

Photoionisation and Photoelectron ionisation rate calculations for NRL new bins for X-rays

Theoretical Calculation of altitude of unit optical depth (referred here as “Table data”)

$$\tau(z)=1=\sigma^a H n(z)$$

$$\text{Exponential density: } n(z)=n_0 \exp\left(\frac{-z}{H}\right)$$

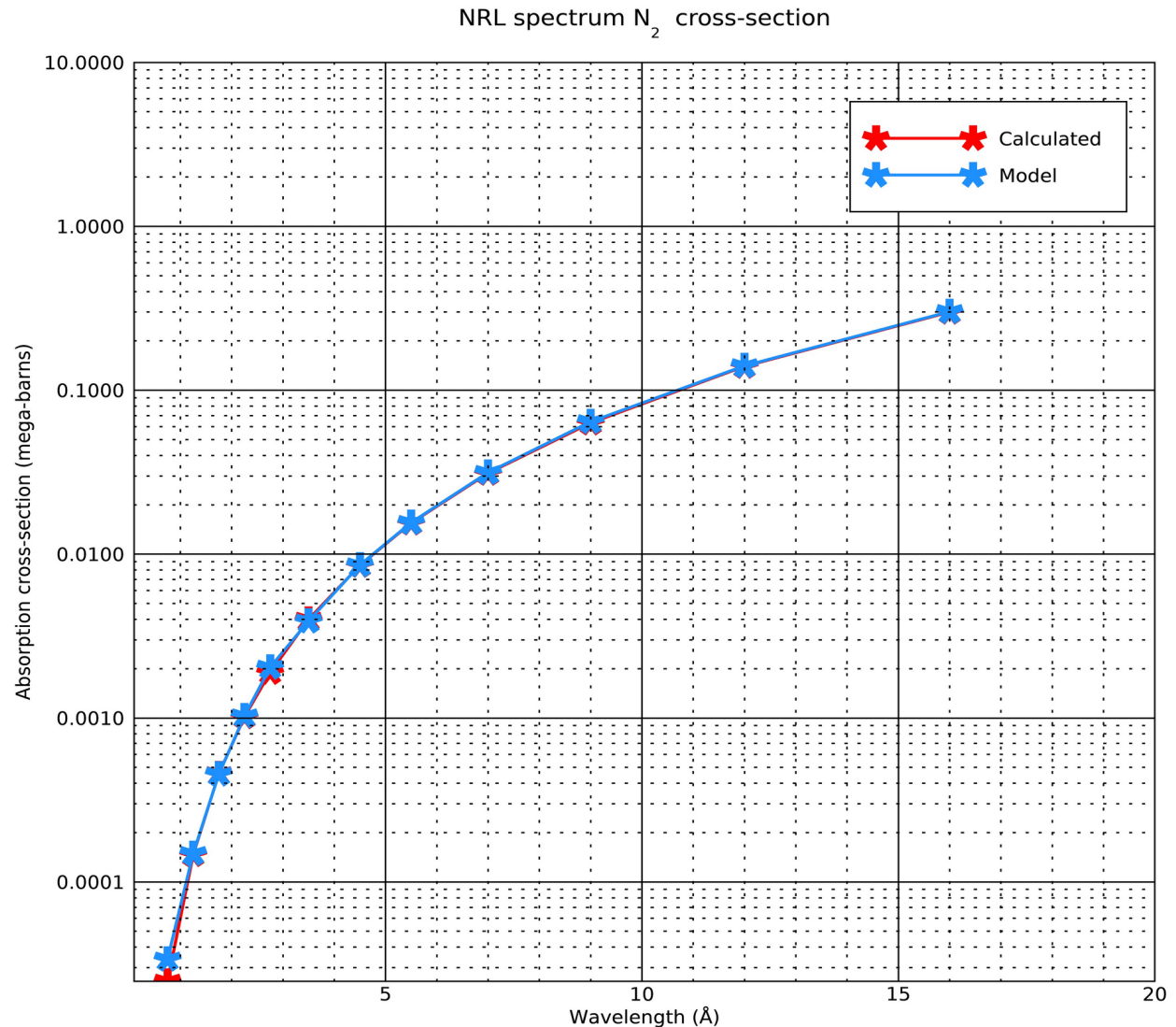
$$\text{Altitude of unit optical depth: } z=H \ln(H n_0 \sigma^a)$$

Assuming: Scale Height $H=7 \text{ km}$, $n_0=2.7 \times 10^{19} \text{ cm}^{-3}$, σ^a for N_2 as given, we find the value for z for optical depth $\tau=1$ by using the above formula

