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Data Warehouse & Data Mining

Assignment - 1

Implementation of Decision Tree Classifier

Data Set:

Age	Income	Student	Credit-Rating	Buys Computer
≤ 30	high	no	fair	no
≤ 30	high	no	excellent	no
31-40	high	no	fair	yes
> 40	medium	no	fair	yes
> 40	low	yes	fair	yes
> 40	low	yes	excellent	no
31-40	low	yes	excellent	yes
≤ 30	medium	no	fair	no
≤ 30	^{low} medium	yes	fair	yes
> 40	medium	yes	fair	yes
≤ 30	medium	yes	excellent	yes
31-40	medium	no	excellent	yes
31-40	high	yes	fair	yes
> 40	medium	no	excellent	no

First we need to calculate Information gain for every attribute other than target attribute which is Buys-Computer

From the attribute which has highest information gain we can partition the dataset from that attribute and continue the process.

Partition is stopped when the following conditions met:

- i. All samples belong to the same class
- ii. No samples left
- iii. No Remaining Attributes for further Partitioning

~~Info~~ Entropy of Target = $-\sum_{i=1}^m P_i \log_2(P_i)$

Class P: Buys-Computer = "yes" = 9

Class N: Buys-Computer = "no" = 5

$$E(\text{Buys-Computer}) = -\frac{9}{14} \log_2\left(\frac{9}{14}\right) - \frac{5}{14} \log_2\left(\frac{5}{14}\right)$$

$$E(\text{Target}) = 0.940$$

$$E(\text{Buys-Computer, Age}) = P(\leq 30) \cdot E(\text{target}, \leq 30) + P(31-40) \cdot E(\text{target}, 31-40) + P(>40) \cdot E(\text{target}, >40)$$

Age		Buys-Computer	
		Yes	No
	≤ 30	2	3
	31-40	4	0
	>40	3	2

$$= P(Low) \cdot E(2,3) + P(31-40) \cdot E(4,1) + P(>40) \cdot E(3,2)$$

$$= \frac{5}{14} \left[-\frac{2}{5} \log_2\left(\frac{2}{5}\right) - \frac{3}{5} \log_2\left(\frac{3}{5}\right) \right] + \frac{4}{14} \left[-\frac{4}{4} \log_2\left(\frac{4}{4}\right) - \frac{0}{4} \log_2\left(\frac{0}{4}\right) \right] \\ + \frac{5}{14} \left[-\frac{3}{5} \log_2\left(\frac{3}{5}\right) - \frac{2}{5} \log_2\left(\frac{2}{5}\right) \right]$$

$$= \frac{5}{14} (0.970) + \frac{4}{14} \cdot 0 + \frac{5}{14} (0.970)$$

$E(\text{Buys Comp, age})$

$$= 0.6935$$

$$\text{Information Gain (Target)} = E(\text{Target}) - E(\text{Target, age})$$

$$= 0.940 - 0.6935$$

$$\text{Gain (Target)}_{\text{Age}} = 0.246$$

$$E(\text{Target, Income}) = P(\text{high}) \cdot E(\text{Target, high}) + \\ P(\text{medium}) \cdot E(\text{Target, medium}) + \\ P(\text{Low}) \cdot E(\text{Target, Low})$$

	Buys Computer	
	yes	No
High	2	2
medium	4	2
Low	3	1

$$= \frac{4}{14} \cdot E(2,2) + \frac{6}{14} E(4,2) + \frac{4}{14} E(3,1)$$

$$= \frac{4}{14} \left[-\frac{2}{4} \log_2\left(\frac{2}{4}\right) - \frac{2}{4} \log_2\left(\frac{2}{4}\right) \right] + \\ \frac{6}{14} \left[-\frac{4}{6} \log_2\left(\frac{4}{6}\right) - \frac{2}{6} \log_2\left(\frac{2}{6}\right) \right] + \\ \frac{4}{14} \left[-\frac{3}{4} \log_2\left(\frac{3}{4}\right) - \frac{1}{4} \log_2\left(\frac{1}{4}\right) \right]$$

$$= \frac{4}{14}(1) + \frac{6}{14}(0.918) + \frac{4}{14}(0.811)$$

$$E(\text{target, Income}) = 0.910$$

$$\begin{aligned} \text{Gain (Target)}_{\text{Income}} &= E(\text{Target}) - E(\text{Target, Income}) \\ &= 0.940 - 0.910 \end{aligned}$$

$$\text{Gain (Target)}_{\text{income}} = 0.03$$

$$E(\text{-target, Student}) = P(\text{Yes}) \cdot E(\text{target, yes}) + P(\text{No}) \cdot E(\text{target, no})$$

