

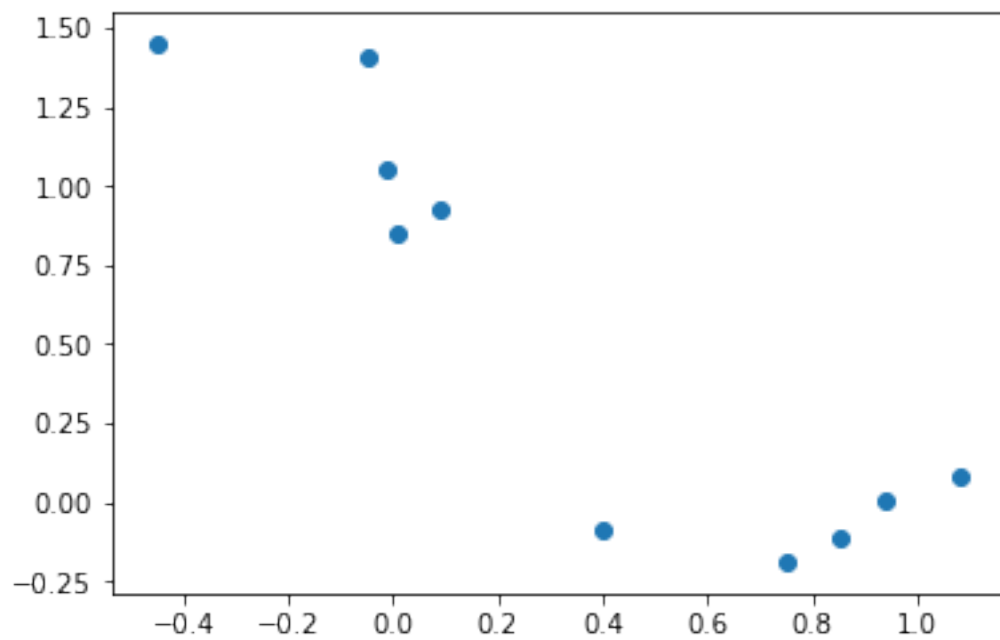
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March 24, 2019

```
In [175]: %matplotlib inline
import numpy as np
import matplotlib.pyplot as plt
d1 = [[1.08, .08], [0.75, -0.19], [0.85, -0.11], [0.94, 0.01], [0.4, -0.09], [1.25, -.21], [1.19, 0.07], [0.99, 0.04], [0.69, -0.02]]
d2 = [[0.01, 0.85], [-0.01, 1.05], [0.09, 0.93], [-0.05, 1.41], [-0.45, 1.45], [0.07, 1.20], [-0.3, 1.1], [0.0, 1.0], [0.0, 1.0]]
d1 = np.array(d1)
d2 = np.array(d2)
d1train = d1[0:5]
d2train = d2[0:5]
d1test = d1[5:10]
d2test = d2[5:10]
d = np.concatenate((d1,d2),0)
dtest = np.concatenate((d1test,d2test),0)
print(d)
print(d[1,:])
dtrain = np.concatenate((d1train,d2train),0)
print('Training data is :\n', dtrain)
dtrainx = dtrain[:,0]
dtrainy = dtrain[:,1]
w1 = [0,0]
w2 = [0,0]
w1 = np.array(w1)
w2 = np.array(w2)
T = [[1.0,0.0], [1.0,0.0], [1.0,0.0], [1.0,0.0], [1.0,0.0], [0.0,1.0], [0.0,1.0], [0.0,1.0], [0.0,1.0]]
T = np.array(T, dtype = float)
plt.scatter(x = dtrainx, y = dtrainy)
print('scatter plot is:')
plt.show()
```

```
[[ 1.08  0.08]
 [ 0.75 -0.19]
 [ 0.85 -0.11]
 [ 0.94  0.01]
 [ 0.4  -0.09]
 [ 1.25 -0.21]
 [ 1.19  0.07]
 [ 0.99  0.04]
 [ 0.69 -0.02]
```

```
[ 1.32  0.02]
[ 0.01  0.85]
[-0.01  1.05]
[ 0.09  0.93]
[-0.05  1.41]
[-0.45  1.45]
[ 0.07  1.2 ]
[-0.33  0.88]
[-0.06  1.08]
[-0.33  1.1 ]
[-0.24  1.01]]
[ 0.75 -0.19]
Training data is :
[[ 1.08  0.08]
 [ 0.75 -0.19]
 [ 0.85 -0.11]
 [ 0.94  0.01]
 [ 0.4  -0.09]
 [ 0.01  0.85]
 [-0.01  1.05]
 [ 0.09  0.93]
 [-0.05  1.41]
 [-0.45  1.45]]
scatter plot is:
```



```

In [176]: def compute_prob(xk,w1,w2):
            e1 = xk.dot(w1)
            e2 = xk.dot(w2)
            s = np.exp(e1) + np.exp(e2)
            p = [np.exp(e1)/s,np.exp(e2)/s]
            p = np.array(p)
            return p

In [177]: def compute_y(d,w1,w2):
            y = np.zeros([int(d.size/2),2])
            for i in range(int(d.size/2)):
                x = d[i,:]
                y[i,:] = compute_prob(x,w1,w2)
            print(y)
            return y

In [178]: def compute_cross_entropy(y,t):
            J = 0
            for i in range(2):
                for j in range(int(y.size/2)):
                    J -= t[j][i]*np.log(y[j][i])
            return J

In [179]: def g_descent(t,x,w1,w2,eta):
            w1n = w1
            w2n = w2

            for i in range(int(x.size/2)):
                y = compute_prob(x[i,:],w1n,w2n)
                w1n = w1n + eta*(float(t[i,0])-y[0])*x[i,:]
                w2n = w2n + eta*(float(t[i,1])-y[1])*x[i,:]
            return w1n,w2n

In [ ]:

In [180]: w1x = w1
            w2x = w2
            J = np.zeros(20)
            for i in range(20):
                w1x,w2x = g_descent(T,dtrain,w1x,w2x,0.1)
                y = compute_y(dtrain,w1x,w2x)
                J[i] = compute_cross_entropy(y,T)

            print('Test data')
            y1 = compute_y(dtest,w1x,w2x)

            plt.plot(range(20),J)
            plt.show

