

# 281 Live Session

Week 12 — 2023/4/5

# Agenda

- Final project updates
- Linear Classifiers overview
- Practical applications of SVMs
- Exercise: Face Classification (Part 1)

# Project Updates

Order: Vehicles, Satellite, Recycling, Fruit

This week: PCA results

Next week: Confusion matrix

# Big picture

1: Perspective Projection

2: Image Formation

3: Image Artifacts

4: Convolution

5: Fourier

6: Pyramids, Edges, and Features

7: Image Analysis

8: Least-Squares

9: Total and Iterative Least-Squares

10: Clustering

11: Dimensionality Reduction

12: Linear Classifiers

13: Nonlinear Classifiers

12.1 Least-Squares for Classification

12.2 Logistic Regression for Classification

12.3 Linear Discriminant Analysis (LDA)

12.4 Receiver Operating Curve

12.5 Linear Discriminant Analysis, an Example

12.6 Multiclass and Nonlinear Classifiers

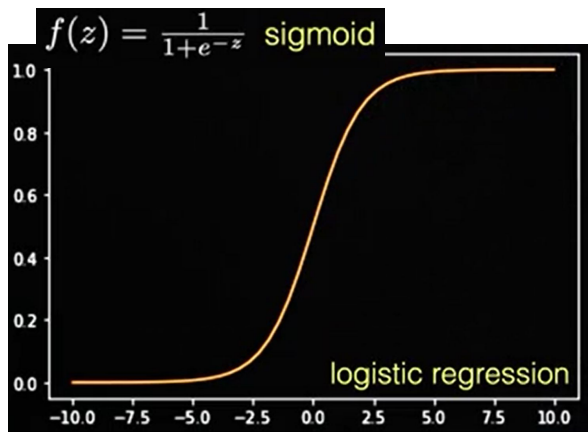
12.7 Margins

12.8 Maximizing Margins

Intuition goals:

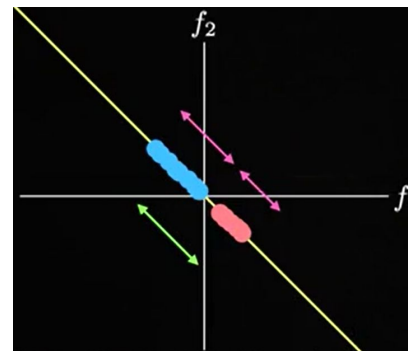
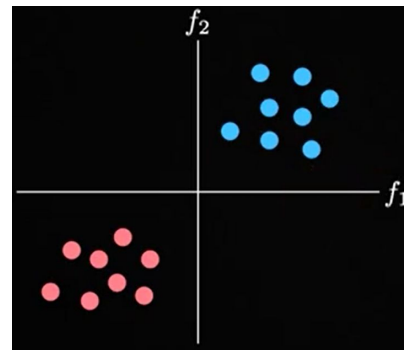
- What is a classifier model?
- How do we evaluate quality of fit?
- Is it better to have more false positives or false negatives? Why?
- What is the goal of an LDA classifier?
- What is the goal of an SVM classifier?
- Why do we maximize the margin?

# Overview – Linear classifiers



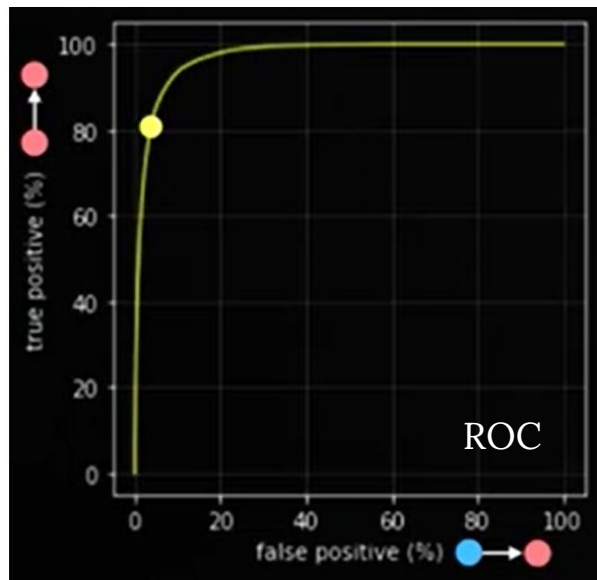
$y$  -> class label  
 $w\mathbf{x}$  -> model output  
 $f(z)$  -> sigmoid

$$P(Y = y \mid X = \vec{x}) = [f(\vec{w}^t \vec{x})]^y \cdot [1 - f(\vec{w}^t \vec{x})]^{1-y}$$



Two covariance matrices - within & across

# Overview – Classifier evaluation



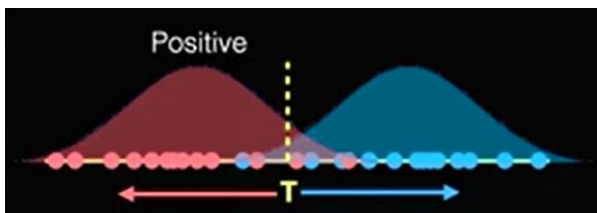
Confusion Matrix

		Expected			
		1	2	3	4
Predicted	1	52	3	7	2
	2	2	28	2	0
	3	5	2	25	12
	4	1	1	9	40

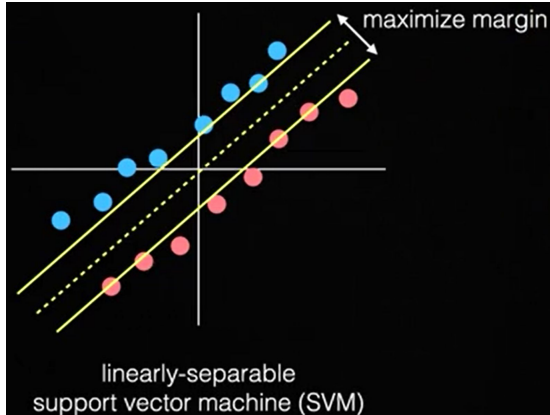
Distributions must be separable to perform classification

