

COMPUTER PROJECT #3

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ABSTRACT

A staggered grid Navier-Stokes solver is implemented to solve a driven cavity problem, and a channel flow problem. The Pressure, u-velocity and v-velocity are all staggered and solved for separately. The necessary equations and the implemented code is provided in this paper.

NOMENCLATURE

- u Velocity in the x-direction (m/s)
 u_i Velocity in the x-direction referencing neighbor $i(N, E, S, W, P)$ lowercase (n, e, s, w) indicates averaged values
 u_P^{old} Velocity in the x-direction from previous iteration on node center
 v Velocity in the y-direction
 v_i Velocity in the y-direction referencing neighbor $i(N, E, S, W, P)$ lowercase (n, e, s, w) indicates averaged values
 v_P^{old} Velocity in the y-direction from previous iteration on node center
 P Pressure
 i' Correction term for $i(u, v, P)$
 $a_{i,j}$ Coefficient for final discretized equation referencing neighbor $i(N, E, S, W, P)$ on $j(u, v, P)$ mesh
 $\tilde{a}_{P,j}$ Coefficient for final discretized equation referencing center P on $j(u, v, P)$ mesh and divided by Ω correction factor
 Ω non-linear correction factor for momentum equations
 Ω_P linear correction factor for pressure equation
 α Pressure blending factor

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1 INTRODUCTION

In order to solve the Navier Stokes equation in two dimensions a staggered grid approach was used. This where the u , v , and P values were all saved in separate locations on the grid. This allowed for many of the oscillations to be minimized and for the solution to converge to a correct solution.

Two cases were considered in this problem. These cases were a driven cavity and a channel flow. The inputs and requirements are shown on the problem outline.

The numerical method, application with code, and results are shown in the following sections.

2 NUMERICAL METHOD

In order to solve using this method, a staggered grid was utilized. Fig. 1 shows how the u , v , and P values were saved on the grid. The momentum equation is discretized from Eq. 1 to 2.

$$\frac{\partial(\rho uu)}{\partial x} + \frac{\partial(\rho vu)}{\partial y} = -\frac{\partial P}{\partial x} + \frac{\partial}{\partial x} \left(\mu \frac{\partial u}{\partial x} \right) + \frac{\partial}{\partial y} \left(\mu \frac{\partial u}{\partial y} \right) + \frac{\partial}{\partial x} \left(\mu \frac{\partial u}{\partial x} \right) + \frac{\partial}{\partial y} \left(\mu \frac{\partial v}{\partial y} \right) \quad (1)$$

$$u_P = (1 - \Omega)u_P^{old} + \frac{1}{\tilde{a}_{P,u}} [a_{E,u}u_E + a_{W,u}u_W + a_{N,u}u_N + a_{S,u}u_S + dy(P_w - P_e)]$$

where:

$$\begin{aligned} a_{E,u} &= \max(-\rho u_e dy, 0) + \mu dy/dx \\ a_{N,u} &= \max(-\rho v_n dx, 0) + \mu dx/dy \\ a_{W,u} &= \max(\rho u_w dy, 0) + \mu dy/dx \\ a_{S,u} &= \max(\rho v_s dx, 0) + \mu dx/dy \end{aligned} \quad (2)$$

The following equations (Eq. 3 and 4) show the discretized equations used for v velocity momentum.

$$\frac{\partial(\rho uv)}{\partial x} + \frac{\partial(\rho vv)}{\partial y} = -\frac{\partial P}{\partial x} + \frac{\partial}{\partial x} \left(\mu \frac{\partial v}{\partial x} \right) + \frac{\partial}{\partial y} \left(\mu \frac{\partial v}{\partial y} \right) + \frac{\partial}{\partial x} \left(\mu \frac{\partial u}{\partial x} \right) + \frac{\partial}{\partial y} \left(\mu \frac{\partial v}{\partial y} \right) \quad (3)$$

