

Range Optimised Duoram

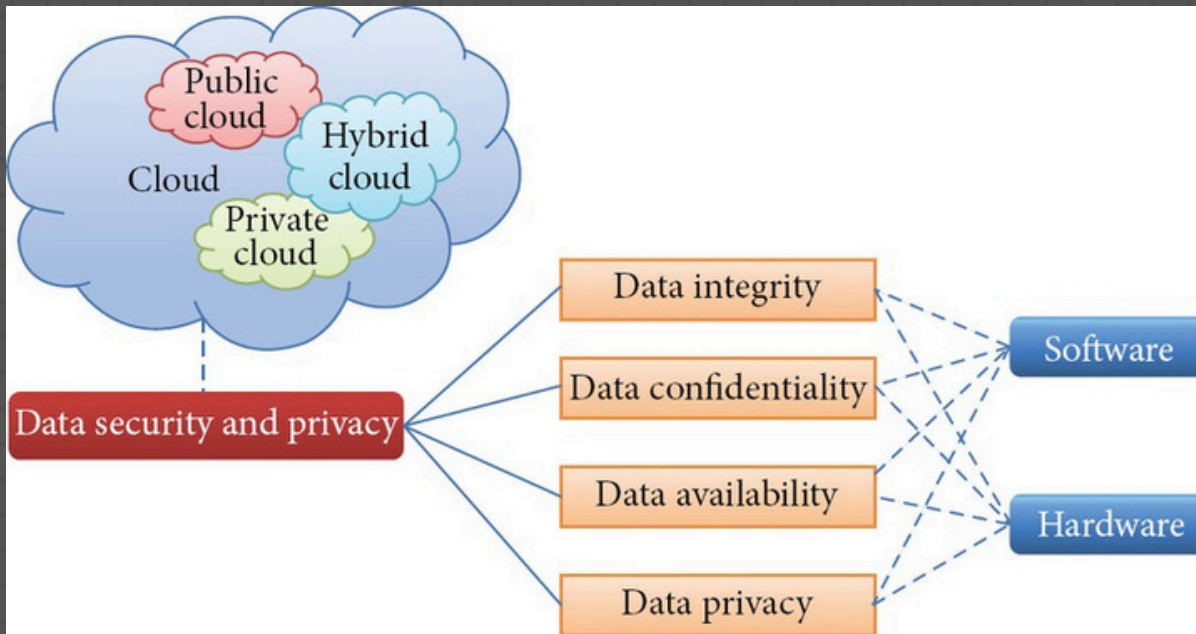
UGP PRESENTATION



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INTRODUCTION



SRC: SAGE JOURNALS

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ENCRYPTING

2

ACCESS PATTERN
LEAKS

3

ORAM

4

COMPUTATIONAL
COSTLY

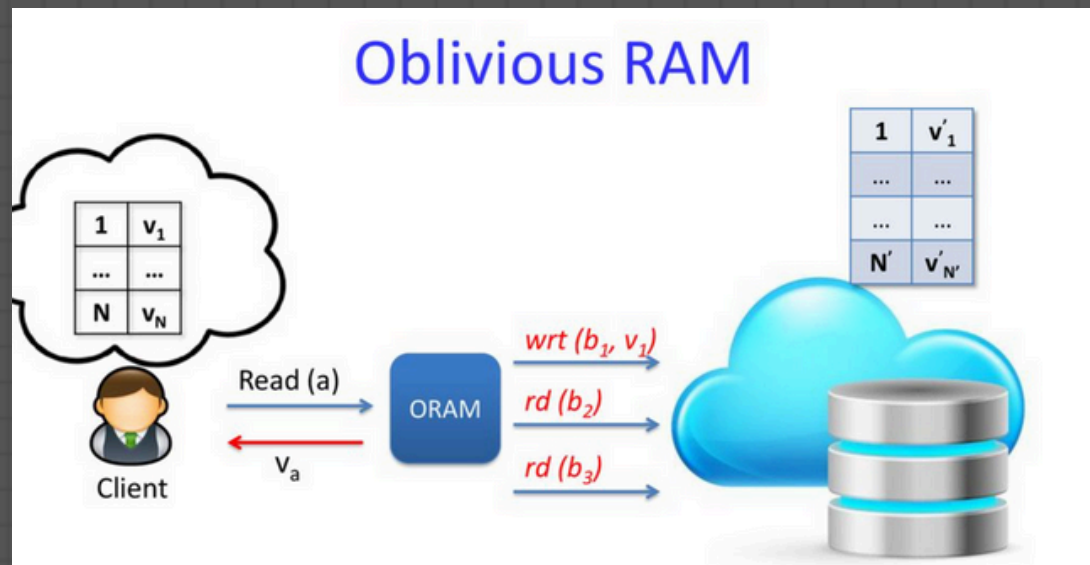
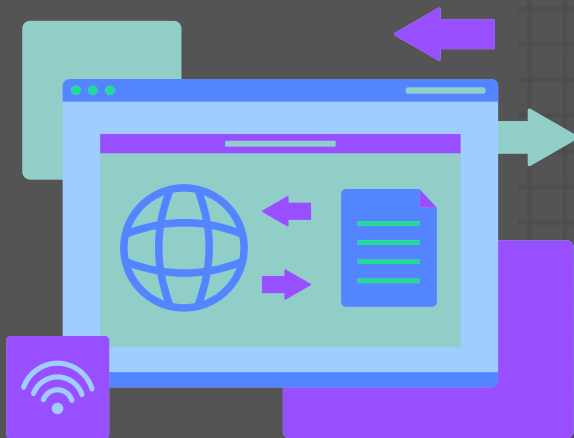
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TRADE OFF BTW COST
& PRIVACY

