

Sean Reilly

6.1: 8, 12, 16, 26, 28, 48, 52, 72 (7th edition)

8.

$$26 * 25 * 24 = 15,600$$

12.

$$2^7 - 2^0 = 127$$

16.

$$62500 + 3750 + 100 + 1 = 66351$$

26.

$$a) 10 * 9 * 8 * 7 = 5040$$

$$b) 10 * 10 * 10 * 5 = 5000$$

c) The remaining digit must be different from 9 and can be at any of the 4 positions. Then there are  $9 * 4 = 36$  such strings.

28.

$$10 * 10 * 10 * 26 * 26 * 26 * 2 = 35,152,000$$

48.

$$16 + 32 - 4 = 44$$

52.

$$38 + 23 - 7 = 54$$

72.

Basis: Let  $m = 2$ . Therefore  $P(2)$  is true because there are  $n_1$  ways to do first task and  $n_2$  ways to do the second task, then by definition there will be  $n_1 n_2$  ways to do the procedure, which is the product of 2 tasks.

Inductive: if  $P(m)$  is true, then so is  $P(m+1)$ . In other words, if the product rule holds for  $m$  tasks, then it holds for  $m+1$  tasks. So assume that  $P(m)$  is true for some  $m \geq 2$ ; we'll try to prove  $P(m+1)$ . To that end suppose that we have  $m+1$  tasks, and that task  $T_k$  can be performed in  $n_k$  ways, here  $k=1, \dots, m+1$ . We'd like to show that the entire set of  $m+1$  tasks can be performed in  $n_1 n_2 \dots n_m n_{m+1}$  ways. By mathematical induction  $P(m)$  is true for all positive integers  $n(n \geq 2)$