

# 8Queens\_Problem\_using\_Genetic\_Algorithm

February 20, 2022

The goal of this assignment is to implement a genetic algorithm to solve 8 queens problem

Import necessary libraries

```
[1]: import random
import matplotlib.pyplot as plt
```

```
[2]: class Individual:
    def __init__(self, indiv):
        self.indiv = indiv
        self.fitness = self.fitnessfunction()
        self.si = 2          #any nonsensical number

    def fitnessfunction(self) -> int:
        nonattacking = 0
        for i in range(len(self.indiv)):
            h = i - 1
            j = i + 1
            right = left = 1
            while (h >= 0 or j < len(self.indiv)):
                if h >= 0 :
                    if self.indiv[h] != self.indiv[i] and self.indiv[h] != self.
↪indiv[i]-left and self.indiv[h] != self.indiv[i]+left :
                        nonattacking += 1
                    left += 1
                    h -= 1
                if j < len(self.indiv):
                    if self.indiv[j] != self.indiv[i] and self.indiv[j] != self.
↪indiv[i]-right and self.indiv[j] != self.indiv[i]+right :
                        nonattacking += 1
                    right += 1
                    j += 1
            nonattacking = nonattacking/2
        return nonattacking
```

Selection of parents

```
[3]: def roulette(population):
    x = random.random()
```

```

current = 0
for individual in population:
    current += individual.si
    if current > x:
        return individual

```

```

[4]: def newPopulation(population):
    newPopulation = []
    while len(newPopulation) < PopulationSize:
        parent1 = roulette(population).indiv
        parent2 = roulette(population).indiv
        crossover = random.randint(0, 7)
        child1 = parent1[:crossover] + parent2[crossover:]
        child2 = parent2[:crossover] + parent1[crossover:]
        mutation(child1)
        mutation(child2)
        newPopulation.append(Individual(child1))
        newPopulation.append(Individual(child2))
    sumfitness = sum(c.fitness for c in newPopulation)
    for individual in newPopulation:
        individual.si = individual.fitness / sumfitness
    avgfitness = sumfitness/PopulationSize
    return (newPopulation, avgfitness)

```

Defining mutation

```

[5]: def mutation(child):
    if(random.random() < MutationPct):
        index = random.randint(0,7)
        child[index] = random.randint(1,8)

```

```

[6]: def myplot(numofgenerations, avgfitnessarray):
    plt.plot(numofgenerations, avgfitnessarray)
    plt.ylabel("Average fitness")
    plt.xlabel("Generation")
    #plt.yticks(range(0,30,2))
    #plt.xticks(range(0,100,10))
    plt.ylim(0,28)
    plt.tight_layout()
    plt.show()

```

```

[7]: #MutationPct can be a random value between 0.0 and 1.0
MutationPct = 0.3
#PopulationSize can be 10,100,500,1000 etc
PopulationSize = 100
#Number of Iterations
NumIterations = 500
population = []

```

```
[8]: for i in range(PopulationSize):
      population.append(Individual(random.sample(range(1,9),8)))
      sumfitness = sum(c.fitness for c in population)
      for individual in population:
          individual.si = individual.fitness / sumfitness
      avgfitness = sumfitness/PopulationSize
      print("Initial population")
      for individual in population:
          print(individual.indiv, ' ', individual.fitness, ' ', individual.si)
```

