order=(3, 0, 0) seasonal_order=(1, 1, 2, 12); AIC=nan, BIC=nan, **Fit** time=nan seconds

Total fit time: 30.781 seconds

Statespace Model Results

Dep. Variable:	y	No. Observations:	204
Model:	SARIMAX(3, 0, 0)x(0, 1, 1, 12)	Log Likelihood	-258.300
Date:	Sat, 09 Feb 2019	AIC	530.601
Time:	20:57:56	BIC	553.403
Sample:	0	HQIC	539.836
	- 204		

Covariance Type: opg

	coef	std err	z	P> z 	[0.025	0.975]
intercept	0.1649	0.097	1.705	0.088	-0.025	0.354
x1	3.924e-07	2.43e-09	161.812	0.000	3.88e-07	3.97e-07
ar.L1	0.0949	0.043	2.205	0.027	0.011	0.179
ar.L2	0.4145	0.035	11.907	0.000	0.346	0.483
ar.L3	0.3531	0.053	6.601	0.000	0.248	0.458
ma.S.L12	-0.4635	0.058	-8.008	0.000	-0.577	-0.350
sigma2	0.8461	0.057	14.925	0.000	0.735	0.957

Ljung-Box (Q): 59.80 **Jarque-Bera (JB):** 124.59

Prob(Q): 0.02 **Prob(JB):** 0.00

Heteroskedasticity (H): 12.75 **Skew:** 0.29

Prob(H) (two-sided): 0.00 **Kurtosis:** 6.90

(<https://www.machinelearningplus.com/wp-content/uploads/2019/02/Model-Summary-2-min.png>)

So, we have the model with the exogenous term. But the coefficient is very small for x1, so the contribution from that variable will be negligible. Let's forecast it anyway.

We have effectively forced the latest seasonal effect of the latest 3 years into the model instead of the entire history.

Alright let's forecast into the next 24 months. For this, you need the value of the seasonal index for the next 24 months.

