

SCHOOL OF
COMPUTING

DESIGN AND ANALYSIS OF ALGORITHMS
LAB WORKBOOK
WEEK - 7

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Question 1: Let there be 14 jobs with the profit of
22,19,29,28,30,21,27,25,24,26,14,27,19,11 with deadlines 3,3,8,6,7,5,10,4,6,12,13,2,14,1

Implement the greedy algorithm for the Job Sequencing with Deadlines and determine the optimal sequence of jobs that maximizes total profit.

WORKING:

Job sequencing (Greedy method)

Q) Let there be 14 Jobs with the profit of 22, 19, 29, 28, 30, 21, 27, 25, 24, 26, 14, 27, 19, 11 with deadlines - 3, 3, 8, 6, 7, 5, 10, 4, 6, 12, 13, 2, 14, 1.

Sol:- Number of Jobs (N) = 14

Profits corresponding to Jobs J_1 to J_{14} are P_1 to P_{14}

$$(P_1 \text{ to } P_{14}) = (22, 19, 29, 28, 30, 21, 27, 25, 24, 26, 14, 27, 19, 11)$$

$$(D_1 \text{ to } D_{14}) = (3, 3, 8, 6, 7, 5, 10, 4, 6, 12, 13, 2, 14, 1)$$

Step-1: Arrange the jobs in descending order based on profits. and write corresponding deadlines.

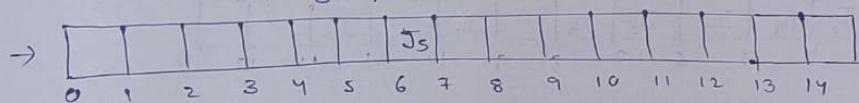
30, 29, 28, 27, 27, 26, 25, 24, 22, 21, 19, 19, 14, 11

7 8 6 10 2 12 4 6 3 5 3 14 13 1

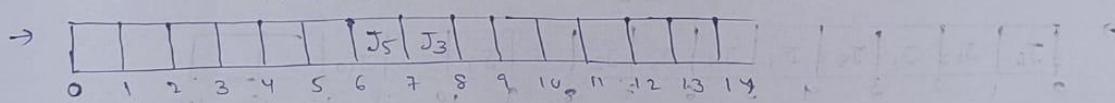
$J_5 \quad J_3 \quad J_4 \quad J_7 \quad J_2 \quad J_{10} \quad J_8 \quad J_9 \quad J_1 \quad J_6 \quad J_2 \quad J_{13} \quad J_{11} \quad J_{14}$

Step-2: Create slots and Assign jobs

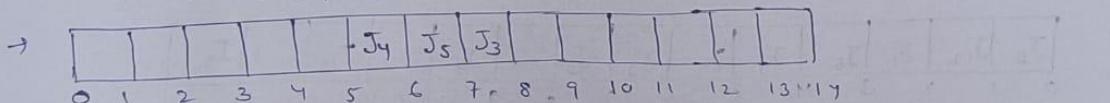
$J_5, P_5 = 30, D_5 = 7$



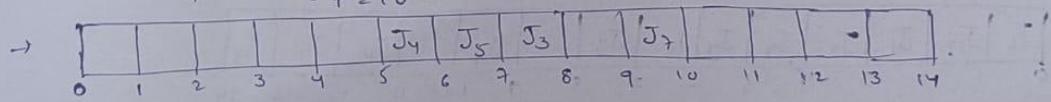
$J_3, P_3 = 29, D_3 = 8$



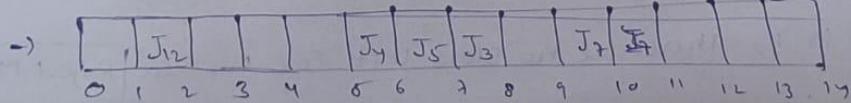
$J_4, P_4 = 28, D_4 = 6$



$J_7, P_7 = 27, D_7 = 10$



$J_{12}, P_{12} = 27, D_{12} = 2$



$J_{10}, P_{10} = 26, D_{10} = 12$

	J_{12}				J_4	J_8	J_3		J_7	J_{10}		
0	1	2	3	4	5	6	7	8	9	10	11	12

$J_8, P_8 = 25, D_8 = 4$

	J_{12}		J_8		J_4	J_5	J_3		J_7	J_{10}		
0	1	2	3	4	5	6	7	8	9	10	11	12

$J_9, P_9 = 24, D_9 = 6$ As slot [5-6] is filled check [4-5]. As it is empty add it with J_9

	J_{12}		J_8	J_9	J_4	J_5	J_3		J_7	J_{10}		
0	1	2	3	4	5	6	7	8	9	10	11	12

$J_1, P_1 = 22, D_1 = 3$

	J_{12}	J_1	J_8	J_9	J_4	J_5	J_3		J_7	J_{10}		
0	1	2	3	4	5	6	7	8	9	10	11	12

$J_6, P_6 = 21, D_6 = 5, A = [5-4]$ slot is already assigned, check previous slots, As only [0-1] is free add it with J_6

	J_6	J_{12}	J_1	J_8	J_9	J_4	J_5	J_3		J_7	J_{10}	
0	1	2	3	4	5	6	7	8	9	10	11	12

$J_2, P_2 = 19, D_2 = 3$. All slots before deadline i.e., 3 are allocated already. So, no slot for J_2