Calculated	Results				
Bin #	λ min (Å)	λ max (Å)	Mean λ (Å)	Mean σN_2 abs (mega-barns)	Alt of tau=1 (km)
1	0.5	1	0.75	2.48e-5	43
2	1	1.5	1.25	1.47e-4	55.5
3	1.5	2	1.75	4.57e-4	63.5
4	2	2.5	2.25	1.02e-3	69.1
5	2.5	3	2.75	1.9e-3	73.3
6	3	4	3.5	4.0e-3	78.7
7	4	5	4.5	8.55e-3	84
8	5	6	5.5	1.55e-2	88.1
9	6	8	7	3.12e-2	93
10	8	10	9	6.32e-2	98
11	10	14	12	0.14	103.5
12	14	18	16	0.30	109

Calculated and Model N₂ absorption cross-sections

1. The red line is the table (slide 2) N₂ cross-sections and the blue line is the photoelectron model N₂ absorption cross-sections
2. The model calculates the cross-sections at these wavelengths by interpolating the Henke + Fennelly data at the solar flux wavelength bins
3. The slide 2 cross-sections are average values at the solar flux wavelengths
4. The cross-section of the first bin is different in the model and the table.
5. Changing the cross-sections only changes the altitude of unit optical depth in the first bin by 1 km.
6. From the Henke + Fennelly data, and the model value is more accurate than the table value.



NRL Spectra- Binning Procedure

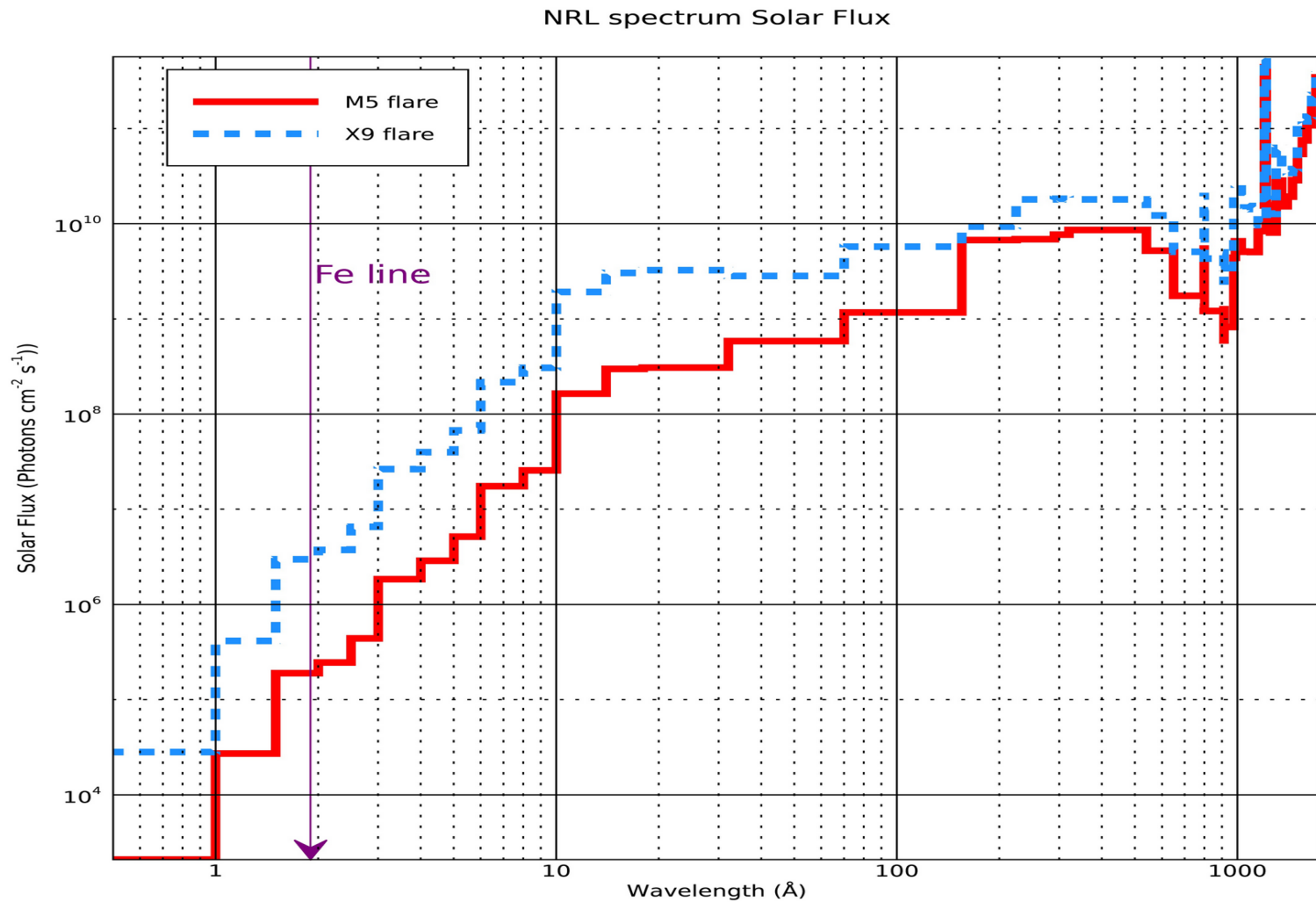
The binning procedure for xray flare ionization parameterization (Done by NRL) as below:

1. "Break up the three shortest wavelength bins of Solomon and Qian into 12 higher resolution bins. Bins to be expanded are the 0.5-4 A, 4-8A and 8-18A"
2. The selection of bins gives roughly 5 km resolution between 60-100 km.

wave_low	wave_low
0.5	1
1	1.5
1.5	2
2	2.5
2.5	3
3	4
4	5
5	6
6	8
8	10
10	14
14	18
18	32
32	70
70	155
155	224
224	290
290	320
320	540

NRL Spectra

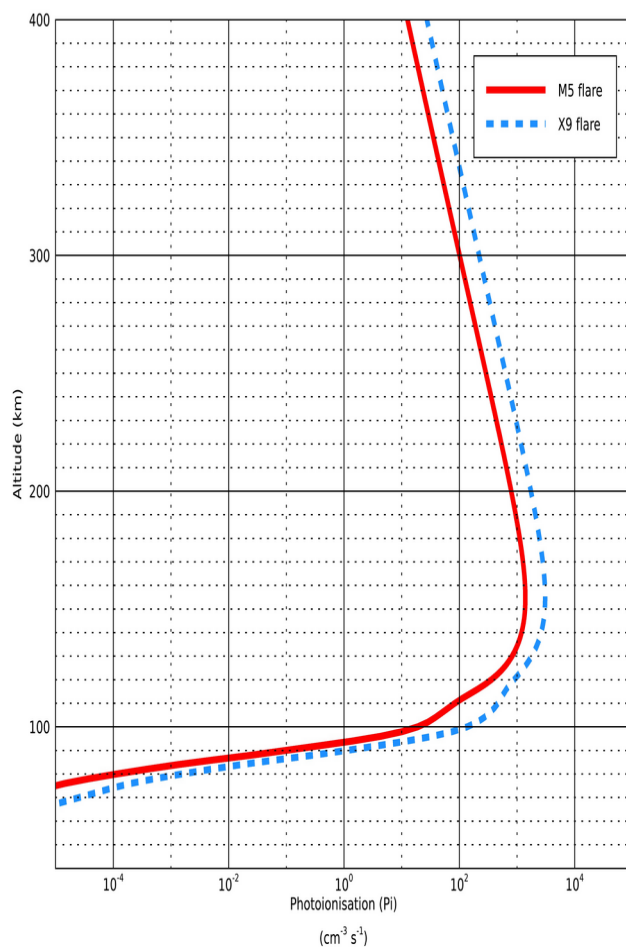
1. This is the NRL spectra for two flares m5 and x9.



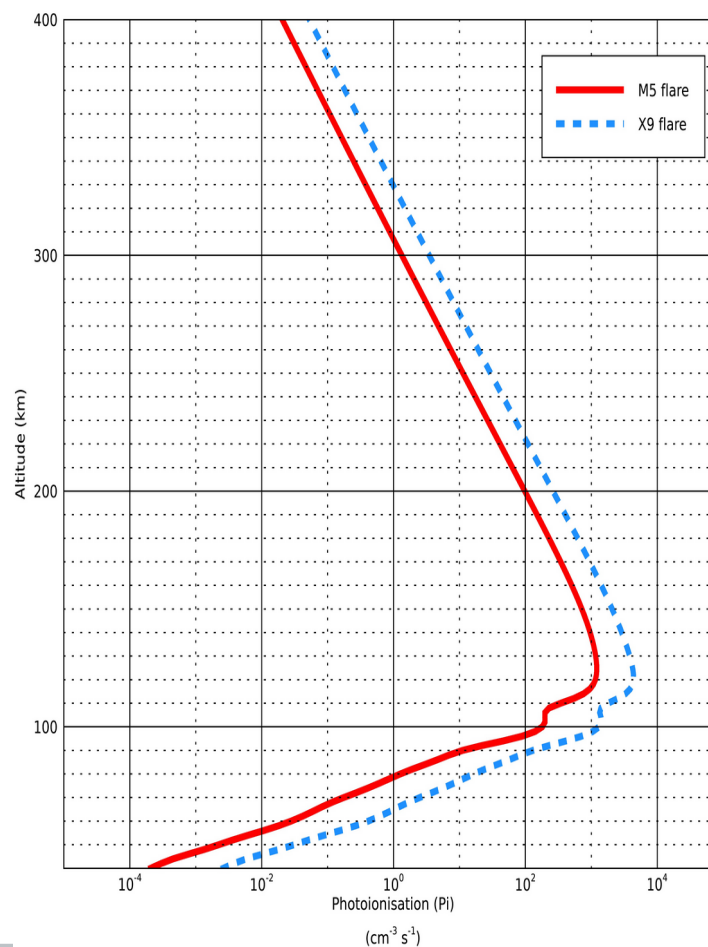
Photoionisation rates for the two spectra

1. If we take the altitude bin in the model to be $\Delta z = 0.5$ to 1 km, the deviation in calculating the altitude of unit optical depth is minimum, so $\Delta z = 1$ km in the model.