		Bsys - Computer	
		Yes	No
Student	Yes	26	01
	No	03	14

$$= \frac{7}{14} E(6,1) + \frac{7}{14} E(3,4)$$

$$= \frac{7}{14} \left[\left(-\frac{6}{7} \log_2 \frac{6}{7} - \frac{1}{7} \log_2 \frac{1}{7} \right) + \right.$$

$$\left. \frac{7}{14} \left[\left(-\frac{3}{7} \log_2 \frac{3}{7} - \frac{4}{7} \log_2 \frac{4}{7} \right) \right] \right]$$

$$= \frac{7}{14} (0.919) + \frac{7}{14} (0.985)$$

$$E(\text{target, student}) = 0.788$$

$$\text{Gain (Target)}_{\text{Student}} = E(\text{Target}) - E(\text{Target, Student})$$

$$= 0.940 - 0.788$$

$$= 0.152$$

$$E(\text{target}, \text{Credit_Rating}) = P(\text{fair}) \cdot E(\text{target}, \text{fair}) + P(\text{excellent}) \cdot E(\text{target}, \text{excellent})$$

Credit_Rating		Buys - Computer	
		Yes	No
fair		3	3
excellent		6	2

$$= \frac{6}{14} \cdot E(3) + \frac{8}{14} E(6)$$

$$= \frac{6}{14} (1) + \frac{8}{14} (0.811)$$

$$E(\text{target}, \text{Credit}) = 0.892$$

$$\begin{aligned} \text{Gain}_{\text{Credit}}(\text{Target}) &= E(\text{Target}) - E(\text{target}, \text{Credit}) \\ &= 0.940 - 0.892 \\ &= 0.048 \end{aligned}$$

By Comparing Information ^{Gain} from 4 attributes

Age	Income	Student	Credit_Rating
0.246	0.03	0.152	0.048

Age has highest Information Gain.

1hr

230

Income	Student	Credit-Rating	Class
high	no	fair	no
high	no	excellent	no
medium	no	fair	no
low	yes	fair	yes
medium	yes	excellent	yes

31-11

Income	Student	Credit-Rating	Class
high	no	fair	yes
low	yes	excellent	yes
medium	no	excellent	yes
high	yes	fair	yes

240

Income	Student	Credit-Rating	Class
medium	no	fair	yes
low	yes	fair	yes
low	yes	excellent	no
medium	yes	fair	yes
medium	no	excellent	no

→ In the samples of 31-40, all belong to same class of the target SD. 31-40 group buys computer.

Now consider ≤ 30 group/node.

Entropy of ≤ 30

$$E(\text{target}_{\leq 30}) = E(2, 3) \quad \begin{array}{l} 2 - \text{Yes's} \\ 3 - \text{No's} \end{array}$$

$$= -\frac{2}{5} \log_2\left(\frac{2}{5}\right) - \frac{3}{5} \log_2\left(\frac{3}{5}\right)$$

$$E(\text{target}_{\leq 30}) = 0.970$$

$$E(\text{target}_{\leq 30}, \text{income}) = P(\text{high})E(y, \text{high}) + P(\text{medium})E(y, \text{medium}) + P(\text{low})E(y, \text{low})$$

	yes	no
high	2	2
medium	1	1
low	1	0

$$= \frac{2}{5} E(0, 2) + \frac{2}{5} E(2, 2) + \frac{1}{5} E(1, 0)$$

$$= \frac{2}{5}(0) + \frac{2}{5} + \frac{1}{5}(0)$$

$$= 0.4$$

$$\text{Gain}(\text{target}_{\leq 30}, \text{income}) = E(\text{target}_{\leq 30}) - E(\text{target}_{\leq 30}, \text{income})$$

$$= 0.970 - 0.4$$

$$= 0.570$$

$$E(\text{target}_{\leq 30}, \text{student}) = P(\text{no}) \cdot E(y, \text{no}) + P(\text{yes}) \cdot E(y, \text{yes})$$

$$= \frac{3}{5} E(0, 3) + \frac{2}{5} E(2, 0)$$

$$= \frac{3}{5}(0) + \frac{2}{5}(0)$$

$$= 0$$

$$\begin{aligned} \text{Gain}(\text{target}, \leq 30)_{\text{Student}} &= 0.970 - 0 \\ &= 0.970 \end{aligned}$$

