

CS 32 Week 5

Discussion 1I

Srinath

Outline

- Inheritance
- Polymorphism
- Destruction
- Recursion
- Worksheet 5

Inheritance

Inheritance : What is it?

Inheritance is an **is-a relationship**. We use inheritance only if an is-a relationship is present between the two classes.

Examples?

- A Circle is a Shape
- A Car is a Vehicle
- A Bear is an Animal

Inheritance : Declaration

Say, **Circle** is inherited from **Shape**

Shape is called the **Base** class, **Circle** is called **Derived** class.

Say, **Car** is inherited from **Vehicle**

Base class : **Vehicle**

Derived class : **Car**

Inheritance : Declaration

Say, **Circle** is inherited from **Shape**

Shape is called the **Base** class, **Circle** is called **Derived** class.

Say, **Car** is inherited from **Vehicle**

Base class : **Vehicle**

Derived class : **Car**

CODE

```
class Circle : public Shape {  
    ....  
}  
  
class Car : public Vehicle {  
    ....  
}  
  
Shape* shape = new Shape(..)  
  
Circle* circle = new Circle(..)
```

Inheritance : Construction

CODE

```
class Vehicle {
    public:
        Vehicle(string name){
            m_owner=name;
        }
        string m_vehicleNo;
        string getOwner(){return m_owner;}
    private:
        string m_owner;
}

class Car : public Vehicle {
    public:
        Car(string name, string model);
        string m_company;
        string getModel(){return m_model;}
    private:
        string m_model;
}
```

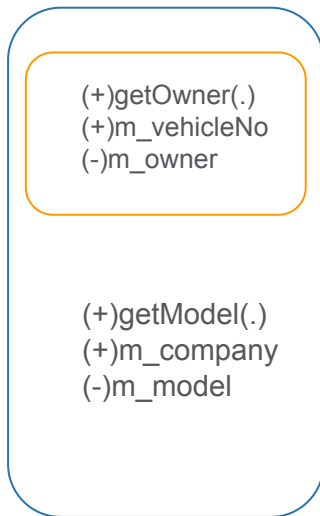
Memory Structure

Inheritance : Construction

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class Car : public Vehicle {  
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Memory Structure

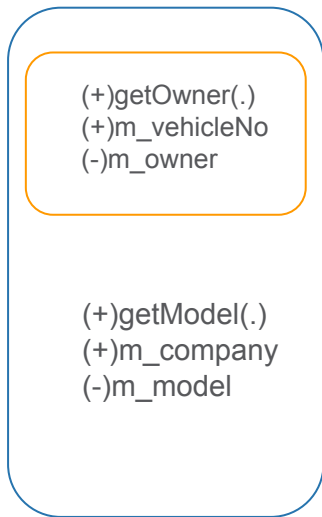


Inheritance : Construction

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class Vehicle {  
    public:  
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        string m_model;  
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Memory Structure



Constructing derived classes?

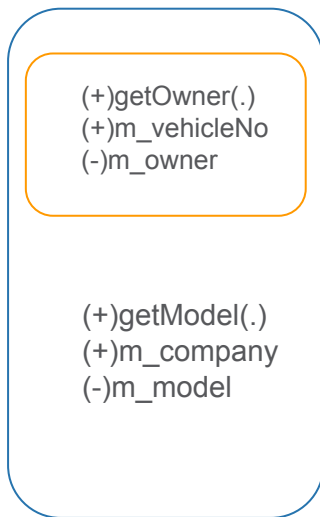
Inheritance : Construction

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        string getOwner(){return m_owner;}
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        string m_owner;
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class Car : public Vehicle {
    public:
        Car(string name, string model);
        string m_company;
        string getModel(){return m_model;}
    private:
        string m_model;
}
```

Memory Structure



Constructing derived classes?

Review: Order of Construction

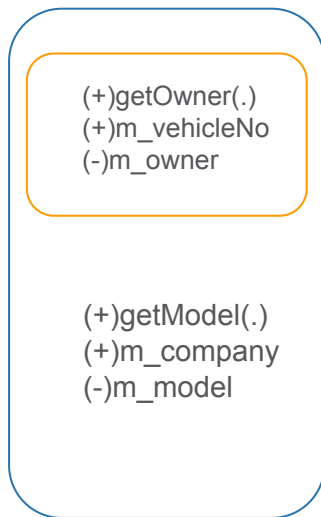
1.?
2. Initialise data members...
3. Parse the body...

Inheritance : Construction

CODE

```
class Vehicle {  
    public:  
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Memory Structure



Constructing derived classes?

Review: Order of Construction

1. Construct the Base part
2. Initialise data members...
3. Parse the body...

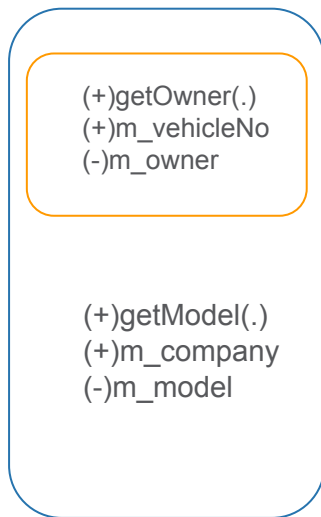
Inheritance : Construction

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}
```

Memory Structure



Constructing derived classes?

Review: Order of Construction

1. Construct the Base part
2. Initialise data members...
3. Parse the body...

Constructor for derived class