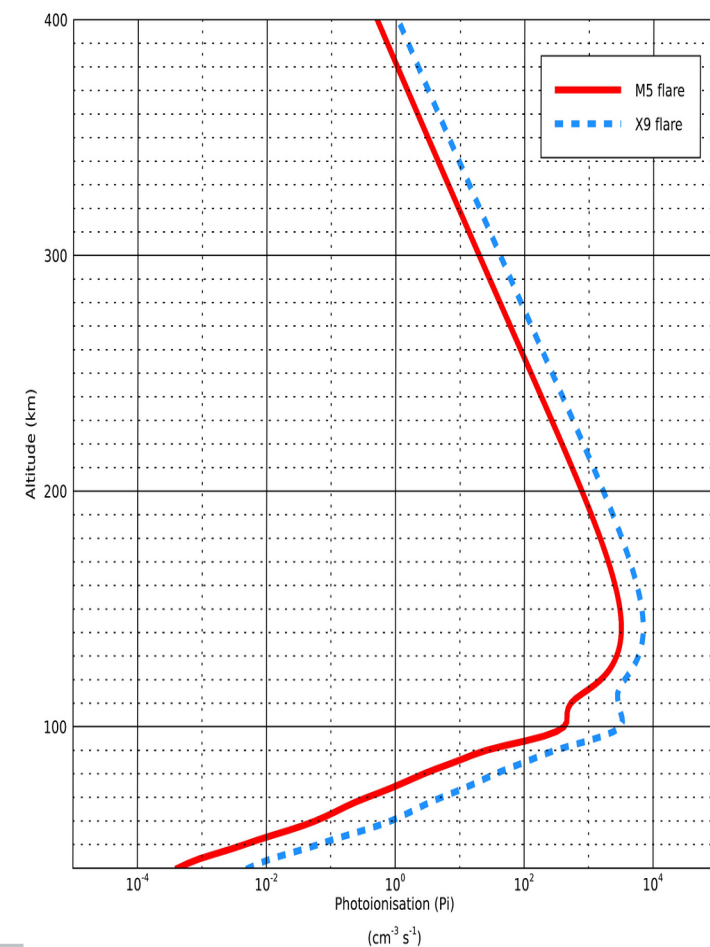
NRL spectrum O Photoionization



NRL spectrum O₂ Photoionization

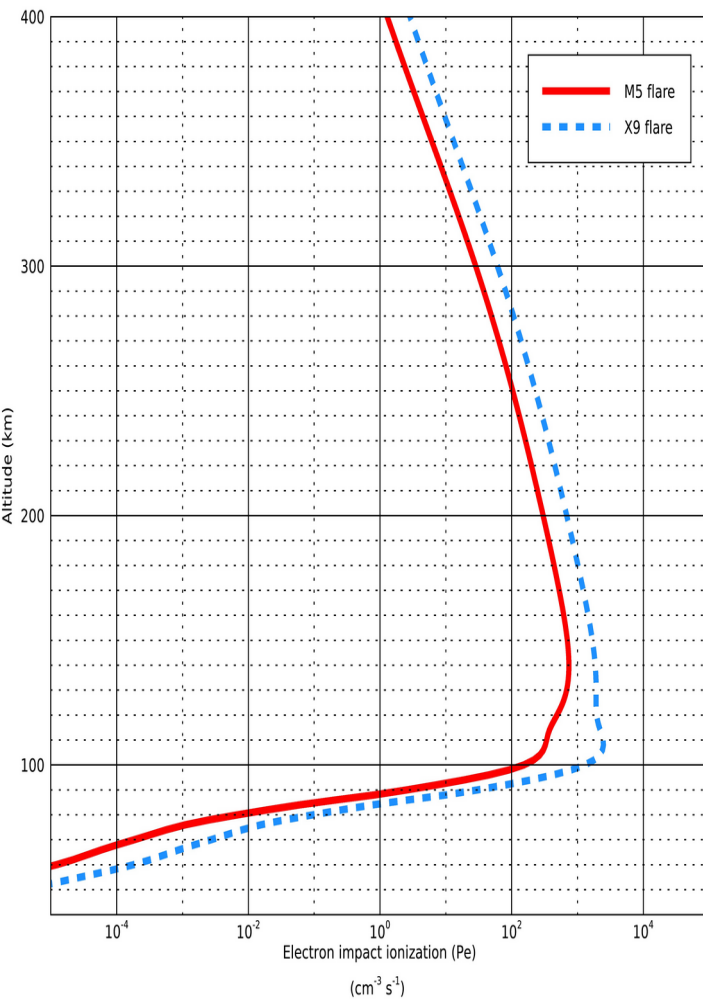


NRL spectrum N₂ Photoionization