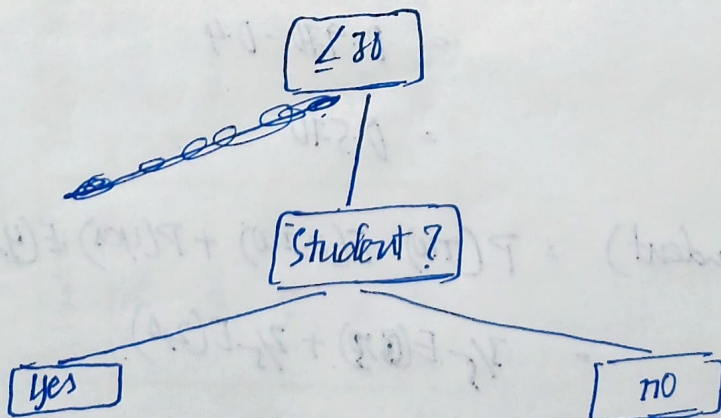
$$\begin{aligned} E(\underbrace{\text{target}, \leq 30}_y, \text{Credit-Rating}) &= P(\text{fair}) \cdot E(y, \text{fair}) + P(\text{excellent}) \cdot E(y, \text{excellent}) \\ &= \frac{3}{5} E(1, 2) + \frac{2}{5} E(1, 1) \\ &= 0.6591 \end{aligned}$$

$$\begin{aligned} \text{Gain}(\text{target}, \leq 30)_{\text{Credit-Rating}} &= 0.970 - 0.6591 \\ &= 0.310 \end{aligned}$$

By Comparing Information Gain from 3 attributes
in ≤ 30 group

Income	Student	Credit-Rating
0.570	0.6591	0.310
	0.970	

Student has highest Information Gain.



≤ 80

Student?

No

Yes

Income	Credit	Class
high	fair	no
high	excellent	no
high med	fair	no

Income	Credit	Class
low	fair	yes
med.	excellent	yes
		yes

As samples of both yes & no have ~~class~~ Pure class
~~their data~~ further Partitioning is not needed.

≤ 80

Student?

no

yes

no

yes

Now Consider >40 group

$$E(\underbrace{\text{target}, >40}_K) = E(1,2)$$

1 - yes's
2 - no's

$$= 0.970$$

$$E(K, \text{income}) = P(\text{medium}) \cdot E(K, \text{med}) + P(\text{Low}) \cdot E(K, \text{Low})$$

$$= \frac{1}{5} E(2,1) + \frac{4}{5} E(1,1)$$

$$= \cancel{0.950} 0.951$$

$$E(K, \text{Student}) = P(\text{yes}) \cdot E(K, \text{yes}) + P(\text{no}) \cdot E(K, \text{no})$$

$$= \frac{1}{5} E(2,1) + \frac{4}{5} E(1,1)$$

$$= 0.951$$

$$E(K, \text{Credit Rating}) = P(\text{fair}) E(K, \text{fair}) + P(\text{excellent}) \cdot E(K, \text{excellent})$$

