

1a.

Truth table 1 for AND operation is

X1	X2	AND
0	0	0
0	1	0
1	0	0
1	1	1

1b.

The values of w_1, w_2 and b are

$$w_1 = 1$$

$$w_2 = 1$$

$$b = -1$$

The equation of y will be

$$y = \emptyset(x_1 + x_2 - 1)$$

1c.

Truth table 2 for OR operation is

X1	X2	OR
0	0	0
0	1	1
1	0	1
1	1	1

1d.

The values of w_1, w_2 and b are

$$w_1 = 1$$

$$w_2 = 1$$

$$b = 0$$

The equation of y will be

$$y = \emptyset(x_1 + x_2)$$

1e.

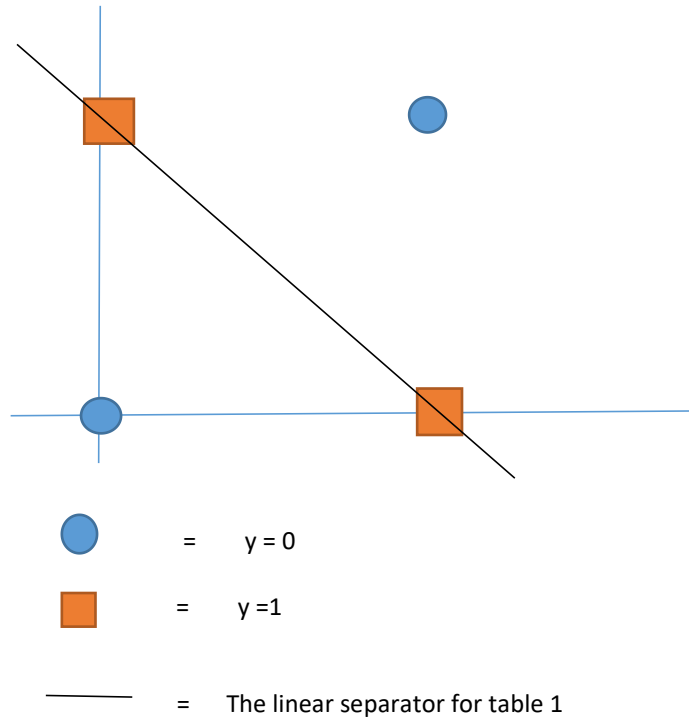
Truth Table 3 for XOR Operation is

X1	X2	XOR
0	0	0
0	1	1
1	0	1
1	1	0

1f.

The linear separator depicted in figure 1 is given by the formula
 $y = 0(x_1 + x_2 - 1)$, this is failing to create an XOR function

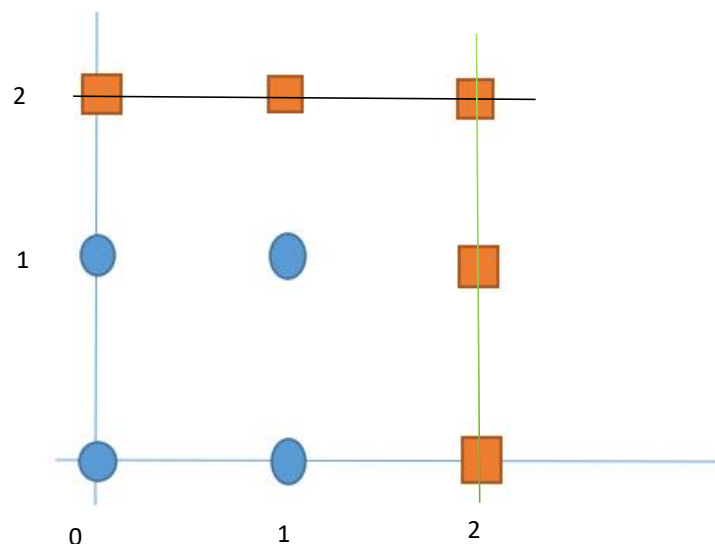
If we draw a graph for XOR points we will be having something like



Clearly if we look at the graph we can say that XOR is not linearly separable and we cannot find a linearly separable equation for XOR operation. The equation given for Truth table 1 cannot be used to create logical XOR because for the case $x = [1,1]$ we have $y = 1$ where as we actually need to get $y = 0$

1g.

The graph for the given question will be as follows



We can see from the graph clearly that this is not linearly separable. This function cannot be learned from a linear perceptron but it can be learned from a Multilayer perceptron.

Let there be two functions y_1 and y_2 , representing the two linear perceptrons given in the graph.

$$y_1 = \phi_1(x_1 - 2)$$

$$y_2 = \phi_1(x_2 - 2)$$

$$\text{Where } \phi_1(z) = \begin{cases} 0 & \text{if } z < 0 \\ 1 & \text{if } z \geq 0 \end{cases}$$

Now the resultant y is OR of y_1 and y_2 .

$$y = \phi(y_1 + y_2 - 1)$$

$$\text{Where } \phi(z) = \begin{cases} 0 & \text{if } z \leq 0 \\ 1 & \text{if } z > 0 \end{cases}$$

We get the desired output from the equation of y .

2.

The Accuracy Scores are as follows

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Perceptron
Accuracy: 0.8004
F1-Score: 0.8330545332887253
Precision: 0.8311081441922563
Recall: 0.8350100603621731
Time taken for perceptron to execute training and classification: 0.8120155334472656
Time taken for our model implementation is approximately 1.18
```

The code is attached when submitting the assignment.

