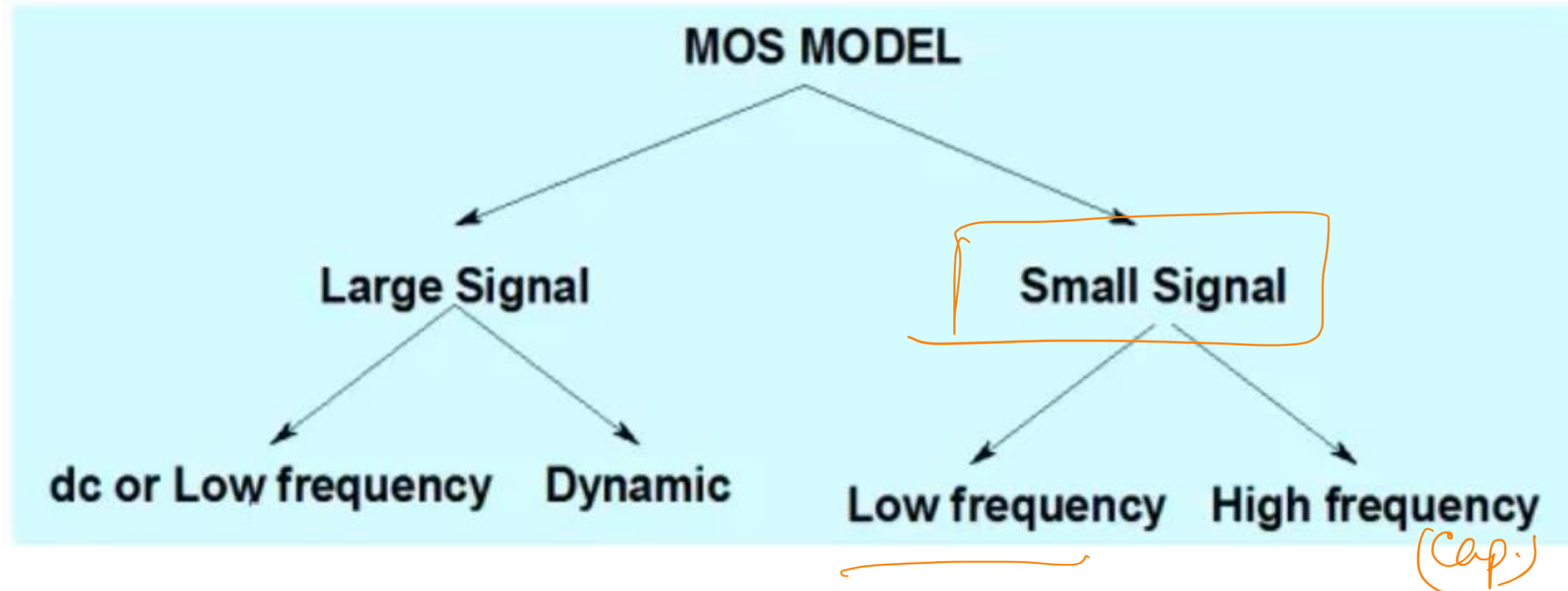
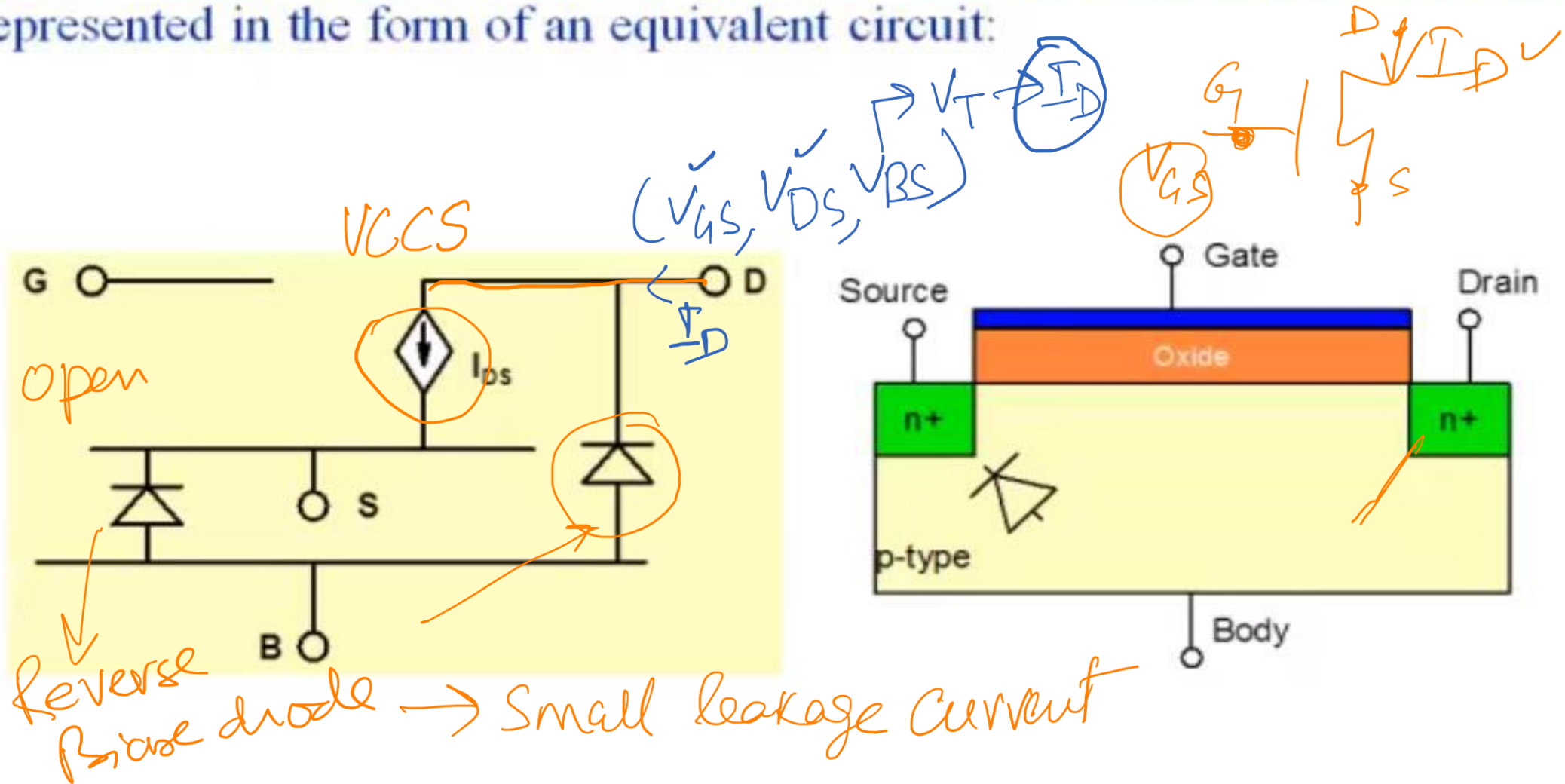