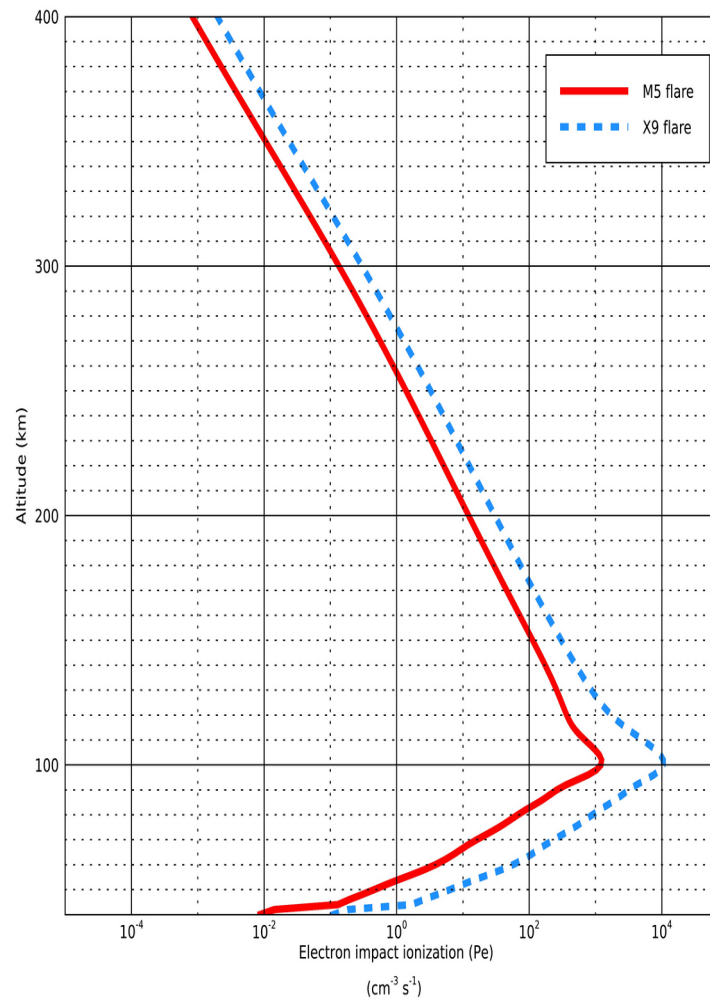


Photoelectron ionisation rates for the two spectra

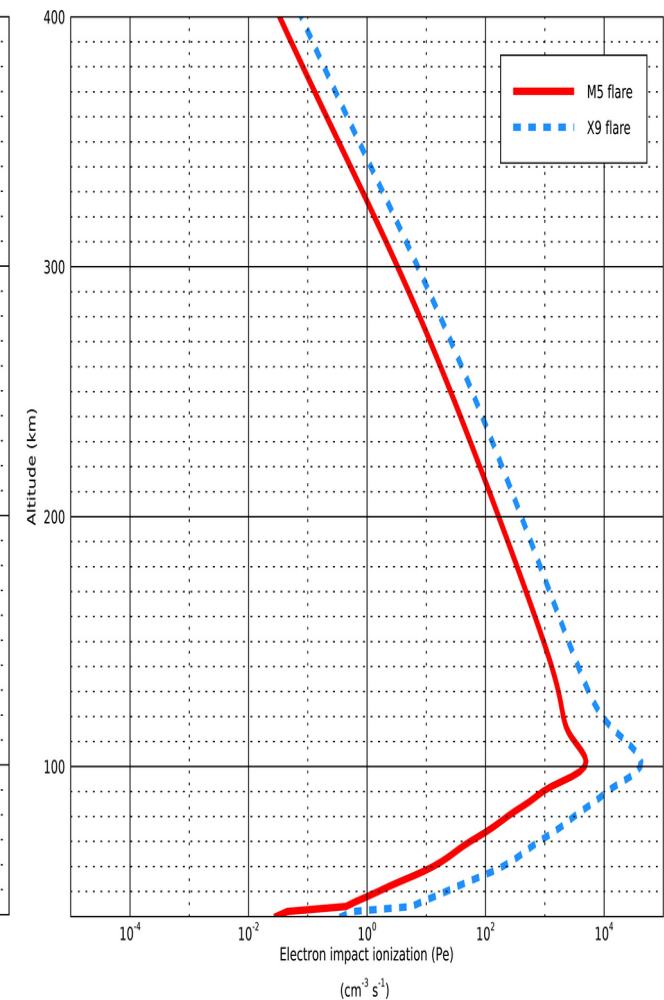
NRL spectrum O Electron impact ionization



