

Given: Covariance Matrix : $\begin{bmatrix} 14 & 0.7 \\ 0.7 & 2.81 \end{bmatrix}$

PCA

For eigen vectors, we solve $\det \begin{bmatrix} (14-d) & 0.7 \\ 0.7 & (2.81-d) \end{bmatrix} = 0$.

we get $d = \underbrace{14.0436, 2.76}_{\text{greater.}}$

$\therefore d = 14.0436$

Now, $\begin{bmatrix} 14 & 0.7 \\ 0.7 & 2.81 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} = 14.0436 \begin{bmatrix} x_1 \\ x_2 \end{bmatrix}$

We assume $x_1 = 1$ & get $x_2 = 0.0623$.

\therefore Eigen vector, $e = \begin{bmatrix} 1 \\ 0.0623 \end{bmatrix} = \begin{bmatrix} e_x \\ e_y \end{bmatrix}$

Let eqn of the line of new axis be $y = mx + c$

Now, $m = \frac{e_y}{e_x}$

OR, $y = 0.0623x + c$

Also, the line passes through mean. ($\mu = \begin{bmatrix} \mu_x \\ \mu_y \end{bmatrix} = \begin{bmatrix} 7 \\ 3.7 \end{bmatrix}$)

$\therefore \mu_y = 0.0623 \mu_x + c$

OR, $3.7 = 0.0623 \times 7 + c$

OR $c = 3.2639$

\therefore eqn of line is $y = 0.0623x + 3.2639$

