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Introduction to Algorithm Analysis

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1. $4000 < n < n \lg(n) < (1.1)^n < n \ln(n) < n^{\lg(n)} < n^{\sqrt[3]{n}} < n^{\sqrt{n}} < n^2 < n^3 < 2^n < 3^n < 2^{n+3} < n! < n^n$

2. Big-O notation: $f(n) O(g(n))$ iff $f(n) \leq (c_0 * g(n))$ for all $n \geq k$ where C and K are positive

Big- Θ notation: $f(n) = \Theta * g(n)$ iff $f(n) \leq (c_1 * g(n))$ for all $n > k$ and $f(n) \geq c_2 * g(n)$ whenever $n > k$ where c_1, c_2, k are positive

Since $\lg(1) = 0$, this means $k=1$, so proof holds so long as $n > 1$.

3.

a. $\sum_{j=1}^n \left(\frac{j^2}{5} + 2 \right) \in \sum_{i=1}^n \Theta(j^2)$

b. $\sum_{j=1}^n \left(\frac{j^2}{5 \cdot 4} + 3 \right) \in \sum_{i=1}^n \Theta(j^2)$

c. $\sum_{j=1}^n \left(\frac{j^1}{5} + 2 \right) \in \sum_{i=1}^n \Theta(j^1)$