NRL spectrum O_2 Electron impact ionization

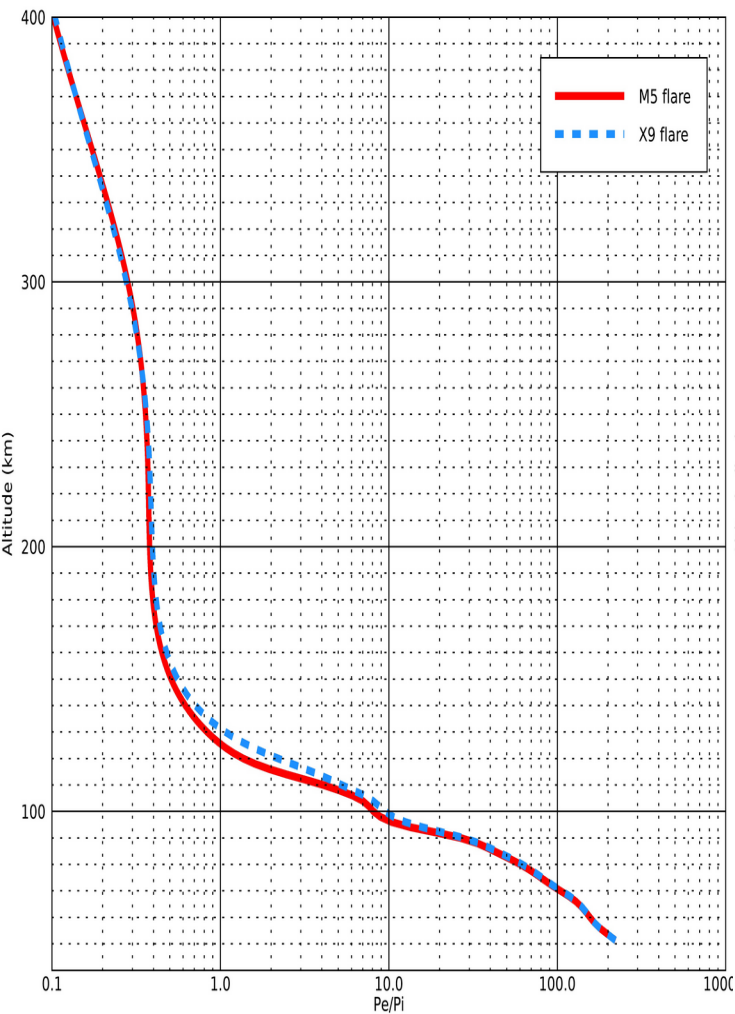


NRL spectrum N_2 Electron impact ionization

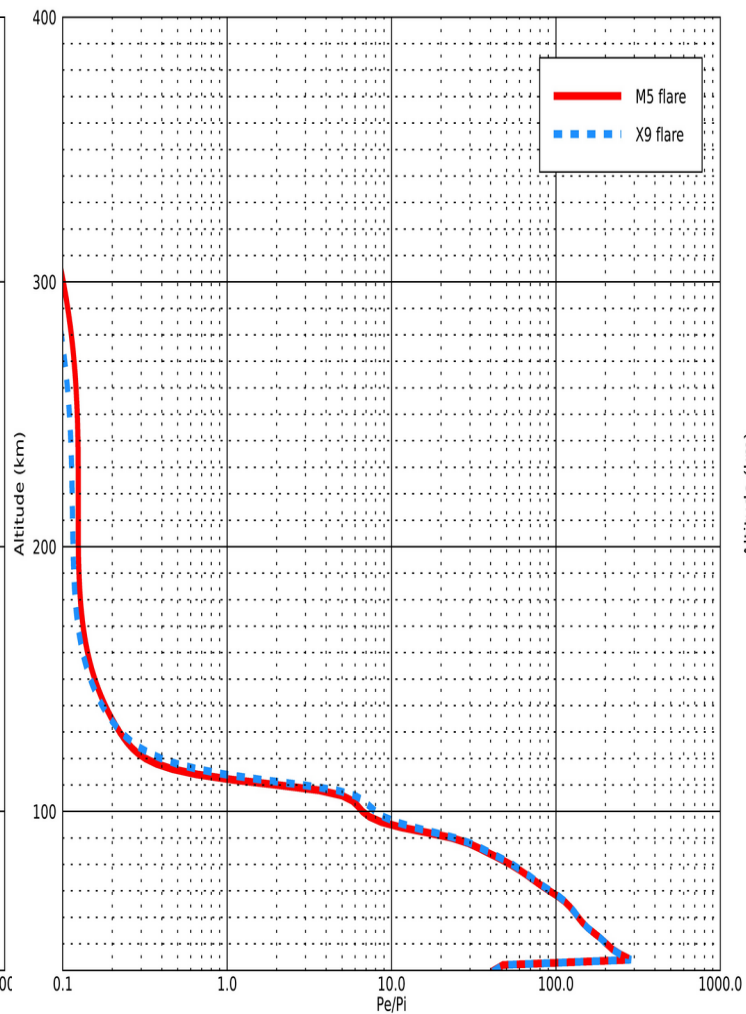


Pe/Pi ratios for the two spectra

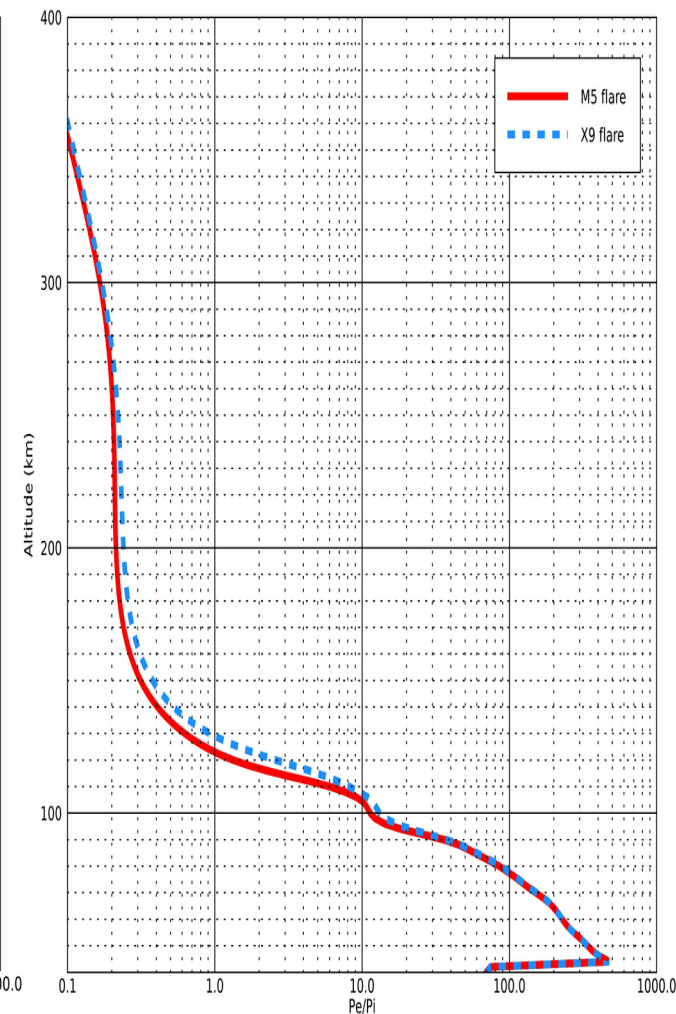
NRL spectrum O Pe/Pi



NRL spectrum O₂ Pe/Pi



NRL spectrum N₂ Pe/Pi



Explanation of plots of slides 6-8

1. These are the 3 plots :
 - i. Photoionisation rates (P_i)
 - ii. Photoelectron ionisation rates (P_e)
 - iii. P_e/P_i ratios
2. Basically, the x9 flare is stronger than the m5 flare, so the P_i and the P_e are larger for the x9, which is expected
3. With increased solar flux from the M5 to X9 flare, there is an increase in photoionisation and photoelectron production.

Results of the Model- M5 flare

O2 data						
Bin #	λ min (Å)	λ max (Å)	Mean λ (Å)	Mean σ_{O2abs} (mega-barns)	Alt of tau~1 (km)	pe/pi