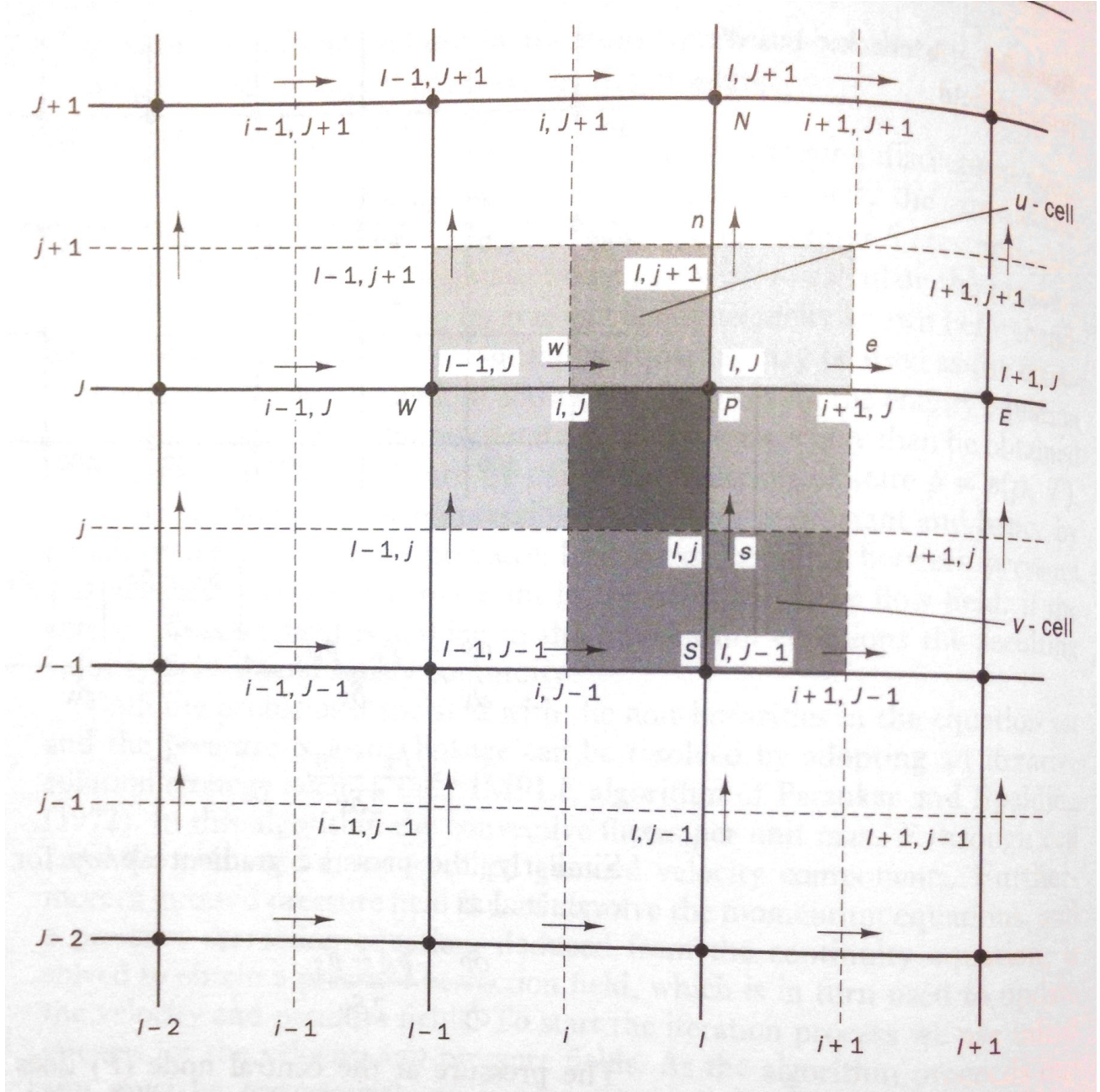


FIGURE 1. REPRESENTATION OF STENCIL FOR GRID GENERATION

$$v_P = (1 - \Omega)v_P^{old} + \frac{1}{\tilde{a}_{P,v}} [a_{E,v}v_E + a_{W,v}v_W + a_{N,v}v_N + a_{S,v}v_S + dy(P_s - P_n)]$$

where:

$$a_{E,v} = \max(-\rho u_e dy, 0) + \mu dy/dx$$

$$a_{N,v} = \max(-\rho v_n dx, 0) + \mu dx/dy$$

$$a_{W,v} = \max(\rho u_w dy, 0) + \mu dy/dx$$

$$a_{S,v} = \max(\rho v_s dx, 0) + \mu dx/dy$$

(4)

It should be noted that these equations took into account the spacing on the boundary. That is, if there was a ghost node that was used in the coefficient calculations, then the $\mu dx/dy$ like terms became $\mu 2dx/dy$ terms on the North and South boundaries for the u momentum calculations.

The pressure was discretized from continuity, staggered control volume equations, and velocity correction terms. Thus, the continuity equation shown in Eq. 5 is discretized to Eq. 6.

$$\frac{\partial(\rho u)}{\partial x} + \frac{\partial(\rho v)}{\partial y} = 0 \quad (5)$$

$$\begin{aligned} P'_P &= P'_P + \frac{\Omega_P}{a_{P,P}} (a_{E,P}P'_E + a_{W,P}P'_W + a_{N,P}P'_N + a_{S,P}P'_S - S - a_{P,P}P'_P) \\ P &= P^{old} + \alpha P' \end{aligned} \quad (6)$$

It should be noted that momentum is non-linear so the relaxation factors used were $\Omega \approx 0.6$ and the $\Omega_P \approx 1.7$ while $\alpha \approx 0.3$ for the linear pressure equation.

These equations were implemented into a code structure shown in the diagram in Fig. 2. The code is referenced in Sec. A. It is also noted that the velocity correction terms were also implemented as shown in Eq. 7 and implemented as depicted in Fig. 2.

$$\begin{aligned} u'_P &= \frac{dy}{a_{W,u}} (P_W - P_P) \\ v'_P &= \frac{dx}{a_{S,u}} (P_S - P_P) \end{aligned} \quad (7)$$

3 RESULTS

3.1 Driven Cavity

The following plots show the u, v, P and the iterations required to converge. Additionally, the $x = 0.5$ u values are provided.

The below two plots show the u (left) and v (right) velocity contours.