Initial population

[3, 7, 5, 2, 1, 6, 4, 8]	25.0	0.010813148788927335
[6, 8, 5, 3, 7, 2, 1, 4]	21.0	0.009083044982698962
[1, 2, 8, 4, 6, 5, 7, 3]	16.0	0.006920415224913495
[6, 1, 4, 2, 5, 8, 3, 7]	25.0	0.010813148788927335
[7, 4, 8, 6, 5, 2, 1, 3]	22.0	0.009515570934256055
[6, 5, 2, 3, 8, 4, 7, 1]	23.0	0.009948096885813149
[4, 3, 1, 2, 8, 6, 5, 7]	22.0	0.009515570934256055
[6, 7, 2, 3, 4, 1, 8, 5]	20.0	0.00865051903114187
[7, 6, 5, 4, 8, 3, 1, 2]	17.0	0.007352941176470588
[2, 8, 5, 7, 3, 6, 4, 1]	26.0	0.01124567474048443
[8, 4, 7, 1, 3, 5, 6, 2]	26.0	0.01124567474048443
[4, 5, 7, 3, 1, 2, 8, 6]	25.0	0.010813148788927335
[6, 1, 7, 2, 8, 3, 4, 5]	24.0	0.010380622837370242
[4, 5, 8, 3, 1, 6, 2, 7]	25.0	0.010813148788927335
[2, 4, 8, 5, 7, 1, 3, 6]	26.0	0.01124567474048443
[4, 2, 5, 3, 7, 6, 8, 1]	25.0	0.010813148788927335
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[8, 2, 1, 7, 3, 6, 4, 5]	23.0	0.009948096885813149
[3, 6, 7, 2, 4, 1, 8, 5]	27.0	0.011678200692041523
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[5, 7, 8, 4, 2, 1, 6, 3]	24.0	0.010380622837370242
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[3, 2, 5, 8, 4, 7, 6, 1]	23.0	0.009948096885813149
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[5, 1, 7, 3, 8, 2, 4, 6]	26.0	0.01124567474048443
[1, 6, 8, 7, 2, 4, 3, 5]	25.0	0.010813148788927335
[5, 2, 8, 1, 4, 3, 7, 6]	24.0	0.010380622837370242
[5, 3, 4, 2, 6, 1, 8, 7]	19.0	0.008217993079584774
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[3, 1, 4, 7, 6, 5, 2, 8]	23.0	0.009948096885813149
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[6, 8, 7, 4, 5, 2, 3, 1]	19.0	0.008217993079584774
[6, 8, 4, 3, 1, 7, 5, 2]	23.0	0.009948096885813149
[2, 3, 6, 8, 7, 1, 4, 5]	25.0	0.010813148788927335
[7, 5, 6, 1, 8, 4, 3, 2]	22.0	0.009515570934256055
[7, 6, 2, 8, 4, 3, 5, 1]	21.0	0.009083044982698962
[8, 7, 4, 5, 2, 6, 3, 1]	20.0	0.00865051903114187
[6, 8, 5, 4, 3, 7, 1, 2]	20.0	0.00865051903114187
[2, 3, 1, 8, 7, 4, 6, 5]	24.0	0.010380622837370242
[5, 7, 4, 8, 3, 1, 2, 6]	23.0	0.009948096885813149
[1, 4, 5, 8, 7, 6, 3, 2]	20.0	0.00865051903114187
[6, 8, 7, 4, 3, 2, 1, 5]	21.0	0.009083044982698962
[3, 5, 8, 7, 2, 4, 1, 6]	24.0	0.010380622837370242
[5, 1, 4, 6, 2, 7, 3, 8]	25.0	0.010813148788927335
[3, 4, 8, 5, 6, 2, 1, 7]	24.0	0.010380622837370242
[5, 2, 6, 3, 8, 7, 4, 1]	25.0	0.010813148788927335
[3, 1, 5, 8, 4, 6, 2, 7]	22.0	0.009515570934256055
[2, 4, 6, 7, 3, 1, 5, 8]	26.0	0.01124567474048443
[8, 4, 6, 1, 2, 3, 5, 7]	22.0	0.009515570934256055
[7, 4, 2, 1, 8, 3, 6, 5]	20.0	0.00865051903114187
[4, 1, 6, 8, 5, 7, 3, 2]	24.0	0.010380622837370242
[3, 5, 6, 2, 1, 7, 4, 8]	26.0	0.01124567474048443
[3, 6, 2, 8, 4, 5, 7, 1]	23.0	0.009948096885813149
[4, 1, 7, 3, 5, 8, 2, 6]	25.0	0.010813148788927335
[6, 5, 2, 8, 7, 4, 1, 3]	26.0	0.01124567474048443
[6, 4, 3, 5, 7, 2, 8, 1]	24.0	0.010380622837370242
[7, 3, 6, 1, 8, 2, 4, 5]	21.0	0.009083044982698962
[5, 4, 2, 7, 1, 3, 6, 8]	24.0	0.010380622837370242
[8, 7, 4, 6, 5, 2, 1, 3]	25.0	0.010813148788927335
[4, 3, 5, 7, 1, 6, 8, 2]	25.0	0.010813148788927335
[3, 5, 7, 6, 1, 8, 2, 4]	23.0	0.009948096885813149
[6, 5, 4, 3, 2, 8, 7, 1]	17.0	0.007352941176470588
[2, 6, 8, 1, 5, 3, 7, 4]	26.0	0.01124567474048443
[5, 7, 2, 4, 1, 3, 8, 6]	26.0	0.01124567474048443
[5, 2, 3, 6, 1, 4, 7, 8]	18.0	0.007785467128027681
[1, 8, 7, 6, 3, 4, 2, 5]	21.0	0.009083044982698962
[3, 7, 2, 5, 1, 6, 8, 4]	24.0	0.010380622837370242