1	0.5	1	0.75	6.21E-05	46	334.877
2	1	1.5	1.25	2.73E-04	58	186.124
3	1.5	2	1.75	8.33E-04	65	130.288
4	2	2.5	2.25	1.88E-03	71	100.69
5	2.5	3	2.75	3.66E-03	75	81.527
6	3	4	3.5	6.95E-03	79	64.223
7	4	5	4.5	1.50E-02	83	48.239
8	5	6	5.5	2.66E-02	87	37.862
9	6	8	7	5.25E-02	90	28.251
10	8	10	9	1.05E-01	94	19.552
11	10	14	12	2.25E-01	99	12.552
12	14	18	16	4.71E-01	103	6.794

N2 data						
Bin #	λ min (Å)	λ max (Å)	Mean λ (Å)	Mean σ_{N2abs} (mega-barns)	Alt of tau~1 (km)	pe/pi
1	0.5	1	0.75	3.38E-05	46	556.789
2	1	1.5	1.25	1.49E-04	58	311.116
3	1.5	2	1.75	4.55E-04	65	217.68
4	2	2.5	2.25	1.03E-03	71	166.914
5	2.5	3	2.75	2.04E-03	75	134.397
6	3	4	3.5	3.91E-03	79	105.002
7	4	5	4.5	8.59E-03	83	77.558
8	5	6	5.5	1.56E-02	87	59.911
9	6	8	7	3.15E-02	90	43.828
10	8	10	9	6.43E-02	94	29.971
11	10	14	12	1.41E-01	99	19.047
12	14	18	16	3.02E-01	103	10.275

