

# Topic 10: Feature Extraction

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- 1 What is a feature of an object or image?
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- 5 Corner Point Detection
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# What is a feature?



- ▶ A feature is a property of an object. Eg: Size of an object, Shape of an object.
- ▶ Features of Image may be of any of the following types
  - Feature of an image may be given in terms of features of pixels
  - Some properties of image such as
    - ▶ Histogram of the image
    - ▶ Fourier Transform(FT) of image or some properties of FT
    - ▶ Edge map of the image
    - ▶ **Features of some important points in image**
  - Some properties of blocks of image
    - ▶ Local(block) average
    - ▶ Local(block) histogram
  - Some properties of objects in the image
    - ▶ Area, diameter, perimeter texture etc.



- ▶ Feature Extraction: Process of extracting features of image(object) such that
  - feature values of images of different types of scenes(objects) are very different, but very close for similar scenes(objects)
- ▶ Need of feature extraction
  - Using raw data(image) for Image matching or classification is not effective as
    - ▶ Images of the same scene taken at different time or different cameras may be different
    - ▶ Raw data may have more redundant or irrelevant data for classification
    - ▶ Raw data is generally large, and hence computation time will be high

# Feature Selection

- ▶ Suppose an object or an image is represented by a feature vector  $f = (f_1, f_2, \dots, f_n)$ , where each  $f_i$  is a feature
- ▶ The process of dropping some of the features in  $f$  such that matching or classification accuracy improves
- ▶ Some feature selection methods
  - if  $\text{Similarity}(f_i, f_j)$  is high then drop  $f_i$  or  $f_j$
  - Some important similarity metrics
    - ▶ Normalized Cross Correlation(NCC) (more the NCC, more the similarity)
    - ▶ Mutual Information(MI)(more the MI, More the similarity)
    - ▶ Mean Squared Difference(MSD)(Lesser the MSD, more the similarity )



- ▶ Consider the problem: Given two images, check if they are of the same scene
- ▶ We can solve this problem,  
If we can find some points in one image that can be
  - Found in another image as well
  - Found precisely – well localized
  - Found reliably – well matched(the features of the corresponding points are matched)

when both images are of the same scene

- Such points are called as important points

# Other uses of such important points



- ▶ Want to compute a fundamental matrix to recover geometry (To do 3D reconstruction).
- ▶ Robotics/Vision: To find how a bunch of points move from one frame to another.
- ▶ Object tracking
- ▶ Build a panorama...

# Suppose you want to build a panorama



# How do we build panorama?



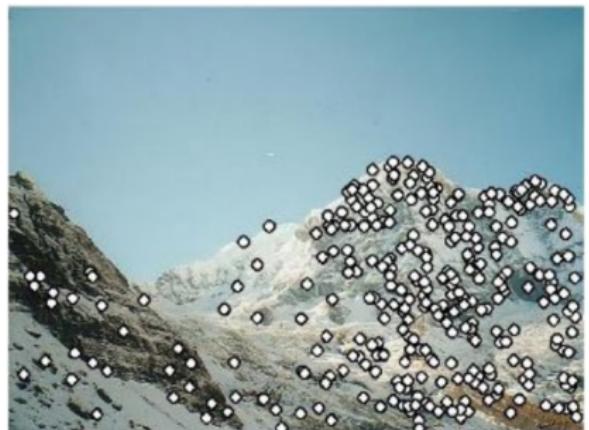
We need to match(align) the images.



