# ST 512 Homework 3

```
library(dplyr)
```

Attaching package: 'dplyr'

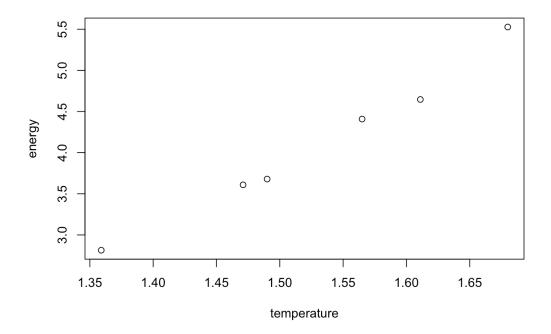
The following objects are masked from 'package:stats':

filter, lag

The following objects are masked from 'package:base':

intersect, setdiff, setequal, union

```
lamp <- read.table("lamp.txt", header = TRUE)
with(lamp, plot(energy ~ temperature))</pre>
```



```
lamp.model <- lm(log(energy) ~ temperature, data = lamp)</pre>
```

```
summary(lamp.model)
```

```
Call:
```

lm(formula = log(energy) ~ temperature, data = lamp)

#### Residuals:

1 2 3 4 5 6 -0.004769 0.012439 -0.007643 0.018037 -0.024505 0.006442

#### Coefficients:

Residual standard error: 0.01734 on 4 degrees of freedom Multiple R-squared: 0.9957, Adjusted R-squared: 0.9946 F-statistic: 918.5 on 1 and 4 DF, p-value: 7.061e-06

2.068 = estimate for O2 # #1 (2 points) Report the least-squares estimates of the parameters  $\theta$ 1 and  $\theta$ 2 for the lamp data. Show work or computer code.

#### $\theta 1 = .171 \ \theta 2 = 2.066$

```
model1 <- nls(energy \sim th1 * exp(th2 * temperature), data = lamp summary(model1)
```

Formula: energy ~ th1 \* exp(th2 \* temperature)

#### Parameters:

Estimate Std. Error t value Pr(>|t|)
th1 0.17075 0.02099 8.135 0.00124 \*\*
th2 2.06582 0.07810 26.452 1.21e-05 \*\*\*

Signif. codes: 0 '\*\*\* 0.001 '\*\* 0.01 '\* 0.05 '.' 0.1 ' ' 1

Residual standard error: 0.077 on 4 degrees of freedom

Number of iterations to convergence: 3
Achieved convergence tolerance: 9.712e-09

## #2

(1 point) Use your model fit from question 1 to predict the energy output of this lamp when the temperature is x = 1.4 (which corresponds to 1400 K). Show work or computer code.

## 3.084 energy per cm<sup>2</sup> per second

```
y_value <- .171 * exp(2.066 * 1.4)
```

# #3

Using the model in equation 2, calculate an F-statistic and a corresponding p-value to test for differences among the seasons when comparing days with the same temperature, precipitation, and type of day. That is, in notation, test H0:  $\beta 4 = \beta 5 = 0$ . Be sure to report both the F-statistic and the p-value, and be sure to give the associated df for the F-statistic. Show some work or computer code.

### F-statistic = .213, p-value = .8086, DF = 2

```
trailuser <- read.table("trailuser.txt", header = TRUE, strings/
trailuser$dayType <- as.factor(trailuser$dayType)
trailuser$season <- as.factor(trailuser$season)

contrasts(trailuser$dayType)</pre>
```

weekend weekend 1

## contrasts(trailuser\$season)

```
spring summer fall 0 0 spring 1 0 summer 0 1
```

```
additive_model <- lm(volume \sim avgtemp + precip + dayType + seasesummary(additive_model)
```

### Call:

lm(formula = volume ~ avgtemp + precip + dayType + season, data = trailuser)

#### Residuals:

```
Min 10 Median 30 Max -238.22 -42.98 16.33 47.33 217.44
```

#### Coefficients:

```
Estimate Std. Error t value Pr(>|t|)
                           83.261 -0.339 0.736027
(Intercept)
               -28.186
                 6.923
                            1.796 3.855 0.000262 ***
avgtemp
              -165.044
                           43.371 -3.805 0.000309 ***
precip
                86.200
                           29.380 2.934 0.004579 **
dayTypeweekend
                10.551
                           40.845 0.258 0.796948
seasonspring
                           63.647 -0.179 0.858336
               -11.404
seasonsummer
```

Signif. codes: 0 '\*\*\* 0.001 '\*\* 0.01 '\* 0.05 '.' 0.1 ' ' 1

Residual standard error: 97.94 on 67 degrees of freedom Multiple R-squared: 0.4573, Adjusted R-squared: 0.4168 F-statistic: 11.29 on 5 and 67 DF, p-value: 6.428e-08

```
full_model <- lm(volume ~ avgtemp + precip + dayType + season, or
reduced_model <- lm(volume ~ avgtemp + precip + dayType, data =
anova_results <- anova(reduced_model, full_model)
anova_results
```

#### Analysis of Variance Table

# #4

(1 point) Choose the best interpretation of the outcome from your test in question 3.

A. There is mildly strong evidence that trail usage differs among the three

seasons.

B. If we compare days with identical temperature, precipitation, and day type (that is, whether the day is a weekday or not), then there is mildly strong evidence that trail usage differs among the three seasons.

C. There is no evidence that trail usage differs among the three seasons.

D. If we compare days with identical temperature and precipitation, and day type (that is, whether the day is a weekday or not), then there is no evidence that trail usage differs among the three seasons.