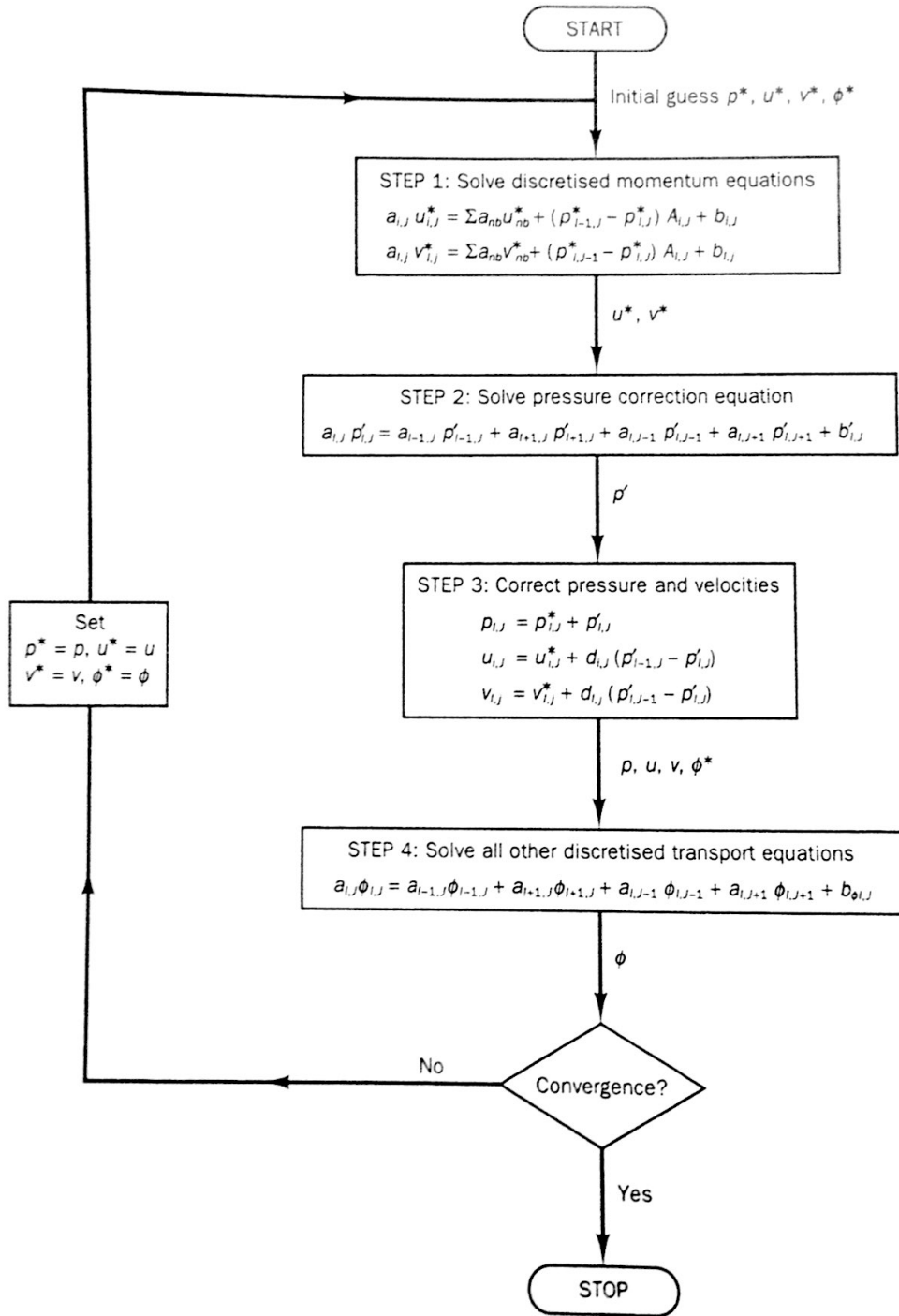
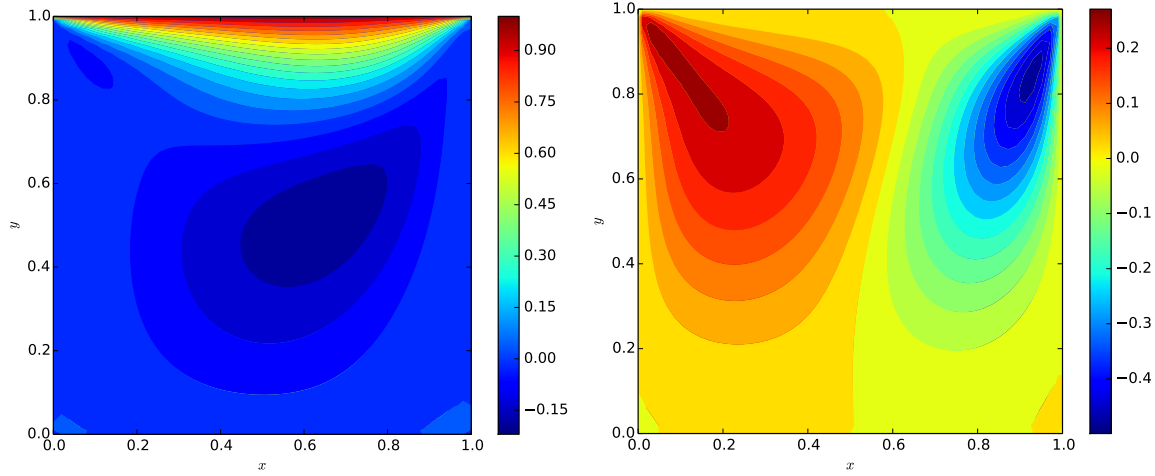
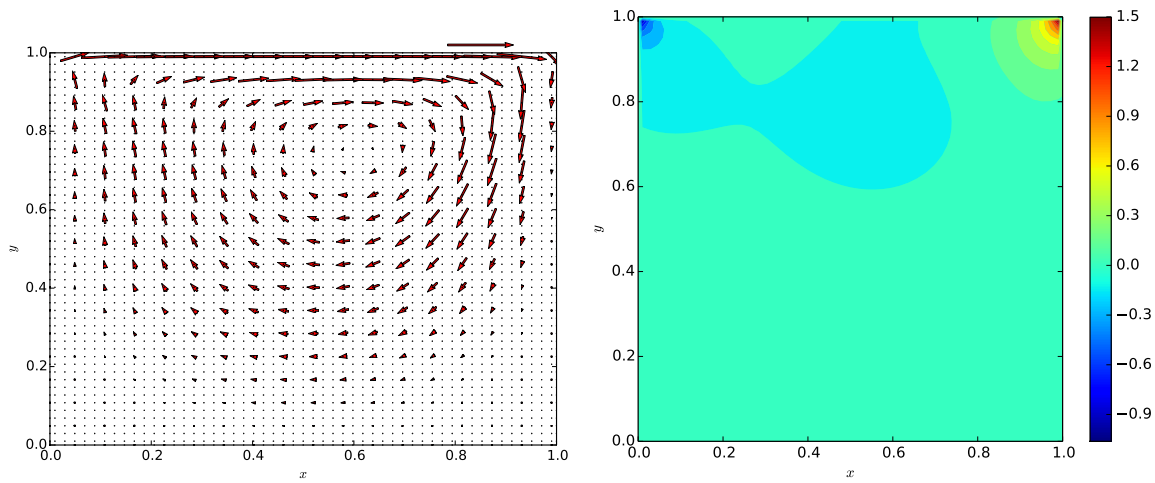