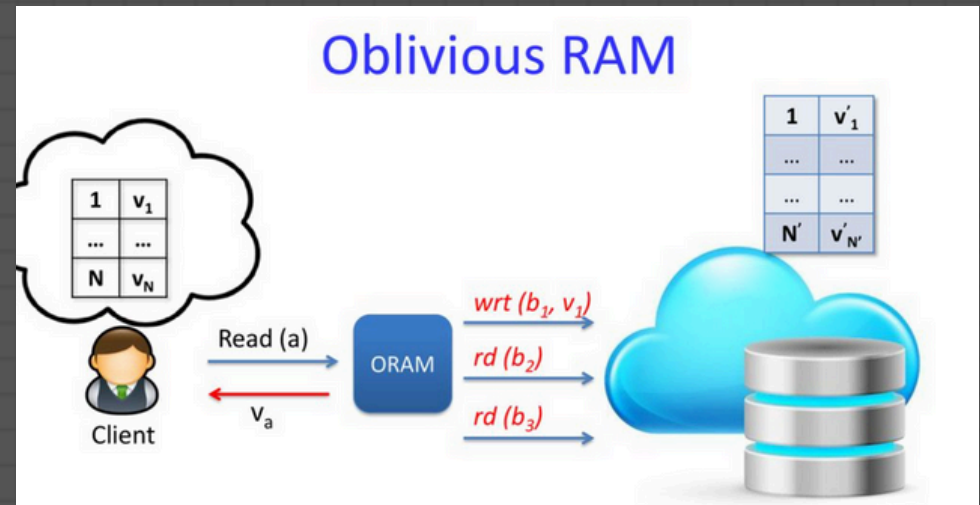
WHY CARE ABOUT ACCESS PATTERN PRIVACY

In secure systems like encrypted databases or cloud storage, even encrypted data leaks information through access patterns (e.g., repeated access to the same location reveals user preferences).

Oblivious RAM (ORAM) protocols mask these patterns, making all accesses appear indistinguishable to prevent such leaks.



ORAM TO THE RESCUE



1

ORAM (Oblivious RAM) hides which data the user is accessing from the server.

2

It works by reading and writing extra data and shuffling block locations after each access.

3

This makes every access look the same to the server, protecting user privacy.

DIFFERENTIAL PRIVACY

- *Differential Privacy ensures that the output of a computation doesn't significantly change when a single individual's data is added or removed, protecting their presence.*
- *It is controlled by two parameters: ϵ (privacy loss) and δ (failure probability), where smaller values imply stronger privacy.*



Analysis \mathcal{M} satisfies differential privacy if...

For all D_1 and D_2 which **differ in one individual's data...**

Answer A and answer B are **indistinguishable**

DIFFERENTIAL PRIVACY EXAMPE

Suppose a researcher wants to know:

"Have you ever cheated in an exam?"

*But of course, people may not feel safe answering honestly,
even if the survey is anonymous.*

*So, to protect individuals' privacy, we use the randomized
response technique.*



Randomized Response Mechanism:

Each person does the following privately:

Flip a coin.

