CS 32 Week 8 Discussion 11

Srinath

Outline

- Trees
- Binary Search Trees
- Worksheet 8

Trees



Trees:

Kind of data structure that holds hierarchy. Can be thought of as extension to linked lists

ROOT Level 0 Level 1 Parent Node-Level 2 Child Node Level 3 Leaf Node

Terms: parent, child, root, leaf, sibling, height, subtree

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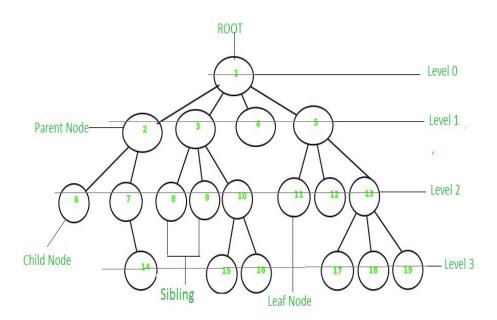
ROOT Level 0 Level 1 Parent Node-Level 2 Child Node Level 3 Leaf Node

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Code??

Trees:

Kind of data structure that holds hierarchy. Can be thought of as extension to linked lists



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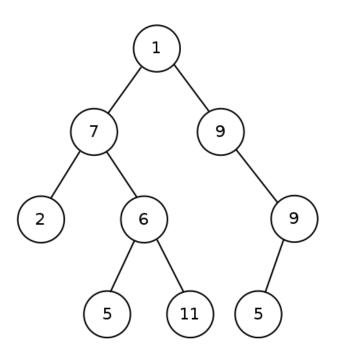
```
Struct Node{
  int val;
  vector<Node*> children;
};

Node* root = new Node();
root→val = 100;

Node* root = NULL; // empty tree
```

Trees: Binary Tree

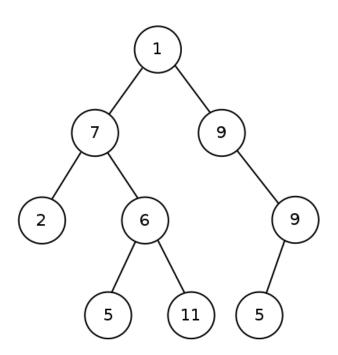
A simplified tree, each node has at most 2 children.



Code??

Trees: Binary Tree

A simplified tree, each node has at most 2 children.



```
Struct Node{
  int val;
  Node* left;
  Node* right;
};

Node* root = new Node();
root—val = 100;

Node* root = NULL; // empty tree
```

```
Insert a new value (n) at given Node* p
void insert(Node* p, int n){
}
```

Insert a new value (n) at given Node* p

```
void insert(Node* p, int n){
    // create a new node
    Node* myNode = new Node();
    myNode→val = n;
    if (p==NULL){ // empty tree
        p = myNode;
    }else{
        (p→children).push_back(myNode);
    }
    return;
}
```

```
Node * root = NULL;
insert(root, 190);
```

Insert a new value (n) at given Node* p

```
void insert(Node* p, int n){
    // create a new node
    Node* myNode = new Node();
    myNode→val = n;
    if (p==NULL){ // empty tree
        p = myNode;
    }else{
        (p→children).push_back(myNode);
    }
    return;
}
```

```
Node * root = NULL; insert(root, 190);
```

Are we missing anything?

Insert a new value (n) at given Node* p

```
void insert(Node* & p, int n){
    // create a new node
    Node* myNode = new Node();
    myNode→val = n;
    if (p==NULL){ // empty tree
        p = myNode;
    }else{
        (p→children).push_back(myNode);
    }
    return;
}
```

```
Node * root = NULL; insert(root, 190);
```

Are we missing anything?

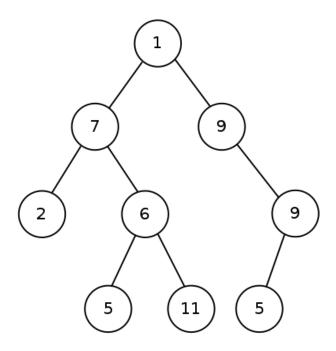
 Yes, 'root' won't be modified as we are passing by value

To go through all nodes of a Tree. **Pre-Order:** parent, then children **Post-Order:** children, then parent

In-Order: left subtree, parent, right subtree (defined for binary

trees)

Pre-Order : Post-Order : In-Order :

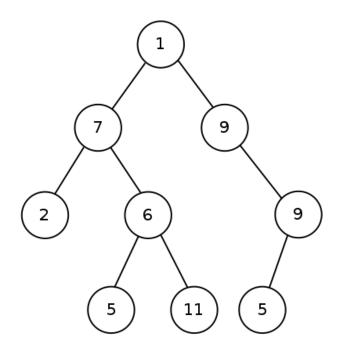


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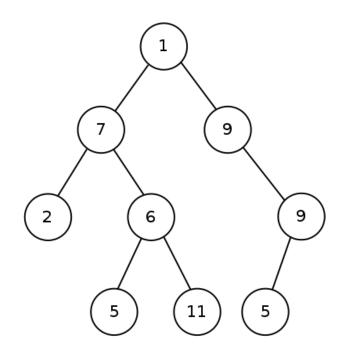
trees)

Pre-Order: 1, 7, 2, 6, 5, 11, 9, 9, 5 **Post-Order:** 2, 5, 11, 6, 7, 5, 9, 9, 1 **In-Order:** 2, 7, 5, 6, 11, 1, 9, 5, 9



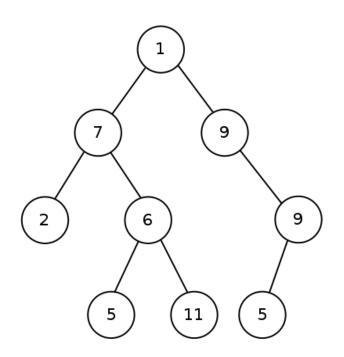
Code for pre-order traversal?

```
void pre-order-traversal(Node* root){
```



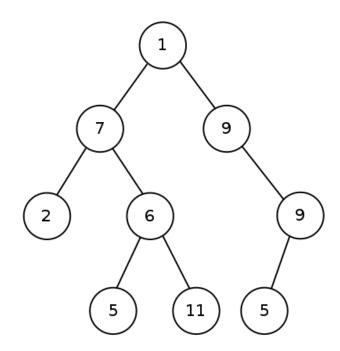
Code for pre-order traversal?

```
void pre-order-traversal(Node* root){
    // base case
    if(root == NULL) return;
    cout << root->val << " "; // curr node
    // then children
    for(int i=0; i<(root→children).size(); i++){
        pre-order-traversal((root→children)[i]);
    }
    return;
}</pre>
```



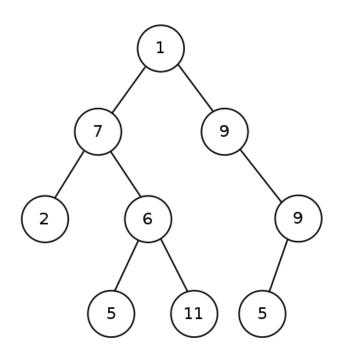
Code for post-order traversal?

```
void post-order-traversal(Node* root){
}
```



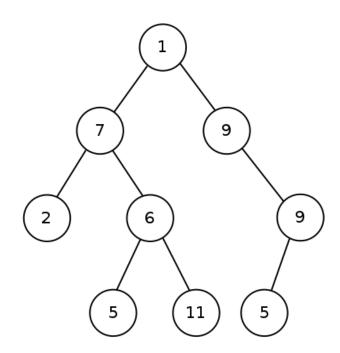
Code for post-order traversal?

```
void post-order-traversal(Node* root){
    // base case
    if(root == NULL) return;
    // first children
    for(int i=0; i<(root→children).size(); i++){
        post-order-traversal((root→children)[i]);
    }
    // curr node
    cout << root->val << " ";
    return;
}</pre>
```



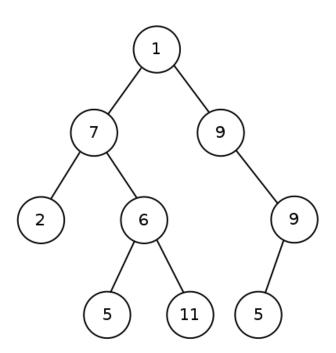
Code for in-order traversal? (for a binary tree)

void in-order-traversal(Node* root){
}



Code for in-order traversal? (for a binary tree)

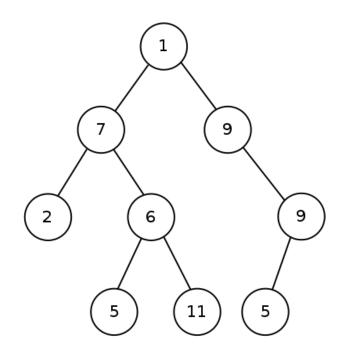
```
void in-order-traversal(Node* root){
    if(root == NULL) return;
    in-order-traversal(root→left);
    cout << root->val << " ";
    in-order-traversal(root→right);
}</pre>
```



Trees: Height

How to find height of a Tree?

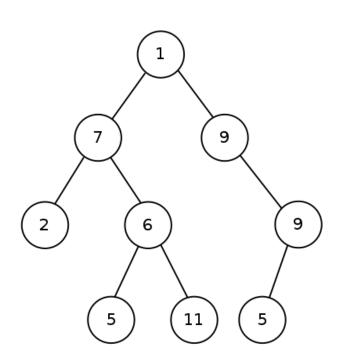
```
int height(Node* root){
}
```



Trees: Height

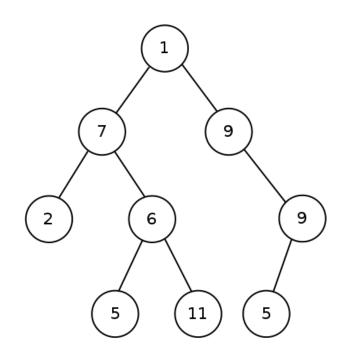
How to find height of a Tree?

```
int height(Node* root){
    if(root == NULL || (root->children).empty()) return 0;
    int maxChildHt = INT_MIN;
    for(int i=0; i<(root→children).size(); i++){
        maxChildHt = max(maxChildHt, height((root→children)[i]));
    }
    return 1+maxChildHt;
}</pre>
```



Trees: Deletion

How to delete a particular value (k) from tree.



Binary Search Trees (BST)

BST: Definition

Organised binary tree such that the following property holds

Given any node **p**, Let **x** be any node in **left-subtree** of **p**, Let **y** be any node in **right-subtree** of **p**,

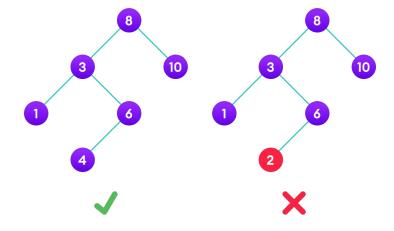
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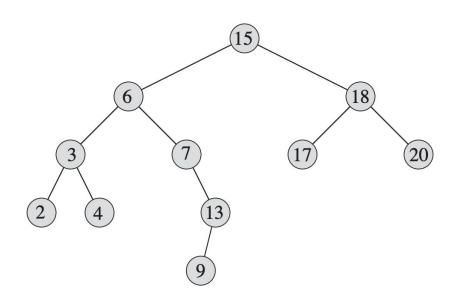
then



Src: https://cdn.programiz.com/sites/tutorial2program/files/bst-vs-not-bst.png

BST: Insertion

Insert a new value (n) in BST rooted at 'root' Insert should be in such a way that BST property is still valid after insertion.

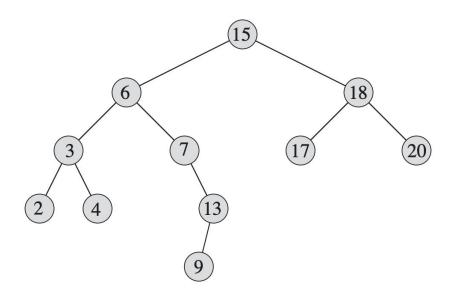


BST: Insertion

Insert a new value (n) in BST rooted at 'root'

Insert should be in such a way that BST property is still valid after insertion.

```
void insert(Node* & root, int n){
      if(root == NULL){
             root = new Node();
             root \rightarrow val = n;
             root→left = NULL; root→right = NULL:
             return;
      if(n < root→val){ // insert left
             insert(root→left, n);
      }else if (n > root→val){ // insert right
                    insert(root→right, n);
             else{ // equal case (already exists)
                    return;
```

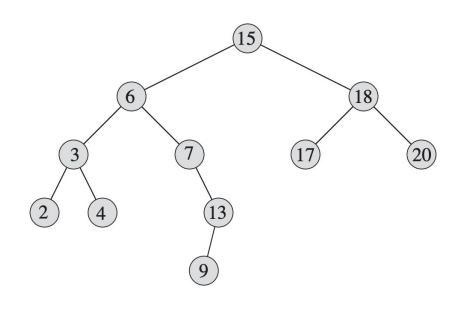


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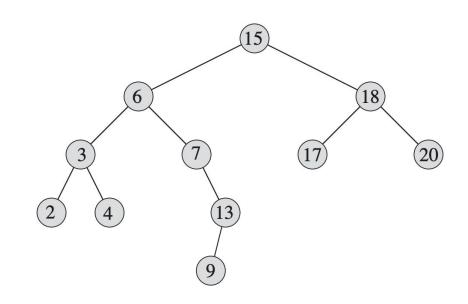
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             root→left = NULL; root→right = NULL:
             return:
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```

Time Complexity: O(log N) - Average case



BST : Lookup | Search

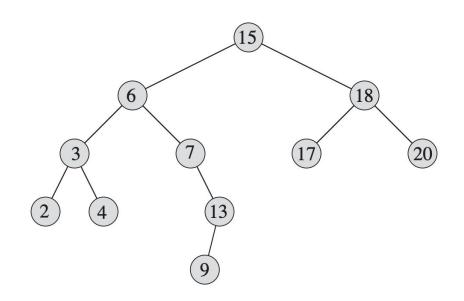
Does a given value (n) exist in BST rooted at 'root'?



BST : Lookup | Search

Does a given value (n) exist in BST rooted at 'root'?

```
bool search(Node* root, int n){
    if(root == NULL) return false;
    if(root→val == n) return true;
    if(n < root→val) return search(root→left, n);
    else return search(root→right, n);
}
```

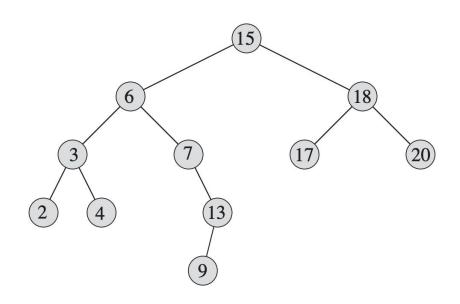


BST : Lookup | Search

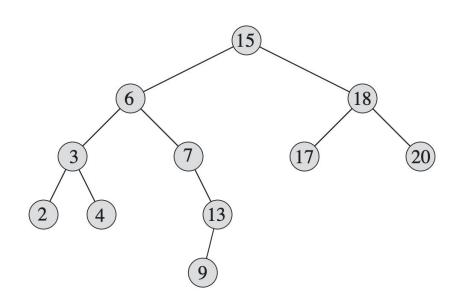
Does a given value (n) exist in BST rooted at 'root'?

Time Complexity: O(log N) - Average case

```
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    if(n < root→val) return search(root→left, n);
    else return search(root→right, n);
}</pre>
```

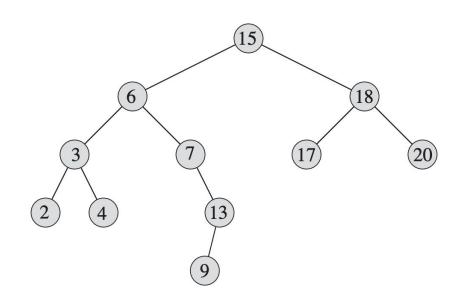


Pre-Order, Post-Order and In-Order Similar to Binary Tree



Pre-Order, Post-Order and In-Order Similar to Binary Tree

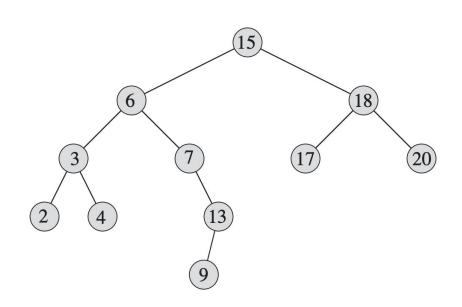
```
void in-order(Node* root){
    if(root == NULL) return;
    in-order(root→left);
    cout << root→val << " ";
    in-order(root→right);
}</pre>
```



Pre-Order, Post-Order and In-Order Similar to Binary Tree

```
void in-order(Node* root){
    if(root == NULL) return;
    in-order(root→left);
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```

Time Complexity : O(N)

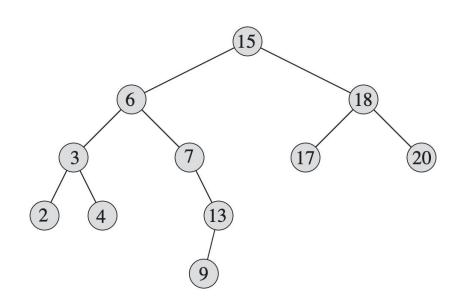


Pre-Order, Post-Order and In-Order Similar to Binary Tree

What does in-order traversal print??

```
void in-order(Node* root){
    if(root == NULL) return;
    in-order(root→left);
    cout << root→val << " ";
    in-order(root→right);
}</pre>
```

Time Complexity : O(N)



BST: Traversal

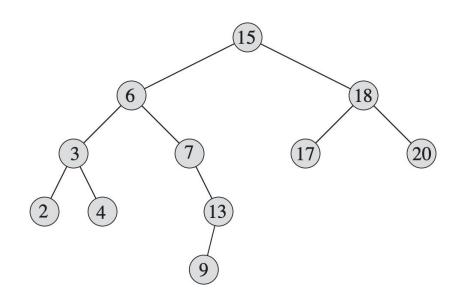
Pre-Order, Post-Order and In-Order Similar to Binary Tree

What does in-order traversal print??

Sorted order of elements

```
void in-order(Node* root){
    if(root == NULL) return;
    in-order(root→left);
    cout << root→val << " ";
    in-order(root→right);
}</pre>
```

Time Complexity : O(N)

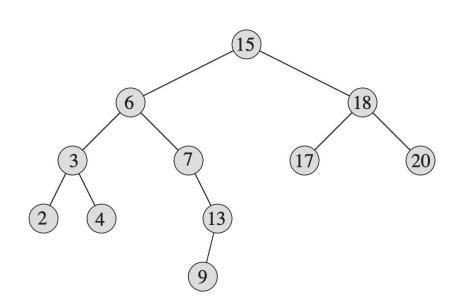


BST: Deletion

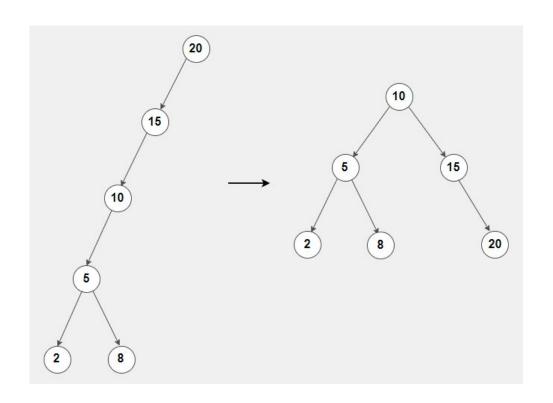
Delete a given value(k) from BST??

```
void delete(Node* root, int k){
}
```

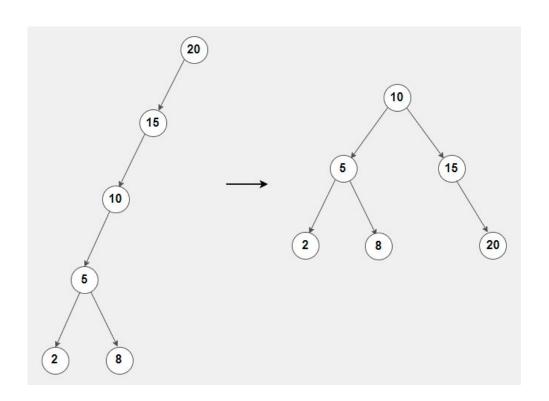
Time Complexity:



BST: Balanced vs Unbalanced



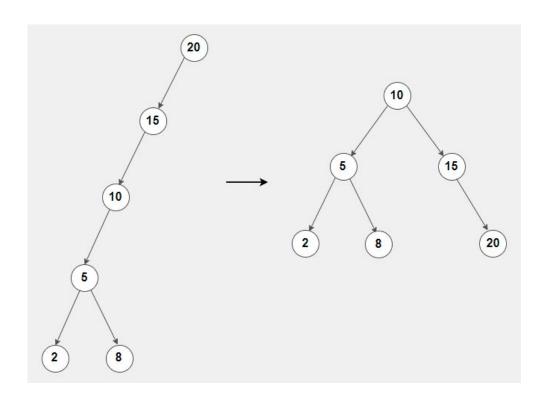
BST: Balanced vs Unbalanced



Balancing schemes

- AVL Tree
- Red-Black Tree
- 2-3 Tree
- etc....

BST: Balanced vs Unbalanced



Balancing schemes

- AVL Tree
- Red-Black Tree
- 2-3 Tree
- etc....

Basic operations on balanced ones has O(log N) complexity.

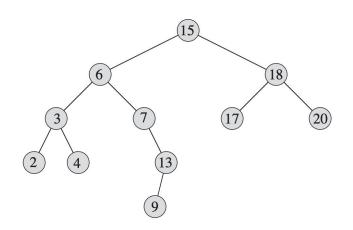
Unbalanced might go to worst case of **O(N)**

Keep in mind the **cost of balancing**.

Find k'th smallest element in a BST??

BST Node is defined as

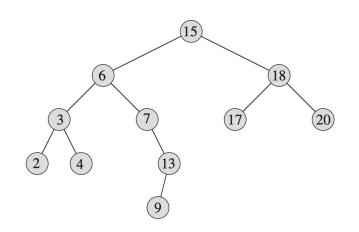
```
struct Node{
    int val;
    Node* left;
    Node* right;
    int m_size; //number of nodes in subtree.
}
```



Find k'th smallest element in a BST??

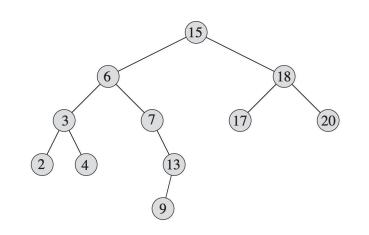
```
BST Node is defined as
```

```
struct Node{
      int val;
      Node* left;
      Node* right;
      int m_size; //number of nodes in subtree.
int Ksmallest(Node* root, int k){
      int I size = 0;
      if(root→left != NULL) I_size = root→left→m_size;
      if(I size==k-1) return root→val;
      if(I size < k-1) return Ksmallest(root→right, k-1- I size);
      else return Ksmallest(root→left, k);
```



```
Find k'th smallest element in a BST??
BST Node is defined as
struct Node{
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```

Time Complexity: O(log N) - Average case



Given N elements, what is time-complexity of converting them to BST structure ??

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O(N log N)

How to find median of an input data stream ??

BST: Usage

STL **Set**, **Multiset** and **Map** use self-balancing BST.

#include <set> // includes both set and multiset

// declaration

set<type> s; // a set do not keep duplicates multiset<type> ms; // a multiset can have duplicates

#include <map> // for map usage

// declaration

map<keyType, valueType> mp;
// stores paired data, (key, value)
// auto sorted by keys
// do not allow duplicate keys

refer www.cplusplus.com for detailed usage

References

BST

https://www.programiz.com/dsa/binary-search-tree

Content in some of the slides is taken from Yiyou Chen.