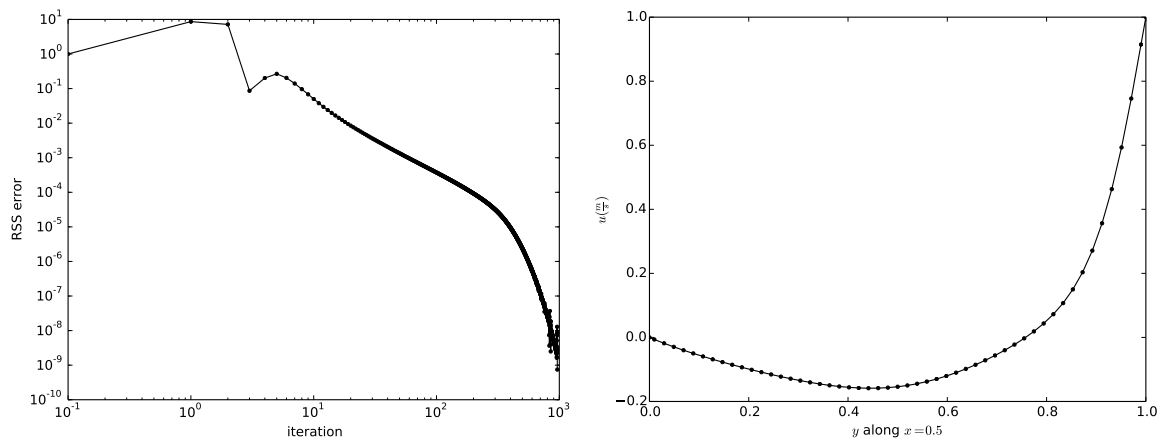
FIGURE 2. Outline of code structure



The below two plots show the vector plots of velocity magnitude (left) and the pressure contour (right).



The below two plots show the error vs iterations (left) and the $x = 0.5$ u values (right).



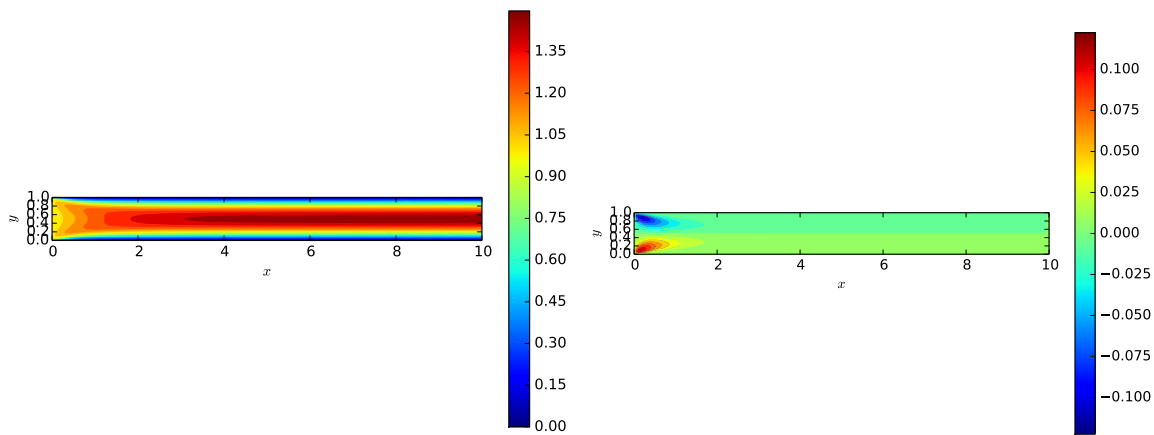
The final mass imbalance for this 51X51 cell simulation was shown to be 1.60E-017.

3.2 Channel Flow

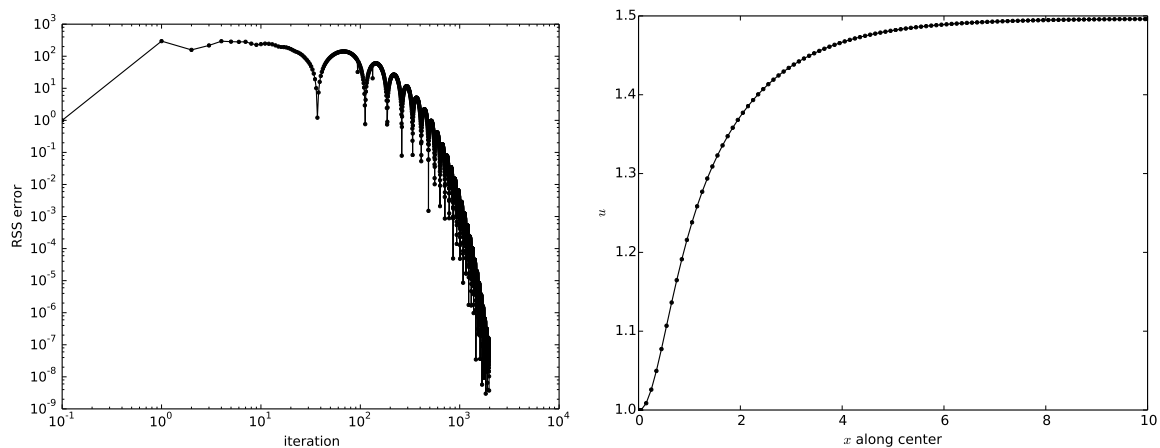
For this solution to function properly, the proper boundary condition needed to be applied. Since the channel was long enough, the boundary condition to be applied was in the u momentum solver. We just set the outside condition to be equal to the flow directly upstream. This allowed for flow to flow outside of the wall boundary.

In addition to the plot provided in the above section. The u velocity for the centerline of the duct is shown. The wall shear stress is also shown along both the upper and lower walls from the inlet to the outlet.