**MOS models :** The classification of models can be done on the basis of magnitude and frequency of applied voltages

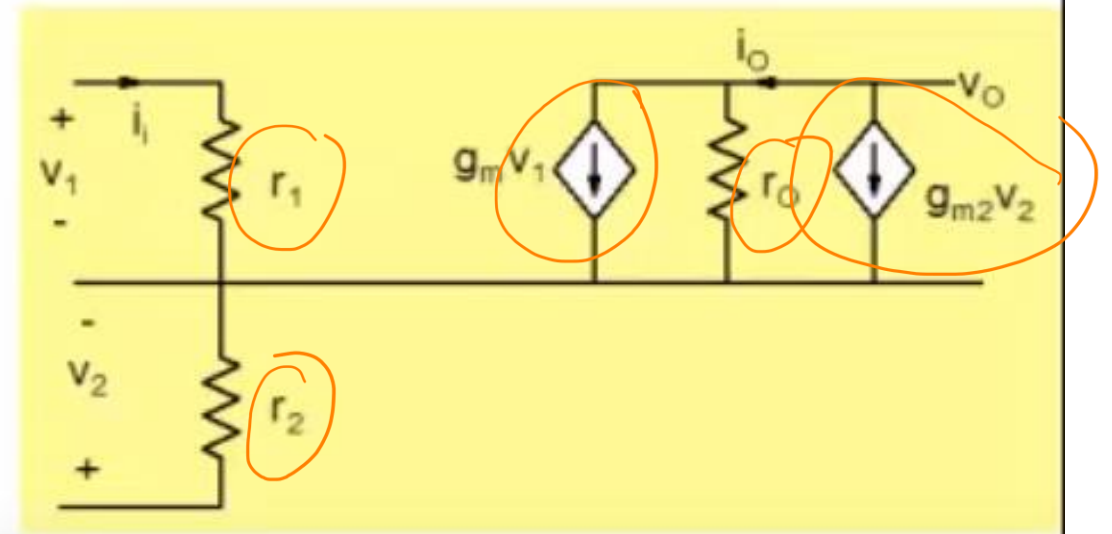
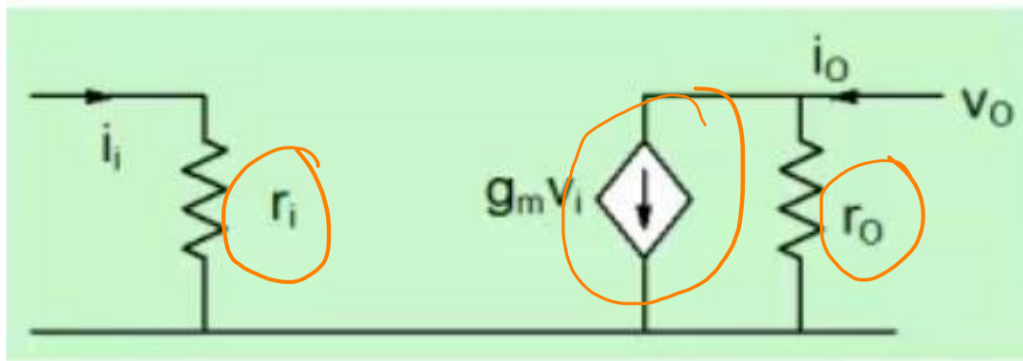
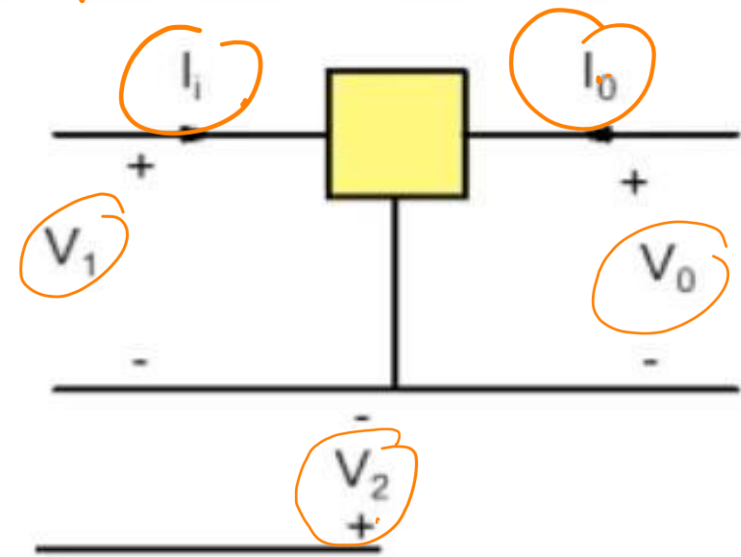
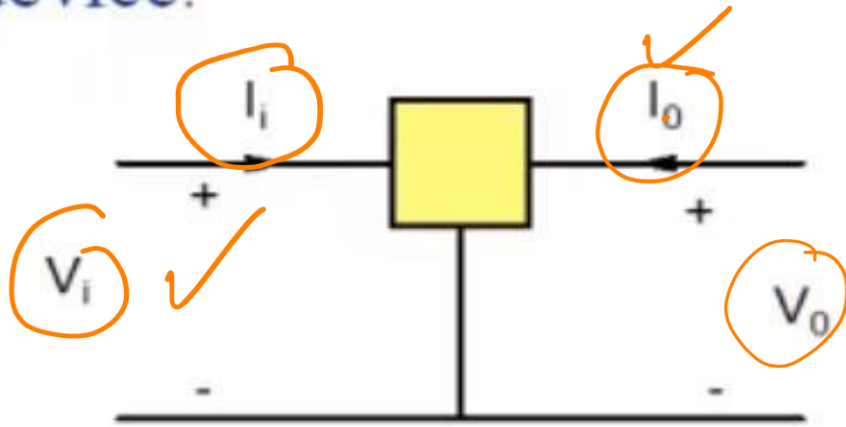


The dc model of the transistor in triode and saturation region can be represented in the form of an equivalent circuit:



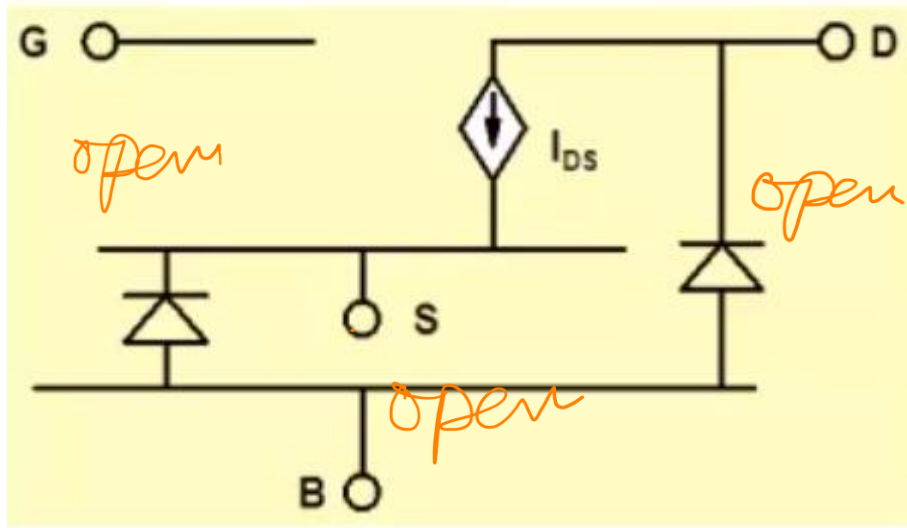
Series resistance associated with gate, source, drain and body terminals is not shown but can play an important role.

Complete small signal model (dc) for a 3-terminal unilateral device.



## Small Signal Model (dc/low frequency)

Saturation



$$I_{ds} = \frac{\beta_N}{2} (V_{gs} - V_{THN})^2 (1 + \lambda_n V_{ds})$$

Small signal (dc)

Bias

$$V_{gs} = V_{GSQ} + v_{gs}$$

Bias Small

$$V_{ds} = V_{DSQ} + v_{ds}$$

$$V_{sb} = V_{SBQ} + v_{sb}$$

$$I_{ds} = I_{DSQ} + i_{ds}$$



$$I_{DSQ} + i_{ds} = \frac{\beta_N}{2} \left[ V_{GSQ} + v_{gs} - V_{THN} (V_{BSQ} + v_{bs}) \right]^2 (1 + \lambda_n V_{DSQ} + \lambda_n v_{ds})$$

not really multiplication, but function

$$V = IR$$

$$I = \frac{V}{R}$$

$$i_{ds} \cong I_{DSQ} \left\{ \lambda_n v_{ds} + \frac{2v_{gs}}{V_{GSQ} - V_{THN}} + \frac{\gamma \times v_{bs}}{(V_{GSQ} - V_{THN}) \times \sqrt{2\phi_F - V_{BSQ}}} \right\}$$

