

CS2202 - Computer Organization

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Lecture Assignment 2

1. a). global CPI for each implementation

class	A	B	C	D
CPI for P_1	1	2	3	3
IC in P_1	10^5	2×10^5	5×10^5	2×10^5
CPI for P_2	2	2	2	2

$$\text{Total IC} : 1.0 \times 10^6$$

$$\text{clock rate}_1 = 2.5 \text{ GHz}$$

$$\text{clock rate}_2 = 3 \text{ GHz}$$

$$P_1 : IC = 1.0 \times 10^6$$

$$P_2 : IC = 1.0 \times 10^6$$

$$\text{clock cycle}_1$$

$$\text{clock cycle}_2$$

$$\begin{aligned} &= 10^5 + 4 \times 10^5 + 15 \times 10^5 + 6 \times 10^5 \\ &= 26 \times 10^5 = 2.6 \times 10^6 \end{aligned}$$

$$\begin{aligned} &= 2(10^5 + 2 \times 10^5 + 5 \times 10^5 + 2 \times 10^5) \\ &= 2 \times 10^6 \end{aligned}$$

$$\text{Average CPI}_1 = \frac{2.6 \times 10^6}{1.0 \times 10^6} = \underline{2.6}$$

$$\text{Average CPI}_2 = \frac{2 \times 10^6}{1.0 \times 10^6} = \underline{2}$$

$$b). \text{ clock cycle}_1 = 2.6 \times 10^6$$

$$\text{clock cycle}_2 = 2 \times 10^6$$

$$c). \text{ CPU time}_1 = \frac{\text{clock cycle}_1}{\text{clock Rate}_1} = \frac{2.6 \times 10^6}{2.5 \times 10^9} = \frac{26}{25} \times 10^{-3} \text{ s}$$

$$\text{CPU time}_2 = \frac{\text{clock cycle}_2}{\text{clock Rate}_2} = \frac{2 \times 10^6}{3 \times 10^9} = \frac{2}{3} \times 10^{-3} \text{ s}$$

$$\frac{\text{CPU time}_1}{\text{CPU time}_2} = \frac{\frac{26}{25}}{\frac{2}{3}} = \frac{26 \times 3}{2 \times 25} = 1.56$$

$$\text{CPU time}_1 = 1.56 \text{ CPU time}_2$$

P_2 is 1.56 times faster than P_1 .

2. a). add x_{30}, x_5, x_6

$$80000000_{16} + D0000000_{16} = 150000000_{16}$$

$$(8 + D)_{16} = 8_{10} + 13_{10} = 21_{10} = 15_{16}$$

we can see the result is 36 bits, but reg max size is 32 bits.

This is overflow.

b). sub x_{30}, x_5, x_6

$$80000000_{16} - D0000000_{16}$$

$8_{16} = 1000$ negative number

$D = 1101$ negative number

$$\begin{array}{r} 1000 \\ - 1101 \rightarrow 0010 + 1 = 0011 \end{array}$$

$$\Rightarrow \begin{array}{r} 1000 \\ 0011 \\ \hline 1011 = B \end{array}$$

$$\Rightarrow 80000000_{16} - 70000000_{16} = B0000000_{16}$$

No overflow.

3. a.

$$23/2 = 11 \quad 1$$

$$11/2 = 5 \quad 1$$

$$5/2 = 2 \quad 1$$

$$2/2 = 1 \quad 0$$

$$1/2 = 0 \quad 1$$

$$23 = 10111$$

$$112/2 = 56 \quad 0$$

$$56/2 = 28 \quad 0$$

$$28/2 = 14 \quad 0$$

$$14/2 = 7 \quad 0$$

$$7/2 = 3 \quad 1$$

$$3/2 = 1 \quad 1$$

$$1/2 = 0 \quad 1$$

$$112 = 1110000$$

$$23_{10} = 00010111_2 = 11101000_2 + 1_2 = 11101001_2 = 233_{10}$$

$$112 = 01110000_2 = 10001111_2 + 1_2 = 10010000_2 = 144_{10}$$

Hence numbers in two complement are -233 and -144 .

The two's complement format result

$$-233 - 144 = -377 \text{ under min value of } -128.$$

so, result is -128 .

b). Same steps above, but

$$-233 - (-144) = -89 \text{ in range of } (-128, 127).$$

So, result is -89.

128 64 32 16 8 4 2 1

$$4 \cdot 64 = 0100\ 0000_2, 14 = 0000\ 1110$$

multiplicand

0100 0000

product

0000 0000 | 0000 1110 →

00000 0000 0000 111

01000 0000 0000 111 →

0010000 000 0000 11

0110000 000 0000 11 →

00110000 000 0000 1

0111 0000 000 0000 1 →

00111 0000 000 0000 →

0000 0011 1000 0000

$$6. a) 0x0C000000 = 0000\ 1100\ 00...0$$

sign exponent 23 bits fraction

$$00011000 = 24$$

$$\text{using } (-1)^S \cdot (1 + \text{Fraction}) \cdot 2^{\text{exp} - 127}$$

$$(-1)^0 (1 + 0) \cdot 2^{-103} = 1.0 \times 10^{-103}$$

b). binary of 63.25

$$63/2 = 31 \quad 1$$

$$31/2 = 15 \quad 1$$

$$15/2 = 7 \quad 1$$

$$7/2 = 3 \quad 1$$

$$3/2 = 1 \quad 1$$

$$1/2 = 0 \quad 1$$

$$(63)_{10} = 0011111_2$$

$$0.25 \times 2 = 0.5 \quad 0$$

$$0.5 \times 2 = 1.0 \quad 1$$

$$0.25_{10} = 0.01_2$$

$$63.25_{10} = 0011111.01_2 = 1.111101 \times 2^5$$

$$\text{adjusted exponent } 5 + 127 = 132_{10} = 10000100_2$$

$$\text{Sign} = 0$$

$$\text{fraction } 1111010000000000000000 \quad (23 \text{ bits})$$

single precision IEEE 754 format is

$$0100001001110100000000000000$$

$$5. 62_{10} = 111110_2$$

$$21_{10} = 010101_2$$

← Quot

Divisor →

Remainder

000 000	010101 000000	000 000 111 1110
000 000	0010101 000 00	000 000 111 1110
00 00 00	000101 010 000	000 000 111 1110
000 000	000 010 101 000	000 000 111 1110
000 000	000 001 010 100	000 000 111 1110
000 000	000 000 101 010	000 000 111 1110
000 001	000 000 101 010	000 000 010 100
000 001	000 000 010 101	000 000 010 100
000 010	000 000 001 010	000 000 010 100

rem > div, shift q left
with 1, shift div right

rem < div

shift q left with 0
shift div right

$$\text{quotient } 010_2 = 2_{10}$$

$$\text{remainder } 010100_2 = 20_{10}$$