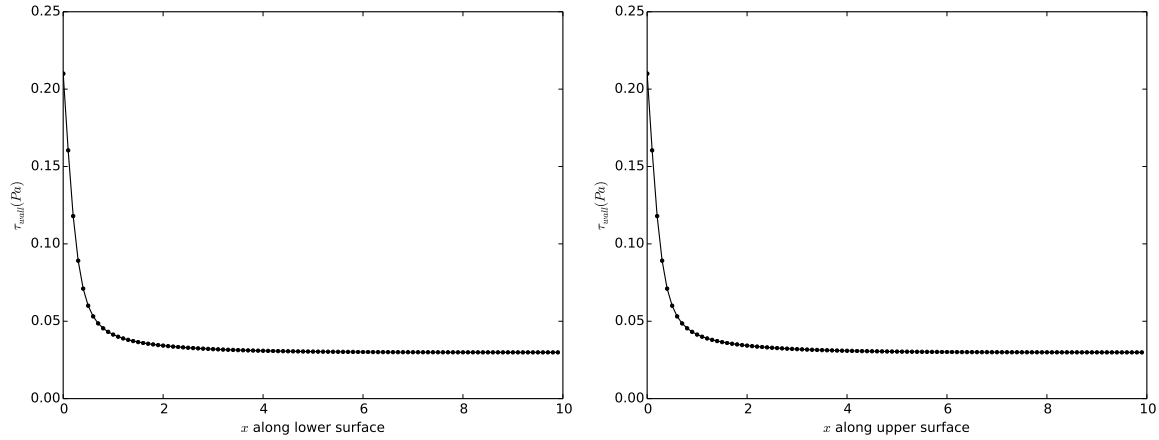
The below two plots show the u (left) and v (right) velocity contours.



The below two plots show the error vs iterations (left) and the $y = 0.5$ u values (right).



The below two plots show the wall shear stress on the lower (left) and upper (right) surfaces.



The final mass imbalance for this 21X100 cell problem was shown to be 7.44E-023

4 CONCLUSION

We have demonstrated a computational fluid dynamics solver for a driven cavity and for a channel flow study. We have shown the staggered grid approach using two dimensional u, v , and P solvers.