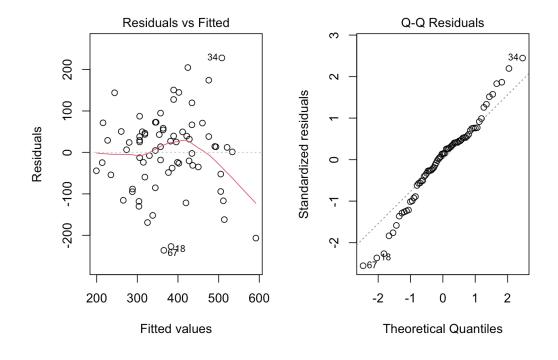
Answer = D

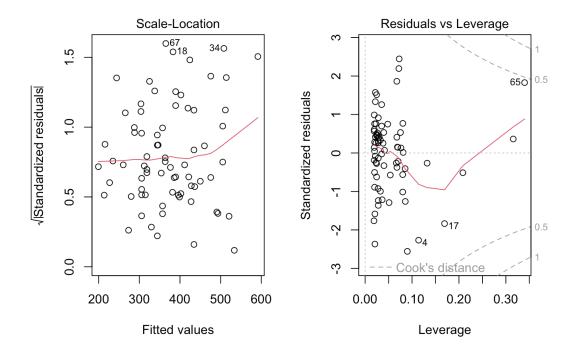
# #5

(2 points) In the model in equation 3, provide a brief non-technical interpretation of why the estimated partial regression coefficient associated with the quadratic effect of avgtemp is negative. That is, what have we learned from the fact that  $\beta^{\circ} < 0$ , and why does this make sense in the context of this particular data set?

While higher avgtemp initially leads to an increase in the number of trail users, there is a point in which further temperature increases result in decreased usage. This suggests that really high temperatures deter users.

```
par(mfrow = c(1, 2))
plot(reduced_model)
```





quadratic\_model <- lm(volume ~ avgtemp + I(avgtemp^2) + precip summary(quadratic\_model)</pre>

## Call:

```
lm(formula = volume ~ avgtemp + I(avgtemp^2) + precip +
dayType,
    data = trailuser)
```

#### Residuals:

```
Min 10 Median 30 Max -246.463 -43.313 7.456 47.170 209.489
```

#### Coefficients:

```
Estimate Std. Error t value Pr(>|t|)
(Intercept)
              -599.94041 249.20172 -2.407 0.018784 *
                            8.64793 3.216 0.001990 **
avgtemp
                27.81275
I(avgtemp^2)
                -0.18344
                            0.07369 - 2.489 0.015248 *
                           41.43765 -3.574 0.000653 ***
precip
              -148.07875
                           27.43205 3.414 0.001083 **
dayTypeweekend
                93.65017
               0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
Signif. codes:
```

Residual standard error: 93.36 on 68 degrees of freedom Multiple R-squared: 0.4995, Adjusted R-squared: 0.47 F-statistic: 16.96 on 4 and 68 DF, p-value: 1.086e-09

# #6

Use the model in equation 3 to complete each of the statements below:

(a) (1 point) "When comparing two week-end days with the same temperature, a day on which it rains 0.25 inches will have an average of **37.02 fewer** trail users than a day on which it doesn't rain."

```
.25 * -148.079
```

[1] -37.01975

b) (1 point) "When comparing two days with the same temperature and precipitation, a weekday will have an average of **93.65 fewer** trail users than a weekend day."

## #7

(1 point) Use the model in equation 3 to predict the trail usage on a weekday when the avgtemp =  $55 \cdot F$  and the precip = 0.15 in. Show some work or computer code.

#### 352.643

[1] 352.643

# #8

(1 point) Use the model in equation 4 to predict the trail usage on a weekday when the avgtemp =  $55 \cdot F$  and the precip = 0.15 in. Show some work or computer code.

#### 314.292

```
trailuser2 <- trailuser |>
  mutate(sqrt_precip = sqrt(precip))
```

1 314.2928

# #9

\*\*I would favor reporting model 4

# #10

a. (1 point) Which of the following statements provides the best interpretation of the fact that β3 > 0? Choose the best answer. A. As BP increases, the slope of the association between Y and BMI increases. B. As BP increases, the slope of the association between Y and BMI decreases. C. BMI and BP are positively correlated. D. Both choices B and C are reasonable interpretations. E. None of the above are reasonable interpretations.

#### Answer = A

b) (2 points) Use the model to predict the response for someone who has a BMI of 25 and a blood pressure (BP) of 90.

#### 139.35

```
intercept <- 66.45
beta_BMI <- -1.62
beta_BP <- -1.49
beta_interaction <- 0.11

BMI <- 25
BP <- 90

interaction_term <- BMI * BP

predicted_response <- intercept + (beta_BMI * BMI) + (beta_BP * predicted_response)</pre>
```

- [1] 139.35
- c. (4 points) Which of the statements below are supported by the fit and

analysis of the multiple regression model? Choose 'supported' if the statement is supported by the analysis of the multiple regression model, and 'not supported' if it is not supported.

i. Using the conventional threshold for statistical signif- icance, there is statistically significant evidence that the association between BMI and the response depends on the value of BP.

### **SUPPORTED**

ii. The average value of the response is 66.45.

#### **NOT SUPPORTED**

iii. The multiple regression model provides a significantly better fit than a model that includes only an intercept.

#### SUPPORTED

iv. The multiple regression model explains roughly 40% of the variation in the response.

#### SUPPORTED