

**SCHOOL OF
COMPUTING**

DESIGN AND ANALYSIS OF ALGORITHMS
LAB WORKBOOK
WEEK - 7

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CLASS : CSE-B

Question 1: Let there be 14 jobs with the profit of
22,19,29,28,30,21,27,25,24,26,14,27,19,11 with deadlines 3,3,8,6,7,5,10,4,6,12,13,2,14,1

Implement the greedy algorithm for the Job Sequencing with Deadlines and determine the optimal sequence of jobs that maximizes total profit.

WORKING:

Job sequencing (Greedy method)

g) Let there be 14 Jobs with the profit of 22, 19, 29, 28, 30, 21, 27, 25, 24, 26, 14, 27, 19, 11 with deadlines - 3, 3, 8, 6, 7, 5, 10, 4, 6, 12, 13, 2, 14, 1.

sol: Number of Jobs (N) = 14

Profits corresponding to Jobs J_1 to J_{14} are P_1 to P_{14}

$(P_1 \text{ to } P_{14}) = (22, 19, 29, 28, 30, 21, 27, 25, 24, 26, 14, 27, 19, 11)$

$(D_1 \text{ to } D_{14}) = (3, 3, 8, 6, 7, 5, 10, 4, 6, 12, 13, 2, 14, 1)$

Step-1: Arrange the jobs in descending order based on profits and write corresponding deadlines.

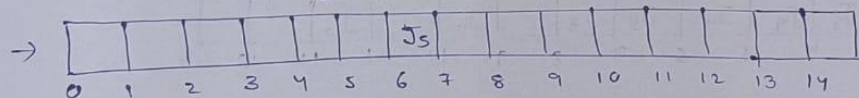
30, 29, 28, 27, 27, 26, 25, 24, 22, 21, 19, 19, 14, 11

7 8 6 10 2 12 4 6 3 5 3 14 13 1

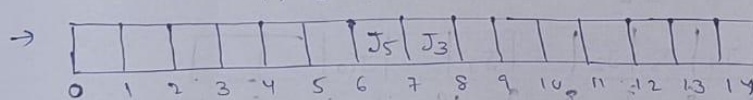
J_5 J_3 J_4 J_7 J_{12} J_{10} J_8 J_9 J_1 J_6 J_2 J_{13} J_{11} J_{14}

Step-2: Create slots and Assign jobs

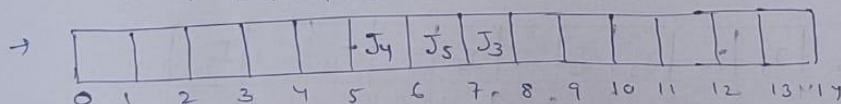
$J_5, P_5 = 30, D_5 = 7$



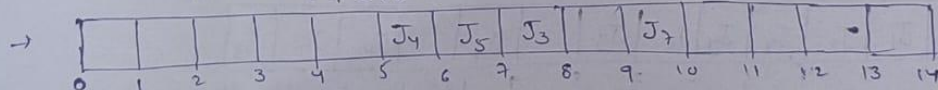
$J_3, P_3 = 29, D_3 = 8$



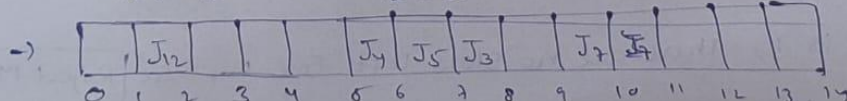
$J_4, P_4 = 28, D_4 = 6$



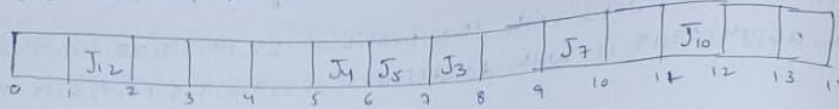
$J_7, P_7 = 27, D_7 = 10$



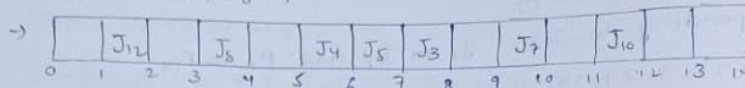
$J_{12}, P_{12} = 27, D_{12} = 2$



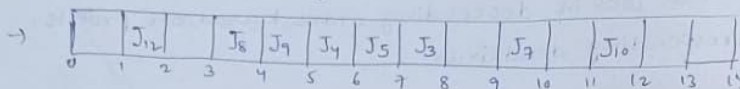
$J_{10}, P_{10} = 26, D_{10} = 12$



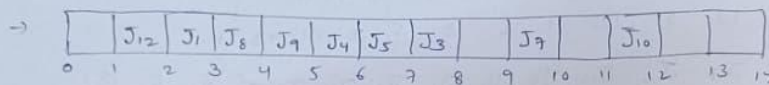
$J_8, P_8 = 25, D_8 = 4$



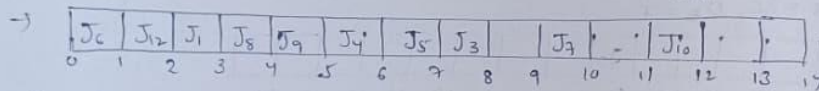
$J_9, P_9 = 24, D_9 = 6$ As slot [5-6] is filled check [4-5], As it is empty slot it with J_9