Results of the Model- X9 flare

O2 data							N2 data						
Bin #	λ min (A)	λ max (A)	Mean λ (A)	Mean σ_{O2abs} (mega-barns)	Alt of tau~ 1 (km)	pe/pi	Bin #	λ min (A)	λ max (A)	Mean λ (A)	Mean σ_{N2abs} (mega-barns)	Alt of tau~ 1 (km)	pe/pi
1	0.5	1	0.75	6.21E-05	46	334.877	1	0.5	1	0.75	3.38E-05	46	556.789
2	1	1.5	1.25	2.73E-04	58	186.124	2	1	1.5	1.25	1.49E-04	58	311.116
3	1.5	2	1.75	8.33E-04	65	130.287	3	1.5	2	1.75	4.55E-04	65	217.68
4	2	2.5	2.25	1.88E-03	71	100.69	4	2	2.5	2.25	1.03E-03	71	166.914
5	2.5	3	2.75	3.66E-03	75	81.527	5	2.5	3	2.75	2.04E-03	75	134.397
6	3	4	3.5	6.95E-03	79	64.223	6	3	4	3.5	3.91E-03	79	105.002
7	4	5	4.5	1.50E-02	83	48.239	7	4	5	4.5	8.59E-03	83	77.558
8	5	6	5.5	2.66E-02	87	37.862	8	5	6	5.5	1.56E-02	87	59.911
9	6	8	7	5.25E-02	90	28.251	9	6	8	7	3.15E-02	90	43.828
10	8	10	9	1.05E-01	94	19.552	10	8	10	9	6.43E-02	94	29.971
11	10	14	12	2.25E-01	99	12.552	11	10	14	12	1.41E-01	99	19.047
12	14	18	16	4.71E-01	103	6.794	12	14	18	16	3.02E-01	103	10.275

Comparisons of the model data with calculated N₂ results

Calculated	Results					N2 data	Model	Results				Altitude Difference (km)
Bin #	λ min (Å)	λ max (Å)	Mean λ (Å)	Mean σ_{N2abs} (mega-barns)	Alt of tau=1 (km)	Bin #	λ min (Å)	λ max (Å)	Mean λ (Å)	Mean σ_{N2abs} (mega-barns)	Alt of tau~1 (km)	
1	0.5	1	0.75	2.48e-5	43	1	0.5	1	0.75	3.38E-05	46	3
2	1	1.5	1.25	1.47e-4	55.5	2	1	1.5	1.25	1.49E-04	58	2.5
3	1.5	2	1.75	4.57e-4	63.5	3	1.5	2	1.75	4.55E-04	65	1.5
4	2	2.5	2.25	1.02e-3	69.1	4	2	2.5	2.25	1.03E-03	71	1.9
5	2.5	3	2.75	1.9e-3	73.3	5	2.5	3	2.75	2.04E-03	75	1.5
6	3	4	3.5	4.0e-3	78.7	6	3	4	3.5	3.91E-03	79	0.3
7	4	5	4.5	8.55e-3	84	7	4	5	4.5	8.59E-03	83	1
8	5	6	5.5	1.55e-2	88.1	8	5	6	5.5	1.56E-02	87	1.1
9	6	8	7	3.12e-2	93	9	6	8	7	3.15E-02	90	3
10	8	10	9	6.32e-2	98	10	8	10	9	6.43E-02	94	4
11	10	14	12	0.14	103.5	11	10	14	12	1.41E-01	99	4.5
12	14	18	16	0.30	109	12	14	18	16	3.02E-01	103	6

Conclusion And Assumptions Made

1. The MSIS value for $n_0 = 1.9 \text{ E19 cm}^3$, however, we have assumed $n_0 = 2.7 \text{ E19 cm}^3$
2. Scale height $H = 7 \text{ km}$ in calculation of table in slide 2, however, in the model scale height changes for the altitudes of unit optical depth.
3. The difference in altitude of unit optical depth between the model data and the calculated data is due to the difference in the assumptions made in its calculations and the different values calculated by the model.
4. An altitude binning of $\Delta z = 0.5$ to 1 km is good for getting the correct altitude of optical depth.
5. The N_2 cross-section of the first bin in the model is significantly different than that given in the table of slide 2, which causes a difference of about 1 km in the altitude of unit optical depth calculation.
6. In the calculations, it is assumed that the all the atmosphere is N_2 and also the solar zenith angle is zero degree. The model has a zenith angle of 1 degree, which does not cause any appreciable changes in the altitudes.
7. The p_e/p_i ratios for N_2 and O_2 for both the M5 and X9 flares are also given in the tables in slides 10 and 11. They are equal for both of the flare conditions for each species and bin.
8. Also, the plots of the spectra are added in the beginning. The X9 is the stronger flare and so the photo-ionisation and photo-electron ionisation rates are greater in the X9 flare case.