These are some of the doubts that i've had while deriving the equations. While we derived the stress balance equation at the liquid -gas interface, we did the following,

1.

$$\left[ \left( -p + 2\mu \frac{\partial u_r}{\partial r} \right) + \mu \left( \frac{1}{r} \frac{\partial u_r}{\partial \theta} - \frac{u_\theta}{r} + \frac{\partial u_\theta}{\partial r} \right) \left( \frac{-1}{r} \frac{\partial h}{\partial \theta} \right) + \mu \left( \frac{\partial u_z}{\partial r} + \frac{\partial u_r}{\partial z} \right) \left( \frac{-\partial h}{\partial z} \right) \right]$$

$$(1)$$

$$\frac{1}{\left(\sqrt{\left(\frac{1}{r}\frac{\partial h}{\partial \theta}\right)^2+1}\right)}\frac{1}{\sqrt{\left(\frac{\partial h}{\partial z}\right)^2+\left(\frac{1}{r}\frac{\partial h}{\partial \theta}\right)^2+1}}$$