If heads, answer truthfully.

If tails, flip the coin again:

If heads, answer "Yes".

If tails, answer "No".



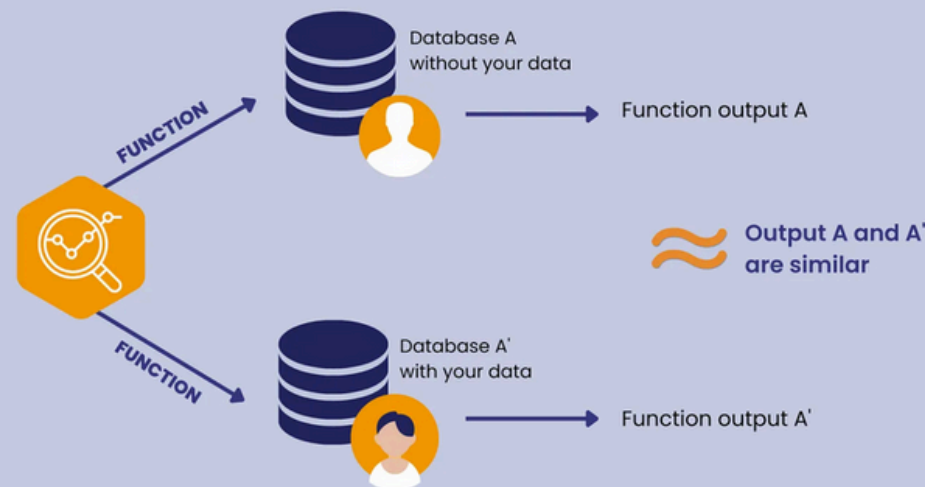
Let's assume 1000 people participate.

*Because of the second coin flip (when the first is
tails), random noise is introduced. So even if
someone says "Yes", you can't tell if:*

They actually cheated and told the truth, or

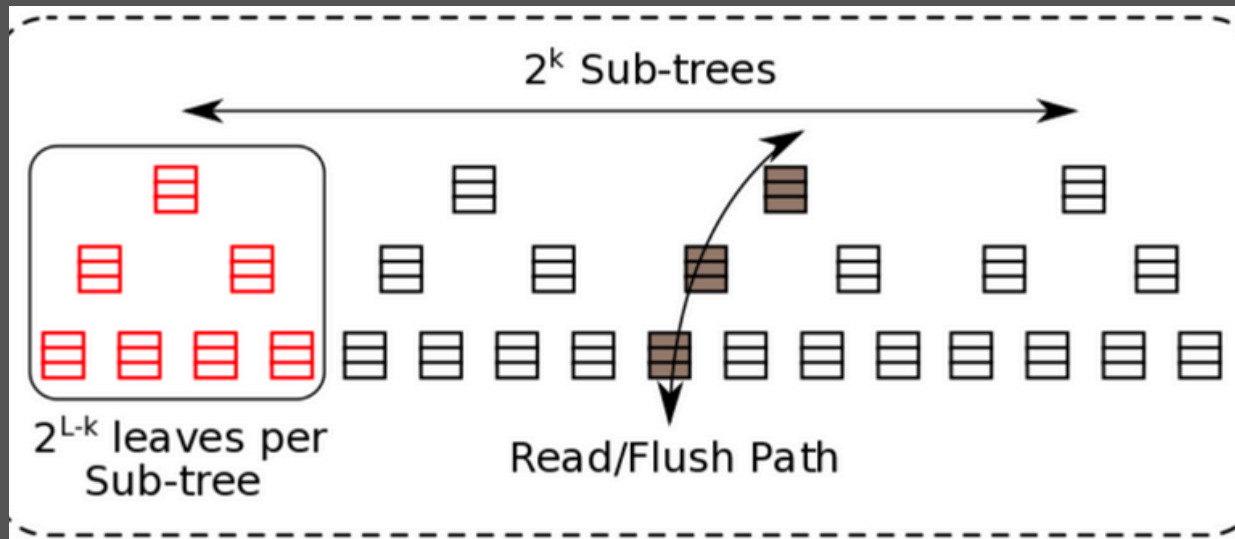
The randomization made them say "Yes".

