

Shane Riegodedios

Ryan Leroux

Dr. Torben

Intro to Algorithm Analysis – Assignment 2

1.

1. $M(3) = 3$

$M(4) = 3$

$M(5) = 3$

$M(6) = 3$

$M(7) = 3$

$M(8) = 4$

2. $M(n) = 1 + M(n-1)$

2.

$f(n) = 1000000$

$f(n \cdot \ln(n)) = 87,847.5$

$f(n \cdot \sqrt{n}) = 10,000$

$f(n^2) = 1,000$

$f(n^3) = 100$

$f(1.1^n) = 144.95$

$f(2^n) = 19.93$

$f(n!) = \text{no solution}$

$f(n^n) = 7.066$

3.

1.

$$\frac{2n^3 + 9n^2 + 7n + 13}{n^3} \leq \frac{c \cdot n^3}{n^3}$$
$$2 + \frac{9}{n} + \frac{7}{n^2} + \frac{13}{n^3} \leq c$$
$$c \geq 31$$
$$n \geq n_0 = 1$$

2.

$$n^4 - n^3 \in O(n^3) \quad n > 1$$

$$\frac{n^4 - n^3}{n^3} \approx n - 1$$

$n > C + 1$ implies $n - 1 > C$ and $f(n) > C n^3$
 $n > 1$, $n > K$, and $n > C + 1$ implies $n > K \wedge f(n) > C n^3$