Error tolerance depends on specific application domain

False Positive (I)  
False Negative (II)



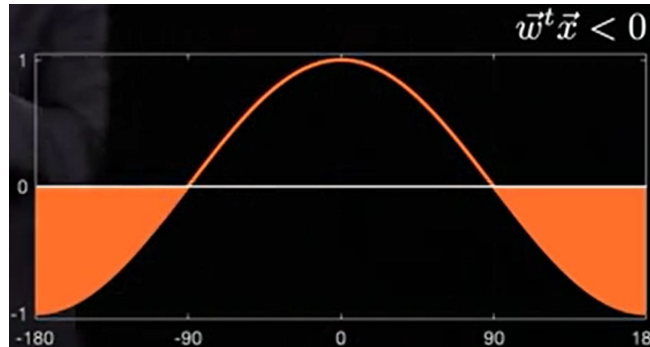
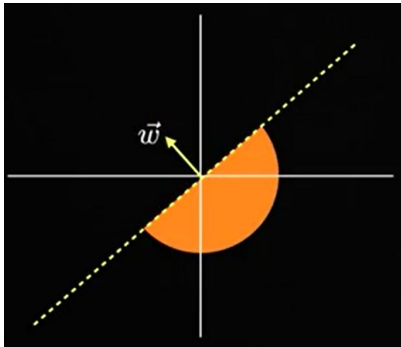
# Overview — Support vector machines (SVMs)



goal is to maximize distance between boundary points

classification  $\rightarrow$  sign of dot product between  $w$  and our boundary plane

minimize inverse of  $\lambda \|w\|$  subject to classification constraint



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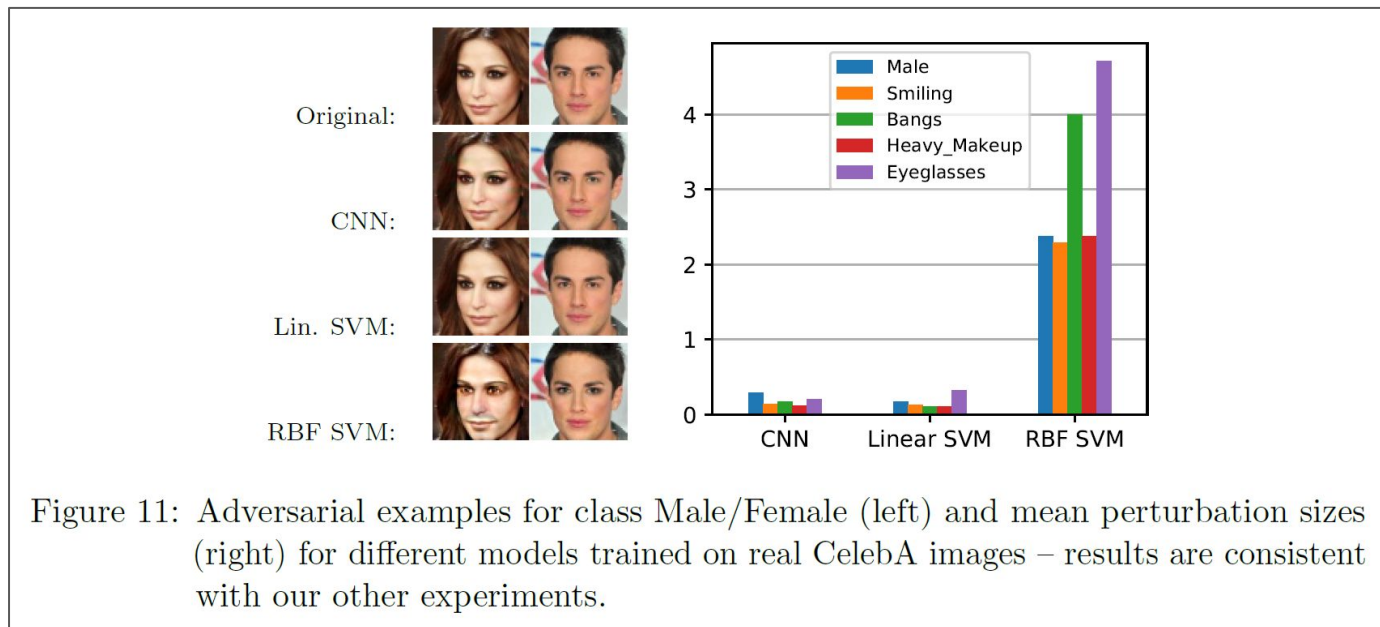
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# Practical Applications of SVMs

Maximizing the margin produces a more robust classifier



# Group Exercise – Face Classification Part 1



# Upcoming ToDo's

Watch Async lectures for Unit 12

Final Projects - Confusion Matrix

Final Presentations will be in class April 19th

Final Reports will be due Sunday April 23rd