

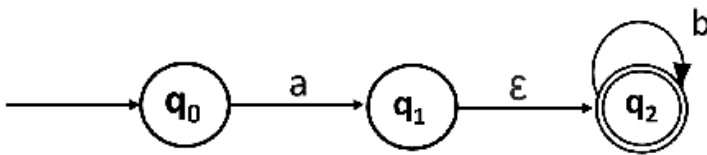
Eliminating ϵ Transitions

NFA with ϵ can be converted to NFA without ϵ , and this NFA without ϵ can be converted to DFA. To do this, we will use a method, which can remove all the ϵ transition from given NFA. The method will be:

1. Find out all the ϵ transitions from each state from Q . That will be called as $\epsilon\text{-closure}\{q_i\}$ where $q_i \in Q$.
2. Then δ' transitions can be obtained. The δ' transitions mean a ϵ -closure on δ moves.
3. Repeat Step-2 for each input symbol and each state of given NFA.
4. Using the resultant states, the transition table for equivalent NFA without ϵ can be built.

Example:

Convert the following NFA with ϵ to NFA without ϵ .



Solutions: We will first obtain ϵ -closures of q_0 , q_1 and q_2 as follows:

$\epsilon\text{-closure}(q_0) = \{q_0\}$
 $\epsilon\text{-closure}(q_1) = \{q_1, q_2\}$
 $\epsilon\text{-closure}(q_2) = \{q_2\}$

Now the δ' transition on each input symbol is obtained as:

$\delta'(q_0, a) = \epsilon\text{-closure}(\delta(\delta^*(q_0, \epsilon), a))$
 $= \epsilon\text{-closure}(\delta(\epsilon\text{-closure}(q_0), a))$
 $= \epsilon\text{-closure}(\delta(q_0, a))$
 $= \epsilon\text{-closure}(q_1)$
 $= \{q_1, q_2\}$

$\delta'(q_0, b) = \epsilon\text{-closure}(\delta(\delta^*(q_0, \epsilon), b))$
 $= \epsilon\text{-closure}(\delta(\epsilon\text{-closure}(q_0), b))$

$$= \epsilon\text{-closure}(\delta(q_0, b))$$

$$= \Phi$$

Now the δ' transition on q_1 is obtained as:

$$\begin{aligned}\delta'(q_1, a) &= \epsilon\text{-closure}(\delta(\delta^+(q_1, \epsilon), a)) \\ &= \epsilon\text{-closure}(\delta(\epsilon\text{-closure}(q_1), a)) \\ &= \epsilon\text{-closure}(\delta(q_1, q_2), a) \\ &= \epsilon\text{-closure}(\delta(q_1, a) \cup \delta(q_2, a)) \\ &= \epsilon\text{-closure}(\Phi \cup \Phi) \\ &= \Phi\end{aligned}$$

$$\begin{aligned}\delta'(q_1, b) &= \epsilon\text{-closure}(\delta(\delta^+(q_1, \epsilon), b)) \\ &= \epsilon\text{-closure}(\delta(\epsilon\text{-closure}(q_1), b)) \\ &= \epsilon\text{-closure}(\delta(q_1, q_2), b) \\ &= \epsilon\text{-closure}(\delta(q_1, b) \cup \delta(q_2, b)) \\ &= \epsilon\text{-closure}(\Phi \cup q_2) \\ &= \{q_2\}\end{aligned}$$

The δ' transition on q_2 is obtained as:

$$\begin{aligned}\delta'(q_2, a) &= \epsilon\text{-closure}(\delta(\delta^+(q_2, \epsilon), a)) \\ &= \epsilon\text{-closure}(\delta(\epsilon\text{-closure}(q_2), a)) \\ &= \epsilon\text{-closure}(\delta(q_2, a)) \\ &= \epsilon\text{-closure}(\Phi) \\ &= \Phi\end{aligned}$$

$$\begin{aligned}\delta'(q_2, b) &= \epsilon\text{-closure}(\delta(\delta^+(q_2, \epsilon), b)) \\ &= \epsilon\text{-closure}(\delta(\epsilon\text{-closure}(q_2), b)) \\ &= \epsilon\text{-closure}(\delta(q_2, b)) \\ &= \epsilon\text{-closure}(q_2) \\ &= \{q_2\}\end{aligned}$$

Now we will summarize all the computed δ' transitions:

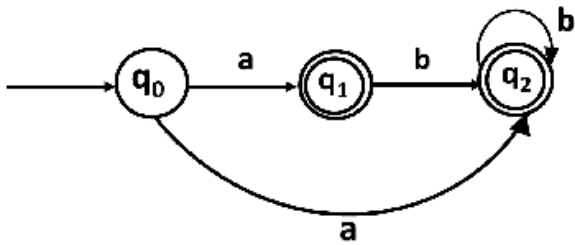
$$\begin{aligned}\delta'(q_0, a) &= \{q_0, q_1\} \\ \delta'(q_0, b) &= \Phi \\ \delta'(q_1, a) &= \Phi \\ \delta'(q_1, b) &= \{q_2\} \\ \delta'(q_2, a) &= \Phi \\ \delta'(q_2, b) &= \{q_2\}\end{aligned}$$

The transition table can be:

States	a	b
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$\rightarrow q_0$	$\{q_1, q_2\}$	Φ
$*q_1$	Φ	$\{q_2\}$
$*q_2$	Φ	$\{q_2\}$

State q_1 and q_2 become the final state as ϵ -closure of q_1 and q_2 contain the final state q_2 . The NFA can be shown by the following transition diagram:



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