$$I_{DSQ} = \beta (V_{GS} - V_T)^2$$

$$V_{GS} - V_T = \sqrt{\frac{I_{DSQ}}{\beta}}$$

$$i_{ds} = \frac{v_{ds}}{r_o} + g_m v_{gs} + g_{mb} v_{bs}$$

$$r_o = \frac{1}{\lambda_n I_{DSQ}}$$

$$g_m = \frac{2I_{DSQ}}{V_{GSQ} - V_{THN}} = \sqrt{2I_{DSQ}\beta}$$

$$g_{mb} = g_m \cdot \eta$$

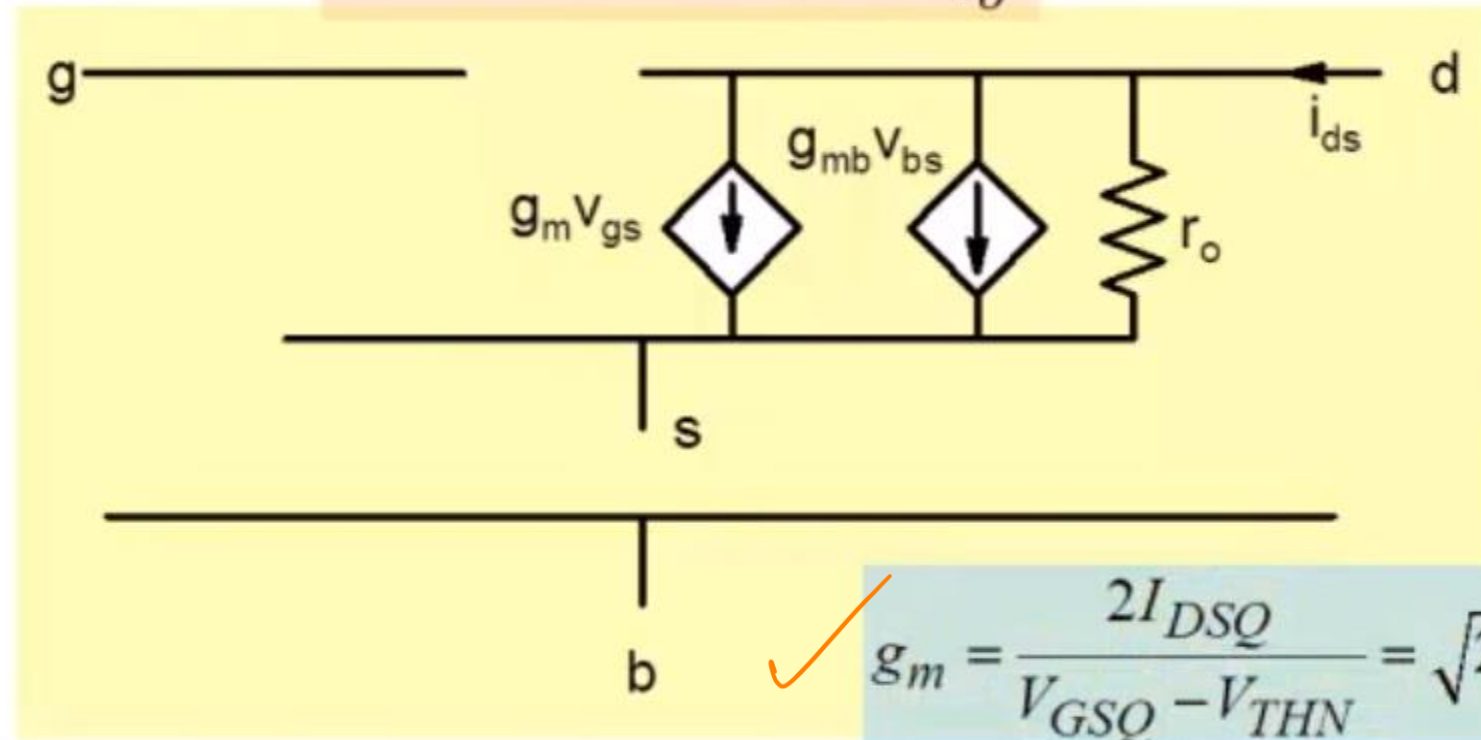
$$\eta = \frac{\gamma}{2\sqrt{2\phi_F + V_{SBQ}}}$$

$$i_{ds} \cong I_{DSQ} \cdot A_{v_{ds}} \cdot \frac{v_{ds}}{I_{DSQ}}$$

$$r_o \equiv \frac{1}{A_{v_{ds}} I_{DSQ}}$$

## Low frequency Small Signal model

$$i_{ds} = g_m v_{gs} + g_{mb} v_{bs} + \frac{v_{ds}}{r_o}$$



$$g_m = \frac{2I_{DSQ}}{V_{GSQ} - V_{THN}} = \sqrt{2I_{DSQ}\beta}$$

$$r_o = \frac{1}{\lambda_n I_{DSQ}}$$

$$g_{mb} = g_m \cdot \eta$$

$$\eta = \frac{\gamma}{2\sqrt{2\Phi_F + V_{SBQ}}}$$

The small signal approximation  $i_{ds} = g_m v_{gs}$  is accurate when

$$v_{gs} \ll 2(V_{GS} - V_{THN})$$

In BJT:

$$v_{be} < V_T = \frac{kT}{q} = 26 \text{ mV}$$

In MOS

$$\frac{v_{gs}}{V_{GS} - V_{THN}} \ll 2$$

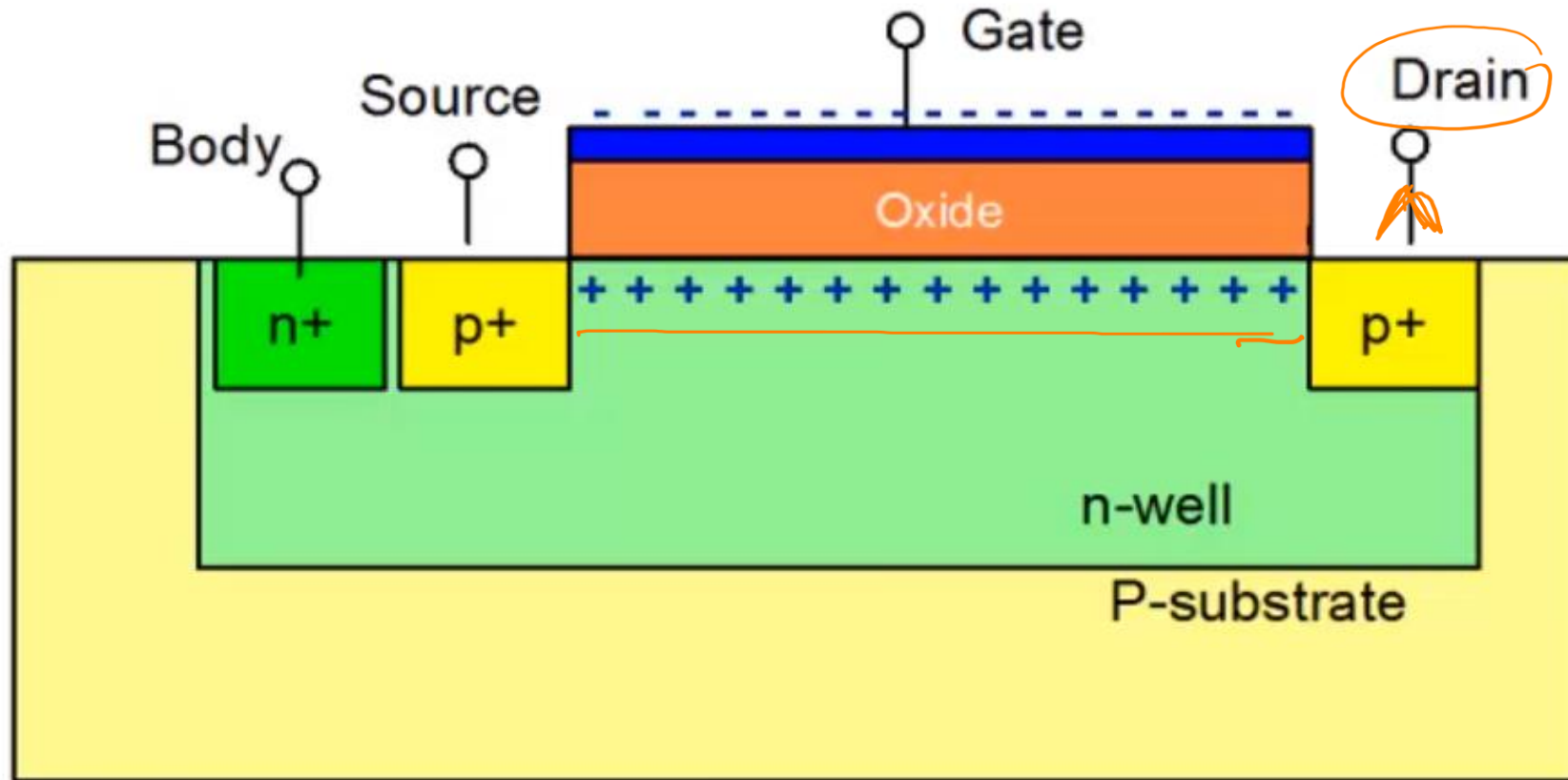
$$v_{gs} \ll 0.2 (V_{GS} - V_T) \ll 2 \ll 200 \text{ mV}$$

5%

100%

$\frac{v_{gs}}{V_{GS} - V_T}$	+0.1	-0.1	+0.2	-0.2	...
$\rightarrow \text{Error \%}$	-4.7	5.26	-9.1	11.1	...

