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Assignment 3

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Download all python codes from

https://github.com/srikaran-p/AI1103/tree/main/ Assignment3/codes

and latex codes from

https://github.com/srikaran-p/AI1103/tree/main/ Assignment3

PROBLEM

(GATE-MA 2015 Q17) Let *X* be a random variable having the distribution function

$$F(x) = \begin{cases} 0 & \text{if } x < 0\\ \frac{1}{4} & \text{if } 0 \le x < 1\\ \frac{1}{3} & \text{if } 1 \le x < 2\\ \frac{1}{2} & \text{if } 2 \le x < \frac{11}{3}\\ 1 & \text{if } x \ge \frac{11}{3} \end{cases}$$
(0.0.1)

Then E(X) is equal to ...

SOLUTION

The PDF for the above CDF is

$$P(x) = \begin{cases} \frac{1}{4} & \text{if } x = 0\\ \frac{1}{12} & \text{if } x = 1\\ \frac{1}{6} & \text{if } x = 2\\ \frac{1}{2} & \text{if } x = \frac{11}{3}\\ 0 & \text{if otherwise} \end{cases}$$
(0.0.2)

$$E(X) = 0\left(\frac{1}{4}\right) + 1\left(\frac{1}{12}\right) + 2\left(\frac{1}{6}\right) + \left(\frac{11}{3}\right)\left(\frac{1}{2}\right) \quad (0.0.3)$$

$$E(X) = 2.25 \quad (0.0.4)$$

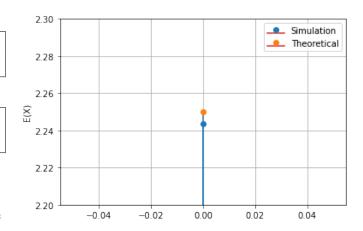


Fig. 0: Plot for Simulation v/s Theoretical