

Integrating Scientific Simulations with Machine Learning Algorithms

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Welcome



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► Thanks for showing up on the last day!

What do we have in store

- ▶ Session 1:
 - ▶ Introduction
 - ▶ Seed matrices
 - ▶ Demo & Hands on: AD basics in PyTorch, Tapenade & Enzyme
- ▶ Session 2:
 - ▶ Interfacing in PyTorch
 - ▶ Demo & Hands on: Example 1
 - ▶ Demo & Hands on: Example 2

Resources: <https://tinyurl.com/siamcse23>

Our goals for this tutorial

Participants will . . .

- ▶ be able to use AD tools effectively,
- ▶ imagine what ML frameworks do “behind the scenes”,
- ▶ understand how ML frameworks and simulation code can be interfaced
- ▶ understand enough about AD concepts that you can diagnose problems

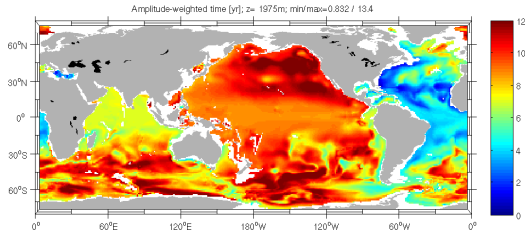
What we assume about you

Computational scientists facing challenging problems, through advanced modeling and simulation, using the most capable computers.

- ▶ large complex codes
- ▶ continuously developed
- ▶ including sophisticated math/physics
- ▶ using multiple libraries
- ▶ performance is essential
- ▶ parallelism involved

Why derivatives?

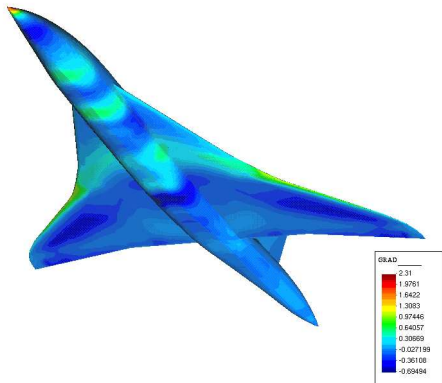
Sensitivity Analysis:



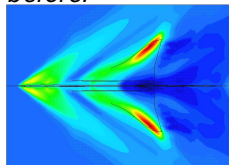
Find sensitivity of the computed field *wrt* one input parameter

Why derivatives?

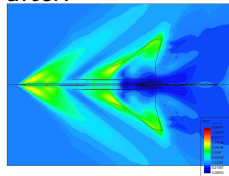
Gradient-driven optimization



before:



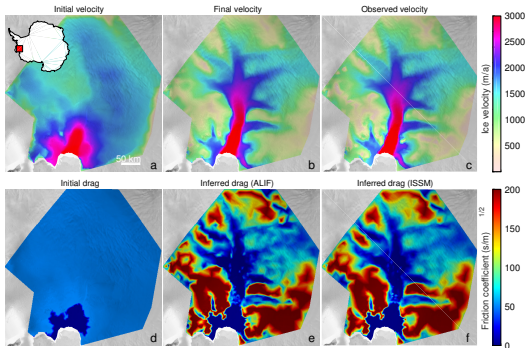
after:



Why derivatives?

Inverse problems:

from measurements and model, estimate hidden parameters



Other uses: Reduced models, Error estimation, Mesh adaption, Uncertainty Quantification, Backpropagation for ML training. . .

What is AD?

The chain rule applied to algorithms

See any algorithm/program $P: \{I_1; I_2; \dots I_p; \}$ as:

$$F: \mathbb{R}^n \rightarrow \mathbb{R}^m \quad F = f_p \circ f_{p-1} \circ \dots \circ f_1$$

Define for short:

$$V_0 = \mathbf{input} \quad \text{and} \quad V_k = f_k(V_{k-1})$$

Apply the chain rule:

$$F'(V_0) = f'_p(V_{p-1}) \times f'_{p-1}(V_{p-2}) \times \dots \times f'_1(V_0)$$

...and transform P to make it compute that.

Cost considerations

$$F'(V_0) = f'_p(V_{p-1}) \times f'_{p-1}(V_{p-2}) \times \cdots \times f'_1(V_0)$$

is often expensive:

- ▶ in computation time
- ▶ in storage space

What can save us:

- ▶ The shapes of the f'_k matter
- ▶ The final usage may not require the full F' but only a projection

Classical projections of F'

- ▶ $F' \times \dot{V}_0$, “forward” or “tangent” mode
- ▶ $\overline{V}_p \times F'$ “reverse” or “adjoint” mode

When full F' needed, use multi-directional AD
→ $F' \times Id$ (or $Id \times F'$),
→ possibly compressed as $F' \times S$ (or $S \times F'$)

For higher-order derivatives, differentiate F'
If directional, differentiate $F' \times \dot{V}_0$

Focus on forward mode: $F' \times \dot{V}_0$

$$F' \times \dot{V}_0 = f'_p(V_{p-1}) \times f'_{p-1}(V_{p-2}) \times \cdots \times f'_1(V_0) \times \dot{V}_0$$

\dot{V}_0 is a vector \Rightarrow compute from right to left!

This corresponds to P's original order

\Rightarrow interleave derivative and primal computation.

Easy!

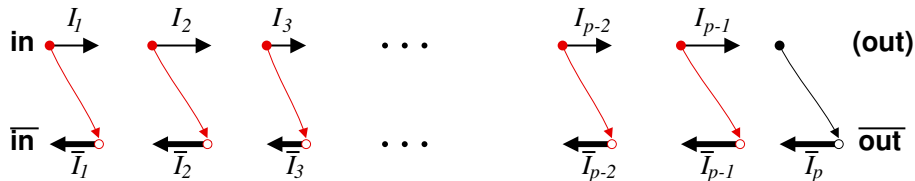


Focus on reverse mode: $\overline{V_p} \times F'$

$$\overline{V_p} \times F' = \overline{V_p} \times f'_p(V_{p-1}) \times f'_{p-1}(V_{p-2}) \times \cdots \times f'_1(V_0)$$

Vector now on the left \Rightarrow compute from left to right

Not so easy, but worth the effort!

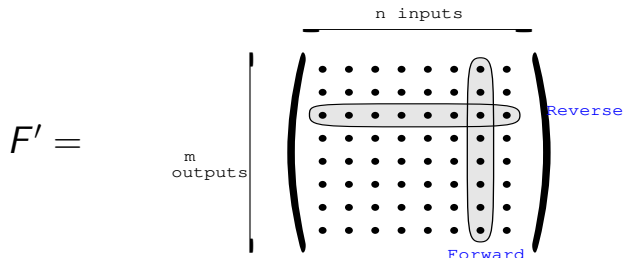


A **forward sweep**, and then a **backward sweep**

The derivative instructions form the **backward sweep**
“**Data-flow reversal**” to get V_k ’s in **reverse order**

Cost model

$$F : \text{in} \in \mathbb{R}^n \rightarrow \text{out} \in \mathbb{R}^m$$



- ▶ full F' cost grows like n using the forward mode
Good if $n \leq m$
- ▶ full F' cost grows like m using the reverse mode
Good if $n \gg m$ (e.g. $m = 1$ for a gradient)

End of basics

Let's look in detail !