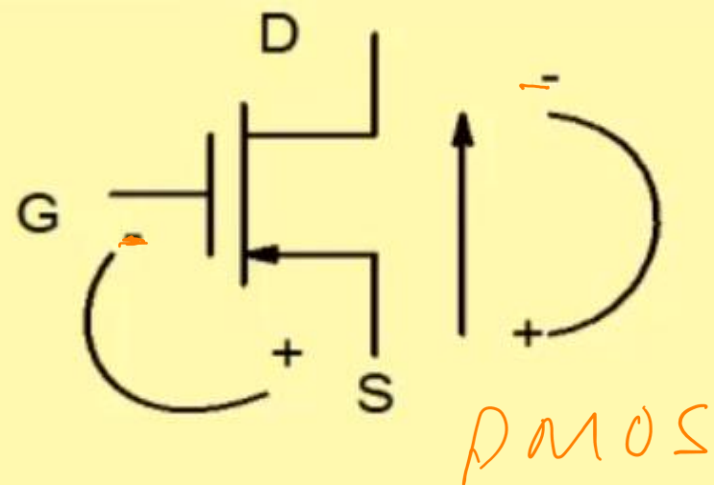
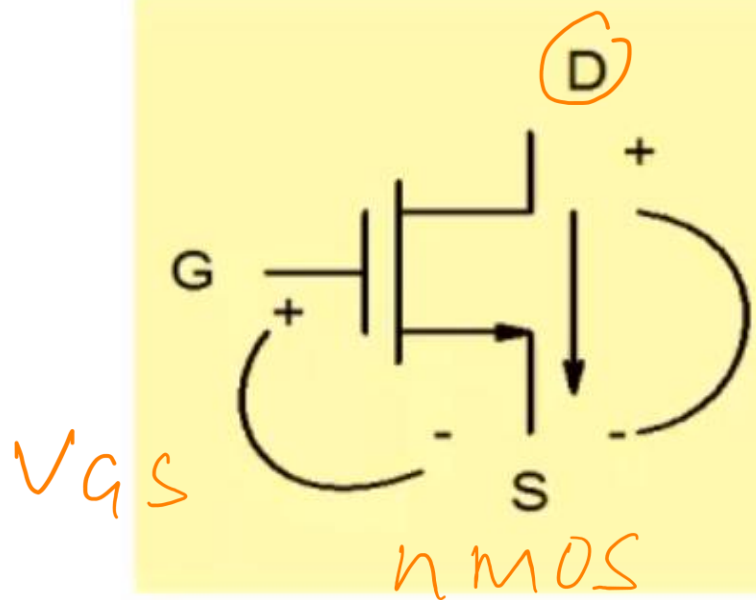
# PMOS



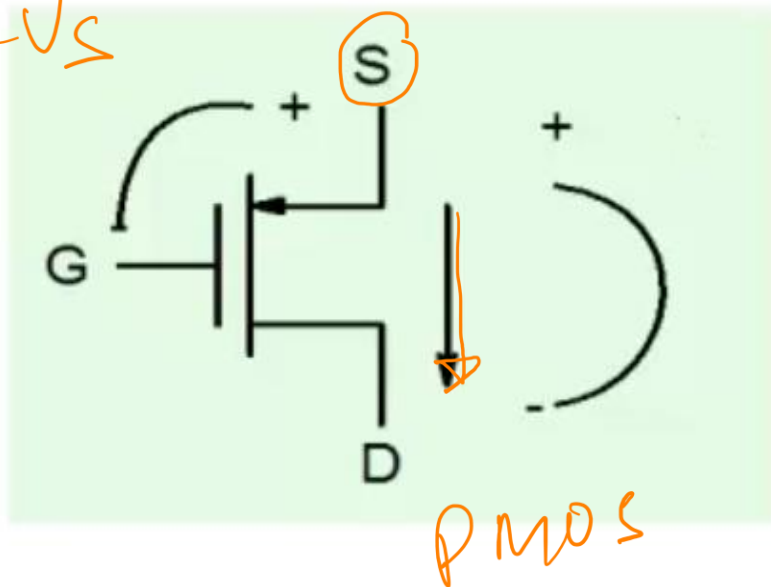
$V_{GS}$  is negative ; Threshold voltage  $V_{TP}$  is negative

$V_{DS}$  is negative ;  $I_{DS}$  is negative





$$V_{GS} = V_G - V_S$$



$$V_{GSN} \rightarrow V_{SGP}$$

$$I_{DSN} \rightarrow I_{SDP}$$

$$V_{DSN} \rightarrow V_{SDP}$$

## Transformations

$$V_{GSN} \rightarrow V_{SGP}$$

$$V_{DSN} \rightarrow V_{SDP}$$

$$V_{BSN} \rightarrow V_{SBP}$$

$$V_{THN} \rightarrow -V_{THP}$$

$$I_{DSN} \rightarrow I_{SDP}$$

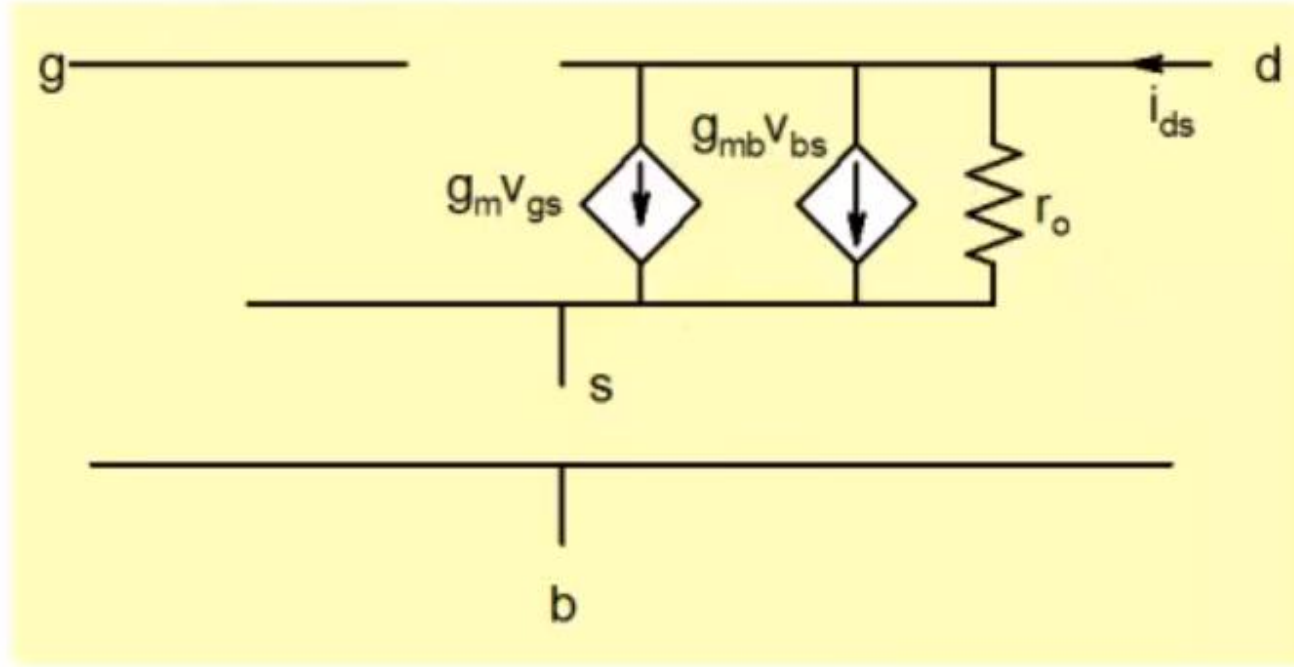
$$I_{DS} = \frac{\beta_N}{2} (V_{GS} - V_{THN})^2 [1 + \lambda_n V_{DS}] \rightarrow$$

$$I_{SD} = \frac{\beta_P}{2} (V_{SG} + V_{THP})^2 [1 + \lambda_p V_{SD}]$$

$$i_{sd} = g_m v_{sg} + g_{mb} v_{sb} + \frac{v_{sd}}{r_o}$$

$$i_{ds} = g_m v_{gs} + g_{mb} v_{bs} + \frac{v_{ds}}{r_o} \text{ same as NMOS}$$