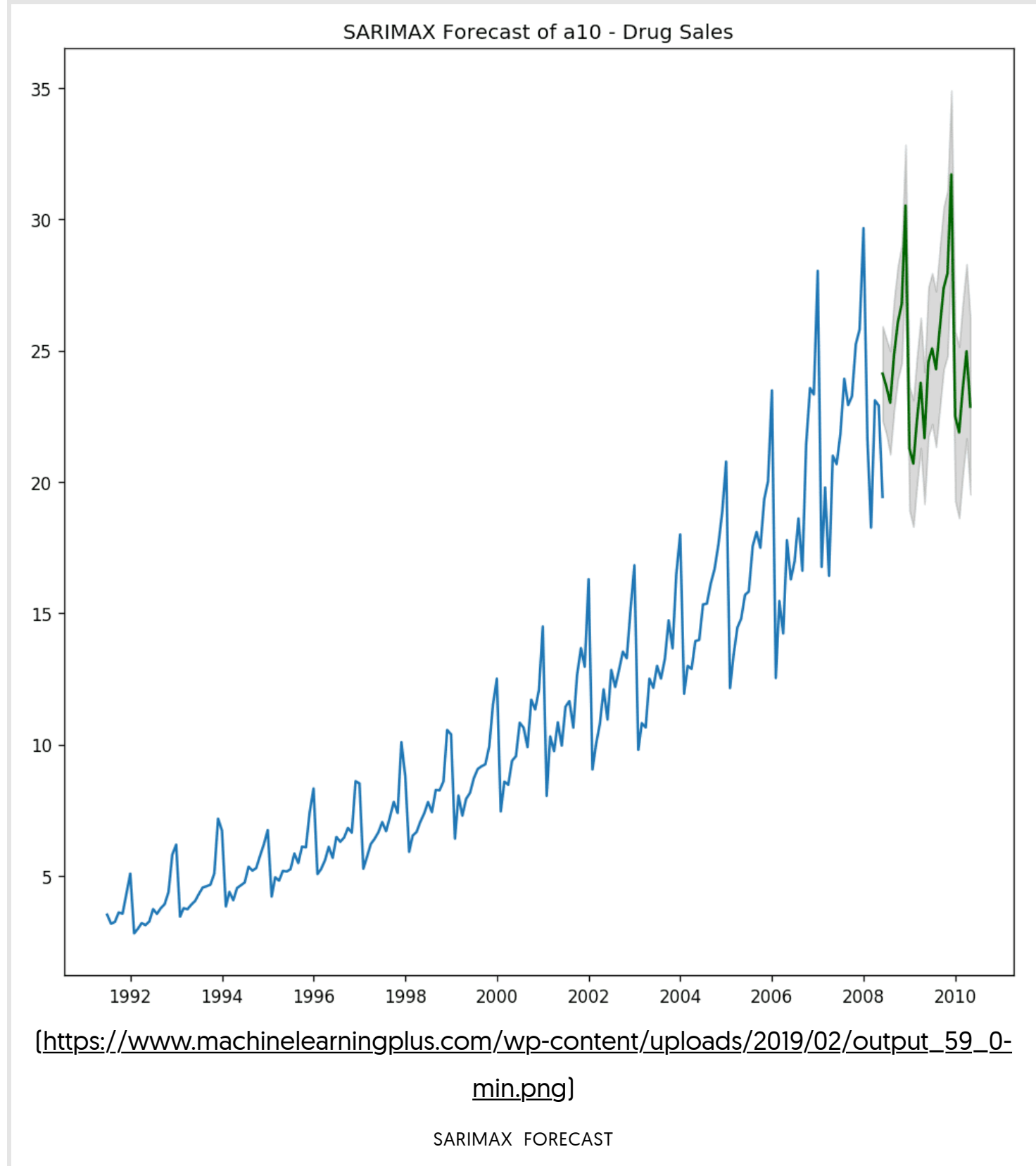
```
# Forecast
n_periods = 24
fitted, confint = sxmodel.predict(n_periods=n_periods,
                                  exogenous=np.tile(seasonal_index.value, 2).re
shape(-1,1),
                                  return_conf_int=True)

index_of_fc = pd.date_range(data.index[-1], periods = n_periods, freq='MS')

# make series for plotting purpose
fitted_series = pd.Series(fitted, index=index_of_fc)
lower_series = pd.Series(confint[:, 0], index=index_of_fc)
upper_series = pd.Series(confint[:, 1], index=index_of_fc)

# Plot
plt.plot(data['value'])
plt.plot(fitted_series, color='darkgreen')
plt.fill_between(lower_series.index,
                 lower_series,
                 upper_series,
                 color='k', alpha=.15)

plt.title("SARIMAX Forecast of a10 - Drug Sales")
plt.show()
```



16. Practice Exercises

In the AirPassengers dataset, go back 12 months in time and build the SARIMA forecast for the next 12 months.

1. Is the series stationary? If not what sort of differencing is required?
2. What is the order of your best model?
3. What is the AIC of your model?
4. What is the MAPE achieved in OOT cross-validation?

5. What is the order of the best model predicted by `auto_arima()` method?

17. Conclusion

Congrats if you reached this point. Give yourself a BIG hug if you were able to solve the practice exercises.

I really hope you found this useful?

We have covered a lot of concepts starting from the very basics of forecasting, AR, MA, ARIMA, SARIMA and finally the SARIMAX model. If you have any questions please write in the comments section. Meanwhile, I will work on the next article.

Happy Learning!

You may also like:

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Name



abu bakar siddique • 6 months ago

The computed initial AR coefficients are not stationary
You should induce stationarity, choose a different model order, or you can pass your own start_params...

What should i do now...?

[see more](#)

1 | • [Reply](#) • [Share](#) ›



Julien ➔ abu bakar siddique • 5 months ago • edited

I have the same issue...

Running this code seems to provide a ValueError:

```
from statsmodels.tsa.arima_model import ARIMA
# 1,1,2 ARIMA Model
model = ARIMA(df.value, order=(1,1,2))
model_fit = model.fit(dispatch=0)
print(model_fit.summary())
```

[see more](#)

^ | v • Reply • Share ›



Selva Prabhakaran Mod → Julien • 2 months ago

Probably some problem with the data you're using

^ | v • Reply • Share ›



Akshita Gupta • 7 months ago

This article is quite informative. But I would like to ask what needs to be done if the data presents the double seasonality.

1 ^ | v • Reply • Share ›



Selva Prabhakaran Mod → Akshita Gupta • 2 months ago

You might want to look at multiseasonal time series forecasting algo. The 'forecast' package in R has an implementation.