# Matching with Features



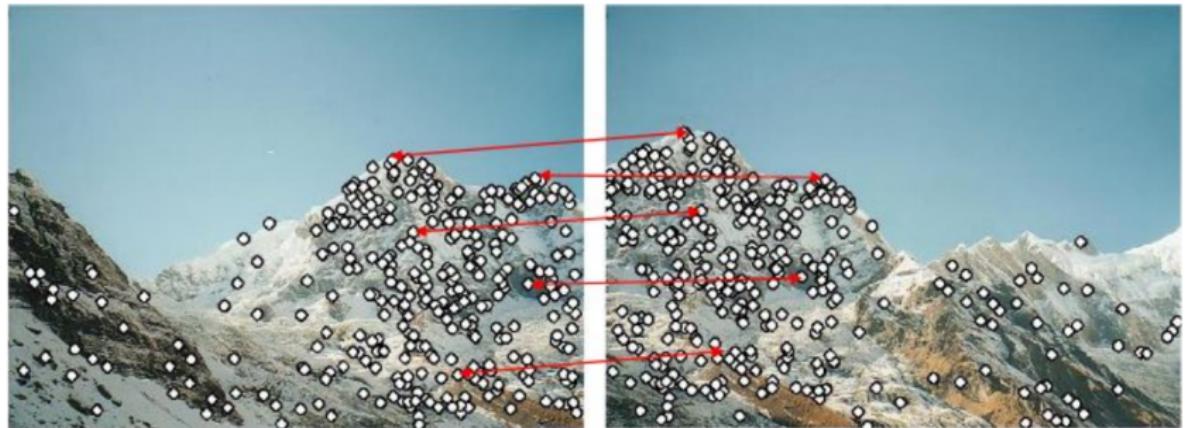
Detect features (feature points) in both images.



# Matching with Features



- ▶ Detect features (feature points) in both images.
- ▶ Match features- find corresponding pairs.



# Matching with Features

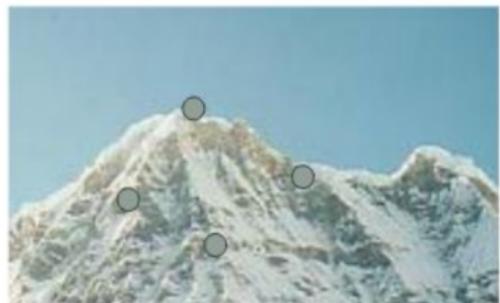


- ▶ Detect features (feature points) in both images.
- ▶ Match features- find corresponding pairs.
- ▶ Use these pairs to align images



## Problem 1:

- ▶ Detect the same point independently in both the images.



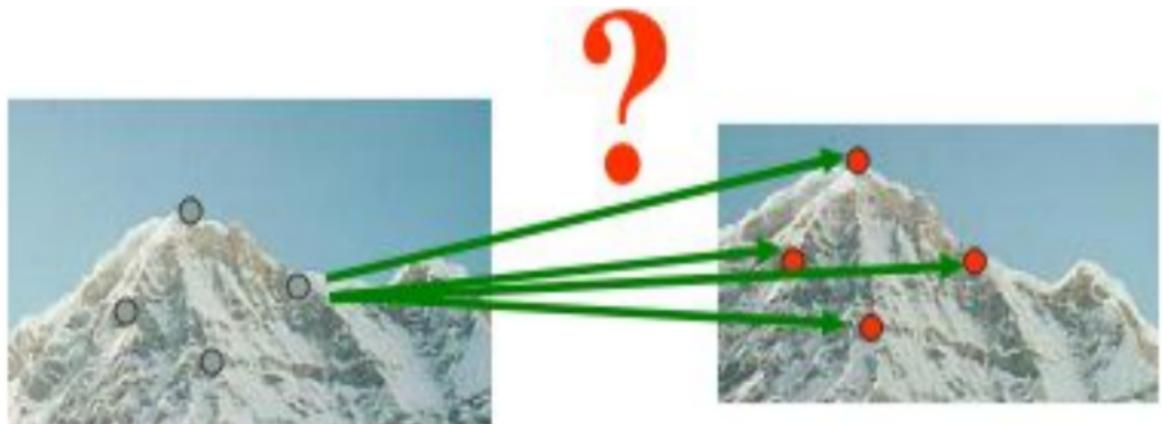
no chance to match!