A Code

A.1 Subroutines

```

1  MODULE types
2      !purpose: define data type struct
3      IMPLICIT NONE
4      ! Properties of fluid flow
5      REAL    :: Omega = 0.6 ! Relaxation factor for momentum non-linear
6      REAL    :: OmegaP= 1.7 ! Relaxation factor for pressure correction linear
7      REAL    :: alpha = 0.3 ! relaxation factor for pressure correction
8      REAL    :: mu = 0.01  ! dynamic viscosity
9      REAL    :: rho= 1.    ! density
10     REAL    :: Convergence = 1.e-14
11     REAL    :: Convergence2= 1.e-9
12     INTEGER  :: max_iter = 1000000
13     INTEGER  :: max_iter2= 700
14     INTEGER  :: max_iter3= 7000
15     TYPE:: dat
16         REAL:: xu,yv,xp,yp
17         REAL:: u,v,u_old,v_old !u,v is in bottom left corner, or south and west sides of cell
18         REAL:: APu,AEu,ANu,ASu,AWu,Apv,AEv,ANv,ASv,AWv,APp,AEp,ANp,AWp,ASp
19         REAL:: P,Pp,P_old
20         REAL:: S ! source terms
21         INTEGER:: n
22     END TYPE dat
23 CONTAINS
24     SUBROUTINE set_xy ( struct,dx,dy,nx,ny,x,y)
25         real,intent(in)    :: dx,dy,x,y
26         integer,intent(in) :: nx,ny ! size of struct in x and y directions
27         type(dat),dimension(0:nx-1,0:ny-1),intent(inout):: struct ! data contained from 0:nx-1 where cells 0 and nx-1 are
            boundary nodes (cell volume approaches 0 on boundary nodes)
28         integer :: i,j,n ! for do loops and n is counter for cell number
29         real    :: xi,yi ! x and y values for each cell
30         ! left boundary
31         struct(0,:)%xp= 0.
32         struct(0,0)%yp= 0.

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33      strct(0,1:ny-1)%yp= reshape((/ (i*dy - dy/2. ,i=1,ny-1) /),(/ ny-1/))
34      strct(0,ny+0)%yp= y
35      ! bottom boundary
36      strct(0,0)%xp= 0.
37      strct(1:nx-1,0)%xp= reshape((/ (i*dx - dx/2. ,i=1,nx-1) /),(/ nx-1/))
38      strct(nx+0,0)%xp= x
39      strct(:,0)%yp= 0.
40      ! right boundary
41      strct(nx+0,:)%xp= x
42      strct(nx+0,:)%yp= strct(0,:)%yp
43      ! top boundary
44      strct(:,ny+0)%xp= strct(:,0)%xp
45      strct(:,ny+0)%yp= y
46
47      n=1                      ! cell number 1
48      DO i=1,ny-1              ! 1 to ny-2 for boundary nodes (we only are iterating through the middle values)
49          yi = i*dy - dy/2.    ! y coordinate
50          DO j=1,nx-1
51              xi = j*dx - dx/2. ! x coordinate
52              strct(j,i)%n = n  ! input n node
53              strct(j,i)%xp= xi ! x coordinate to strct
54              strct(j,i)%yp= yi ! y coordinate to strct
55              n=n+1             ! count cell numbers up one
56          END DO
57      END DO
58      ! set xu and yv to similar values (but for the staggered grids of each)
59      strct%xu = strct%xp - dx/2.
60      strct%yv = strct%yp - dy/2.
61      strct(:,ny)%yv=y         !top
62      strct(:,0)%yv=0.         !bottom
63      strct(0:1,:)%xu=0.       !left
64      strct(nx,:)%xu=x         !right
65  END SUBROUTINE set_xy
66
67  SUBROUTINE mom_uv(strct,dx,dy,nx,ny)
68      ! requires uniform grid of dx and dy spacing
69      REAL,INTENT(IN)      :: dx,dy
70      INTEGER,INTENT(IN)   :: nx,ny! size of strct in x and y directions
71      TYPE(dat),DIMENSION(0:nx+1,0:ny+1),INTENT(INOUT):: strct ! data contained from 0:nx+1 where cells 0 and
72      ! nx+1 are boundary nodes (cell volume approaches 0 on boundary nodes)
73      REAL      :: mdot ! temporary value for mass flow values
74      INTEGER   :: i,j,iter=0!loop iterators
75      REAL      :: error=1.,error2=1.
76
77      ! mdot and Au values
78      !$OMP PARALLEL DO
79      DO i=1,nx
80          DO j=1,ny
81              mdot = rho*(strct(i+1,j)%u_old+strct(i,j)%u_old)/2.*dy ! east face
82              strct(i,j)%AEu = max(-mdot,0.) + mu*dy/dx
83              mdot = rho*(strct(i-1,j+1)%v_old+strct(i,j+1)%v_old)/2.*dx ! north face
84              strct(i,j)%ANu = max(-mdot,0.) + mu*2.*dx/dy
85          ELSE
86              strct(i,j)%ANu = max(-mdot,0.) + mu*dx/dy
87          END IF
88          mdot = rho*(strct(i-1,j)%u_old+strct(i,j)%u_old)/2.*dy ! West face
89          strct(i,j)%AWu = max(mdot,0.) + mu*dy/dx
90          mdot = rho*(strct(i-1,j)%v_old+strct(i,j)%v_old)/2.*dx ! south face
91          IF (j==1) THEN
92              strct(i,j)%ASu = max(mdot,0.) + mu*2.*dx/dy
93          ELSE
94              strct(i,j)%ASu = max(mdot,0.) + mu*dx/dy
95          END IF
96          strct(i,j)%APu = strct(i,j)%AEu + &

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97         strect(i,j)%ANu + &
98         strect(i,j)%AWu + &
99         strect(i,j)%ASu
100     strect(i,j)%APu      = strect(i,j)%APu/Omega
101 END DO
102 !SOMP END PARALLEL DO
103
104 ! mdot and Av values
105 !SOMP PARALLEL DO
106 DO i=1,nx
107     DO j=1,ny
108         mdot = rho*(strect(i+1,j-1)%u_old+strect(i+1,j)%u_old)/2.*dy ! east face
109         IF (i==nx) THEN
110             strect(i,j)%AEv = max(-mdot,0.) + mu*2.*dy/dx
111         ELSE
112             strect(i,j)%AEv = max(-mdot,0.) + mu*dy/dx
113         END IF
114         mdot = rho*(strect(i,j+1)%v_old+strect(i,j)%v_old)/2.*dx ! north face
115         strect(i,j)%ANv = max(-mdot,0.) + mu*dx/dy
116         mdot = rho*(strect(i,j-1)%u_old+strect(i,j)%u_old)/2.*dy ! West face
117         IF (i==1) THEN
118             strect(i,j)%AWv = max(mdot,0.) + mu*2.*dy/dx
119         ELSE
120             strect(i,j)%AWv = max(mdot,0.) + mu*dy/dx
121         END IF
122         mdot = rho*(strect(i,j-1)%v_old+strect(i,j)%v_old)/2.*dx ! south face
123         strect(i,j)%ASv = max(mdot,0.) + mu*dx/dy
124         strect(i,j)%APv = strect(i,j)%AEv + &
125             strect(i,j)%ANv + &
126             strect(i,j)%AWv + &
127             strect(i,j)%ASv
128         strect(i,j)%APv = strect(i,j)%APv/Omega
129     END DO
130 END DO
131 !SOMP END PARALLEL DO
132
133 ! solve u-momentum
134 error2 = 1.
135 DO iter=1,max_iter
136     error2=error
137     error = 0.
138     DO i=2,nx
139         DO j=1,ny
140             strect(i,j)%u = (1.-Omega)*strect(i,j)%u_old &
141                 + &
142                 (1./strect(i,j)%APu) &
143                 * (&
144                     strect(i,j)%AEu*strect(i+1,j)%u + &
145                     strect(i,j)%ANu*strect(i,j+1)%u + &
146                     strect(i,j)%AWu*strect(i-1,j)%u + &
147                     strect(i,j)%ASu*strect(i,j-1)%u + &
148                     (strect(i-1,j)%P_old-strect(i,j)%P_old) &
149                     *dy &
150                 )
151             error = error + (strect(i,j)%u - strect(i,j)%u_old)**2
152         END DO
153     END DO
154     strect(nx+1,:)%u=strect(nx,:)%u
155     error=sqrt(error)
156     IF (abs(error - error2)<Convergence) EXIT ! error stops changing convergence
157 END DO
158 WRITE(*,*) sum(rho*dy*strect(0,:)%u)/sum(rho*dy*strect(nx+1,:)%u),iter
159 WRITE(*,*) iter,abs(error-error2)
160
161