## Small Signal Model



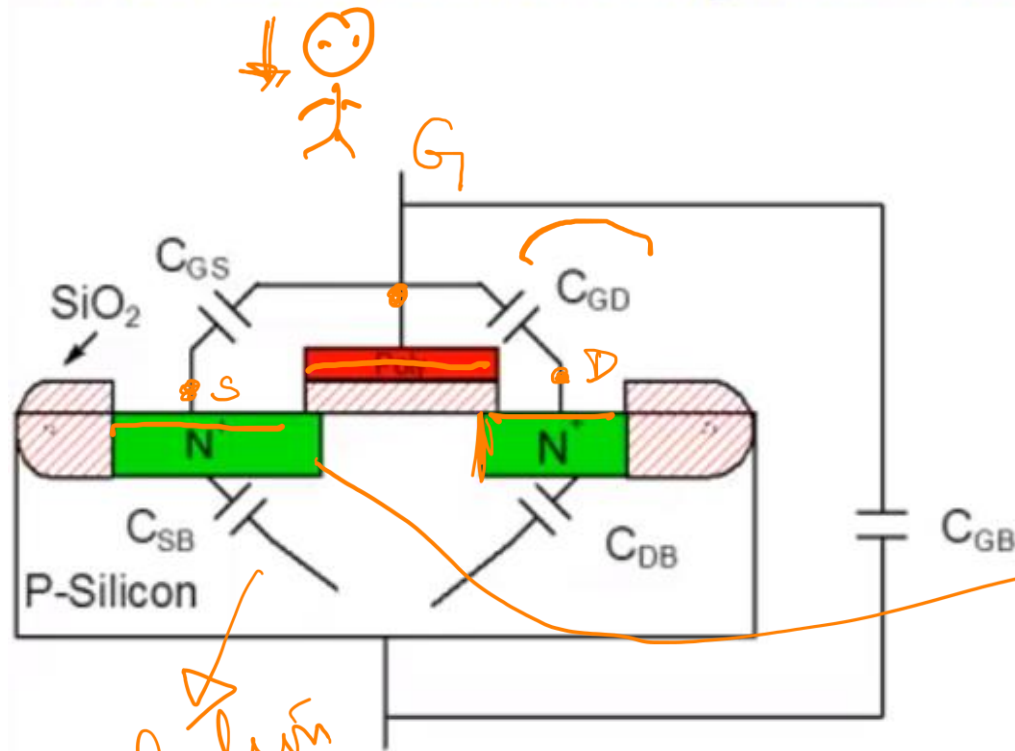
$$g_m = \frac{2I_{SDQ}}{V_{SGQ} + V_{THP}}$$

$$r_o = \frac{1}{\lambda_p I_{SDQ}}$$

# Capacitance Model

## Saturation

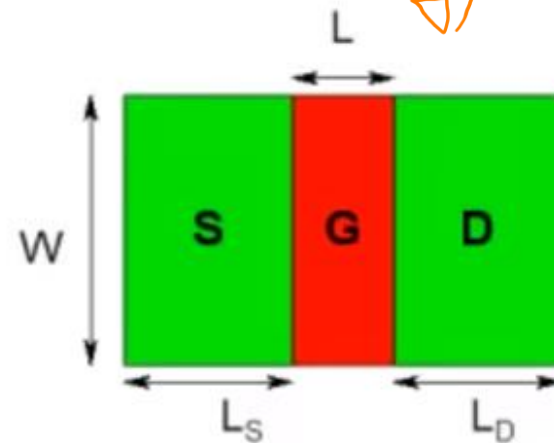
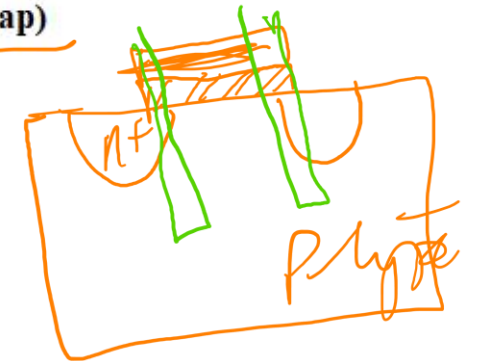
- There are five distinct components of capacitance as illustrated below



$$C_{gs} \cong \frac{2}{3} C_{ox'} \cdot W \cdot L + C_{gso} \cdot W$$

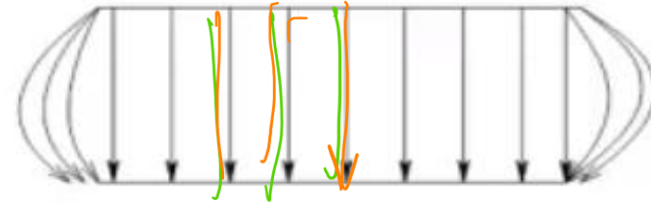
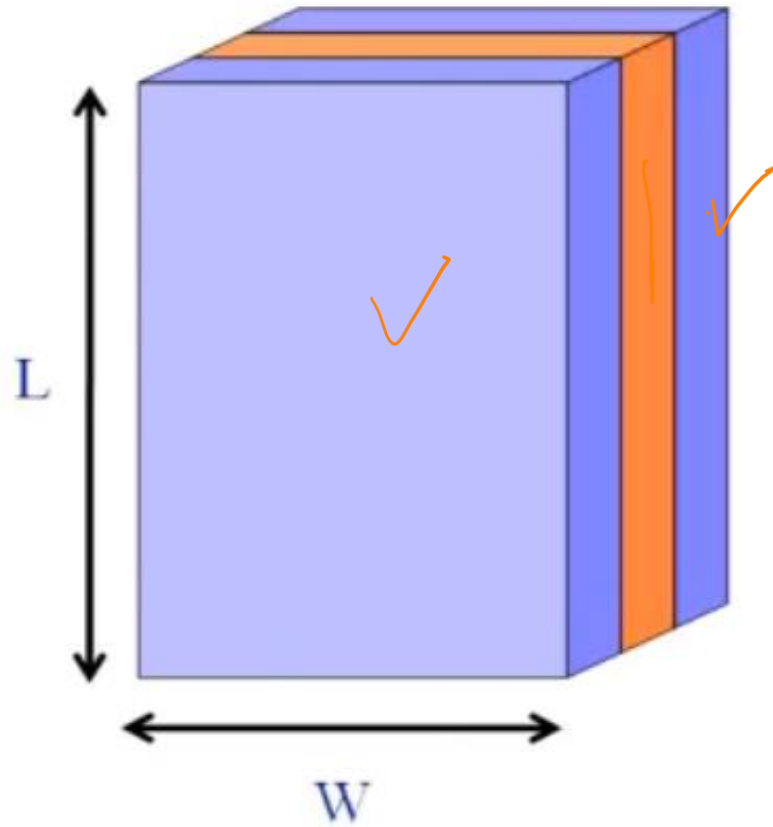
(Channel) (overlap)

$$C_{gd} = C_{GDO} \cdot W$$



Depletion cap  
(PN jn)

## Capacitances: Area and Perimeter Components

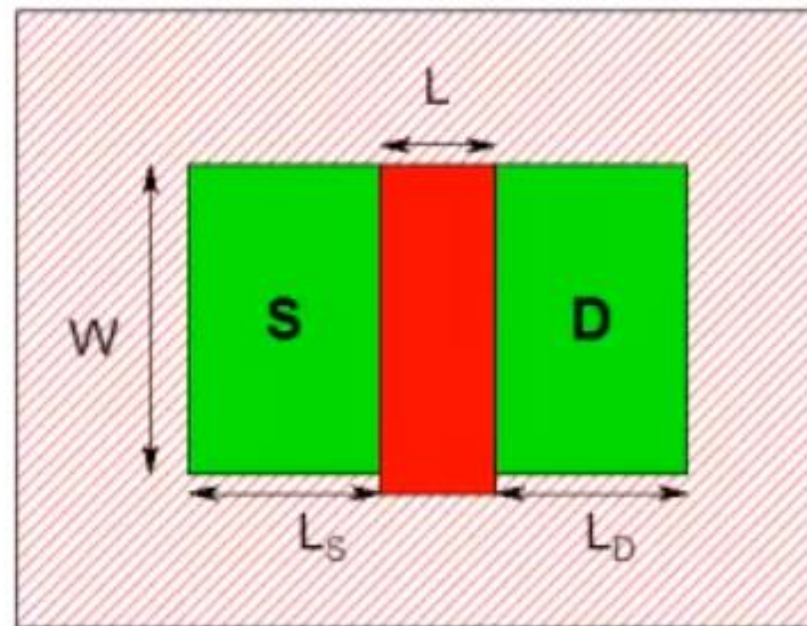
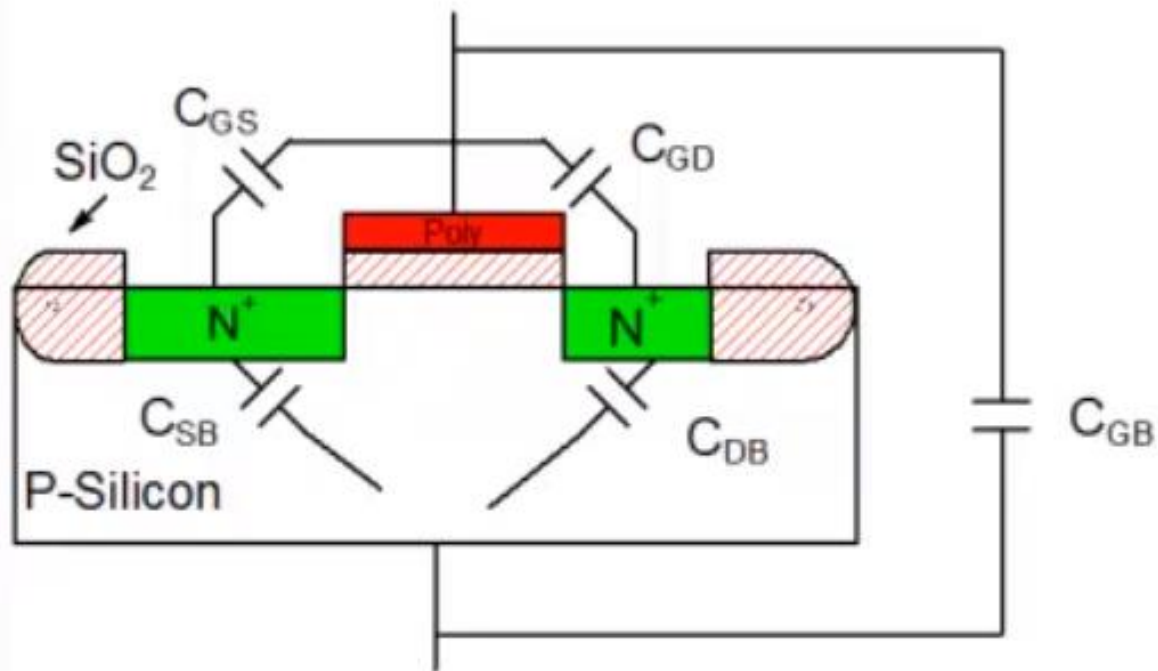