# Matching with Features

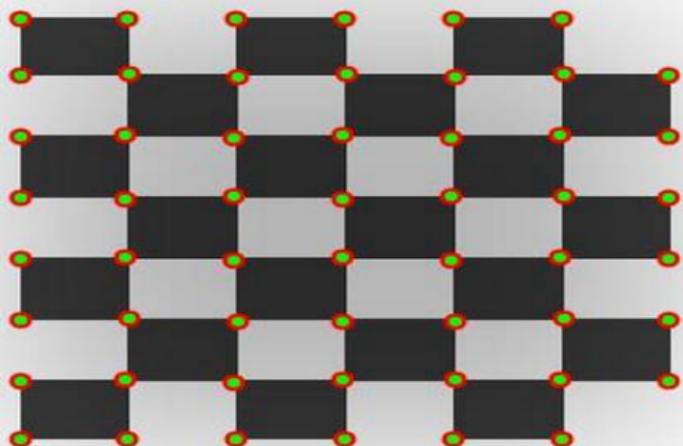


## Problem 2:

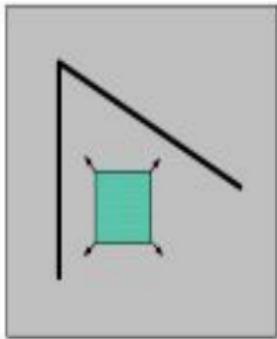
- ▶ For each point correctly recognize the corresponding one



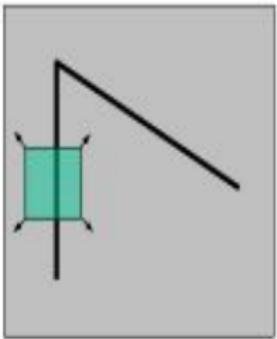
## What is a corner point



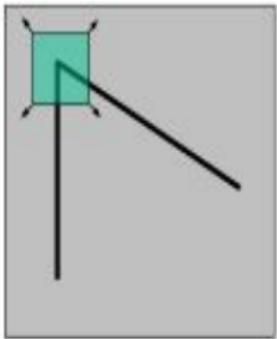
# Corner points -important points (cont.)



"flat":  
no change in all  
directions



"edge":  
no change along the  
edge direction

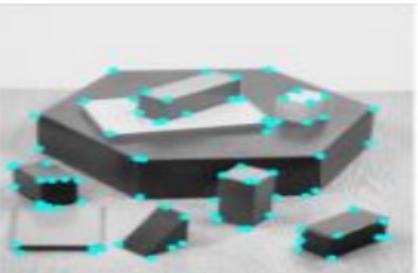


"corner":  
significant change in  
all directions

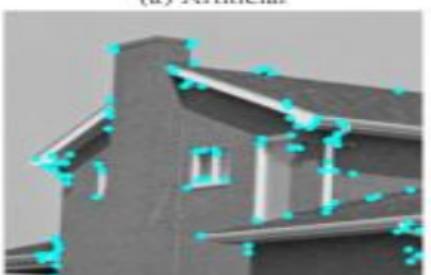
# Corner points -important points (cont.)



(a) Artificial



(b) Block



(c) House



(d) Lab

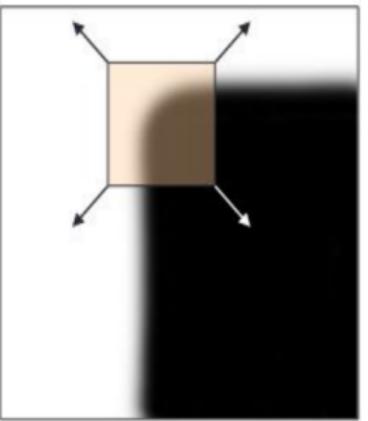
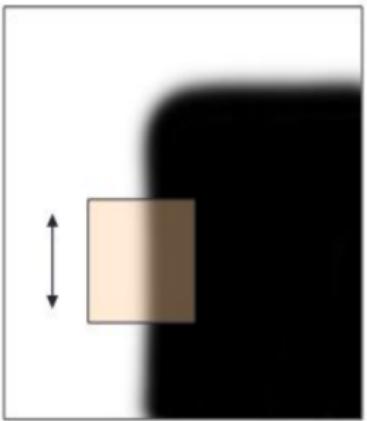
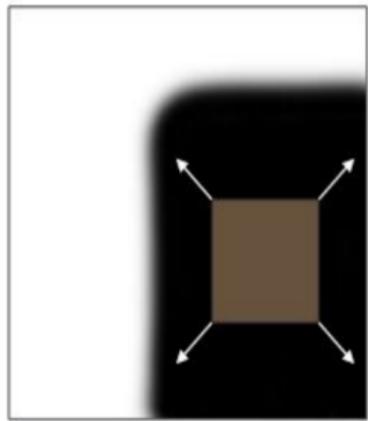


- ▶ Key property: in the region around a corner, image gradient has two or more dominant directions.