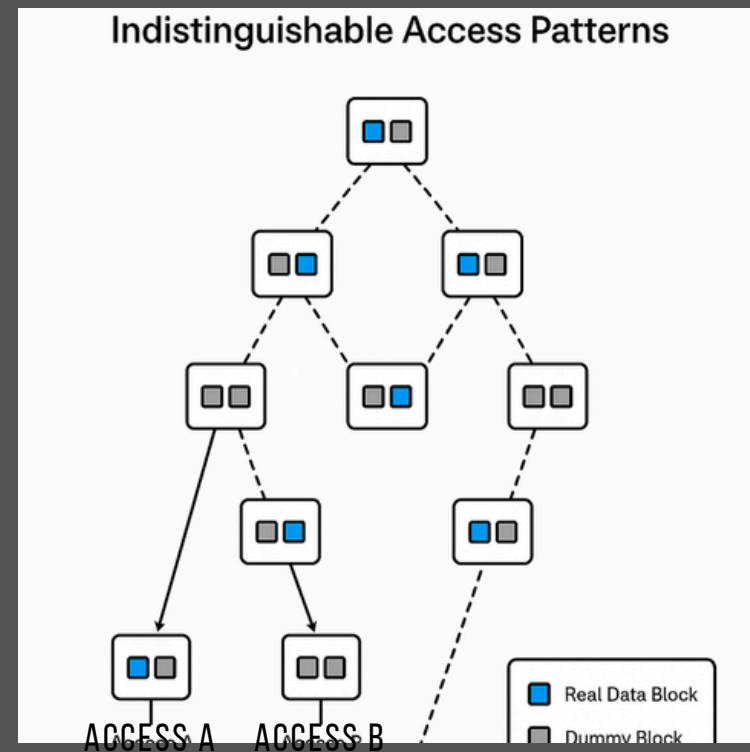
This gives each participant plausible deniability.



ABOUT THE ROOT ORAM

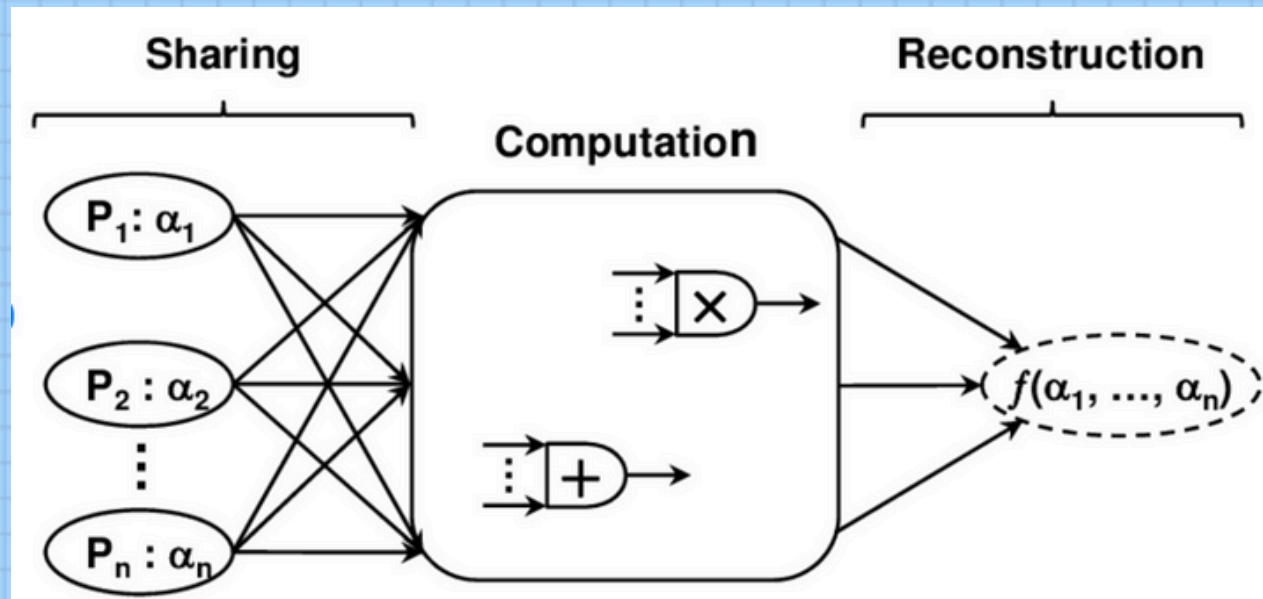
- *Root ORAM splits the data into subtrees and stores them in separate roots. To access a block, the client downloads a path from the corresponding root to a leaf and reshuffles the block along a new random path to hide access patterns.*





In differentially private ORAMs (like Root ORAM), this is done by using a differential privacy mechanism, which assigns higher probabilities to access paths that are closer to the previously used path, and lower probabilities to others, in a way that the overall leakage remains within a DP bound.