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162      ! solve v-momentum
163      error2 = 1.
164      DO iter=1,max_iter
165          error2=error
166          error = 0.
167          DO i=1,nx
168              DO j=2,ny
169                  strtct(i,j)%v = (1.-Omega)*strtct(i,j)%v_old &
170                      + &
171                      (1./ strtct(i,j)%APv) &
172                      * (&
173                          strtct(i,j)%AEv*strtct(i+1,j)%v +&
174                          strtct(i,j)%ANv*strtct(i,j+1)%v +&
175                          strtct(i,j)%AWv*strtct(i-1,j)%v +&
176                          strtct(i,j)%ASv*strtct(i,j-1)%v +&
177                          (strtct(i,j-1)%P_old-strtct(i,j)%P_old) * &
178                          dy &
179                      )
180                  error = error + (strtct(i,j)%v - strtct(i,j)%v_old)**2
181              END DO
182          END DO
183          error=sqrt(error)
184          IF (abs(error - error2)<Convergence) EXIT ! error stops changing convergence
185      END DO
186      WRITE(*,*) iter ,abs(error-error2)
187  END SUBROUTINE mom_uv
188
189  SUBROUTINE vel_correction(strtct,dx,dy,nx,ny)
190      ! requires uniform grid of dx and dy spacing
191      REAL,INTENT(IN) :: dx,dy
192      INTEGER,INTENT(IN) :: nx,ny! size of strtct in x and y directions
193      TYPE(dat),DIMENSION(0:nx+1,0:ny+1),INTENT(INOUT) :: strtct ! data contained from 0:nx+1 where cells 0 and
194          nx+1 are boundary nodes (cell volume approaches 0 on boundary nodes)
195      INTEGER :: i,j,iter=0 !loop iterators
196      REAL :: error,error2
197      REAL :: S_sum
198      !$OMP PARALLEL DO
199      DO i=1,nx
200          DO j=1,ny
201              IF (i==nx) THEN
202                  strtct(i,j)%AEp = 0.
203              ELSE
204                  strtct(i,j)%AEp = rho*dy*dy / strtct(i+1,j)%APu
205              END IF
206              IF (j==ny) THEN
207                  strtct(i,j)%ANp = 0.
208              ELSE
209                  strtct(i,j)%ANp = rho*dx*dx / strtct(i,j+1)%APv
210              END IF
211              IF (i==1) THEN
212                  strtct(i,j)%AWp = 0.
213              ELSE
214                  strtct(i,j)%AWp = rho*dy*dy / strtct(i,j)%APu
215              END IF
216              IF (j==1) THEN
217                  strtct(i,j)%ASp = 0.
218              ELSE
219                  strtct(i,j)%ASp = rho*dx*dx / strtct(i,j)%APv
220              END IF
221              strtct(i,j)%APp = strtct(i,j)%AEp + &
222                  strtct(i,j)%ANp + &
223                  strtct(i,j)%AWp + &
224                  strtct(i,j)%ASp
225          END DO
226      END DO

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226 !$OMP END PARALLEL DO
227 error =1.
228 error2=1.
229 DO iter=1,max_iter2
230     error2=error
231     error=0.
232     S_sum = 0.
233     !$OMP PARALLEL DO
234     DO i=1,nx
235         DO j=1,ny
236             strt(i,j)%S = &          ! source terms
237             (rho*strt(i+1,j)%u-rho*strt(i,j)%u)*dy&
238             + (rho*strt(i,j+1)%v-rho*strt(i,j)%v)*dx
239         END DO
240     END DO
241     !$OMP END PARALLEL DO
242     DO i=1,nx
243         DO j=1,ny
244             strt(i,j)%Pp = strt(i,j)%Pp + (OmegaP/strt(i,j)%APp)&
245             *(&
246             + strt(i,j)%AEp*strt(i+1,j)%Pp&
247             + strt(i,j)%AWp*strt(i-1,j)%Pp&
248             + strt(i,j)%ANp*strt(i,j+1)%Pp&
249             + strt(i,j)%ASp*strt(i,j-1)%Pp&
250             - strt(i,j)%S          &
251             - strt(i,j)%APp*strt(i,j)%Pp&
252             )
253         END DO
254     END DO
255     !$OMP PARALLEL DO
256     DO i=1,nx
257         DO j=1,ny
258             strt(i,j)%P=strt(i,j)%P_old+alpha*strt(i,j)%Pp
259         END DO
260     END DO
261     !$OMP END PARALLEL DO
262     DO i=1,nx
263         DO j=1,ny
264             error = error + (strt(i,j)%P - strt(i,j)%P_old)**2
265             S_sum = S_sum + strt(i,j)%S**2
266             IF (ISNAN(strt(i,j)%Pp)) THEN
267                 WRITE(*,*) "error on ",i,j
268                 STOP
269             END IF
270         END DO
271     END DO
272     IF (abs(error - error2)<Convergence) THEN ! error stops changing convergence
273         EXIT
274     END IF
275 END DO
276 WRITE(*,*) iter,S_sum,abs(error-error2) ! output iterations along with RSS of source term
277 !$OMP PARALLEL DO
278 DO i=2,nx
279     DO j=1,ny
280         strt(i,j)%u=strt(i,j)%u + (strt(i-1,j)%Pp - strt(i,j)%Pp) *dy/strt(i,j)%APu
281     END DO
282 END DO
283 !$OMP END PARALLEL DO
284 !$OMP PARALLEL DO
285 DO i=1,nx
286     DO j=2,ny
287         strt(i,j)%v=strt(i,j)%v + (strt(i,j-1)%Pp - strt(i,j)%Pp) *dx/strt(i,j)%APv
288     END DO
289 END DO
290 !$OMP END PARALLEL DO

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```

291  END SUBROUTINE vel_correction
292
293  SUBROUTINE Solve_NS (strct ,dx,dy,nx,ny)
294      REAL,INTENT(IN)      :: dx,dy
295      INTEGER,INTENT(IN)    :: nx,ny! size of strct in x and y directions
296      TYPE(dat),DIMENSION(0:nx+1,0:ny+1),INTENT(INOUT):: strct ! data contained from 0:nx+1 where cells 0 and
        nx+1 are boundary nodes (cell volume approaches 0 on boundary nodes)
297      INTEGER :: i,j,iter=0!loop iterators
298      REAL    :: error2=1.,error_RSS=0.
299
300      open(unit=8,file="output/iter.txt")
301      108 FORMAT(2ES16.7)
302      WRITE(8,108) 0.1,1.
303      DO iter=1,max_iter3
304          ! step 1 solve discretised momentum equations
305          CALL mom_uv(strct,dx,dy,nx,ny)
306
307          ! step 2 Solve pressure correction equation
308          ! step 3 Correct pressure and velocities
309          CALL vel_correction(strct,dx,dy,nx,ny)
310
311          ! step 4 Solve all other discretised transport equations
312          ! not implemented
313
314          ! if no convergence, then iterate
315          error2 = error_RSS
316          error_RSS = 0.
317          DO i=1,nx
318              DO j=1,ny
319                  error_RSS = error_RSS + (strct(i,j)%u-strct(i,j)%u_old)**2
320                  error_RSS = error_RSS + (strct(i,j)%v-strct(i,j)%v_old)**2
321                  error_RSS = error_RSS + (strct(i,j)%P-strct(i,j)%P_old)**2
322              END DO
323          END DO
324          error_RSS = sqrt(error_RSS)
325
326          ! reset values
327          strct%u_old = strct%u
328          strct%v_old = strct%v
329          strct%P_old = strct%P
330
331          ! if converged then stop
332          WRITE(8,108) REAL(iter),abs(error_RSS-error2)
333          IF (abs(error_RSS-error2) <= Convergence2) THEN
334              WRITE(*,*) "converged on iteration and error big loop = ",iter,abs(error_RSS-error2)
335              EXIT
336          ELSE
337              WRITE(*,*) "iteration and error big loop = ",iter,abs(error_RSS-error2)
338          END IF
339      END DO
340      close(8)
341  END SUBROUTINE Solve_NS
342  END MODULE types