## How to model corner point

- ▶ Consider the window centered at  $(p, q)$  with size  $a \times b$  in the image, say  $W_1$
- ▶ Move the window with displacement vector  $(u, v)$  the resultant window as  $W_2$
- ▶ If  $\|W_2 - W_1\|^2$  is large for two or more displacement vectors  $(u, v)$ s than  $(p, q)$  is called as a corner point
- ▶ Note that  $(u, v)$  provide direction to move the window

# Corner points -important points (cont.)





- ▶ How to find whether or not the difference is large in two or more directions efficiently?
- ▶ To do that efficiently, the difference between two windows separated by the displacement vector  $(u, v)$  is defined as:

$$E(u, v) = \sum_{x,y} w(x, y) [I(x + u, y + v) - I(x, y)]^2$$

Window function -  $w(x, y)$

Shifted Intensity -  $I(x + u, y + v)$

Intensity -  $I(x, y)$

## Objective:

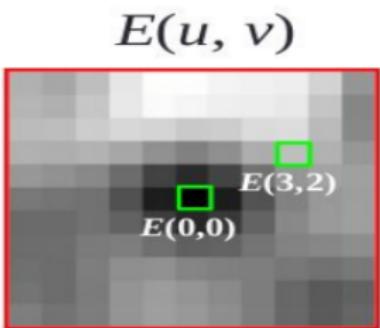
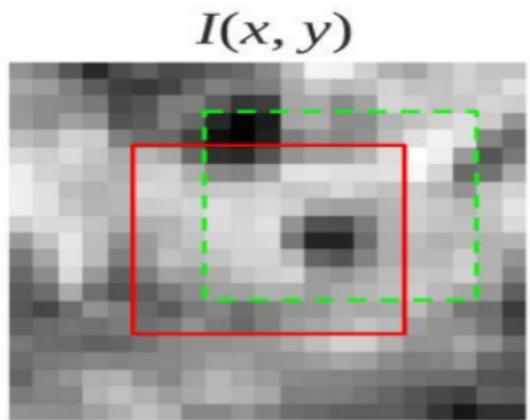
- ▶ Find each window that produce a large E value for two or more  $(u, v)$  ( ie for two or more directions).

# Harris Corner point Detection (cont.)



Change in appearance for the shift  $[u,v]$

$$E(u, v) = \sum_{x,y} w(x, y) [ I(x + u, y + v) - I(x, y) ]^2$$





## Taylor Series Expansion Approximation up to first derivative for 2D:

- ▶  $f(x + u, y + v) = f(x, y) + uf_x(x, y) + vf_y(x, y)$
- ▶ Applying Taylor series approximation for  $I(x + u, y + v)$  in  $E(u, v)$  we get,

$$E(u, v) = \sum_{x,y} w(x, y) [ I(x, y) + ul_x(x, y) + vl_y(x, y) - I(x, y) ]^2$$

- ▶  $E(u, v) = \sum_{x,y} w(x, y) [ ul_x(x, y) + vl_y(x, y) ]^2$
- ▶  $E(u, v) = \sum_{x,y} w(x, y) [ u^2 l_x^2(x, y) + v^2 l_y^2(x, y) + 2uv l_x(x, y)l_y(x, y) ]$

# Harris Corner point Detection (cont.)



we can rewrite as matrix equation:

$$E(u, v) \approx [u \quad v] \sum_{x,y} w(x, y) \begin{bmatrix} I_x^2(x, y) & I_x(x, y)I_y(x, y) \\ I_x(x, y)I_y(x, y) & I_y^2(x, y) \end{bmatrix} \begin{bmatrix} u \\ v \end{bmatrix}$$

Written in a simple form as:

$$E(u, v) \approx [u \quad v] M \begin{bmatrix} u \\ v \end{bmatrix}$$

Where

$$M = \sum_{x,y} w(x, y) \begin{bmatrix} I_x^2 & I_x I_y \\ I_x I_y & I_y^2 \end{bmatrix}$$

