## **Virtual Lecture Notes (Part 1)**

## **Calculating the Greatest Common Divisor Recursively**

The greatest common divisor (GCD) of two integer values, x and y, is the largest number that evenly divides both x and y. Euclid discovered that the greatest common divisor of x and y must always be the same as that of x and r, where r is the remainder of x divided by y.

Euclid's algorithm for finding the Greatest Common Divisor:

- 1. Divide the larger number by the smaller number.
- 2. If there is no remainder, the smaller number is the GCD.
- 3. Otherwise, the smaller number becomes the larger and the remainder becomes the smaller, and go back to Step 1.

## Example

```
x = 126, y = 90 x \text{ or } y \neq 0 \therefore 126 / 90 = 1 \text{ remainder } 36
x = 90, y = 36 \text{ x or } y \neq 0 \therefore 90 / 36 = 2 \text{ remainder } 18
x = 36, y = 18 \text{ x or } y \neq 0 \therefore 36 / 18 = 2 \text{ remainder } 0
x = 18, y = 0 x \text{ or } y = 0 \therefore GCD = 18

Base Case: GCD(x, y) = y if y is a divisor of x

Recursive Cases: GCD(x, y) = GCD(y, x) if x < n,
GCD(x, y) = GCD(y, x\%y) otherwise.
```

## **Implementation**

```
//precondition x, y non-negative int gcd(int x, int y)  \{ \\  if(x < y) \\  return gcd(y, x);  Else if(y == 0)  return x; \\  else \\  return gcd(y, x%y);  }
```