Assignment 3

Perambuduri Srikaran - AI20BTECH11018

Download all python codes from

https://github.com/srikaran-p/EE3900/tree/main/ Assignment3/codes

Download all latex codes from

https://github.com/srikaran-p/EE3900/tree/main/ Assignment3

PROBLEM

(Ramsey 4.2 Q18) Find the equation of the chord of the circle $\mathbf{x}^T \mathbf{x} - \begin{pmatrix} 6 & 4 \end{pmatrix} \mathbf{x} - 23 = 0$ which has the point $\binom{4}{1}$ as its middle point.

SOLUTION

The general equation of circle is

$$\mathbf{x}^T \mathbf{x} - 2\mathbf{c}\mathbf{x} + f = 0 \tag{0.0.1}$$

where \mathbf{c} is the centre of the circle.

$$\mathbf{c} = \begin{pmatrix} 3 & 2 \end{pmatrix} \qquad (0.0.2)$$

$$\mathbf{O} = \mathbf{c}^T \qquad (0.0.3)$$

$$\mathbf{O} = \mathbf{c}^T \tag{0.0.3}$$

$$\mathbf{M} = \begin{pmatrix} 4 \\ 1 \end{pmatrix} \tag{0.0.4}$$

The line passing through the centre bisects any chord perpendicularly. The direction vector of **OM** is

$$\mathbf{OM} = \mathbf{M} - \mathbf{O} \tag{0.0.5}$$

$$= \begin{pmatrix} 4\\1 \end{pmatrix} - \begin{pmatrix} 3\\2 \end{pmatrix} \tag{0.0.6}$$

$$= \begin{pmatrix} 1 \\ -1 \end{pmatrix} \tag{0.0.7}$$

The normal vector \mathbf{n} is

$$\mathbf{n} = \mathbf{OM} \tag{0.0.8}$$

The equation of line in terms of normal vector

$$\mathbf{n}^{T}(\mathbf{x} - \mathbf{M}) = 0 \tag{0.0.9}$$

$$\begin{pmatrix} 1 & -1 \end{pmatrix} \mathbf{x} = \begin{pmatrix} 1 & -1 \end{pmatrix} \mathbf{M} \tag{0.0.10}$$

$$\begin{pmatrix} 1 & -1 \end{pmatrix} \mathbf{x} = \begin{pmatrix} 1 & -1 \end{pmatrix} \begin{pmatrix} 4 \\ 1 \end{pmatrix} \tag{0.0.11}$$

$$\begin{pmatrix} 1 & -1 \end{pmatrix} \mathbf{x} = 3 \tag{0.0.12}$$

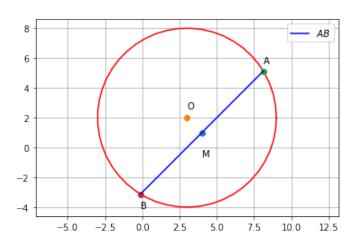


Fig. 0: Plot of the given points and circle