# Harris Corner point Detection (cont.)



► Decompose M as  $M = Q^T A Q$ , where

- A is the diagonal matrix with eigen values of M in the diagonal:

$$A = \begin{bmatrix} \lambda_1 & 0 \\ 0 & \lambda_2 \end{bmatrix}$$

- Each column of Q is an eigen vector of M

► Sub M in E(u,v), we get

$$E(u, v) \approx [u \quad v] Q^T A Q \begin{bmatrix} u \\ v \end{bmatrix}$$



$$E(u, v) \approx (Q [u \quad v]^T)^T A Q \begin{bmatrix} u \\ v \end{bmatrix}$$



## Interpretation of $Q(u, v)^T$

- ▶  $(u, v)^T$  is transformed into a new coordinate system with eigen vectors as axes, say  $(u', v')^T$
- ▶ Hence

$$E(u, v) \approx ([u' \quad v']) A \begin{bmatrix} u' \\ v' \end{bmatrix}$$

- ▶

$$E(u, v) \approx ([u' \quad v']) \begin{bmatrix} \lambda_1 & 0 \\ 0 & \lambda_2 \end{bmatrix} \begin{bmatrix} u' \\ v' \end{bmatrix}$$

- ▶  $E(u, v) = (u'^2\lambda_1 + v'^2\lambda_2)$

# Harris Corner point Detection (cont.)

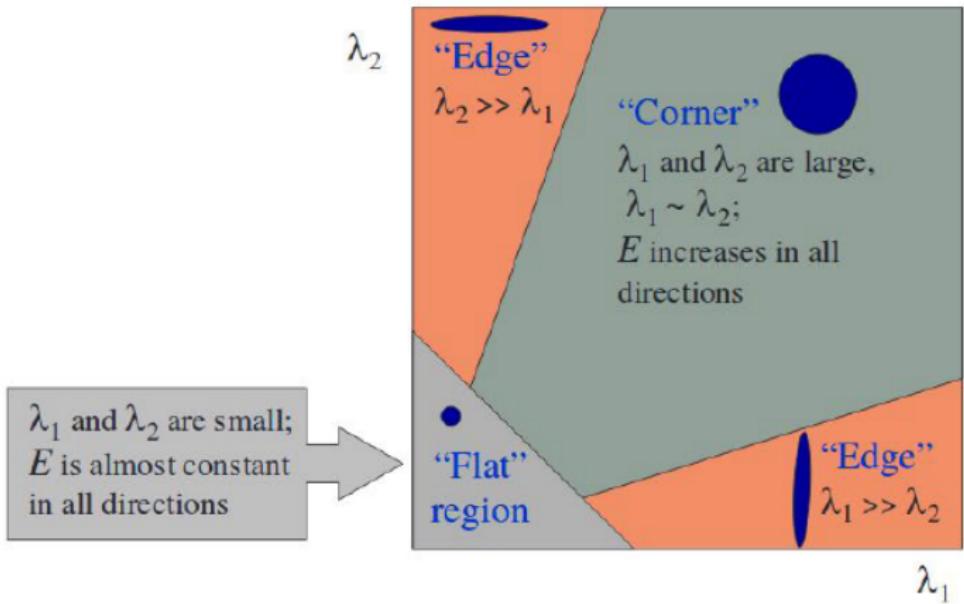


- ▶ **Observation:**  $E(u, v)$  is large when  $\lambda_1$  and  $\lambda_2$  are large
- ▶ As  $(u, v)$  is a directional vector,  $(u', v')$  is also a directional vector in eigen space
- ▶ If we consider  $(u', 0)$  and  $(0, v')$  as two directions,  $E$  is large when  $\lambda_1(\text{length in } (u', 0))$  and  $\lambda_2(\text{length in } (0, v'))$

# Interpreting the eigenvalues



Classification of image points using eigenvalues of  $M$ :