```
public Car::Car(string name, string model): m_model(model)
{ }
```

Will the above construction work?

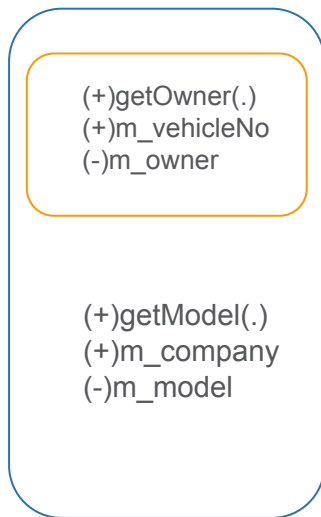
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Memory Structure



Constructing derived classes?

Review: Order of Construction

1. Construct the Base part
2. Initialise data members...
3. Parse the body...

Constructor for derived class

```
public Car::Car(string name, string model): m_model(model)
{ }
```

Will the above construction work?

- No, as `Vehicle` do not have a default constructor.

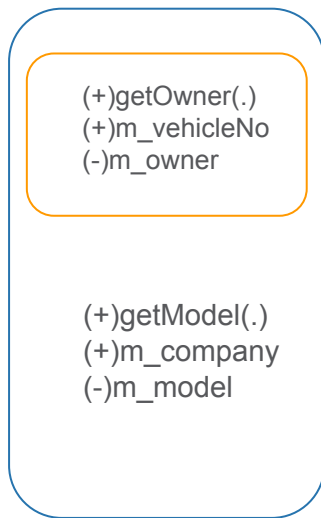
Inheritance : Construction

CODE

```
class Vehicle {
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Memory Structure



Constructing derived classes?

Review: Order of Construction

1. Construct the Base part
2. Initialise data members...
3. Parse the body...

Constructor for derived class

```
public Car::Car(string name, string model): m_model(model)
{ }
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Will the above construction work?

- No, as Vehicle do not have a default constructor.

Correct construction

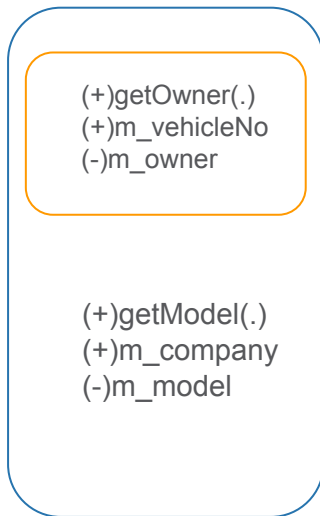
```
public Car::Car(string name, string model): Vehicle(name),
m_model(model) { }
```

Inheritance : Construction

CODE

```
class Vehicle {  
    public:  
        Vehicle(string name){  
            m_owner=name;  
        }  
        string m_vehicleNo;  
        string getOwner(){return m_owner;}  
    private:  
        string m_owner;  
}  
  
class Car : public Vehicle {  
    public:  
        Car(string name, string model);  
        string m_company;  
        string getModel(){return m_model;}  
    private:  
        string m_model;  
}
```

Memory Structure



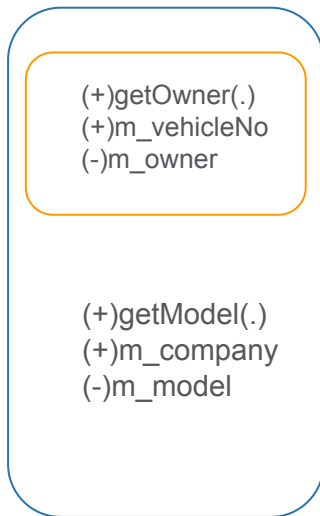
Access

Inheritance : Construction

CODE

```
class Vehicle {  
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            m_owner=name;  
        }  
        string m_vehicleNo;  
        string getOwner(){return m_owner;}  
    private:  
        string m_owner;  
}  
  
class Car : public Vehicle {  
    public:  
        Car(string name, string model);  
        string m_company;  
        string getModel(){return m_model;}  
    private:  
        string m_model;  
}
```

Memory Structure



Access

Can Car directly access m_owner?

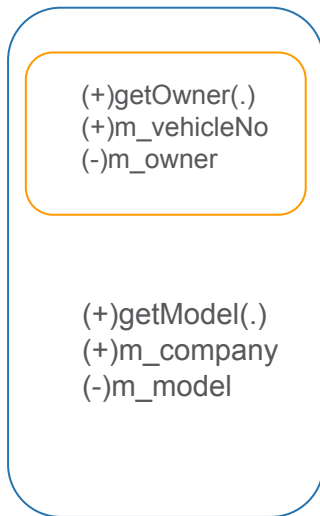
Inheritance : Construction

CODE

```
class Vehicle {
public:
    Vehicle(string name){
        m_owner=name;
    }
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    string getOwner(){return m_owner;}
private:
    string m_owner;
}

class Car : public Vehicle {
public:
    Car(string name, string model);
    string m_company;
    string getModel(){return m_model;}
private:
    string m_model;
}
```

Memory Structure



Access

Can `Car` directly access `m_owner`?

No.

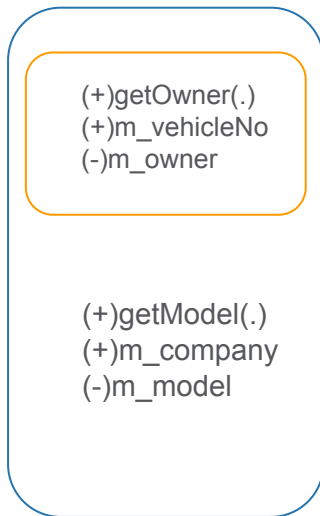
Can `Car` directly access `m_vehicleNo`?

Inheritance : Construction

CODE