THE DISTRIBUTED ORAM



Multi-Party Computation (MPC):

- *Secure MPC allows multiple parties to jointly compute a function over their inputs without revealing those inputs to each other.*
- *Each party learns only the output—nothing more—ensuring privacy even if parties don't fully trust each other.*

7. Eviction and
refreshing blinds

6. Client Processing

5. Server-Side Path
Access

4. Adjust DPFs

3. Read/Write at index
 i^*

2. database as additive
secret shares

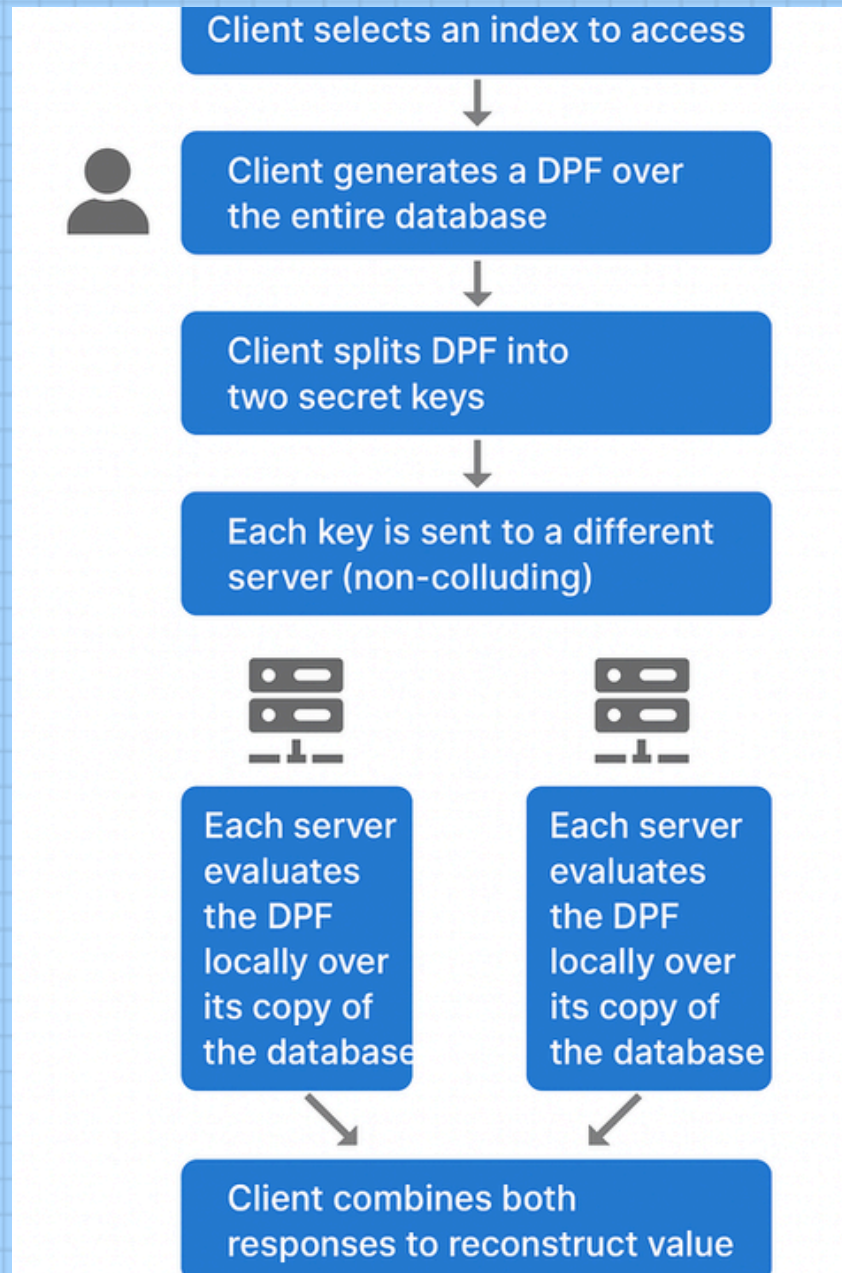
1. Generate DPFs

THE DISTRIBUTED ORAM

*DUORAM = Distributed ORAM for
MPC:*

- *Specially designed for 2-party and 3-party
secure computations.*
- *Stores memory as secret shares (no party knows
the full data).*
- *Enables read/write operations with access
patterns fully hidden.*