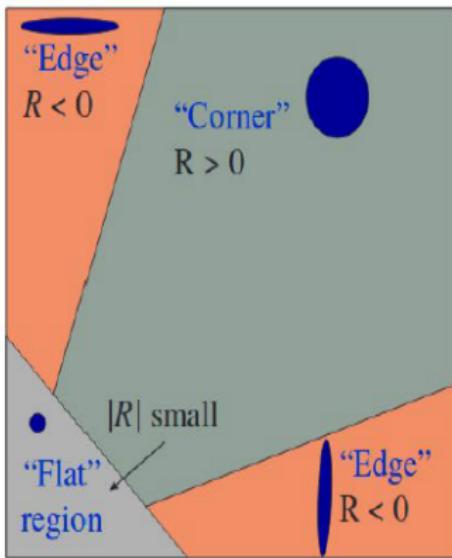
# Harris corner response function

For computational efficiency, use the following

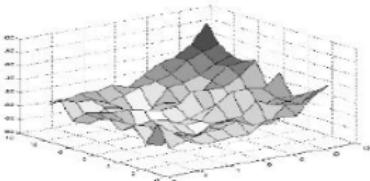


$$R = \det(M) - \alpha \text{trace}(M)^2 = \lambda_1 \lambda_2 - \alpha(\lambda_1 + \lambda_2)^2$$

- ▶  $R$  is large for a corner
- ▶  $R$  is negative with large magnitude for an edge
- ▶  $|R|$  is small for a flat region

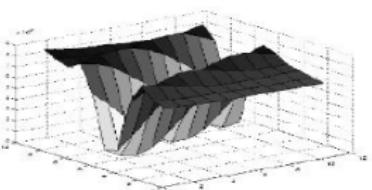


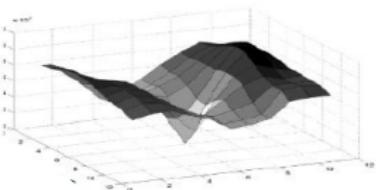
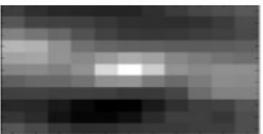
# Low texture region



- ▶ gradients have small magnitude
- ▶ small  $\lambda_1$ , small  $\lambda_2$

# Edge





$$\sum \nabla I (\nabla I)^T$$

# Harris corner point detection algorithm

**Input:**  $I$

**Output:** Set of all corner points in  $I$

**Steps:**

- ▶ Find derivative image  $I$  in  $x$  direction, and call it as  $I_x$
- ▶ Find derivative image  $I$  in  $y$  direction, and call it as  $I_y$
- ▶ Compute the products of derivatives at each pixel:
  - $I_{x2} = I_x I_x;$
  - $I_{y2} = I_y I_y;$
  - $I_{xy} = I_x I_y;$
- ▶ Compute sums of products of derivatives at each pixel
  - $S_{x2} = \text{Conv}(I_{x2}, h);$
  - $S_{y2} = \text{Conv}(I_{y2}, h);$
  - $S_{xy} = \text{Conv}(I_{xy}, h)$

# Harris corner point detection algorithm (cont.)

where  $h$  is the sum filter

- ▶ Compute at for each pixel  $(x, y)$

$$H(x, y) = \begin{bmatrix} S_{x2}(x, y) & S_{xy}(x, y) \\ S_{xy}(x, y) & S_{y2}(x, y) \end{bmatrix}$$

- ▶ Compute corner response function  $R$  at each pixel:  
$$R(x, y) = \text{Det}(H(x, y)) - k(\text{Trace}(H(x, y)))^2$$
- ▶ If  $R(x, y) > T$  then output  $(x, y)$  as key point