```
class Vehicle {  
    public:  
        Vehicle(string name){  
            m_owner=name;  
        }  
        string m_vehicleNo;  
        string getOwner(){return m_owner;}  
    private:  
        string m_owner;  
}  
  
class Car : public Vehicle {  
    public:  
        Car(string name, string model);  
        string m_company;  
        string getModel(){return m_model;}  
    private:  
        string m_model;  
}
```

Memory Structure



Access

Can `Car` directly access `m_owner`?

No.

Can `Car` directly access `m_vehicleNo`?

Yes.

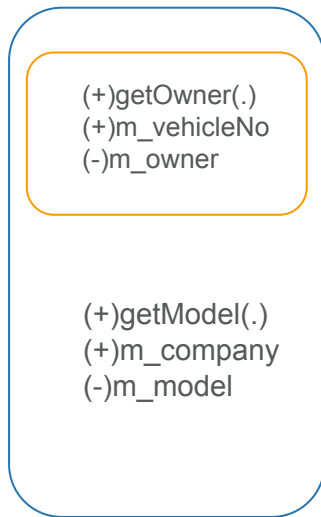
Inheritance : Construction

CODE

```
class Vehicle {
    public:
        Vehicle(string name){
            m_owner=name;
        }
        string m_vehicleNo;
        string getOwner(){return m_owner;}
    private:
        string m_owner;
}

class Car : public Vehicle {
    public:
        Car(string name, string model);
        string m_company;
        string getModel(){return m_model;}
    private:
        string m_model;
}
```

Memory Structure



Access

Can Car directly access m_owner?

No.

Can Car directly access m_vehicleNo?

Yes.

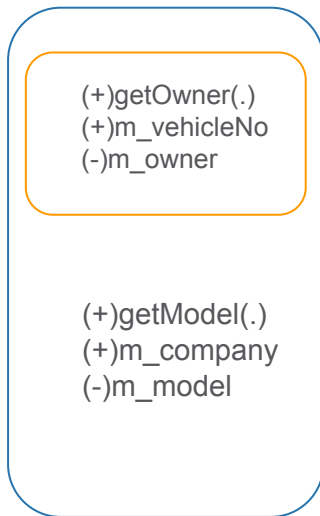
Derived class can only access **public member variables** of its base class, but **not private member variables** of its base class.

Inheritance : Construction

CODE

```
class Vehicle {  
    public:  
        Vehicle(string name){  
            m_owner=name;  
        }  
        string m_vehicleNo;  
        string getOwner(){return m_owner;}  
    private:  
        string m_owner;  
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class Car : public Vehicle {  
    public:  
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```

Memory Structure



Assignment

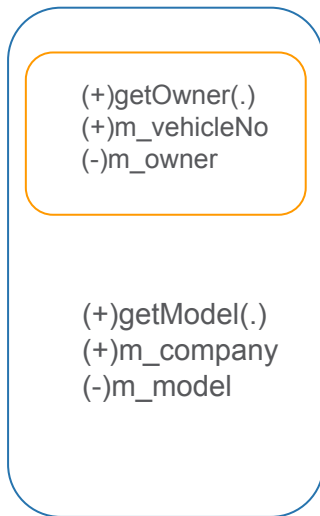
Car * car = new Vehicle(..), is this valid?

Inheritance : Construction

CODE

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class Vehicle {  
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        }  
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    private:  
        string m_owner;  
}  
  
class Car : public Vehicle {  
    public:  
        Car(string name, string model);  
        string m_company;  
        string getModel(){return m_model;}  
    private:  
        string m_model;  
}
```

Memory Structure



Assignment

Car * car = new Vehicle(..), is this valid?

No.

Vehicle * v = new Car(..), is this valid?

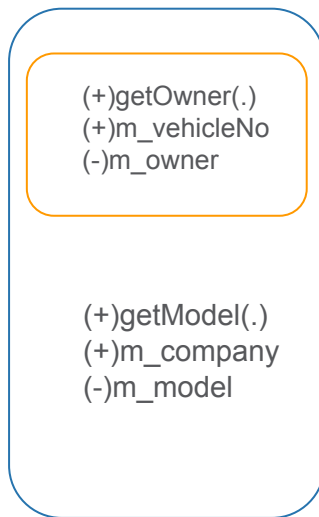
Inheritance : Construction

CODE

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Memory Structure



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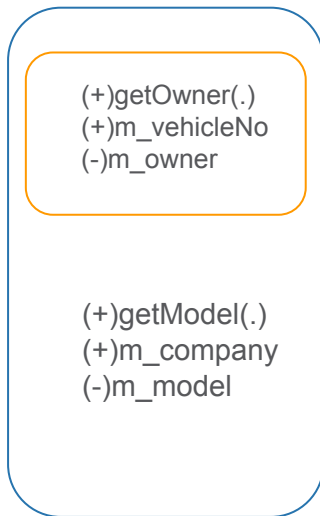
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class Car : public Vehicle {
public:
    Car(string name, string model);
    string m_company;
    string getModel(){return m_model;}
private:
    string m_model;
}
```

Memory Structure



Assignment

Car * car = new Vehicle(..), is this valid?