Fringe



$$C = \frac{\epsilon}{d} \times W \times L + C_p \times (2L + 2W)$$



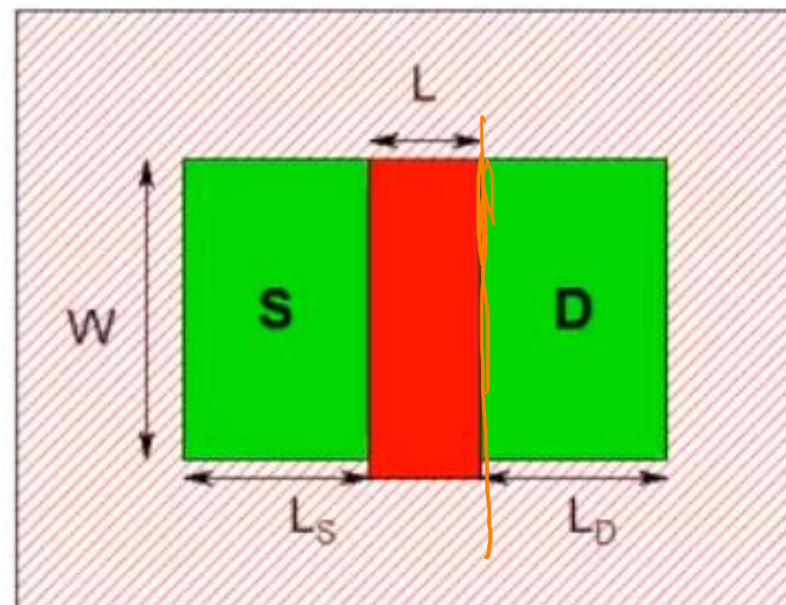


$$C_{sb} = \frac{C_j \cdot A_s}{\left(1 + \frac{V_{SB}}{P_B}\right)^{M_j}} + \frac{C_{jsw} \cdot P_s}{\left(1 + \frac{V_{SB}}{P_{BSW}}\right)^{M_{jsw}}}, \quad P_s = 2L_s + W, \quad A_s = W \cdot L_s$$

*Handwritten notes:*  
 - An arrow points from the  $C_{sb}$  term in the equation to the  $P_s$  term in the second part of the equation.  
 - The  $2W$  term in  $P_s = 2L_s + W$  is crossed out with an 'X'.  
 - A note below the equation states: "already taken in overlap part".

$$C_{db} = \frac{C_{jsw} \cdot P_D}{\left(1 + \frac{V_{DB}}{P_{BSW}}\right)^{M_{jsw}}} + \frac{C_j \cdot A_D}{\left(1 + \frac{V_{DB}}{P_B}\right)^{M_j}} \quad P_D = 2L_D + W$$

$$C_{gb} = C_{GBO} \cdot L \sim \text{often negligible}$$



$V_{DS}$

### Triode/Linear Region

$$C_{gs} = \frac{1}{2} C_{ox'} . W . L + C_{GSO} . W$$

$$C_{gd} = \frac{1}{2} C_{ox'} . W . L + C_{GDO} . W$$

$$C_{sb} = \text{same as before}$$

$$C_{db} = \text{same as before}$$

$$C_{gb} = \text{same as before}$$

Assuming  $V_{DS} \sim 0$

### Cutoff Region

$$C_{gs} = C_{GSO} . W$$

$$C_{gd} = C_{GDO} . W$$

$$C_{sb} = \text{same as before}$$

$$C_{db} = \text{same as before}$$

$$C_{gb} = C_{GBO} . L + C_{ox'} . W . L$$

Assuming Tr. is in accumulation

## Summary

$$C_{gs} \cong \frac{2}{3} C_{ox'} \cdot W \cdot L + C_{gso} \cdot W$$

$$C_{gd} = C_{GDO} \cdot W$$

$$C_{sb} = \frac{C_j \cdot A_s}{\left(1 + \frac{V_{SB}}{P_B}\right)^{M_j}} + \frac{C_{jsw} \cdot P_s}{\left(1 + \frac{V_{SB}}{P_{BSW}}\right)^{M_{jsw}}}, \quad P_s = 2L_s + W, \quad A_s = W \cdot L_s$$

$$C_{db} = \frac{C_{jsw} \cdot P_D}{\left(1 + \frac{V_{DB}}{P_{BSW}}\right)^{M_{jsw}}} + \frac{C_j \cdot A_D}{\left(1 + \frac{V_{DB}}{P_B}\right)^{M_j}}, \quad P_D = 2L_D + W$$

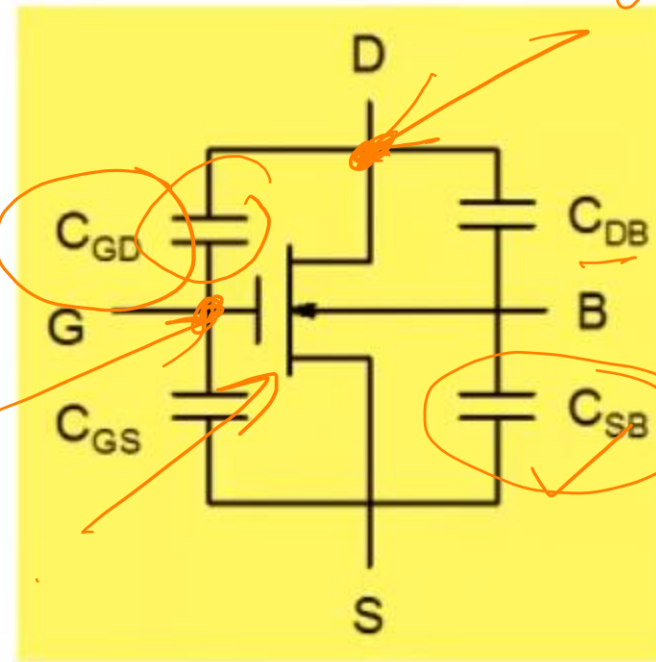
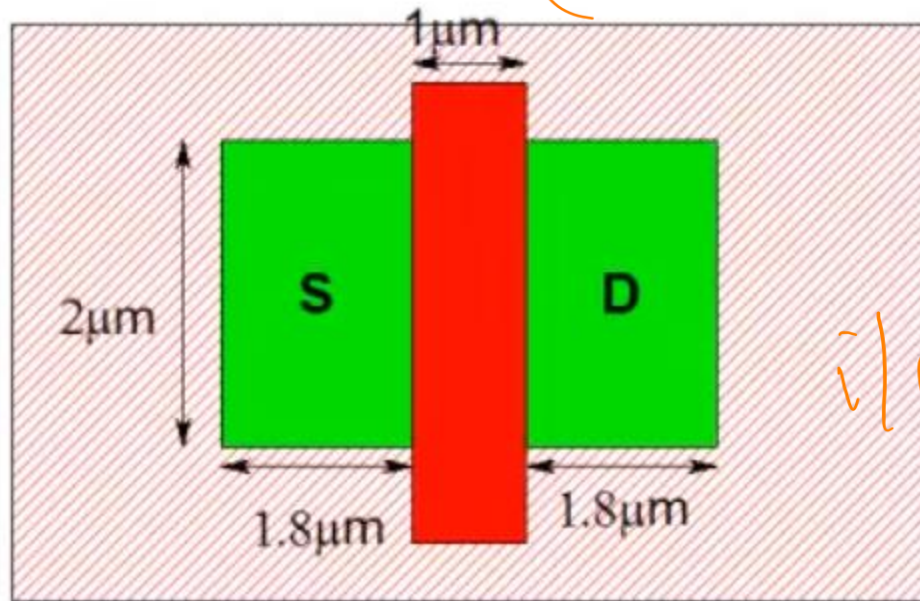
The capacitance model presented herein requires 10 parameters:

$$C_{GSO}, C_{GDO}, C_{GBO}, C'_{OX}, C_J, P_B, M_J, C_{JSW}, P_{BSW}, M_{JSW}$$



# Typical Values of Capacitances

(ingram Tech.)



→ Miller effect (?)

$\frac{d}{dt} C_{gd} \times A_v$

ilp

→ pmos

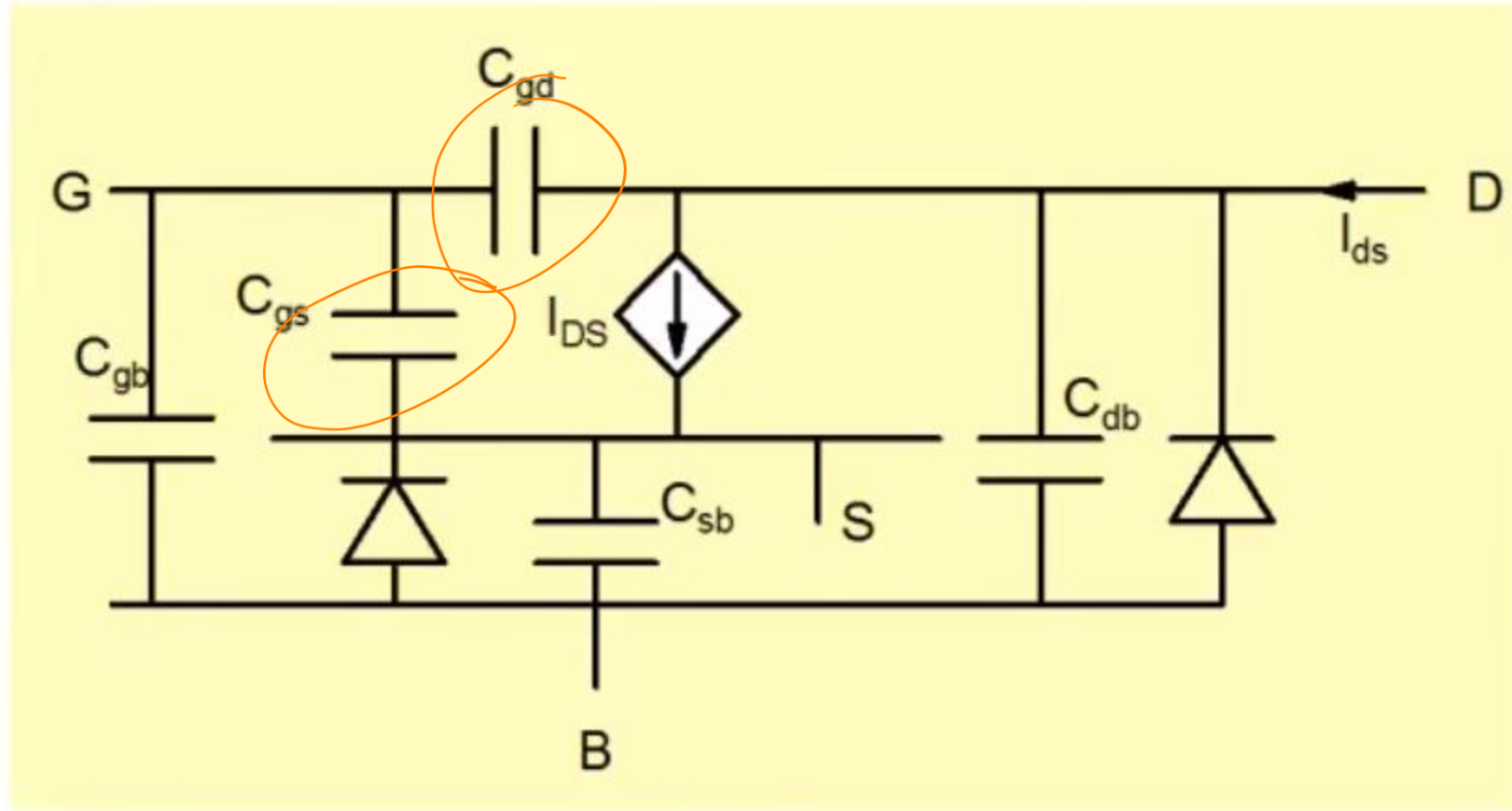
$C_{gs} = 4.1 \text{ fF}$	$C_{gd} = 0.43 \text{ fF}$
$C_{sb} = 4.47 \text{ fF}$	
$C_{db} = 2.75 \text{ fF}$	

← (may look smaller)

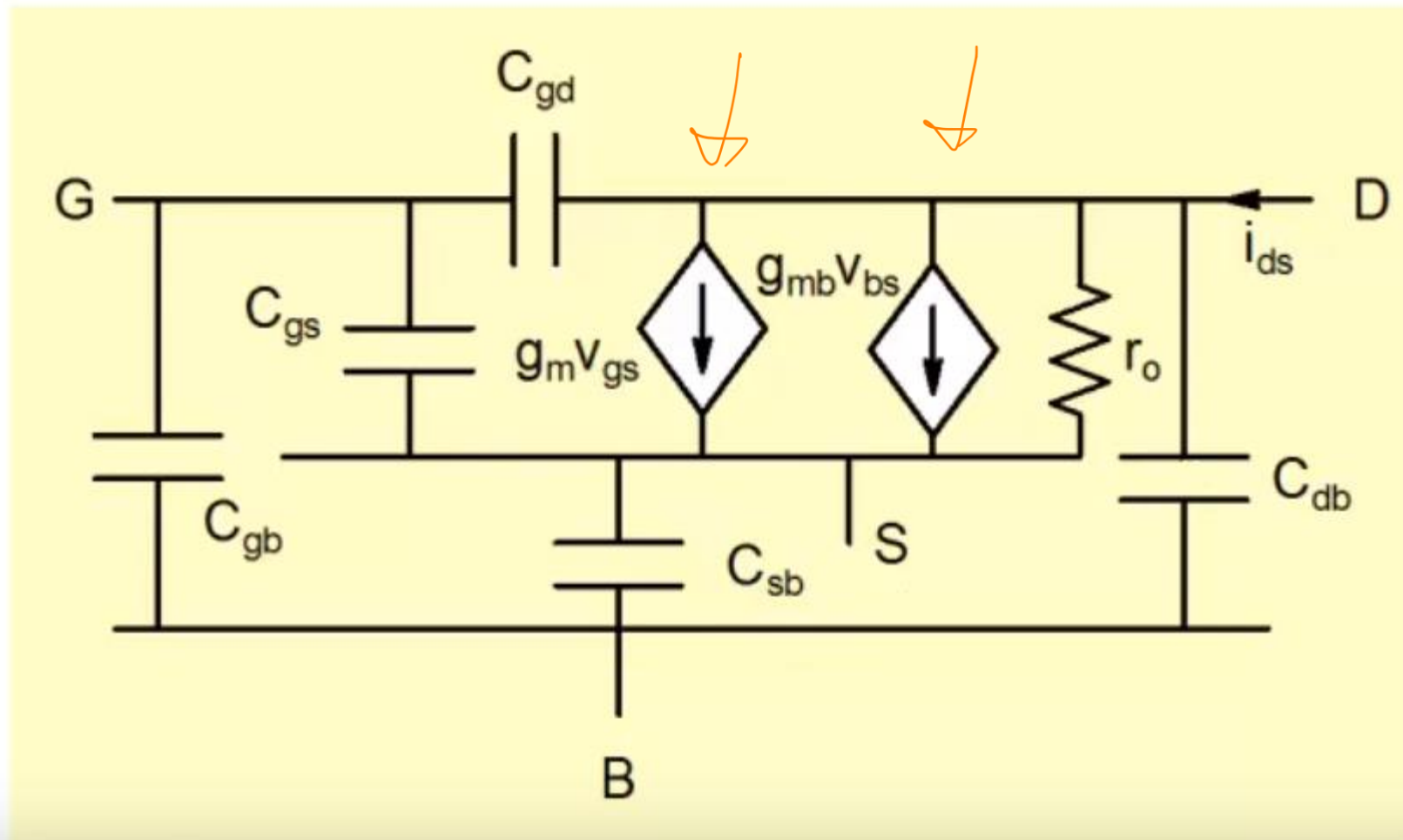
$$V_{SB} = 0; \quad V_{DS} = 2V$$



## Complete Large Signal Model



## High Frequency Small Signal Model



- We have so far discussed simple MOS models which are suitable for 'hand-analysis' of circuits. For more accurate prediction of circuit characteristics using circuit simulation more accurate MOS models are required.

