

# JOB SEQUENCING WITH DEADLINES

**The problem is stated as below.**

- There are  $n$  jobs to be processed on a machine.
- Each  $\text{Job}_i$  has a deadline  $d_i \geq 1$  and profit  $p_i \geq 1$ .
- $P_i$  is earned iff the job is completed by its deadline.
- The job is completed if it is processed on a machine for unit time.
- Only one machine is available for processing jobs.
- Only one job is processed at a time on the machine.

# JOB SEQUENCING WITH DEADLINES (Contd..)

- A feasible solution is a subset of jobs  $J$  such that each job is completed by its deadline.
- An optimal solution is a feasible solution with maximum profit value.

**Example :** Let  $n = 4$ ,  $(p_1, p_2, p_3, p_4) = (100, 10, 15, 27)$ ,  
 $(d_1, d_2, d_3, d_4) = (2, 1, 2, 1)$

# JOB SEQUENCING WITH DEADLINES (Contd..)

Sr.No.	Feasible Solution	Processing Sequence	Profit value
(i)	(1,2)	(2,1)	110
(ii)	(1,3)	(1,3) or (3,1)	115
(iii)	(1,4)	(4,1)	127
(iv)	(2,3)	(2,3)	25
(v)	(3,4)	(4,3)	42
(vi)	(1)	(1)	100
(vii)	(2)	(2)	10
(viii)	(3)	(3)	15
(ix)	(4)	(4)	27

↑ is the optimal one

# GREEDY ALGORITHM TO OBTAIN AN OPTIMAL SOLUTION

- Consider the jobs in the non increasing order of profits subject to the constraint that the resulting job sequence  $J$  is a feasible solution.
- In the example considered before, the non-increasing profit vector is

$$\begin{array}{cccc} (100 & 27 & 15 & 10) & (2 & 1 & 2 & 1) \\ p_1 & p_4 & p_3 & p_2 & d_1 & d_4 & d_3 & d_2 \end{array}$$

# GREEDY ALGORITHM TO OBTAIN AN OPTIMAL SOLUTION (Contd..)

$J = \{ 1 \}$  is a feasible one

$J = \{ 1, 4 \}$  is a feasible one with processing  
sequence ( 4,1)

$J = \{ 1, 3, 4 \}$  is not feasible

$J = \{ 1, 2, 4 \}$  is not feasible

$J = \{ 1, 4 \}$  is optimal

<b>Job</b>	<b>Profit</b>	<b>Deadline</b>
J1	10	2
J2	30	3
J3	60	1
J4	40	3

According to Job order on profits in non increasing order is  $J_3, J_4, J_2, J_1$

<b>Job</b>	<b>Deadline</b>	<b>Operation</b>	<b>Slot</b>	<b>Total Profit</b>
Initialization			[0, 0, 0]	0
$J_3$	1	Assign $J_3$ to Slot <sub>1</sub>	[ $J_3$ , 0, 0]	60
$J_4$	3	Assign $J_4$ to Slot <sub>3</sub> .	[ $J_3$ , 0, $J_4$ ]	100
$J_2$	3	Assign $J_2$ to Slot <sub>2</sub> bcoz Slot <sub>3</sub> is not empty.	[ $J_3$ , $J_2$ , $J_4$ ]	130
$J_1$	2	Reject $J_1$ bcoz no empty Slots before deadline.	[ $J_3$ , $J_2$ , $J_4$ ]	130

<b>Job</b>	<b>Profit</b>	<b>Deadline</b>
$J_1$	15	7
$J_2$	20	2
$J_3$	30	5
$J_4$	18	3
$J_5$	18	4
$J_6$	10	5
$J_7$	23	2
$J_8$	16	7
$J_9$	25	3

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Algorithm JobSequencing(J,p,d,n,slot)
//n is the number of jobs J[1:n], p[1:n], d[1:n]
//contains Job numbers, profits, deadlines
//slot[1:n] is the solution list.
{
    profit=0;
    for i=1 to n do slot[i]=0;
    for i=1 to n do
    {
        j=d[i];
        while(j>0) do
        {
            if (slot[j] == 0) then
            {
                slot[j] = J[i]
                profit = profit + p[i]
                break;
            }
            j=j-1
        }
    }
    print slot & profit;
}

```