THE DISTRIBUTED ORAM



WHERE WE NEED TO FOCUS

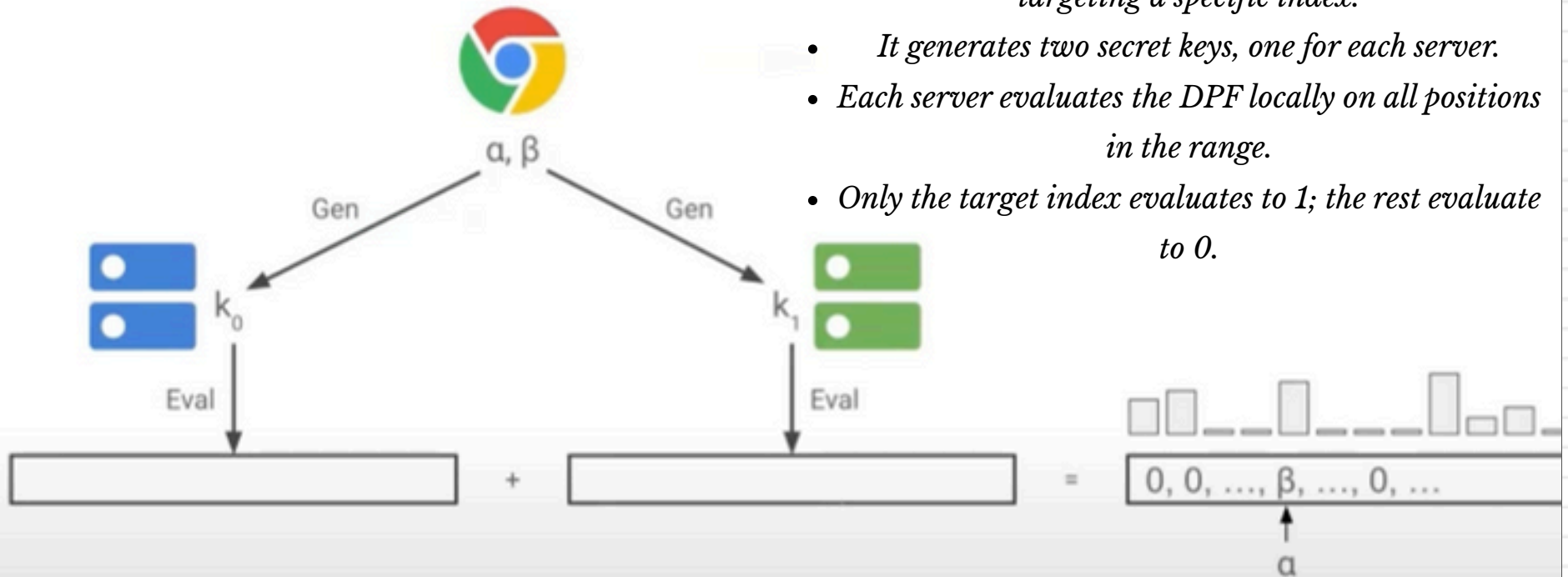
Memory Sharing:

Database is split into additive shares: Party P_0 holds D_0 , P_1 holds D_1 ($D = D_0 + D_1$).

Key Technique:

*Distributed Point Functions (DPFs)
Represent a single index access compactly. Allow reads/writes to be secret-shared and efficient.*

Distributed Point Functions



DISTRIBUTED POINT FUNCTION (DPF)

RETHINKING DPF USAGE FOR EFFICIENT DUORAM

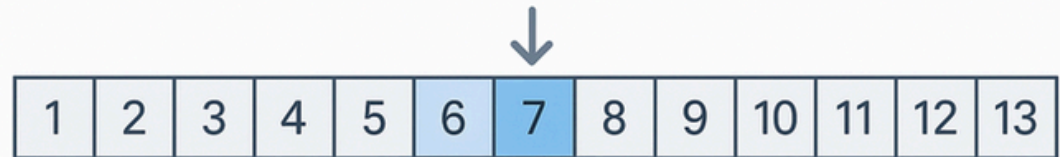
Efficiency Gains

- DPF generation and evaluation cost is linear in the range size ($O(s)$).
- Smaller ranges significantly speed up computation.

