

Context-Free Grammar (CFG)

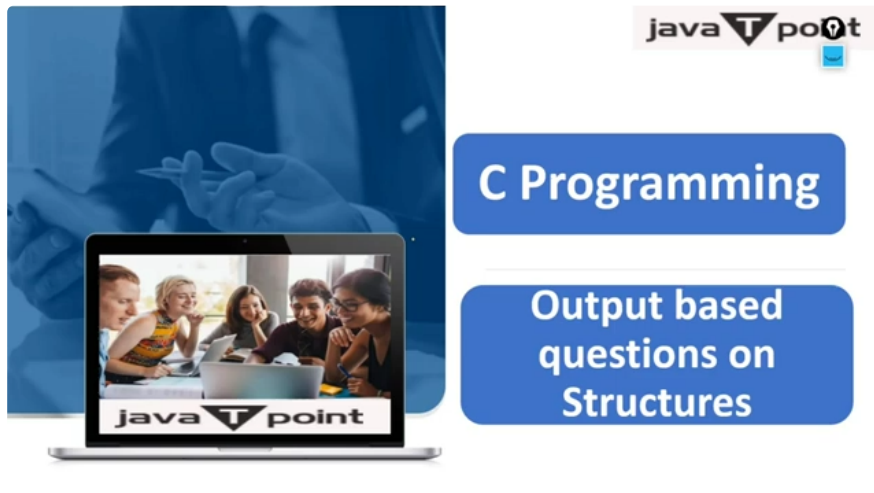
CFG stands for context-free grammar. It is a formal grammar which is used to generate all possible patterns of strings in a given formal language. Context-free grammar G can be defined by four tuples as:

$$G = (V, T, P, S)$$

Where,

G is the grammar, which consists of a set of the production rule. It is used to generate the string of a language.

T is the final set of a terminal symbol. It is denoted by lower case letters.



V is the final set of a non-terminal symbol. It is denoted by capital letters.

P is a set of production rules, which is used for replacing non-terminals symbols (on the left side of the production) in a string with other terminal or non-terminal symbols (on the right side of the production).

S is the start symbol which is used to derive the string. We can derive the string by repeatedly replacing a non-terminal by the right-hand side of the production until all non-terminal have been replaced by terminal symbols.

Example 1:

Construct the CFG for the language having any number of a's over the set $\Sigma = \{a\}$.

Solution:

As we know the regular expression for the above language is

$$\text{r.e.} = a^*$$

Production rule for the Regular expression is as follows:

$$S \rightarrow aS \quad \text{rule 1}$$

$$S \rightarrow \epsilon \quad \text{rule 2}$$

Now if we want to derive a string "aaaaaa", we can start with start symbols.

```

S
aS
aaS    rule 1
aaaS    rule 1
aaaaS    rule 1
aaaaaS    rule 1
aaaaaaS    rule 1
aaaaaaε    rule 2
aaaaaa

```

The r.e. $= a^*$ can generate a set of string $\{\epsilon, a, aa, aaa, \dots\}$. We can have a null string because S is a start symbol and rule 2 gives $S \rightarrow \epsilon$.

Example 2:

Construct a CFG for the regular expression $(0+1)^*$

Solution:

The CFG can be given by,

```

Production rule (P):
S → 0S | 1S
S → ε

```

The rules are in the combination of 0's and 1's with the start symbol. Since $(0+1)^*$ indicates $\{\epsilon, 0, 1, 01, 10, 00, 11, \dots\}$. In this set, ϵ is a string, so in the rule, we can set the rule $S \rightarrow \epsilon$.

Example 3:

Construct a CFG for a language $L = \{wcwR \mid \text{where } w \in (a, b)^*\}$.

Solution:

The string that can be generated for a given language is {aacaa, bcb, abcba, bacab, abbcbbba,}

The grammar could be:

```
S → aSa    rule 1
S → bSb    rule 2
S → c      rule 3
```

Now if we want to derive a string "abbcbbba", we can start with start symbols.

```
S → aSa
S → abSba    from rule 2
S → abbSbba  from rule 2
S → abbcbbba from rule 3
```

Thus any of this kind of string can be derived from the given production rules.

Example 4:

Construct a CFG for the language $L = a^n b^{2n}$ where $n \geq 1$.

Solution:

The string that can be generated for a given language is {abb, aabbbb, aaabbbbbbb....}.

The grammar could be:

```
S → aSbb | abb
```

Now if we want to derive a string "aabbbb", we can start with start symbols.

```
S → aSbb
S → aabbbb
```

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