No.

Vehicle * v = new Car(..), is this valid?

Yes.

You can assign a **derived class pointer/reference** to the **base class pointer/reference**. The conversion is automatic.

In this case, v points to Vehicle part of the Car class(ref memory structure.)

Inheritance : Overriding

You can **override** a member function of your **base** class in the **derived** class

Inheritance : Overriding

You can **override** a member function of your **base** class in the **derived** class

```
Vehicle* vehicle = new Vehicle("bruin");  
Car* car = new Car("bruin", "ferrari");
```

```
vehicle->move();  
car->move();
```

What is the output?

CODE

```
class Vehicle {  
    public:  
        Vehicle(string name){  
            m_owner=name;  
        }  
        string m_vehicleNo;  
        string getOwner(){return m_owner;}  
        void move(){  
            cout<< "Vehicle Moved" <<endl;  
        }  
    private:  
        string m_owner;  
}  
  
class Car : public Vehicle {  
    public:  
        Car(string name, string model);  
        string m_company;  
        string getModel(){return m_model;}  
        void move(){  
            cout<< "Car Moved" <<endl;  
        }  
    private:  
        string m_model;  
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```

Inheritance : Overriding

You can **override** a member function of your **base** class in the **derived** class

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Vehicle* vehicle = new Vehicle("bruin");  
Car* car = new Car("bruin", "ferrari");
```

```
vehicle->move();  
car->move();
```

What is the output?

```
Vehicle Moved  
Car Moved
```

CODE

```
class Vehicle {  
    public:  
        Vehicle(string name){  
            m_owner=name;  
        }  
        string m_vehicleNo;  
        string getOwner(){return m_owner;}  
        void move(){  
            cout<< "Vehicle Moved" <<endl;  
        }  
    private:  
        string m_owner;  
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class Car : public Vehicle {  
    public:  
        Car(string name, string model);  
        string m_company;  
        string getModel(){return m_model;}  
        void move(){  
            cout<< "Car Moved" <<endl;  
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    private:  
        string m_model;  
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Inheritance : Overriding

You can **override** a member function of your **base** class in the **derived** class

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```
vehicle->move();  
car->move();
```

What is the output?

```
Vehicle Moved  
Car Moved
```

How to make **car** object print "Vehicle Moved"?

CODE

```
class Vehicle {  
    public:  
        Vehicle(string name){  
            m_owner=name;  
        }  
        string m_vehicleNo;  
        string getOwner(){return m_owner;}  
        void move(){  
            cout<< "Vehicle Moved" <<endl;  
        }  
    private:  
        string m_owner;  
}  
  
class Car : public Vehicle {  
    public:  
        Car(string name, string model);  
        string m_company;  
        string getModel(){return m_model;}  
        void move(){  
            cout<< "Car Moved" <<endl;  
        }  
    private:  
        string m_model;  
}
```

Inheritance : Overriding

You can **override** a member function of your **base** class in the **derived** class

```
Vehicle* vehicle = new Vehicle("bruin");  
Car* car = new Car("bruin", "ferrari");
```

```
vehicle->move();  
car->move();
```

What is the output?

```
Vehicle Moved  
Car Moved
```

How to make **car** object print "Vehicle Moved"?

It means calling **base class's** functions

```
car.Vehicle::move();
```

CODE

```
class Vehicle {  
    public:  
        Vehicle(string name){  
            m_owner=name;  
        }  
        string m_vehicleNo;  
        string getOwner(){return m_owner;}  
        void move(){  
            cout<< "Vehicle Moved" <<endl;  
        }  
    private:  
        string m_owner;  
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class Car : public Vehicle {  
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        Car(string name, string model);  
        string m_company;  
        string getModel(){return m_model;}  
        void move(){  
            cout<< "Car Moved" <<endl;  
        }  
    private:  
        string m_model;  
}
```

Inheritance : Overriding

Let's try creating an array of different Vehicle's

```
Vehicle* vehicles[3]
vehicles[0] = new Car("bruin1", "Ferrari");
vehicles[1] = new Bus("bruin2", "BruinBus");
vehicles[2] = new Truck("bruin3", "Tesla");
```

CODE

```
class Vehicle {
    ...
    void move(){
        cout<< "Vehicle Moved" <<endl;
    }
    ...
}
class Car : public Vehicle {
    ...
    void move(){
        cout<< "Car Moved" <<endl;
    }
    ...
}
class Bus : public Vehicle {
    ...
    void move(){
        cout<< "Bus Moved" <<endl;
    }
    ...
}
class Truck : public Vehicle {
    ...
    void move(){
        cout<< "Truck Moved" <<endl;
    }
    ...
}
```

Inheritance : Overriding

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vehicles[2] = new Truck("bruin3", "Tesla");
```

```
vehicles[0]->move();
vehicles[1]->move();
vehicles[2]->move();
```

What is the output?

CODE

```
class Vehicle {
    ...
    void move(){
        cout<< "Vehicle Moved" <<endl;
    }
    ...
}
class Car : public Vehicle {
    ...
    void move(){
        cout<< "Car Moved" <<endl;
    }
    ...
}
class Bus : public Vehicle {
    ...
    void move(){
        cout<< "Bus Moved" <<endl;
    }
    ...
}
class Truck : public Vehicle {
    ...
    void move(){
        cout<< "Truck Moved" <<endl;
    }
    ...
}
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Inheritance : Overriding

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```

```
vehicles[0]->move();
vehicles[1]->move();
vehicles[2]->move();
```

What is the output?

```
Vehicle Moved
Vehicle Moved
Vehicle Moved
```

Why so?

