



A pendulum has 2 forces:

- Centripetal (due to angular motion)
- Gravitational ($g = 9.8 \text{ m/s}^2$)

$$F + mg \sin \theta = 0 \rightarrow F = -mg \sin \theta$$

where $F = m \cdot a$ $\xrightarrow{\text{LINEAR ACCELERATION}}$ $= m \cdot L \cdot \alpha$ $\xrightarrow{\text{ANGULAR ACCELERATION}}$

$$\therefore m \cdot L \cdot \alpha = -mg \sin \theta \rightarrow \boxed{\alpha = -(g \sin \theta) / L}$$

Also: $\alpha = \frac{d^2 \theta}{dt^2}$ (second derivative of θ vs time 't')

and $\omega = \frac{d\theta}{dt}$, where $\omega = \text{ang. velocity}$

$$\text{So, } \alpha = \frac{d\omega}{dt} \rightarrow \boxed{\alpha (\Delta t) = \Delta \omega}$$

$$\text{And } \boxed{\Delta \theta = \omega \cdot \Delta t}$$

NUMERICALLY (For coding purposes):

① WE CHOOSE A SMALL TIME INTERVAL Δt ^{any} $\neq 0$

② CALCULATE $\alpha = \frac{-g \sin \theta}{L}$ at a given θ

③ $\Delta \omega = \alpha \cdot \Delta t$

④ $\omega = \omega + \Delta \omega$

⑤ $\Delta \theta = \omega \cdot (\Delta t)$

⑥ $\theta_{\text{new}} = \theta + \Delta \theta$

⑦ CALCULATE NEW (x,y) POSITION AS FOLLOWS:

$$\text{pos } X = x_{\text{init}} + L \sin \theta_{\text{new}}$$

$$\text{pos } Y = y_{\text{init}} + L \cos \theta_{\text{new}}$$



Repeat indefinitely or for a fixed time 't'

VOILA! pendulum oscillates!