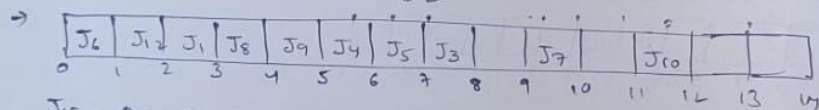
$J_1, P_1 = 22, D_1 = 3$



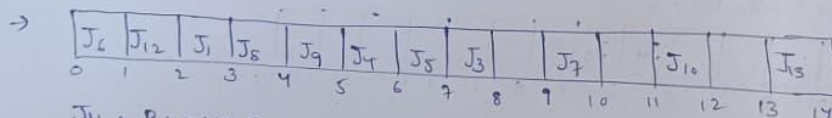
$J_6, P_6 = 21, D_6 = 5, A = [5-4]$ slot is already assigned, check previous slots, As only [0-1] is free slot it with J_6



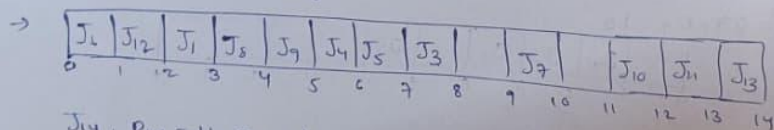
$J_2, P_2 = 19, D_2 = 3$. All slots before deadline i.e., 3 are allocated already. So, no slot for J_2



$J_{13}, P_{13} = 19, D_{13} = 14$



$J_{11}, P_{11} = 14, D_{11} = 13$



$J_{14}, P_{14} = 11, D_{14} = 1$

As deadline is 1, There are no slots left for P_{14} so Reject P_{14}

Final

Total

Final job sequence, {J₅, J₃, J₄, J₇, J₁₂, J₁₀, J₈, J₉, J₁, J₆, J₁₃, J₁₁}

| | | | | | | | | | | | | | | |
|----------------|-----------------|----------------|----------------|----------------|----------------|----------------|----------------|---|----------------|----|-----------------|-----------------|-----------------|----|
| J ₆ | J ₁₂ | J ₁ | J ₈ | J ₉ | J ₄ | J ₅ | J ₃ | | J ₇ | | J ₁₀ | J ₁₁ | J ₁₃ | |
| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 |

$$\text{Total profit} = 21 + 27 + 22 + 25 + 29 + 28 + 30 + 29 + 27 + 26 + 14 + 19 \\ = 292$$

COD

```
//CH.SC.U4CSE24126
#include <stdio.h>
#define MAX 100
struct Job
{
    int id;
    int profit;
    int deadline;
};
void sortJobs(struct Job jobs[], int n)
{
    int i, j;
    struct Job temp;

    for(i = 0; i < n - 1; i++)
    {
        for(j = 0; j < n - i - 1; j++)
        {
            if(jobs[j].profit < jobs[j + 1].profit)
            {
                temp = jobs[j];
                jobs[j] = jobs[j + 1];
                jobs[j + 1] = temp;
            }
        }
    }
}
```

```
27 }
28 int findMaxDeadline(struct Job jobs[], int n)
29 {
30     int i, max = jobs[0].deadline;
31
32     for(i = 1; i < n; i++)
33     {
34         if(jobs[i].deadline > max)
35         {
36             max = jobs[i].deadline;
37         }
38     }
39     return max;
40 }
41 int main()
42 {
43     struct Job jobs[MAX];
44     int n, i, j;
45
46     printf("Enter number of jobs: ");
47     scanf("%d", &n);
48     printf("Enter profits:\n");
49     for(i = 0; i < n; i++)
50     {
```

```
51     jobs[i].id = i + 1;
52     scanf("%d", &jobs[i].profit);
53 }
54 printf("Enter deadlines:\n");
55 for(i = 0; i < n; i++)
56 {
57     scanf("%d", &jobs[i].deadline);
58 }
59 sortJobs(jobs, n);
60 int maxDeadline = findMaxDeadline(jobs, n);
61 int slot[MAX];
62 for(i = 1; i <= maxDeadline; i++)
63 {
64     slot[i] = -1;
65 }
66 int totalProfit = 0;
67 for(i = 0; i < n; i++)
68 {
69     for(j = jobs[i].deadline; j >= 1; j--)
70     {
71         if(slot[j] == -1)
72         {
73             slot[j] = jobs[i].id;
74             totalProfit += jobs[i].profit;
75             break;
76         }
```

```
77     }
78 }
79 printf("\nSlot Arrangement:\n");
80 for(i = 1; i <= maxDeadline; i++)
81 {
82     if(slot[i] == -1)
83         printf("Slot %d : _\n", i);
84     else
85         printf("Slot %d : J%d\n", i, slot[i]);
86 }
87 printf("\nMaximum Profit = %d\n", totalProfit);
88 return 0;
89 }
```

OUTPUT:


```
PS D:\DAA> gcc 6.c -o tree.exe
PS D:\DAA> ./tree.exe
Enter number of jobs: 14
Enter profits:
22 19 29 28 30 21 27 25 24 26 14 27 19 11
Enter deadlines:
3 3 8 6 7 5 10 4 6 12 13 2 14 1

Slot Arrangement:
Slot 1 : J6
Slot 2 : J12
Slot 3 : J1
Slot 4 : J8
Slot 5 : J9
Slot 6 : J4
Slot 7 : J5
Slot 8 : J3
Slot 9 : _
Slot 10 : J7
Slot 11 : _
Slot 12 : J10
Slot 13 : J11
Slot 14 : J13

Maximum Profit = 292
PS D:\DAA> █
```

Time Complexity:

1. Sorting the jobs by profit

We used Bubble Sort in the program.

Time complexity: $O(n^2)$

2. Finding maximum deadline

We check all jobs once.

Time complexity: $O(n)$

3. Assigning jobs to slots

For each job, we may check up to d slots. $O(n^2)$

Total Time Complexity

$$O(n^2) + O(n) + O(n^2) = O(n^2)$$

Space Complexity

We use:

- Job array $\rightarrow O(n)$
- Slot array $\rightarrow O(d)$

Total Space: $O(n)$