Privacy Leakage

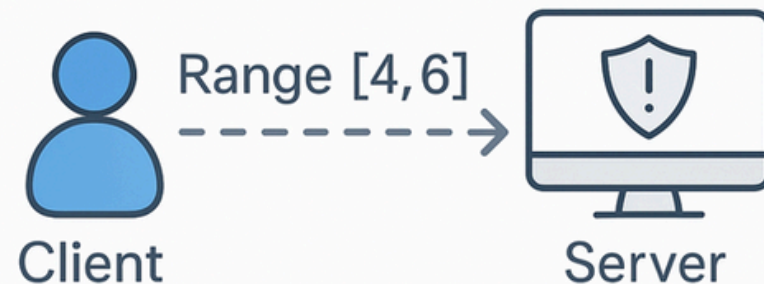
- Sending a small range with the secret key reveals that access lies within it.
- Smaller ranges improve efficiency but increase the adversary's chance of guessing the target.

Smaller Range Improves DPF Efficiency

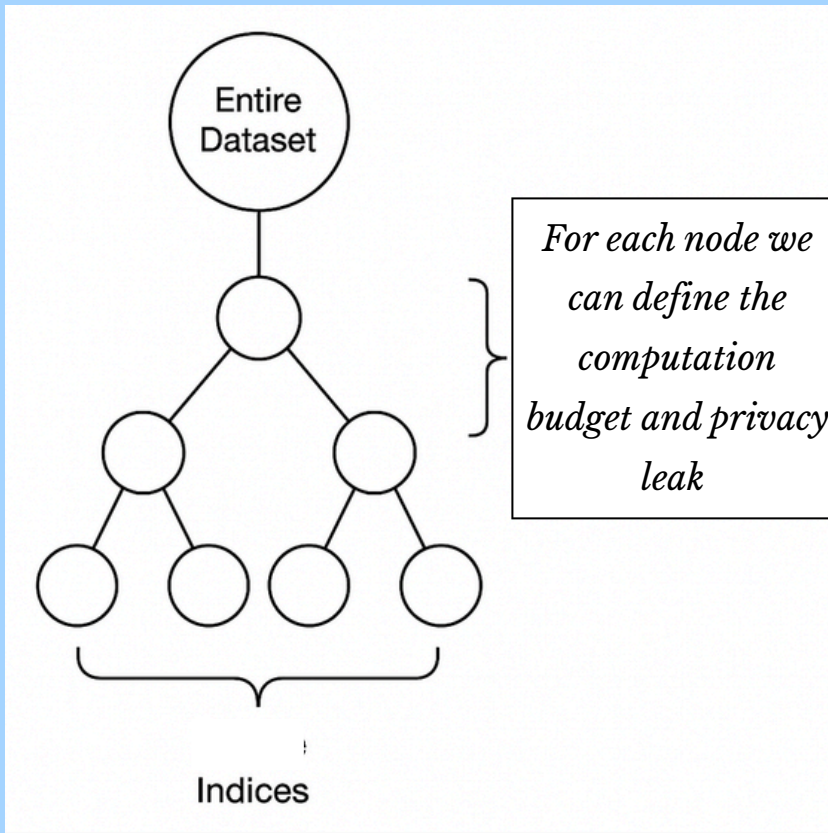


Shorter range

Sending the Range Leaks Privacy



DPFS WITH SMALLER RANGE



Organize n indices in a binary tree (depth = $\log_2 n$)

Each node = a possible query range



Client identifies which index they want to query



Choose a Range (Node on Path to Root)

