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Assignment 2

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Download all python codes from

https://github.com/srikaran-p/AI1103/tree/main/ Assignment2/codes

and latex codes from

https://github.com/srikaran-p/AI1103/tree/main/ Assignment2

PROBLEM

(Gate-EC 17) The input X to the binary Symmetric Channel (BSC) shown in Fig. 0 is '1' with probability 0.8. The cross-over probability is $\frac{1}{7}$. If the received bit Y = 0, the condition probability that '1' was transmitted is ...

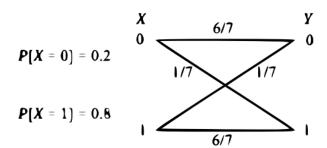


Fig. 0: Binary Symmetric Channel

Solution

$$\Pr(X = 1 | Y = 0) = \frac{\Pr(\{X = 1\}\{Y = 0\})}{\Pr(Y = 0)} \quad (0.0.1)$$

$$\Pr(Y = 0|X = 1) = \frac{\Pr(\{X = 1\}\{Y = 0\})}{\Pr(X = 1)} \quad (0.0.2)$$

From (0.0.2),

$$Pr({X = 1}{Y = 0}) = Pr(Y = 0|X = 1) Pr(X = 1)$$
(0.0.3)

Substituting (0.0.3) in (0.0.1),

$$Pr(X = 1|Y = 0) = \frac{Pr(Y = 0|X = 1) Pr(X = 1)}{Pr(Y = 0)}$$
(0.0.4)

Given data,

$$\Pr(Y = 0|X = 1) = \frac{1}{7}, \Pr(Y = 0|X = 0) = \frac{6}{7}$$
(0.0.5)

$$Pr(Y = 0) = Pr(Y = 0|X = 1) Pr(X = 1) + Pr(Y = 0|X = 0) Pr(X = 0) (0.0.6)$$

Substituting the values from (0.0.5) and the data given in the question in (0.0.6),

$$\Pr(Y=0) = \frac{2}{7} \tag{0.0.7}$$

Substituting (0.0.5), (0.0.7) and the data given in the question in (0.0.4),

$$Pr(X = 1|Y = 0) = 0.4$$
 (0.0.8)

If the received bit is Y = 0, the conditional probability that '1' was transmitted is 0.4.

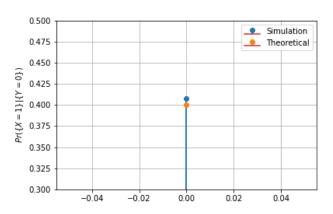


Fig. 0: Plot for Simulation v/s Theoretical