```

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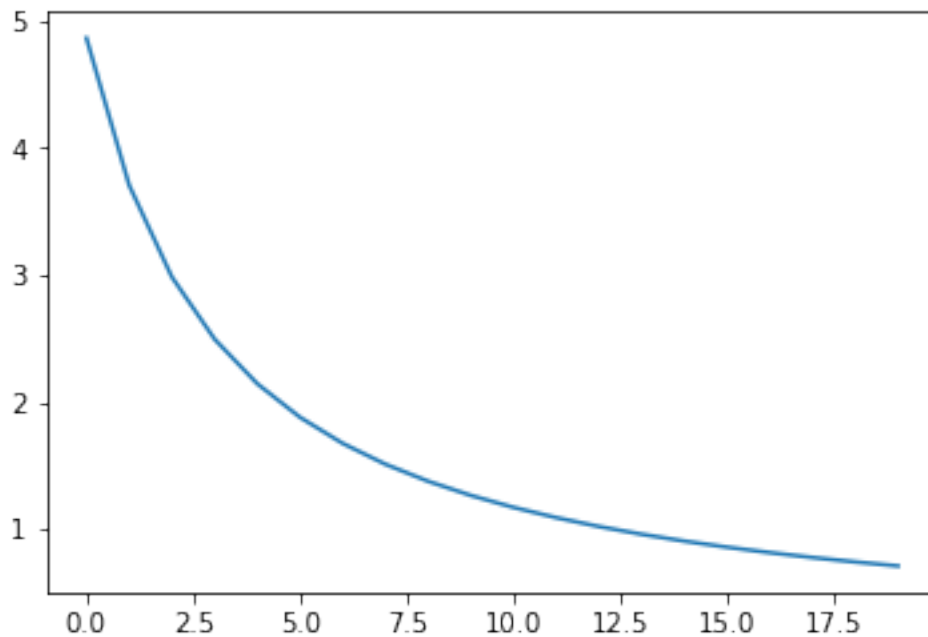
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```

Test data

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```

Out[180]: <function matplotlib.pyplot.show(*args, **kw)>



In []:

In []:

In []: