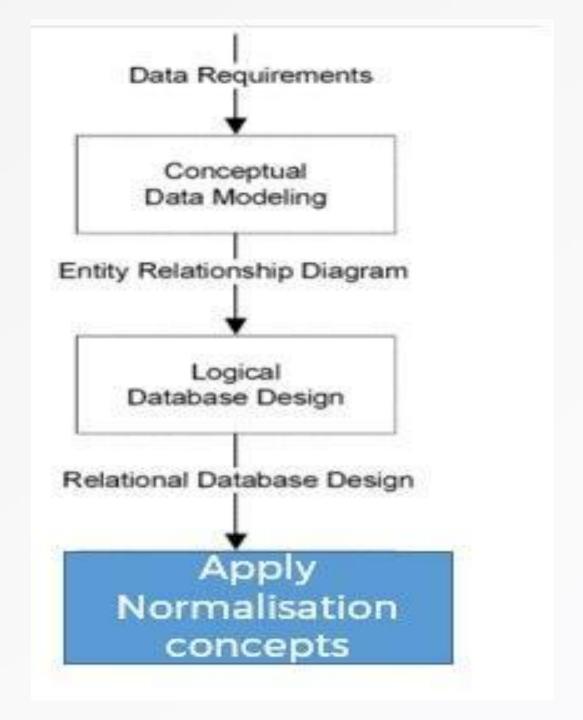
Functional Dependency

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Topics to be covered on

- Functional Dependency
- Types of Functional Dependency
- Armstrong's Axioms
- Closure of Functional Dependency
- Canonical cover of Functional Dependency



Normalization Introduction

- Bottom up approach
- Divides the Larger table into smaller table and links them using relationship
- Reduce the data redundancy
- It overcomes Anomalies
 - Insert
 - Delete
 - Update

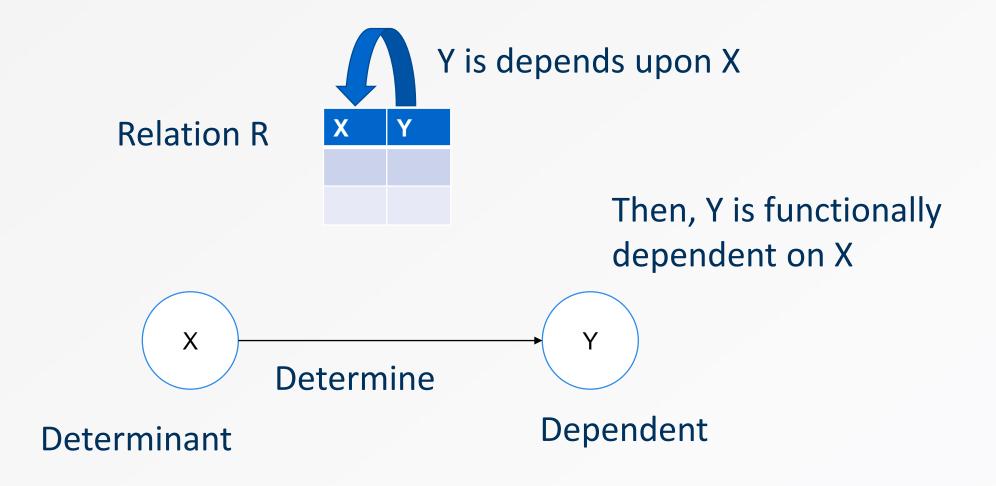
Roll No	Name	Dept	HoD	HoD phone
1	X	Cse	СН	123
2	Υ	Cse	СН	123
3	Z	IT	IH	321
4	A	IT	IH	321

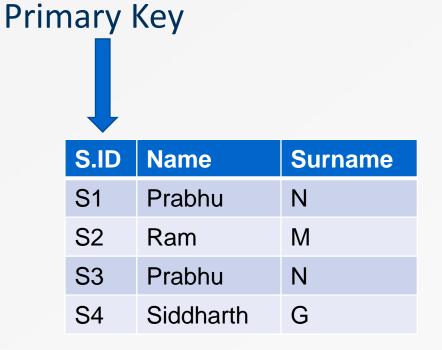
Functional dependency

 The functional dependency is a relationship that exists between two attributes. It typically exists between the primary key and non-key attribute within a table

- Functional Dependency (FD) determines the relation of one attribute to another attribute in a database management system (DBMS) system.
- Functional dependency helps you to maintain the quality of data in the database. A functional dependency is denoted by an arrow →.
- The functional dependency of X on Y is represented by
 - $X \rightarrow Y$.
 - Functional Dependency plays a vital role to find the difference between good and bad database design.

What is functional Dependency

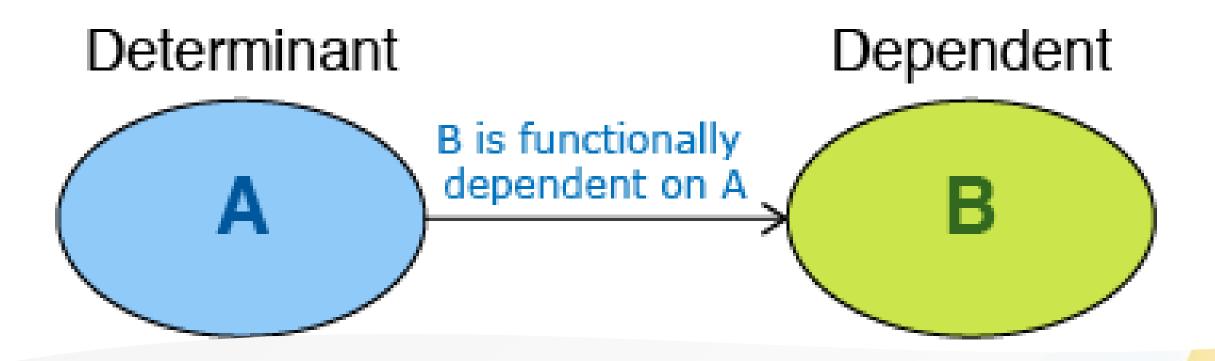




S. ID -> Name (Functionally dependent on ID) S.ID-> Surname

- FD. Table

Hence, Non key attributes that will depends upon key attributes



Functional Dependency

- Just like relationship between entities, attributes within an entity can be dependent on each other. These dependencies are expressed in terms of functional dependency.
- An attribute A is said to functionally determine attribute B if each value of A is associated with only one value of B.
- A is called the **Determinant** while B is called the **Dependent**.

Functional Dependency In DBMS: Examples

• Example-1: Consider a table student_details containing details of some students.

Roll_No	Name	Marks
1.	Anoop	20
2.	Anurag	30
3.	Saurav	40
4.	Rakesh	30
5.	Pritesh	10
6.	Anoop	40

- FD1 : Roll_No → Name
- FD2 : Roll_No → Marks

Example2

Employee_number	Employee Name	Salary	City
1	ANU	10000	BANGALORE
2	AJAY	75000	MYSORE
3	RAHUL	95000	MANGALORE

In this example, if we know the value of Employee number, we can obtain Employee Name, city, salary, etc. By this, we can say that the city, Employee Name, and salary are functionally depended on Employee number.

Key terms

Roll No	Name	Dept_Name	Dept_building
42	Ajith	CSE	AB1
43	Pranesh	IT	AB1
44	Arun	CSE	AB1
45	Arun	MECH	AB2
46	Mano	ECE	AB2
47	Singh	MECH	AB2
48	Rahul	ΙΤ	AB1
49	Mano	ΙΤ	AB1

Valid FD

- roll_no → { name, dept_name, dept_building },→ Here, roll_no can determine values of fields name, dept_name and dept_building, hence a valid Functional dependency
- roll_no → dept_name, Since, roll_no can determine whole set of {name, dept_name, dept_building}, it can determine its subset dept_name also.
- dept_name → dept_building, Dept_name can identify the dept_building accurately, since departments with different dept_name will also have a different dept_building
- More valid functional dependencies: roll_no → name, {roll_no, name} → {dept_name, dept_building}, etc.

Invalid FD

- name → dept_name Students with the same name can have different dept_name, hence this is not a valid functional dependency.
- dept_building → dept_name There can be multiple departments in the same building, For example, in the above table departments MECH and ECE are in the same building AB2, hence dept_building → dept_name is an invalid functional dependency.
- More invalid functional dependencies: name → roll_no, {name, dept_name} → roll_no, dept_building → roll_no, etc.

Functional Dependency Type	Description
Full Functional Dependency	If A and B are attributes of a relation, B is fully functionally dependent on A if it is functionally dependent on A, but not on any subset of A.
Partial Functional Dependency	If A and B are attributes of a relation, B is partially dependent on A if it is dependent on subset of A.
Transitive Functional Dependency	If A, B, and C are attributes of a relation such that if A -> B and B -> C, then C is transitively dependent on A via B.

Types of Functional Dependencies

There are three types of functional dependencies

Fully Functional Dependency

- Example:
- ABC→D
- {D is fully functional dependency on ABC}

• D cannot depends on any subset of ABC

The combination of P.ID, Name, and Order ID will determine the

• BC→D ★ price of the product then the below table is called fully FD

• C→D	*
-------	---



P.ID	Name	Order date	Price
P1	Headphone	01/01/2023	400
P2	Speaker	15/02/2023	500
P1	Speaker	17/03/2023	550
P4	Headphone	01/01/2023	400
P5	Headphone	02/02/2022	450

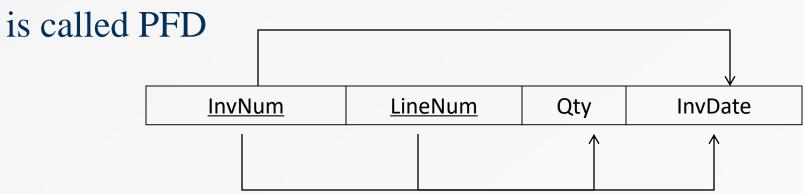
Example:2

- {Emp_num,Proj_num} -> Hour
- Is a full functional dependency. Here, Hour is the working time by an employee in a project

Partial dependency

A **partial dependency** exists when an attribute B is functionally dependent on an attribute A, and A is a component of a multipart candidate key.

A Attribute can be uniquely identified by subset of an attribute



Candidate keys: {InvNum, LineNum}
InvDate is *partially dependent* on {InvNum, LineNum} as
InvNum is a determinant of InvDate and InvNum is part
of a candidate key

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Example:2

- If {Emp_num,Proj_num} → Emp_name
- but also determine Emp_num → Emp_name then Emp_name is partially functionally dependent on {Empl_num,Proj_num}.

Transitive dependency

Transitive dependency

Consider attributes A, B, and C, and where

 $A \rightarrow B$ and $B \rightarrow C$.

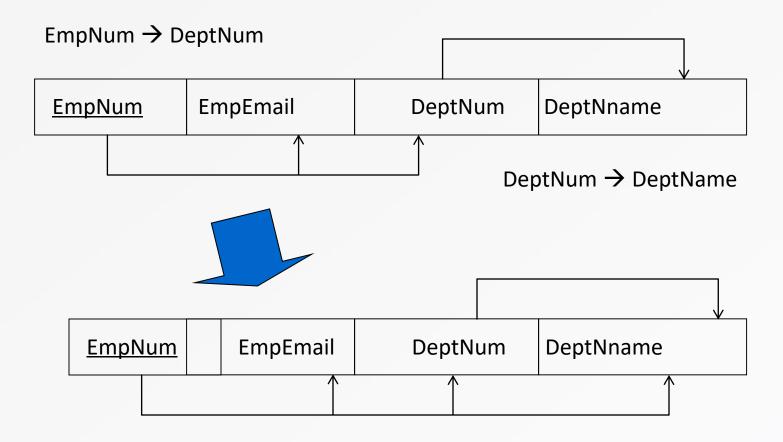
Functional dependencies are transitive, which means that we also

have the functional dependency $A \rightarrow C$

We say that C is transitively dependent on A through B.

91.2914

Transitive dependency



DeptName is *transitively dependent* on EmpNum via DeptNum EmpNum → DeptName

91.2914

Example:2

If {Pulsar} -> model then model -> CC

Example:

Consider a relation which is used to store marks scored by students in various courses. Student(StudentId, Name, ContactNo, Course, Marks, Grade)

STUDENTID	NAME	CONTACT NO	COURSE	MARKS	GRADE
1	James Potter	111-111-1111	OOP	80	B+
1	James Potter	111-111-1111	DBMS	95	A+
2	Ethan McCarty	222-222-3222	ООР	75	В
3	Emily Rayner	333-333-3333	PF	75	В

StudentId	>	Name	Full functional dependency
Studentld, Name	\longrightarrow	ContactNo	Partial functional dependency (StudentId)
StudentId		Course	No functional dependency
Studentld, Course		Marks	Full functional dependency
Marks	$\!$	Grade	Full functional dependency
Studentld, Course	$\!$	Grade	Transitive functional dependency
StudentId		ContactNo	Full functional dependency

Example

- Which functional dependency types is/are present in the following dependencies?
- 1. Empno -> EName, Salary, Deptno, DName
- 2DeptNo -> Dname DName-> E.Name
- 3. Ename-> Salary
- Full functional dependency
- Transitive functional dependency
- Partial functional dependency

Functional Dependency In DBMS: Armstrong's Axioms

Axioms in database management systems was introduced by William W. Armstrong in late 90's and these axioms play a vital role while implementing the concept of functional dependency in DBMS for database normalization. There exists six inferences known a s "Armstrong's Axioms" which are discussed below.

- 1. Reflexive : It means, if set "B" is a subset of "A", then $A \rightarrow B$.
- **2.** Augmentation : It means, if $A \rightarrow B$, then $AC \rightarrow BC$.
- 3. Transitive : It means, if $A \rightarrow B \& B \rightarrow C$, then $A \rightarrow C$.
- **4.** Decomposition : It means, if $A \rightarrow BC$, then $A \rightarrow B \& A \rightarrow C$.
- **5.** Union : It means, if $A \rightarrow B \& A \rightarrow C$, then $A \rightarrow BC$.
- **6.** Pseudo-Transitivity: It means, if $A \rightarrow B$ and $DB \rightarrow C$, then $DA \rightarrow C$.

Closure Of Functional Dependency

- The Closure Of Functional Dependency means the complete set of all possible attributes that can be functionally derived from given functional dependency using the inference rules known as Armstrong's Rules.
- If "F" is a functional dependency then closure of functional dependency can be denoted using "{F}+".

There are three steps to calculate closure of functional dependency

- Step-1: Add the attributes which are present on Left Hand Side in the original functional dependency.
- Step-2: Now, add the attributes present on the Right Hand Side of the functional dependency.
- Step-3: With the help of attributes present on Right Hand Side, check the other attributes that can be derived from the other given functional dependencies. Repeat this process until all the possible attributes which can be derived are added in the closure.

Closure Of Functional Dependency: Examples

- Example-1: Consider the table student_details having (Roll_No, Name,Marks, Location)
 as the attributes and having two functional dependencies.
- FD1 : Roll_No → Name, Marks
- FD2 : Name → Marks, Location

Find the clousure of the given functional dependency:!!

- Step-1: Add attributes present on the LHS of the first functional dependency to the closure.
- {Roll_no}+ = {Roll_No}
- Step-2: Add attributes present on the RHS of the original functional dependency to the closure.
- {Roll_no}+ = {Roll_No, Name, Marks}

Example-1:

- FD1 : Roll_No → Name, Marks
- FD2 : Name → Marks, Location
- Step-3: Add the other possible attributes which can be derived using attributes present on the RHS of the closure.

Therefore, complete closure of Roll_No will be:

- {Roll_no}+ = {Roll_No, Marks, Name, Location}
- Similarly, we can calculate closure for other attributes too i.e "Name".
- {Name}+ = {Name}
- {Name}+ = {Name, Marks, Location}
- {Marks}+ = {Marks}and
- {Location}+ = { Location}

Example-2:

- Consider a relation R(A,B,C,D,E) having below mentioned functional dependencies.
- FD1 : A → BC
- FD2: $C \rightarrow B$
- FD3 : D → E
- FD4 : E → D
- Now, we need to calculate the closure of attributes of the relation R. The closures will be:
- $\{A\}^+ = \{A, B, C\}$
- $\{B\}^+ = \{B\}$
- $\{C\}^+ = \{B, C\}$
- $\{D\}^+ = \{D, E\}$
- {E}⁺ = {E,D}

Example-3:

Consider a relation R(A,B,C,D,E,F)

F:

- E->A,
- E->D,
- A->C,
- A->D,
- AE->F,
- AG->K.

The closure of E or E+ is as follows -

```
• E+ = E
   =EA {for E->A add A}

    =EAD {for E->D add D}

   =EADC {for A->C add C}
   =EADC {for A->D D already added}
   =EADCF {for AE->F add F}
   =EADCF {for AG->K don't add k AG ⊄ E+)
```

Example-4:

Consider a relation R(A,B,C,D,E,F)

- F:
- E->A,
- E->D,
- A->C,
- A->D,
- AE->F,
- AG->K.
- Find the closure of A or A+

Example-5:

- We are given the relation R(A, B, C, D, E). This means that the table R has five columns: A, B, C, D, and E. We are also given the set of functional dependencies:
- {A->B,
- B->C,
- C->D,
- D->E}.

What is {A}+?

Example-6:

- Let's look at another example. We are given R(A, B, C, D, E, F). The functional dependencies are
- {AB->C, BC->AD, D->E, CF->B}.

• What is {A, B}+?

Example-7:

• Let the relation R(A,B,C,D,E,F)

• F: B->C, BC->AD, D->E, CF->B.

Find the closure of B.

Example-8:

- Consider a relation R (A, B, C, D, E, F, G) with the functional dependencies-
- Find the closure of A?
- A → BC
- BC \rightarrow DE
- D → F
- $CF \rightarrow G$

Closure of attribute A-

```
• A+ = \{A\}
• = { A , B , C }
                                     (Using A \rightarrow BC)
• = { A , B , C , D , E }
                                     ( Using BC \rightarrow DE )
• = { A , B , C , D , E , F }
                                     (Using D \rightarrow F)
• = { A , B , C , D , E , F , G } (Using CF → G)

    Thus,

• A+ = { A , B , C , D , E , F , G }
```

Example-9:

- The following functional dependencies are given:
- $\{AB \rightarrow CD, AF \rightarrow D, DE \rightarrow F, C \rightarrow G, F \rightarrow E, G \rightarrow A\}$
- Which one of the following options is false? (GATE 2006)

- CF+ = {ACDEFG}
- $BG+ = \{ABCDG\}$
- AF+ = {ACDEFG}
- $AB+ = \{ABCDFG\}$

Example-10: GATE Question: (GATE-CS-2014)

- Consider the relation scheme R = {E, F, G, H, I, J, K, L, M,
 N} and the set of functional dependencies
- {{E, F} -> {G}, {F} -> {I, J}, {E, H} -> {K, L}, K -> {M}, L -> {N} on R. Find the closure for

- E
- F
- EF
- EFH

Example-11:

- GATE Question: Consider the relation scheme R = {E, F, G, H, I, J, K, L, M, N} and the set of functional dependencies {{E, F} -> {G}, {F} -> {I, J}, {E, H} -> {K, L}, K -> {M}, L -> {N} on R. What is the key for R? (GATE-CS-2014)
- A. {E, F}
- B. {E, F, H}
- C. {E, F, H, K, L}
- D. {E}

Answer:

- Finding attribute closure of all given options, we get:
- $\{E,F\}+=\{EFGIJ\}$
- {E,F,H}+ = {EFHGIJKLMN}
- {E,F,H,K,L}+ = {{EFHGIJKLMN}
- $\{E\}+=\{E\}$
- {EFH}+ and {EFHKL}+ results in set of all attributes, but EFH is minimal. So it will be candidate key. So correct option is (B)

Closure Of Functional Dependency: Calculating Candidate Key

• "A Candidate Key of a relation is an attribute or set of attributes that can determine the whole relation or contains all the attributes in its closure."

Let's try to understand how to calculate candidate keys.

Example-1:

- Consider the relation R(A,B,C) with given functional dependencies :
- FD1 : A → B
- FD2 : B → C
- Find the candidate key for the given relation?
- Now, calculating the closure of the attributes as:
- $\{A\}^+ = \{A, B, C\}$
- $\{B\}^+ = \{B, C\}$
- $\{C\}^+ = \{C\}$
- Clearly, "A" is the candidate key as, its closure contains all the attributes present in the relation "R".

Example-2:

- Consider the relation R(A,B,C,D,E,F,G) with given functional dependencies :
- FD1 : A → B
- FD2 : B → CF
- FD3 : D → EG
- FD4 : E → C
- FD5: $F \rightarrow G$
- FD5: G → D
- Find the candidate key for the given relation?
- Now, calculating the closure of the attributes as :
- {A}+ = {A, B, C, D, E, F, G}
- {B}+ = {B, C, D, E, F, G}
- {C}+ = {C} and so on
- Clearly, "A" is the candidate key as, its closure contains all the attributes present in the relation "R".

EMPLOYEE relation shown in Table 1 has following FD set. {E-ID->E-NAME, E-ID->E-CITY, E-ID->E-STATE, E-CITY->E-STATE} Let us calculate attribute closure of different set of attributes:

- (E-ID)+ = {E-ID, E-NAME, E-CITY, E-STATE}
- (E-ID,E-NAME)+ = {E-ID, E-NAME,E-CITY,E-STATE}
- (E-ID,E-CITY)+ = {E-ID, E-NAME,E-CITY,E-STATE}
- (E-ID,E-STATE)+ = {E-ID, E-NAME,E-CITY,E-STATE}
- (E-ID,E-CITY,E-STATE)+ = {E-ID, E-NAME,E-CITY,E-STATE}
- (E-NAME)+ = {E-NAME}
- (E-CITY)+ = {E-CITY,E-STATE}

- Let R = (A, B, C, D, E, F) be a relation scheme with the following dependencies-
- $C \rightarrow F$
- $E \rightarrow A$
- $EC \rightarrow D$
- $A \rightarrow B$
- Which of the following is a key for R?
- CD
- EC
- AE
- AC
- Also, determine the total number of candidate keys and super keys.

- Let R = (A, B, C, D, E) be a relation scheme with the following dependencies-
- AB → C
- $C \rightarrow D$
- B → E
- Determine the total number of candidate keys and super keys.

- Consider the relation scheme R(E, F, G, H, I, J, K, L, M, N) and the set of functional dependencies-
- $\{E, F\} \rightarrow \{G\}$
- $\{F\} \rightarrow \{I,J\}$
- { E, H } → { K, L }
- { K } → { M }
- $\{L\} \rightarrow \{N\}$
- What is the key for R?
- 1.{ E, F }
- 2. { E, F, H }
- 3.{ E, F, H, K, L }
- 4.{ E }

Example-2

- Consider another relation R(A, B, C, D, E) having the Functional dependencies :
- FD1 : A → BC
- FD2 : C → B
- FD3 : D→ E
- FD4 : E → D
- Now, calculating the closure of the attributes as :
- $\{A\}^+ = \{A, B, C\}$
- $\{B\}^+ = \{B\}$
- $\{C\}^+ = \{C, B\}$
- $\{D\}^+ = \{E, D\}$
- $\{E\}^+ = \{E, D\}$
- {A, D}+ = {A, B, C, D, E}
- $\{A, E\}^+ = \{A, B, C, D, E\}$
- Hence, "AD" and "AE" are the two possible keys of the given relation "R". Any other combination other than these two would have acted as extraneous attributes.

Closure Of Functional Dependency: Key Definitions

- 1. Prime Attributes: Attributes which are indispensable part of candidate keys. For example: "A, D, E" attributes are prime attributes in above example-2.
- 2. Non-Prime Attributes: Attributes other than prime attributes which does not take part in formation of candidate keys.
- 3. Extraneous Attributes: Attributes which does not make any effect on removal from candidate key.

Consider another relation R(A, B, C, D) having the Functional dependencies:

FD1 : A → BC

FD2 : B → C

FD3 : D → AD

What is the candidate key???

- Here, Candidate key can be "AD" only. Hence,
- Prime Attributes : A, D.
- Non-Prime Attributes : B, C
- Extraneous Attributes: B, C(As if we add any of the to the candidate key, it will remain
 unaffected). Those attributes, which if removed does not affect closure of that set.

Canonical Cover Of Functional Dependency

- In any relational model, there exists a set of functional dependencies. These functional dependencies when closely observed might contain redundant attributes.
- The ability of removing these redundant attributes without affecting the capabilities
 of the functional dependency is known as "canonical cover of functional
 dependency".
- Canonical cover of functional dependency is sometimes also referred to as "minimal cover".
- Canonical cover of functional dependency is denoted using "M_c".

Canonical Cover Of Functional Dependency: Example

- Consider a relation R(A,B,C,D) having some attributes and below are mentioned functional dependencies.
- FD1 : B → A
- FD2 : AD → C
- **FD3** : C → ABD

Step-1: Decompose the functional dependencies using Decomposition rule(Armstrong's Axiom) i.e. single attribute on right hand side.

```
FD1: B \rightarrow A
```

$$FD2:AD \rightarrow C$$

$$FD3:C\rightarrow A$$

$$FD4: C \rightarrow B$$

FD5:
$$C \rightarrow D$$

```
1.Transitive: It means, if A \rightarrow B \& B \rightarrow C, then A \rightarrow C.
```

```
2.Decomposition : It means, if A \rightarrow BC,
```

```
then A \rightarrow B \& A \rightarrow C.
```

Example Contd.,

Step-2: Remove extraneous attributes from LHS of functional dependencies by calculating the closure of FD's having two or more attributes on LHS.

```
Here, only one FD has two or more attributes of LHS i.e. AD \rightarrow C.
```

```
{A}^+ = {A} Excluding AD->C
```

Step-3: Remove FD's having transitivity.

 $FD1: {\color{red}B} \to A$

 $FD2: C \rightarrow A$

 $FD3: C \rightarrow B$

 $FD4 : AD \rightarrow C$

 $FD5: C \rightarrow D$

Above FD1, FD2 and FD3 are forming transitive pair. Hence, using Armstrong's law of transitivity i.e. if $X \to Y$, $Y \to Z$ then $X \to Z$ should be removed. Therefore we will have the following FD's left :

FD1: $B \rightarrow A$ FD2: $AD \rightarrow C$

FD3: $C \rightarrow A$ FD4: $C \rightarrow B$

FD5: $C \rightarrow D$

Example Contd.,

```
FD1: B \rightarrow A

FD2: C \rightarrow B

FD3: AD \rightarrow C

FD4: C \rightarrow D

FD4: C \rightarrow D
```

Also, FD2 & FD4 can be clubbed together now. Hence, the canonical cover of the relation R(A,B,C,D) will be:

```
Mc \{R(ABCD)\} = \{B \rightarrow A, C \rightarrow BD, AD \rightarrow C\}
```

```
Consider the following set F of functional dependencies:
F= {
A \rightarrow BC
B \rightarrow C
A \rightarrow B
AB \rightarrow C
Steps to find canonical cover:
```

 There are two functional dependencies with the same set of attributes on the left A → BC A → B These two can be combined to get A → BC. Now, the revised set F becomes:
F= { A → BC B → C AB → C }

2. There is an extraneous attribute in AB \to C because even after removing AB \to C from the set F, we get the same closures. This is because B \to C is already a part of F.

Now, the revised set F becomes:

```
F= {
A → BC
B → C
```

3. C is an extraneous attribute in A \rightarrow BC, also A \rightarrow B is logically implied by A \rightarrow B and B \rightarrow C (by transitivity).

 $A \rightarrow B$

 $B \rightarrow C$

}

4. After this step, F does not change anymore. So,

Hence the required canonical cover is,

$$F_{c^{=}}$$

$$A \rightarrow B$$

$$B \rightarrow C$$

Exercise:

1. Find the canonical cover of FD {A->BC, B->AC, C->AB}

- 2. The following functional dependencies hold true for the relational scheme $R\left(W,X,Y,Z\right)$ –
- $\bullet X \to W$
- $WZ \rightarrow XY$
- $Y \rightarrow WXZ$
- Write the irreducible equivalent for this set of functional dependencies.

3. Suppose a relational schema R(P, Q, R, S), and set of functional dependency as following

Find the canonical cover Fc (Minimal set of functional dependency).

EQUIVALENCE OF FUNCTIONAL DEPENDENCY

- Two or more than two sets of functional dependencies are called equivalence if the right-hand side of one set of functional dependency can be
- determined using the second FD set, similarly the right-hand side of the second FD set can be determined using the first FD set.

- 1: Given a relational schema R(X, Y, Z, W, V) set of functional dependencies P and Q such that:
- P = { $X \rightarrow Y$, $XY \rightarrow Z$, $W \rightarrow XZ$, $W \rightarrow V$ } and
- $Q = \{ X \rightarrow YZ, W \rightarrow XV \}$ using FD sets P and Q

Which of the following options are correct?

- P is a subset of Q
- Q is a subset of P
- P = Q
- P ≠ Q

STEP1: Find the closure of P using FDs of Q

 Using definition of equivalence of FD set, let us determine the right-hand side of the FD set of P using FD set Q.

 Let's find closure of the left side of each FD of P using FD Q.

- X + = XYZ (using $X \rightarrow YZ$)
- XY+ = XYZ (using $X \rightarrow YZ$)
- W+ = WXVYZ (using W \rightarrow XV and X \rightarrow YZ)
- W+ = WXVYZ (using W \rightarrow XV and X \rightarrow YZ)

STEP2: Compare the closure of P with P's FDs

- Now compare closure of each X, XY, W and W calculated using FD Q with the right-hand side of FD P.
- Closure of each X, XY, W and W has all the attributes which are on the right-hand side of each FD of P.
- Hence, we can say P is a subset of Q------1

STEP3: Find the closure of Q using FDs of P

 Using definition of equivalence of FD set, let us determine the right-hand side of the FD set of Q using FD set P.

• Given P = {
$$X \rightarrow Y$$
, $XY \rightarrow Z$, $W \rightarrow XZ$, $W \rightarrow V$ } and Q = { $X \rightarrow YZ$, $W \rightarrow XV$ }

 Let us find closure of the left side of each FD of Q using FD P.

- X+ = XYZ (using $X \rightarrow Y$ and $XY \rightarrow Z$)
- W+ = WXZVY (using W \rightarrow XZ, W \rightarrow V, and X \rightarrow Y)

STEP:4 Compare the clouse of Q with P's FDs

- Now compare closure of each X, W calculated using FD P with the right-hand side of FD Q. Closure of each X and W has all the attributes which are on the right-hand side of each FD of Q.
- Hence, we can say Q is a subset of P-----2

 From 1 and 2 we can say that P = Q, hence option C is correct.

- Given a relational schema R(A, B, C, D) set of functional dependencies P and Q such that:
- P = { A → B, B → C, C → D } and Q = { A → BC, C → D } using FD sets P and Q which of the following options are correct?

- a) P is a subset of Q
- b) Q is a subset of P
- c) P = Q
- d) P ≠ Q

- Given a relational schema R(X, Y, Z) set of functional dependencies P and Q such that:
- P = { X → Y, Y → Z, Z → X } and Q = { X → YZ, Y → X, Z → X } using FD sets P and Q which of the following options are correct?

- P is a subset of Q
- Q is a subset of P
- P = Q
- P ≠ Q

- A relation R (A, C, D, E, H) is having two functional dependencies sets F and G as shown-
- Set P-
- A → C
- AC → D
- E → AD
- E → H
- Set Q-
- A → CD
- E → AH
- which of the following options are correct?
- P is a subset of Q Q is a subset of P P = Q P ≠ Q

Q 1. Suppose, a relational schema R (A, B, C) and set of functional dependencies F and G are as follow:

$$F: \{A \rightarrow B, G: \{A \rightarrow BC, B \rightarrow C, B \rightarrow A, C \rightarrow A\}$$

Check the equivalency of functional dependencies F and G.

Q 2. Suppose, a relational schema R (v w x y z) and set of functional dependencies F and G are as follow:

F:
$$\{ w \rightarrow x, G: \{ w \rightarrow xy, \\ wx \rightarrow y, z \rightarrow wx \}$$

 $z \rightarrow wy, \\ z \rightarrow v \}$

Check the equivalency of functional dependencies F and G.

2. Suppose, a relational schema R (P,Q, R, S) and set of functional dependencies F and G are as follow:

$$F: \{ P \rightarrow Q, \qquad G: \{ P \rightarrow QR, \\ Q \rightarrow R, \qquad R \rightarrow S \}$$

$$R \rightarrow S \}$$

Check the equivalency of functional dependencies F and G.

A relation R (A, C, D, E, H) is having two functional dependencies sets F and G as shown-

Set F-

 $A \to C$

 $AC \to \mathsf{D}$

 $\mathsf{E} \to \mathsf{AD}$

 $\mathsf{E} \to \mathsf{H}$

Set G-

 $A \rightarrow CD$

 $E \rightarrow AH$

Exercise:

Let $F = \{A \rightarrow C, AC \rightarrow D, E \rightarrow AD\}$, and let $G = \{A \rightarrow CD, E \rightarrow AHE\}$. Are they equivalent?

Properties of Decomposition

Decomposition must have the following properties:

1. Decomposition Must be Lossless

2. Dependency Preservation

3. Lack of Data Redundancy

1. Decomposition Must be Lossless

 Decomposition must always be lossless, which means the information must never get lost from a decomposed relation. This way, we get a guarantee that when joining the relations, the join would eventually lead to the same relation in the result as it was actually decomposed.

1. Decomposition Must be Lossless

- Example:
- Original Relation: "Student" with attributes (StudentID, Name, Major, GPA)
- Decomposition:
 - "StudentDetails" (StudentID, Name, Major)
 - "AcademicPerformance" (StudentID, GPA)

2. Dependency Preservation

 Dependency is a crucial constraint on a database, and a minimum of one decomposed table must satisfy every dependency. If {P → Q} holds, then two sets happen to be dependent functionally. Thus, it becomes more useful when checking the dependency if both of these are set in the very same relation.

3. Lack of Data Redundancy

 It is also commonly termed as a repetition of data/information. According to this property, decomposition must not suffer from data redundancy.
 When decomposition is careless, it may cause issues with the overall data in the database. When we perform normalization, we can easily achieve the property of lack of data redundancy

1. Apply Natural Join decomposition on the below two tables:

Cust_ID	Cust_Name	Cust_Age	Cust_Location
C001	Monica	22	Texas
C002	Rachel	33	Toronto
C003	Phoebe	44	Minnesota

Sec_ID	Cust_ID	Sec_Name
Sec1	S001	Accounts
Sec2	S002	Marketing
Sec3	S003	Telecom

Answer: The result will be:

Cust_ID	Cust_Name	Cust_Age	Cust_Location	Sec_ID	Sec_Name
S001	Monica	22	Texas	Sec1	Accounts
S002	Rachel	33	Toronto	Sec2	Marketing
S003	Phoebe	44	Minnesota	Sec3	Telecom