CODE

```
class Vehicle {
    ...
    void move(){
        cout<< "Vehicle Moved" <<endl;
    }
    ...
}
class Car : public Vehicle {
    ...
    void move(){
        cout<< "Car Moved" <<endl;
    }
    ...
}
class Bus : public Vehicle {
    ...
    void move(){
        cout<< "Bus Moved" <<endl;
    }
    ...
}
class Truck : public Vehicle {
    ...
    void move(){
        cout<< "Truck Moved" <<endl;
    }
    ...
}
```

Inheritance : Overriding

Let's try creating an array of different Vehicle's

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```

```
vehicles[0]->move();
vehicles[1]->move();
vehicles[2]->move();
```

What is the output?

```
Vehicle Moved
Vehicle Moved
Vehicle Moved
```

Why so?

- **because of static binding.**

CODE

```
class Vehicle {
    ...
    void move(){
        cout<< "Vehicle Moved" <<endl;
    }
    ...
}
class Car : public Vehicle {
    ...
    void move(){
        cout<< "Car Moved" <<endl;
    }
    ...
}
class Bus : public Vehicle {
    ...
    void move(){
        cout<< "Bus Moved" <<endl;
    }
    ...
}
class Truck : public Vehicle {
    ...
    void move(){
        cout<< "Truck Moved" <<endl;
    }
    ...
}
```


Inheritance : Overriding

Let's try creating an array of different Vehicle's

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```

```
vehicles[0]->move();
vehicles[1]->move();
vehicles[2]->move();
```

What is the output?

What is the output we need?

```
Vehicle Moved
Vehicle Moved
Vehicle Moved
```

CODE

```
class Vehicle {
    ...
    void move(){
        cout<< "Vehicle Moved" <<endl;
    }
    ...
}
class Car : public Vehicle {
    ...
    void move(){
        cout<< "Car Moved" <<endl;
    }
    ...
}
class Bus : public Vehicle {
    ...
    void move(){
        cout<< "Bus Moved" <<endl;
    }
    ...
}
class Truck : public Vehicle {
    ...
    void move(){
        cout<< "Truck Moved" <<endl;
    }
    ...
}
```

Inheritance : Overriding

Let's try creating an array of different Vehicle's

```
Vehicle* vehicles[3]
vehicles[0] = new Car("bruin1", "Ferrari");
vehicles[1] = new Bus("bruin2", "BruinBus");
vehicles[2] = new Truck("bruin3", "Tesla");
```

```
vehicles[0]->move();
vehicles[1]->move();
vehicles[2]->move();
```

What is the output?

Vehicle Moved
Vehicle Moved
Vehicle Moved

What is the output we need?

Car Moved
Bus Moved
Truck Moved

How to achieve this?

CODE

```
class Vehicle {
    ...
    void move(){
        cout<< "Vehicle Moved" <<endl;
    }
    ...
}
class Car : public Vehicle {
    ...
    void move(){
        cout<< "Car Moved" <<endl;
    }
    ...
}
class Bus : public Vehicle {
    ...
    void move(){
        cout<< "Bus Moved" <<endl;
    }
    ...
}
class Truck : public Vehicle {
    ...
    void move(){
        cout<< "Truck Moved" <<endl;
    }
    ...
}
```

Polymorphism

Polymorphism : What is it?

The same object taking **different forms**.

You can access objects of different types through the **same interface**. Each type can provide its **own independent implementation** of this interface.

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You can access objects of different types through the **same interface**. Each type can provide its **own independent implementation** of this interface.

```
Vehicle* vehicles[3]  
vehicles[0] = new Car("bruin1", "Ferrari");  
vehicles[1] = new Bus("bruin2", "BruinBus");  
vehicles[2] = new Truck("bruin3", "Tesla");
```

The compiler knows that these are pointers of type Vehicle, and calls Vehicle's respective functions instead of derived class's functions.

What we need is a specification of which function to be called at run time

How do we tell the compiler to call the appropriate function at run time(dynamic binding)?

Polymorphism : Virtual functions

Name the function as **virtual**, Rest all will be a **magic**.

```
class Vehicle {
    ...
    virtual void move(){
        cout<< "Vehicle Moved" <<endl;
    }
    ...
}
class Car : public Vehicle {
    ...
    virtual void move(){
        cout<< "Car Moved" <<endl;
    }
    ...
}
class Bus : public Vehicle {
    ...
    virtual void move(){
        cout<< "Bus Moved" <<endl;
    }
    ...
}
class Truck : public Vehicle {
    ...
    virtual void move(){
        cout<< "Truck Moved" <<endl;
    }
    ...
}
```

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```

```
vehicles[0]->move();
vehicles[1]->move();
vehicles[2]->move();
```

What is the output?

```
class Vehicle {
    ...
    virtual void move(){
        cout<< "Vehicle Moved" <<endl;
    }
    ...
}
class Car : public Vehicle {
    ...
    virtual void move(){
        cout<< "Car Moved" <<endl;
    }
    ...
}
class Bus : public Vehicle {
    ...
    virtual void move(){
        cout<< "Bus Moved" <<endl;
    }
    ...
}
class Truck : public Vehicle {
    ...
    virtual void move(){
        cout<< "Truck Moved" <<endl;
    }
    ...
}
```

Polymorphism : Virtual functions

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```
Vehicle* vehicles[3]
vehicles[0] = new Car("bruin1", "Ferrari");
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```

```
vehicles[0]->move();
vehicles[1]->move();
vehicles[2]->move();
```

What is the output?

```
Car Moved
Bus Moved
Truck Moved
```

What if a derived class has no implementation for move()?

```
class Vehicle {
    ...
    virtual void move(){
        cout<< "Vehicle Moved" <<endl;
    }
    ...
}
class Car : public Vehicle {
    ...
    virtual void move(){
        cout<< "Car Moved" <<endl;
    }
    ...
}
class Bus : public Vehicle {
    ...
    virtual void move(){
        cout<< "Bus Moved" <<endl;
    }
    ...
}
class Truck : public Vehicle {
    ...
    virtual void move(){
        cout<< "Truck Moved" <<endl;
    }
    ...
}
```


Polymorphism : Virtual functions

Name the function as **virtual**, Rest all will be a **magic**.

```
Vehicle* vehicles[3]
vehicles[0] = new Car("bruin1", "Ferrari");
vehicles[1] = new Bus("bruin2", "BruinBus");
vehicles[2] = new Truck("bruin3", "Tesla");
```

```
vehicles[0]->move();
vehicles[1]->move();
vehicles[2]->move();
```

What is the output?

```
Car Moved
Bus Moved
Truck Moved
```

What if a derived class has no implementation for move()?

- It uses the base class's implementation.

If specified in base class, No need to specify **virtual** in derived class, they will be virtual by default as inherited from base class.

```
class Vehicle {
    ...
    virtual void move(){
        cout<< "Vehicle Moved" <<endl;
    }
    ...
}
class Car : public Vehicle {
    ...
    virtual void move(){
        cout<< "Car Moved" <<endl;
    }
    ...
}
class Bus : public Vehicle {
    ...
    virtual void move(){
        cout<< "Bus Moved" <<endl;
    }
    ...
}
class Truck : public Vehicle {
    ...
    virtual void move(){
        cout<< "Truck Moved" <<endl;
    }
    ...
}
```

Polymorphism : Virtual functions

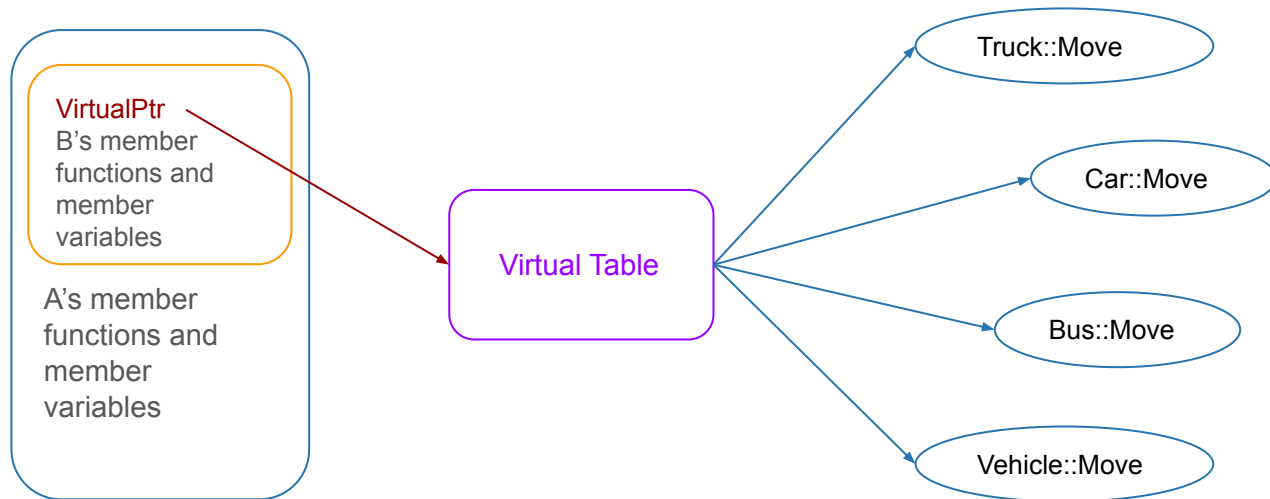
Rest all will be a **magic...** What is this magic?

A is derived from B \rightarrow class A : public B {...}

Polymorphism : Virtual functions

Rest all will be a **magic...** What is this magic?

A is derived from B \rightarrow class A : public B {...}



Each class in which virtual functions are present, has its own virtual ptr pointing to its virtual table.

Polymorphism : Virtual functions

What if we don't want an implementation for move(.) in the **base** class, **Vehicle**?

How can we achieve it?

```
class Vehicle {  
    ...  
    virtual void move(){  
        cout<< "Vehicle Moved" <<endl;  
    }  
    ...  
}  
class Car : public Vehicle {  
    ...  
    virtual void move(){  
        cout<< "Car Moved" <<endl;  
    }  
    ...  
}  
class Bus : public Vehicle {  
    ...  
    virtual void move(){  
        cout<< "Bus Moved" <<endl;  
    }  
    ...  
}  
class Truck : public Vehicle {  
    ...  
    virtual void move(){  
        cout<< "Truck Moved" <<endl;  
    }  
    ...  
}
```

Polymorphism : Pure virtual functions

What if we don't want an implementation for `move(.)` in the **base** class, **Vehicle**?

How can we achieve it?

- **function declaration = 0;**

These are called **Pure Virtual Functions**.

```
class Vehicle {
    ...
    virtual void move() = 0;
    ...
}
class Car : public Vehicle {
    ...
    virtual void move(){
        cout<< "Car Moved" <<endl;
    }
    ...
}
class Bus : public Vehicle {
    ...
    virtual void move(){
        cout<< "Bus Moved" <<endl;
    }
    ...
}
class Truck : public Vehicle {
    ...
    virtual void move(){
        cout<< "Truck Moved" <<endl;
    }
    ...
}
```

Polymorphism : Pure virtual functions

What if we don't want an implementation for `move()` in the **base** class, **Vehicle**?

How can we achieve it?

- **function declaration = 0;**

These are called Pure Virtual Functions.

Sometimes, we do not need implementations where it doesn't make much sense.

Example:

- **Shape's** draw function from class

Base Classes with pure virtual functions are also called **Abstract Base Classes(ABC)**.

```
class Vehicle {
    ...
    virtual void move() = 0;
    ...
}
class Car : public Vehicle {
    ...
    virtual void move(){
        cout<< "Car Moved" <<endl;
    }
    ...
}
class Bus : public Vehicle {
    ...
    virtual void move(){
        cout<< "Bus Moved" <<endl;
    }
    ...
}
class Truck : public Vehicle {
    ...
    virtual void move(){
        cout<< "Truck Moved" <<endl;
    }
    ...
}
```

Polymorphism : Pure virtual functions

What if we don't want an implementation for `move(.)` in the **base** class, **Vehicle**?

How can we achieve it?

- **function declaration = 0;**

These are called Pure Virtual Functions.

Sometimes, we do not need implementations where it doesn't make much sense.

Example:

- **Shape's** draw function from class

Base Classes with pure virtual functions are also called **Abstract Base Classes(ABC)**.

Abstract classes cannot be instantiated

i.e **Vehicle* v1 = new Vehicle();** gives compile error.

```
class Vehicle {
    ...
    virtual void move() = 0;
    ...
}
class Car : public Vehicle {
    ...
    virtual void move(){
        cout<< "Car Moved" <<endl;
    }
    ...
}
class Bus : public Vehicle {
    ...
    virtual void move(){
        cout<< "Bus Moved" <<endl;
    }
    ...
}
class Truck : public Vehicle {
    ...
    virtual void move(){
        cout<< "Truck Moved" <<endl;
    }
    ...
}
```

Destruction

Inheritance : Destruction

Review: Order of Destruction

1. Parse the body...
2. Destroy data members...
3. ...?

Inheritance : Destruction

Review: Order of Destruction

1. Parse the body...
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```
Vehicle* vehicles[3]
vehicles[0] = new Car("bruin1", "Ferrari");
vehicles[1] = new Bus("bruin2", "BruinBus");
vehicles[2] = new Truck("bruin3", "Tesla");
```

```
delete vehicles[0];
delete vehicles[1];
delete vehicles[2];
```

What is the output?

```
class Vehicle {
    ...
    ~Vehicle(){
        cout<< "Vehicle Destroyed" <<endl;
    }
    ...
}
class Car : public Vehicle {
    ...
    ~Car(){
        cout<< "Car Destroyed" <<endl;
    }
    ...
}
class Bus : public Vehicle {
    ...
    ~Bus(){
        cout<< "Bus Destroyed" <<endl;
    }
    ...
}
class Truck : public Vehicle {
    ...
    ~Truck(){
        cout<< "Truck Destroyed" <<endl;
    }
    ...
}
```

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```

```
delete vehicles[0];
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delete vehicles[2];
```

What is the output?

```
Vehicle Destroyed
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Vehicle Destroyed
```

Why so?

```
class Vehicle {
    ...
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        cout<< "Vehicle Destroyed" <<endl;
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}
class Car : public Vehicle {
    ...
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}
class Bus : public Vehicle {
    ...
    ~Bus(){
        cout<< "Bus Destroyed" <<endl;
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class Truck : public Vehicle {
    ...
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delete vehicles[0];
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delete vehicles[2];
```

What is the output?

```
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Vehicle Destroyed
Vehicle Destroyed
```

Why so?

- **because of static binding, even Destructors have to be virtual.**

```
class Vehicle {
    ...
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delete vehicles[0];
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```

What is the output?

```
class Vehicle {
    ...
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        cout<< "Vehicle Destroyed" <<endl;
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    ...
}
class Car : public Vehicle {
    ...
    virtual ~Car(){
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    ...
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    ...
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class Truck : public Vehicle {
    ...
    virtual ~Truck(){
        cout<< "Truck Destroyed" <<endl;
    }
    ...
}
```

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Vehicle Destroyed
Truck Destroyed
Vehicle Destroyed
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    virtual ~Bus(){
        cout<< "Bus Destroyed" <<endl;
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    ...
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    ...
    virtual ~Truck(){
        cout<< "Truck Destroyed" <<endl;
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    ...
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```

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```

```
delete vehicles[0];
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```

What is the output?

```
Car Destroyed
Vehicle Destroyed
Bus Destroyed
Vehicle Destroyed
Truck Destroyed
Vehicle Destroyed
```

if a class is designed to be a
base class, declare a
destructor for it, make it
virtual. (and implement it)

```
class Vehicle {
    ...
    virtual ~Vehicle(){
        cout<< "Vehicle Destroyed" <<endl;
    }
    ...
}
class Car : public Vehicle {
    ...
    virtual ~Car(){
        cout<< "Car Destroyed" <<endl;
    }
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}
class Bus : public Vehicle {
    ...
    virtual ~Bus(){
        cout<< "Bus Destroyed" <<endl;
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    ...
    virtual ~Truck(){
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    }
    ...
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```


Recursion

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You can compare it with mathematical functions

$$f(n) = 2 * f(n-1), f(0)=1$$

Can you guess the closed form for $f(n)$?

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You can compare it with mathematical functions

$$f(n) = 2 * f(n-1), f(0)=1$$

Can you guess the closed form for $f(n)$?

One of the simple, yet powerful concepts in computer science.

Recursion : Guess the next number?

1, 1, 2, 3, 5, 8, 13, 21, 34, ?

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1, 1, 2, 3, 5, 8, 13, 21, 34, ?

It's 55

What's the relation?

Recursion : Guess the next number?

1, 1, 2, 3, 5, 8, 13, 21, 34, ?

It's 55

What's the relation?

$f(n) = f(n-1) + f(n-2)$, $f(0)=1, f(1)=1$

It's called a Fibonacci sequence

Recursion : Reverse a string

Given a string `s`, create string `s_rev` representing reverse of the given string
(Just provide the pseudocode)

Example

`s = "bruin"`

`s_rev = "niurb"`

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Observe that

`s_rev = "niur" + "b" = reverse("ruin") + "b"`

Can you see the recursion??

Recursion : Reverse a string

Given a string `s`, create string `s_rev` representing reverse of the given string
(Just provide the pseudocode)

Example

`s = "bruin"`

`s_rev = "niurb"`

Observe that

`s_rev = "niur" + "b" = reverse("ruin") + "b"`

Can you see the recursion??

```
reverse(string s):
```

```
// base case
```

```
int N = s.length()
```

```
If N == 0 || N == 1:
```

```
    return s;
```

```
return reverse(s[1..N-1]) + "s[0]"
```

Recursion : Merge-Sort

Given two sorted arrays, seq1, seq2 How can we get a single sorted array containing all the elements?

Seq1 : 2, 4, 6, 8, 9, 11, 18, 20, 25

Seq2 : 1, 3, 5, 7, 10, 15, 100

Sorted Array : 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 15, 18, 20, 25, 100

Recursion : Merge-Sort

Given two sorted arrays, seq1, seq2 How can we get a single sorted array containing all the elements?

Seq1 : 2, 4, 6, 8, 9, 11, 18, 20, 25

Seq2 : 1, 3, 5, 7, 10, 15, 100

Sorted Array : 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 15, 18, 20, 25, 100

```
void MERGE(int * A, int p, int q, int r) {  
    int n1 = q-p+1;  
    int n2 = r-q; // not considering q  
    int L[n1+1];  
    int R[n2+1];  
  
    for(int i=0; i<n1; i++){  
        L[i] = A[p+i];  
    }  
    L[n1] = INT_MAX;  
  
    for(int i=0; i<n2; i++){  
        R[i] = A[q+i+1];  
    }  
    R[n2] = INT_MAX;  
  
    int i = 0;  
    int j = 0;  
    for(int k=p; k<=r ; k++){  
        if(L[i] <= R[j]){  
            A[k] = L[i];  
            i = i+1;  
        }else {  
            A[k] = R[j];  
            j = j+1;  
        }  
    }  
    return;  
}
```

The Merge Step

Recursion : Merge-Sort

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Seq1 : 2, 4, 6, 8, 9, 11, 18, 20, 25

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Sorted Array : 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 15, 18, 20, 25, 100

Merge Sort

```
void MERGE_SORT(int * A, int p, int r) {  
    if(p < r){  
        int q = (p+r)/2;  
        MERGE_SORT(A, p, q);  
        MERGE_SORT(A, q+1, r);  
        MERGE(A, p, q, r);  
    }  
}
```

```
void MERGE(int * A, int p, int q, int r) {  
    int n1 = q-p+1;  
    int n2 = r-q; // not considering q  
    int L[n1+1];  
    int R[n2+1];  
  
    for(int i=0; i<n1; i++){  
        L[i] = A[p+i];  
    }  
    L[n1] = INT_MAX;  
  
    for(int i=0; i<n2; i++){  
        R[i] = A[q+i+1];  
    }  
    R[n2] = INT_MAX;  
  
    int i = 0;  
    int j = 0;  
    for(int k=p; k<=r ; k++){  
        if(L[i] <= R[j]){  
            A[k] = L[i];  
            i = i+1;  
        }else {  
            A[k] = R[j];  
            j = j+1;  
        }  
    }  
    return;  
}
```

Recursion : Guidelines

See if the problem can be solved by solving subproblems

Take care of base cases

Often, recursion is leap of faith. You just assume that the subproblems are solved :)

A little more than recursion...

$$A(0, n) = n+1$$

$$A(m+1, 0) = A(m, 1)$$

$$A(m+1, n+1) = A(m, A(m+1, n))$$

A recursion in two variables, calculate $A(4,2)$?

Feel free to use your computers and code it up...

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$$A(0, n) = n+1$$

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A recursion in two variables, calculate $A(4,2)$?

Feel free to use your computers and code it up...

Called as **Ackermann function**. This function grows rapidly

$$A(4,2) = 2^{65536}-3$$

Mere recursion won't help, need to use technique called

Dynamic Programming