^ | v • Reply • Share ›



Abdellah sebti • a month ago

I am truly thankful for this amazing article and your effort, it was one of the best informative article I found

^ | v • Reply • Share ›

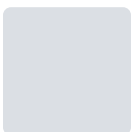


Selva Prabhakaran Mod → Abdellah sebti • a month ago

Thanks very much :)

^ | v • Reply • Share ›

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Asto Maa Sadgamy • 2 months ago

Hi,

Just wondering, Can these model are suitable for long data training and forecasting. let say to train 40K data and forecast next 30k data ? if not could you suggest any time series method for that ?

see more

^ | v · Reply · Share ›



Selva Prabhakaran Mod → Asto Maa Sadgamyia · 2 months ago

Depends on the type of data and the problem you are dealing with. Can't suggest a method without context.

^ | v · Reply · Share ›

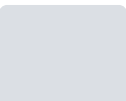


Asto Maa Sadgamyia → Selva Prabhakaran · 2 months ago

I am working on wind speed time series data that covers 10 years of data of 10 mins average. So using these 10 years of wind speed data, can I forecast next 10 years wind speed data ?

see more

^ | v · Reply · Share ›



mjos · 5 months ago

Hi. I'm not sure if the numbering of beta coefficients in the equations for errors (see

...), I'm not sure if the numbering of beta coefficients in the equations for errors (see
"The errors E_t and $E_{(t-1)}$ are the errors from the following equation:") are correct. Could
you please have a look at it?

see more

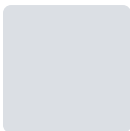
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Selva Prabhakaran Mod → mjos • 2 months ago

Oh, yeah. Its wrong. Thanks for finding this.. and apologies for such a late reply

^ | v • Reply • Share ›



Vũ Trung Nghĩa • 5 months ago

The original serie may be changed many time because differencing, detrend,... So
when my model predict 100 next value, do I need to transform it to the original serie
by the inverse process that I do when differencing, detrend the series or is there
another the way to do that?

see more

^ | v · Reply · Share ›



Selva Prabhakaran Mod ➔ Vũ Trung Nghĩa · 2 months ago

The algo will give do it internally.. just specify the p,d and q. Not required if you use autoarima.

^ | v · Reply · Share ›



Dídac Cortiada · 6 months ago · edited

Great post! Really educational and helpful. Thanks :)

^ | v · Reply · Share ›



Selva Prabhakaran Mod ➔ Dídac Cortiada · 2 months ago

Thanks :)

^ | v · Reply · Share ›



Wael Abu Rezeq · 6 months ago

I would like to thank you for this AMAZING and comprehensive article. I hereby have two questions:

1- If we are not considering seasonality, then $M = 1$ (since the data is on monthly basis) in auto_arima exercise. However, If we have seasonality then $M = 12$ to look at seasonality inside every 12 months. My questions is what if the dataset frequency in days not month, what should these variables hold?

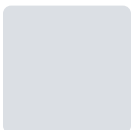
2- We are forecasting the dataset on time series aggregations, what If we want to forecast including other attributes like Region or Sales Channel incorporated with time series (so suppose we want to do the forecast for a dataset that has the attributes of TimeSeries, Region, Value) per region?

Looking forward to hearing from you

Thanks for your great support

see more

^ | v · Reply · Share ›



Phuc Coi · 7 months ago

This is very cool :D

^ | v · Reply · Share ›



Selva Prabhakaran Mod → Phuc Coi • 2 months ago

Thanks :)

^ | v • Reply • Share ›

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Betül Okan • 9 months ago

That's a great article. Everything is explained very well. Thank you very much.

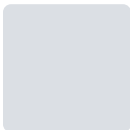
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Selva Prabhakaran Mod → Betül Okan • 7 months ago

Welcome :)

^ | v • Reply • Share ›



Eric Kumar • 9 months ago

Great article, very concise and current. One request. it would be great if the data-sets are linked. If the data sets are linked somewhere, they are hard to find.

Data set for the #10

<https://raw.githubusercontent.com/eric-kumar/10>

see more

^ | v • Reply • Share ›



Selva Prabhakaran Mod → Eric Kumar • 9 months ago • edited

Thanks for pointing it out Eric. I will make them available via links.

EDIT: Updated!

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