[7, 2, 6, 8, 4, 1, 3, 5]	27.0	0.011678200692041523
[6, 7, 4, 3, 8, 2, 5, 1]	23.0	0.009948096885813149
[1, 2, 8, 3, 5, 7, 4, 6]	24.0	0.010380622837370242
[3, 1, 7, 5, 8, 6, 2, 4]	26.0	0.01124567474048443
[6, 4, 5, 8, 2, 7, 1, 3]	25.0	0.010813148788927335
[5, 8, 1, 3, 2, 4, 6, 7]	22.0	0.009515570934256055
[6, 4, 8, 5, 3, 1, 7, 2]	26.0	0.01124567474048443
[6, 8, 4, 1, 2, 3, 5, 7]	22.0	0.009515570934256055
[1, 4, 7, 5, 2, 3, 8, 6]	25.0	0.010813148788927335
[1, 2, 4, 3, 6, 5, 8, 7]	18.0	0.007785467128027681
[6, 3, 1, 5, 2, 4, 7, 8]	24.0	0.010380622837370242
[6, 4, 3, 7, 2, 1, 8, 5]	23.0	0.009948096885813149
[3, 5, 4, 8, 6, 7, 1, 2]	23.0	0.009948096885813149
[6, 2, 7, 3, 5, 8, 1, 4]	25.0	0.010813148788927335
[7, 1, 2, 8, 3, 4, 6, 5]	22.0	0.009515570934256055

```
[9]: count = 0
      numofgenerations = [0]
      avgfitnessarray = [avgfitness]
```

```
[10]: while count < NumIterations:
        count += 1
        numofgenerations.append(count)
        print("Iteration: ", count)
        (population, avgfitness) = newPopulation(population)
        avgfitnessarray.append(avgfitness)
        # print(avgfitness)
        # for individual in population:
        #     print(individual.indiv, ' ', individual.fitness, ' ', individual.
        ↪ si)
        for individual in population:
            if individual.fitness == 28:
                for elem in population:
                    print(elem.indiv)
                print("Resolved: ", individual.indiv)
                myplot(numofgenerations, avgfitnessarray)
                exit(1)
```

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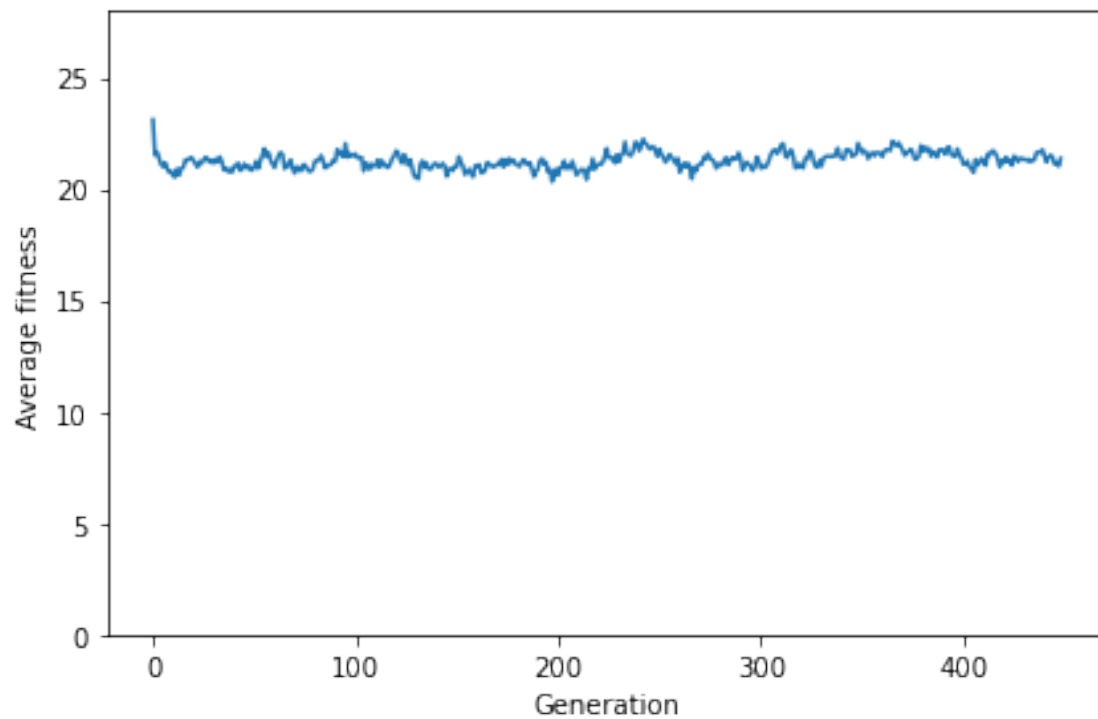
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Resolved: [5, 1, 4, 6, 8, 2, 7, 3]
```



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Iteration: 449
Iteration: 450
Iteration: 451
Iteration: 452
Iteration: 453
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Iteration: 460
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Iteration: 461  
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Iteration: 497  
Iteration: 498  
Iteration: 499  
Iteration: 500

```
[11]: print(count, " Iterations completed")
```

500 Iterations completed