$$= \frac{1}{5} E(3,1) + \frac{4}{5} E(0,2)$$

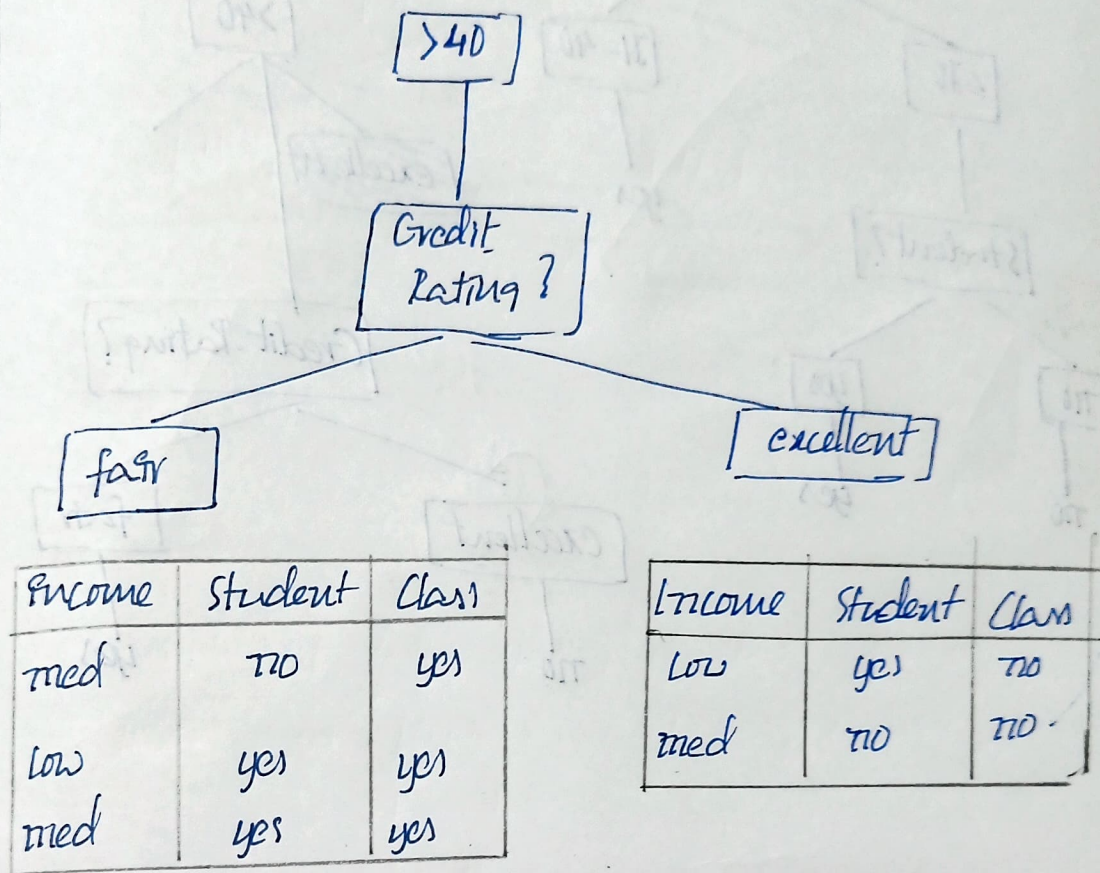
$$= 0$$

$$\text{Gain}_{\text{income}}(\text{target}, >40) = 0.970 - 0.951 = 0.02$$

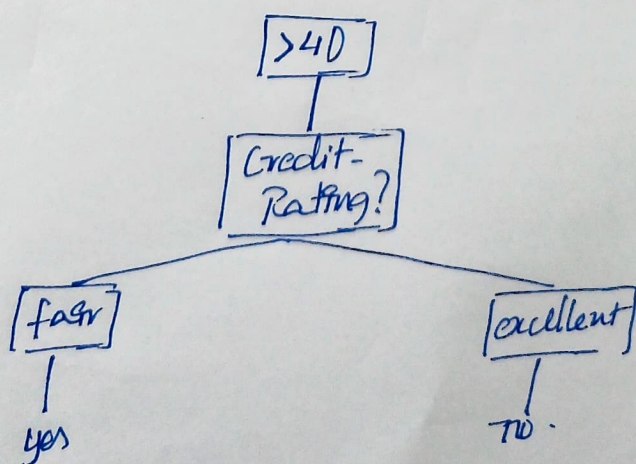
$$\text{Gain}_{\text{Student}}(\text{target}, >40) = 0.970 - 0.951 = 0.02$$

$$\text{Gain}_{\text{credit}}(\text{target}, >40) = 0.970 - 0 = 0.970$$

Credit-Rating has highest information gain in >40 group.



As samples of both fair & excellent have Pure Classes, further Partitioning is not needed and assign the labels respectively.



Root

Age?

≤ 30

31-40

> 40

Student?

no

yes

No

yes

yes

Credit Rating?

fair

excellent

yes

No