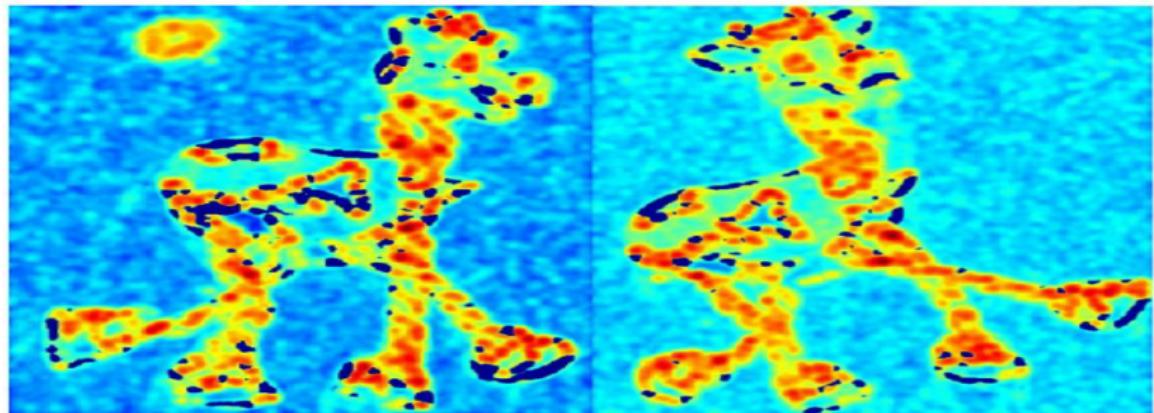
# Harris Detector: Workflow



# Harris Detector: Workflow (cont.)



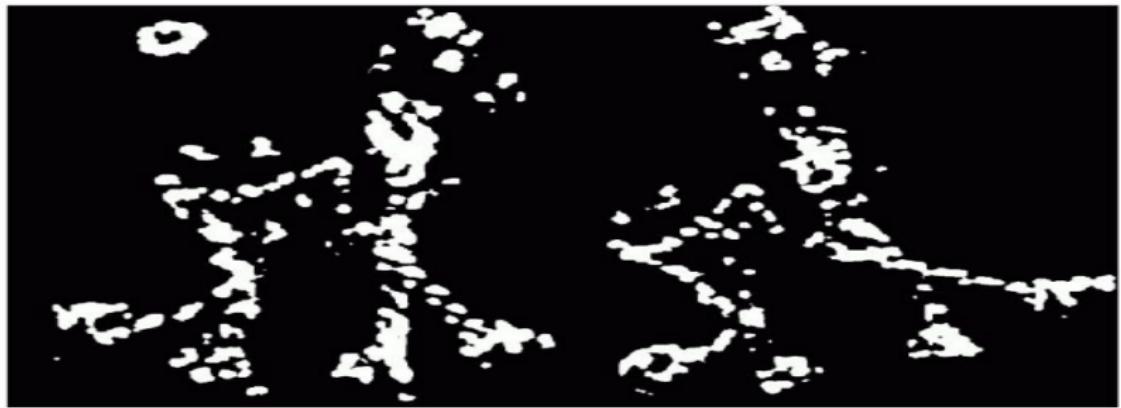
Compute corner response R



# Harris Detector: Workflow (cont.)



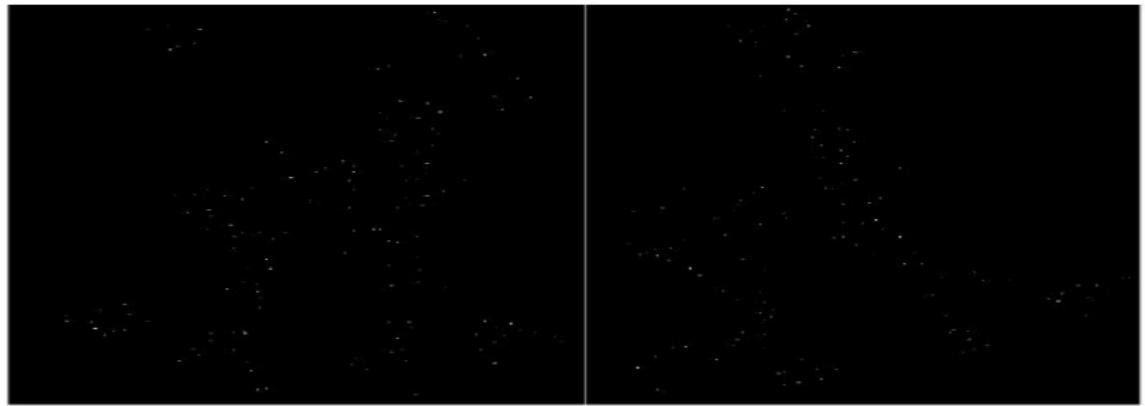
Find the points with large corner response:  $R > \text{threshold}$



# Harris Detector: Workflow (cont.)



Take only the points of local maxima of R



# Harris Detector: Workflow (cont.)

