

Shane Riegodedios

Dr. Antov

Introduction to Algorithm Analysis

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- 1.) [2, 7, 3, 4][1, 8, 5, 6]  
[2, 1, 8, 5, 6, 7, 3]

2.)

```
MergeRank(A[1...n], B[1...m])
  i, j, k, z ← 1, 1, 1, p + q
  while(z > k)
    if(M[p[i], q[j]] = 1)
      R[k] ← p[i]
      k ← k + 1
      i ← i + 1
    else if(M[q[j], q[i]] = 1)
      R[k] ← q[j]
      k ← k + 1
      j ← j + 1
    else
      R[k] ← p[i]
      k ← k + 1
      i ← i + 1
      j ← j + 1
      z ← z - 1
```

This algorithm is correct because given two ranked arrays it will always give a ranking the player i is ranked higher than j, if i beat j. It also controls for duplicates.

$$\Theta(p + q)$$

3.)

```

Rank(A[1...n])
  if (n > 1)
    m ← ⌊ n/2 ⌋
    Rank(A[1...m])
    Rank(A[m+1...n])
    B[1...n] ← MergeRank(A[1...m], A[m+1...n])
    Copy(B[1...n], A[1...n])
  T = 2T(n/2) + Θ(n)
  Θ(n lg n)

```

4.)

```

Rank(A[1...8])
  Rank(A[1...4])
  Rank(A[5...8])
  B[1...4] ← MergeRank(A[1...2], A[3...4])
  Copy(B[1...4], A[1...4])
  A = [2, 1]
  Rank(A[5...8])
  B[1...4] ← MergeRank(A[5...6], A[7...8])
  Copy(B[1...4], A[5...8])
  A = [2, 3, 1, 4]
  Repeat for A[9...16]
    A = [5, 6]
    A = [8, 7]
    A = [8, 5, 6, 7]
  A = [2, 3, 1, 8, 4, 5, 6, 7]

```