- SPICE and its various variants are the most popular circuit simulation tool. In SPICE, there are a number of MOS models that are available including Level-1, level-2, Level-3, BSIM1, BSIM2, BSIM3, BSIM4 etc.

- Level-1 model is the simplest and is basically similar to the large signal model that we have described earlier. A popular model for submicron devices is BSIM3 model.

- \* SPICE- Simulation Program with Integrated Circuit Emphasis ✓

- \* BSIM- Berkeley Short-channel IGFET Model

## BSIM3 : Berkeley Short Channel IGFET (Insulated gate Field Effect) Model

$$I_{ds} = \frac{I_{dso}(V_{dseff})}{1 + \frac{R_{ds}I_{dso}(V_{dseff})}{V_{dseff}}} \left( 1 + \frac{V_{ds} - V_{dseff}}{V_A} \right) \left( 1 + \frac{V_{ds} - V_{dseff}}{V_{ASCBE}} \right)$$

$$I_{dso} = \frac{W_{eff}\mu_{eff}C_{ox}V_{gsteff}(1 - A_{bulk}\frac{V_{dseff}}{2(V_{gsteff} + 2\psi_t)})V_{dseff}}{L_{eff}[1 + V_{dseff} / (E_{sat}L_{eff})]}$$

$$V_A = V_{Asat} + (1 + \frac{P_{vag}V_{gsteff}}{E_{sat}L_{eff}})(\frac{1}{V_{ACLM}} + \frac{1}{V_{ADIBLC}})^{-1}$$

$$V_{ACLM} = \frac{A_{bulk}E_{sat}L_{eff} + V_{gsteff}}{P_{CLM}A_{bulk}E_{sat}}(V_{ds} - V_{dseff})$$

# LATEST MODELS

PTM

Typical SPICE model files for each future generation are available here.

**Attention:** By using a **PTM** file, you agree to acknowledge both the URL of **PTM**: <http://ptm.asu.edu/> and the related publications in all documents and publications involving its usage.

## New!

June 01, 2012:

PTM releases a new set of models for multi-gate transistors (**PTM-MG**), for both HP and LSTP applications. It is based on [BSIM-CMG](#), a dedicated model for multi-gate devices.

**Acknowledgement:** PTM-MG is developed in collaboration with ARM.

Please start from [models](#) and [param.inc](#).

- 7nm PTM-MG [HP NMOS](#), [HP PMOS](#), [LSTP NMOS](#), [LSTP PMOS](#)
- 10nm PTM-MG [HP NMOS](#), [HP PMOS](#), [LSTP NMOS](#), [LSTP PMOS](#)
- 14nm PTM-MG [HP NMOS](#), [HP PMOS](#), [LSTP NMOS](#), [LSTP PMOS](#)
- 16nm PTM-MG [HP NMOS](#), [HP PMOS](#), [LSTP NMOS](#), [LSTP PMOS](#)
- 20nm PTM-MG [HP NMOS](#), [HP PMOS](#), [LSTP NMOS](#), [LSTP PMOS](#)

The entire package is also available here: [PTM-MG](#)

FingFET

November 15, 2008:

PTM releases a new set of models for low-power applications (PTM LP), incorporating high-k/metal gate and stress effect.

- 16nm PTM LP model: [V2.1](#)
- 22nm PTM LP model: [V2.1](#)
- 32nm PTM LP model: [V2.1](#)
- 45nm PTM LP model: [V2.1](#)

September 30, 2008:

PTM releases a new set of models for high-performance applications (PTM HP), incorporating high-k/metal gate and stress effect.

- 16nm PTM HP model: [V2.1](#)
- 22nm PTM HP model: [V2.1](#)



# BSIM Group

[About](#)[News](#)[Models](#)[Publications](#)[Members](#)[Links](#)[BSIM-CMG](#)[BSIM-IMG](#)[BSIM-SOI](#)[BSIM-BULK](#)[BSIM4](#)

BSIM4, as the extension of BSIM3 model, is a physics-based, accurate, scalable, robust technology development. It is developed by the BSIM Research Group in the Department of Electrical Engineering and Computer Sciences (EECS) at the University of California, Berkeley. All suggestions for model improvements are charted by the Compact Model Coalition (CMC).

BSIM4 has been used for the 0.13 um, 90 nm, 65 nm, 45/40 nm, 23/28 nm, and 22/20nm technology nodes.

See BSIM3, a predecessor of BSIM4, [here](#).

## Latest Release

BSIM4 4.8.1 was released on Feb. 15, 2017.

We would like to thank CMC members for testing beta models and providing valuable feedbacks during model development.

Download **BSIM4 4.8.1** model package, including

- Model code in C

Simulation on Insulator

\* PTM Low Power 16nm Metal Gate / High-K / Strained-Si

\* nominal Vdd = 0.9V

.model nmos nmos level = 54

PTM

+version = 4.0	binunit = 1	paramchk= 1	mobmod = 0
+capmod = 2	igcmmod = 1	igbmod = 1	geomod = 1
+diomod = 1	rdsmmod = 0	rbodsmmod= 1	rgatemod= 1
+permod = 1	acnqsmmod= 0	trnqsmmod= 0	
+tnom = 27	toxe = 1.2e-009	toxp = 9e-010	toxm = 1.2e-009
+dtox = 3e-010	epsrox = 3.9	wint = 5e-009	lint = 0
+ll = 0	wl = 0	lln = 1	wln = 1
+lw = 0	ww = 0	lwn = 1	wwn = 1
+lwl = 0	wwl = 0	xpart = 0	toxref = 1.2e-009
+vth0 = 0.68191	k1 = 0.4	k2 = 0	k3 = 0
+k3b = 0	w0 = 2.5e-006	dvt0 = 1	dvt1 = 2
+dvt2 = 0	dvt0w = 0	dvt1w = 0	dvt2w = 0
+dsusb = 0.1	minv = 0.05	voffl = 0	dvtp0 = 1e-011
+dvtp1 = 0.1	lpe0 = 0	lpeb = 0	xj = 5e-009
+ngate = 1e+023	ndep = 7e+018	nsd = 2e+020	phin = 0
+cdsc = 0	cdscb = 0	cdscd = 0	cit = 0
+voff = -0.1014	nfactor = 1.6	eta0 = 0.0095	etab = 0
+vfb = -0.55	u0 = 0.028	ua = 6e-010	ub = 1.2e-018
+uc = 0	vsat = 200000	a0 = 1	ags = 0
+a1 = 0	a2 = 1	b0 = 0	b1 = 0
+keta = 0.04	dwg = 0	dwb = 0	pclm = 0.02
+pdiblc1 = 0.001	pdiblc2 = 0.001	pdiblc3 = -0.005	drout = 0.5
+pvag = 1e-020	delta = 0.01	pscbe1 = 8.14e+008	pscbe2 = 1e-007
+fprout = 0.2	pdits = 0.01	pditsd = 0.23	pditsl = 2300000
+rsh = 5	rdsw = 170	rsd = 75	rdw = 75
+rdswmin = 0	rdwmin = 0	rsdmin = 0	prwg = 0
+prwb = 0	wr = 1	alpha0 = 0.074	alpha1 = 0.005
+beta0 = 30	agidl = 0.0002	bgidl = 2.1e+009	cgidl = 0.0002
+egidl = 0.8	aigbacc = 0.012	bigbacc = 0.0028	cigbacc = 0.002