	J_6	J_{12}	J_1	J_8	J_9	J_4	J_5	J_3		J_7	J_{10}	
0	1	2	3	4	5	6	7	8	9	10	11	12

$J_{13}, P_{13} = 19, D_{13} = 14$

	J_6	J_{12}	J_1	J_8	J_9	J_4	J_5	J_3		J_7	J_{10}	J_{13}
0	1	2	3	4	5	6	7	8	9	10	11	12

$J_{11}, P_{11} = 14, D_{11} = 13$

	J_6	J_{12}	J_1	J_8	J_9	J_4	J_5	J_3		J_7	J_{10}	J_{11}
0	1	2	3	4	5	6	7	8	9	10	11	12

$J_{14}, P_{14} = 11, D_{14} = 1$

As deadline is 1, There are no slots left for P_{14} so Reject 14

Final job sequence, {J₅, J₃, J₄, J₇, J₁₂, J₁₀, J₈, J₉, J₁, J₆, J₁₃, J₁₁}

J ₆	J ₁₂	J ₁	J ₈	J ₉	J ₄	J ₅	J ₃	J ₇	J ₁₀	J ₁₁	J ₁₃
0	1	2	3	4	5	6	7	8	9	10	11

$$\begin{aligned}\text{Total profit} &= 21 + 27 + 22 + 25 + 24 + 28 + 30 + 29 + 27 + 26 + 14 + 19 \\ &= 292\end{aligned}$$

COD

```
//CH.SC.U4CSE24126
#include <stdio.h>
#define MAX 100
struct Job
{
    int id;
    int profit;
    int deadline;
};
void sortJobs(struct Job jobs[], int n)
{
    int i, j;
    struct Job temp;

    for(i = 0; i < n - 1; i++)
    {
        for(j = 0; j < n - i - 1; j++)
        {
            if(jobs[j].profit < jobs[j + 1].profit)
            {
                temp = jobs[j];
                jobs[j] = jobs[j + 1];
                jobs[j + 1] = temp;
            }
        }
    }
}
```

```
27 }
28 int findMaxDeadline(struct Job jobs[], int n)
29 {
30     int i, max = jobs[0].deadline;
31
32     for(i = 1; i < n; i++)
33     {
34         if(jobs[i].deadline > max)
35         {
36             max = jobs[i].deadline;
37         }
38     }
39     return max;
40 }
41 int main()
42 {
43     struct Job jobs[MAX];
44     int n, i, j;
45
46     printf("Enter number of jobs: ");
47     scanf("%d", &n);
48     printf("Enter profits:\n");
49     for(i = 0; i < n; i++)
50     {
```

```
51     jobs[i].id = i + 1;
52     scanf("%d", &jobs[i].profit);
53 }
54 printf("Enter deadlines:\n");
55 for(i = 0; i < n; i++)
56 {
57     scanf("%d", &jobs[i].deadline);
58 }
59 sortJobs(jobs, n);
60 int maxDeadline = findMaxDeadline(jobs, n);
61 int slot[MAX];
62 for(i = 1; i <= maxDeadline; i++)
63 {
64     slot[i] = -1;
65 }
66 int totalProfit = 0;
67 for(i = 0; i < n; i++)
68 {
69     for(j = jobs[i].deadline; j >= 1; j--)
70     {
71         if(slot[j] == -1)
72         {
73             slot[j] = jobs[i].id;
74             totalProfit += jobs[i].profit;
75             break;
76         }
    }
```

```
77     }
78 }
79 printf("\nSlot Arrangement:\n");
80 for(i = 1; i <= maxDeadline; i++)
81 {
82     if(slot[i] == -1)
83         printf("Slot %d : _\n", i);
84     else
85         printf("Slot %d : J%d\n", i, slot[i]);
86 }
87 printf("\nMaximum Profit = %d\n", totalProfit);
88 return 0;
89 }
```

OUTPUT:

```
PS D:\DAA> gcc 6.c -o tree.exe
PS D:\DAA> ./tree.exe
Enter number of jobs: 14
Enter profits:
22 19 29 28 30 21 27 25 24 26 14 27 19 11
Enter deadlines:
3 3 8 6 7 5 10 4 6 12 13 2 14 1

Slot Arrangement:
Slot 1 : J6
Slot 2 : J12
Slot 3 : J1
Slot 4 : J8
Slot 5 : J9
Slot 6 : J4
Slot 7 : J5
Slot 8 : J3
Slot 9 : _
Slot 10 : J7
Slot 11 : _
Slot 12 : J10
Slot 13 : J11
Slot 14 : J13

Maximum Profit = 292
PS D:\DAA>
```

Time Complexity:

1. Sorting the jobs by profit

We used Bubble Sort in the program.

Time complexity: $O(n^2)$

2. Finding maximum deadline

We check all jobs once.

Time complexity: $O(n)$

3. Assigning jobs to slots

For each job, we may check up to d slots. $O(n^2)$

Total Time Complexity

$$O(n^2) + O(n) + O(n^2) = O(n^2)$$

Space Complexity

We use:

- Job array → $O(n)$
- Slot array → $O(d)$

Total Space: $O(n)$