

# 1. Polynomial multiplication.

Given two polynomials  $A(x) = a_0 + a_1x + a_2x^2 + \dots + a_{n-1}x^{n-1}$  and  $B(x) = b_0 + b_1x + b_2x^2 + \dots + b_{n-1}x^{n-1}$ , find the product  $C(x) = A(x) * B(x)$  in  $O(N \log N)$  time using fast fourier transforms.

## Input:

1. The first line contains ***n***, the **degree bound** of polynomials  $A(x)$  and  $B(x)$ .  
*The degree of a polynomial of degree bound ***n*** may be any integer between 0 and ***n*** - 1 (For example the polynomial  $1 + x + x^3$  is degree bound by 4).*

### Constraints:

1.  $1 \leq n \leq 100$
2. ***n*** will always be a power of 2.

2. The second line contains the ***n*** integer coefficients of polynomial  $A(x)$  separated by a whitespace starting from the lowest order coefficient ( $a_0 a_1 a_2 a_3 \dots a_{n-1}$ ). For example if the degree bound ***n*** is 4, the input for the polynomials:  
 $6x^3 + 7x^2 - 10x + 9$  will be "9 -10 7 6". ( $a_3x^3 + a_2x^2 + a_1x + a_0$  will be " $a_0 a_1 a_2 a_3$ ")  
 $x^2 + 3$  will be "3 0 1 0".  
 $x$  will be "0 1 0 0".

### Constraints:

$$-200 \leq a_i \leq 200$$

3. The second line contains the ***n*** integer coefficients of polynomial  $B(x)$  separated by a whitespace starting from the lowest order coefficient ( $b_0 b_1 b_2 b_3 \dots b_{n-1}$ ).

### Constraints:

$$-200 \leq b_i \leq 200$$

Use long not int.

## Output:

Print ***2n*** integer coefficients of  $C(x)$  separated by a whitespace starting from the lowest order coefficient ( $c_0 c_1 c_2 c_3 \dots c_{2n-1}$ ).

### Example 1:

Input:	Output:
4 9 -10 7 6 -5 4 0 -2	-45 86 -75 -20 44 -14 -12 0

Explanation:

$$A(x) = 6x^3 + 7x^2 - 10x + 9$$

$$B(x) = -2x^3 + 4x - 5$$

$$C(x) = -12x^6 - 14x^5 + 44x^4 - 20x^3 - 75x^2 + 86x - 45$$

### Example 2:

Input:	Output:
4 3 0 1 0 0 1 0 0	0 3 0 1 0 0 0 0

Explanation:

$$A(x) = x^2 + 3$$

$$B(x) = x$$

$$C(x) = x^3 + 3x$$