```

A.2 Main program

```

1  ! user defined variables to define finite volume
2  ! x and y direction # of cells
3  #define max_x 101
4  #define max_y 21
5  ! x and y number of cells plus 1
6  #define max_xp 102
7  #define max_yp 22
8  ! x and y number of cells plus 2 (to account for boundary nodes)
9  #define max_x2p 103
10 #define max_y2p 23

```

```

11  ! length of x and y
12  #define len_x 10.
13  #define len_y 1.
14
15  PROGRAM project3
16      USE types !use module defined by types
17      IMPLICIT NONE
18      ! declare variables
19      INTEGER :: i,j!, iter!, max_x=20, max_y=20
20      REAL    :: dx, dy
21      REAL    :: Lu, Ru, Tu, Bu ! boundary condition u velocity values
22      TYPE(dat), DIMENSION(0:max_xp, 0:max_yp) :: data ! 22 if you count edges (thin cell)
23      REAL    :: TIME1, TIME2 ! for time of computation
24
25      ! set dx and dy and gamma and coefficients (without dividing by delta x between node centers)
26      dx=len_x/REAL(max_x)
27      dy=len_y/REAL(max_y)
28      ! initialize data and x,y for middle values
29      CALL set_xy(data, dx, dy, max_xp, max_yp, len_x, len_y)
30
31      !! initialize BC's
32      ! BC's
33      Lu = 1.
34      Ru = 0.
35      Tu = 0.
36      Bu = 0.
37      data%u = 0. ! initialize all data
38      ! left Boundary
39      data(1,:)%u = Lu
40      data(0,:)%u = Lu
41      ! bottom boundary
42      data(:,0)%u = Bu
43      ! right boundary
44      data(max_xp,:)%u = Ru
45      ! top boundary
46      data(:,max_yp)%u = Tu
47
48      ! initialize u
49      data%u_old = data%u
50      ! initialize v
51      data%v_old = 0.
52      data%v = 0.
53      ! initialize P values
54      data%Pp=0.
55      data%P_old=0.
56      data%P = 0.
57
58      ! solving Navier-Stokes 2-D using the staggered grid method
59      CALL CPU_TIME(TIME1)
60      CALL Solve_NS(data, dx, dy, max_x, max_y)
61      CALL CPU_TIME(TIME2)
62      WRITE(*,*) "CPU Time = ", TIME2-TIME1
63
64      ! output
65      ! user will need to specify size of
66      open(unit= 9, file="output/x.txt")
67      open(unit=10, file="output/y.txt")
68      open(unit=11, file="output/xu.txt")
69      open(unit=12, file="output/yv.txt")
70      open(unit=13, file="output/u.txt")
71      open(unit=14, file="output/v.txt")
72      open(unit=15, file="output/P.txt")
73      open(unit=16, file="output/u_spot.txt")
74      open(unit=17, file="output/tau_upper.txt")
75      open(unit=18, file="output/tau_lower.txt")

```

```

76  open(unit=19,file="output/u_center.txt")
77  100 FORMAT (max_x2p ES16.7)
78  101 FORMAT (2ES16.7)
79  102 FORMAT (max_xp ES16.7)
80  WRITE( 9,100) ( data(:,i)%xp,i=0,max_yp )
81  WRITE(10,100) ( data(:,i)%yp,i=0,max_yp )
82  WRITE(11,100) ( data(:,i)%xu,i=0,max_yp )
83  WRITE(12,100) ( data(:,i)%yv,i=0,max_yp )
84  WRITE(13,100) ( data(:,i)%u ,i=0,max_yp )
85  WRITE(14,100) ( data(:,i)%v ,i=0,max_yp )
86  WRITE(15,100) ( data(:,i)%P ,i=0,max_yp )
87  DO i=0,max_xp
88      !IF ( data(i,1)%xu <= 0.51 .AND. data(i,1)%xu >=0.49) THEN
89      IF (data(i,1)%xu <= 0.41 .AND. data(i,1)%xu >=0.39) THEN
90          DO j=0,max_yp
91              WRITE(16,101) data(i,j)%u,data(i,j)%yp
92          END DO
93      END IF
94  END DO
95  WRITE(17,102) ( mu*(data(i,max_y)%u-data(i,max_yp)%u)/dy ,i=0,max_x )
96  WRITE(18,102) ( mu*(data(i,1)%u-data(i,0)%u)/dy ,i=0,max_x )
97  DO i=0,max_xp
98      !IF ( data(i,1)%xu <= 0.51 .AND. data(i,1)%xu >=0.49) THEN
99      DO j=0,max_yp
100          IF (data(i,j)%yp <= 0.51 .AND. data(i,j)%yp >=0.49) THEN
101              WRITE(19,101) data(i,j)%u,data(i,j)%xp
102          END IF
103      END DO
104  END DO
105  close(9);close(10);close(11);close(12);close(13);close(14);close(15);close(16);close(17);close(18);close(19)
106 END PROGRAM project3

```