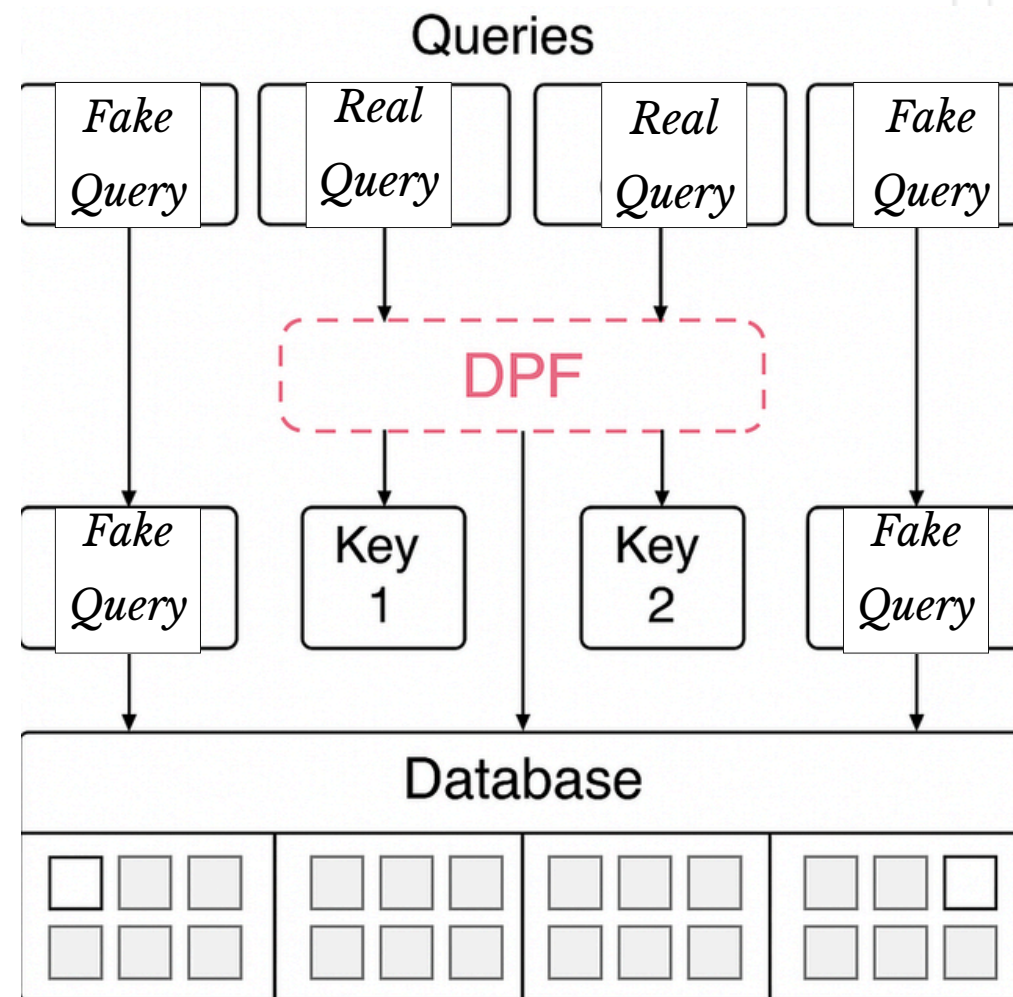


Compute DPF over Range



Ensure Constraints Hold & Send DPF Key + Range → Server

PREVIOUS ATTEMPT: INTRODUCING FAKE QUERIES ALONG WITH SHORT RANGE



How It Works:

- Insert fake queries alongside real queries
- Divide database into smaller segments
- Build DPFs only over accessed segments
- Adjust number of fake queries and segment size

PROBLEM WITH THE PREVIOUS ATTEMPT

- *Fake queries increase communication and computation overhead, reducing the performance gains from smaller DPF domains.*



- *Deterministic fake queries reveal patterns, enabling the server to infer them over time.*



- *Smaller, randomized DPF ranges with DP noise can achieve (ϵ, δ) -privacy more efficiently, without the need for fake queries.*

PROBLEM WITH THE PREVIOUS ATTEMPT

Drawbacks of Fake Queries

Increased Bandwidth & Computation Overhead

Fake queries add communication and computation costs.

This reduces the efficiency of using smaller DPFs.

⚠ Fake Queries Can Be Statistically Distinguishable

Patterns in fake queries may weaken privacy guarantees.

Fake queries introduce new side-channels.

✓ Differential Can Be Achieved Without Fake Queries

Just use smaller DPF ranges with real queries only.

Just using smaller DPF ranges with DP.

WHAT THE FUTURE HOLDS



- *Develop smarter algorithms to dynamically choose range sizes based on real-time privacy and efficiency needs.*
- *Optimise server-side processing for even faster queries.*
- *Explore advanced differential privacy mechanisms to further reduce leakages.*

References

Duoram: A Bandwidth-Efficient Distributed ORAM for 2- and 3-Party Computation

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THANKS

