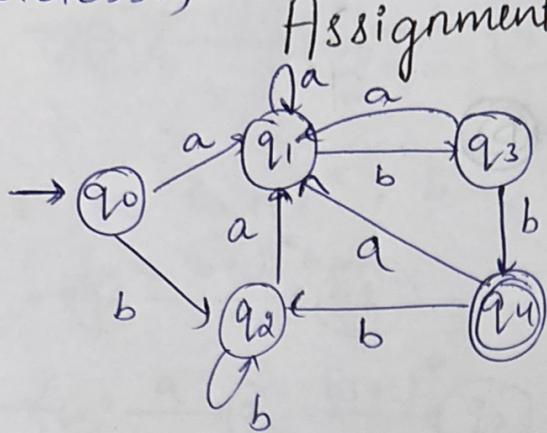


(2301010350)

Assignment - 02

Q1.



Minimize the DFA

 $S_1 \rightarrow$ remove unreachable state. $S_2 \rightarrow$ classes \rightarrow 1. Accepting (final)
2. Non-Accepting (Non-final)

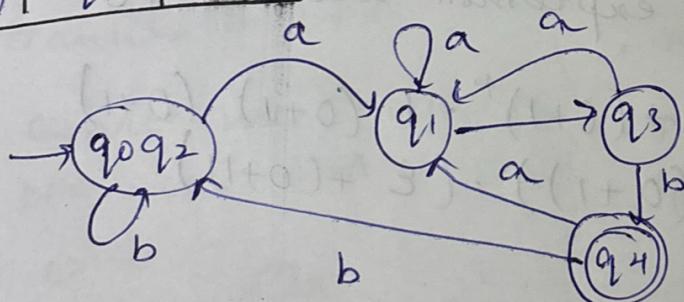
Transition Table

δ	a	b
q_0	q_1	q_2
q_1	q_1	q_3
q_2	q_1	q_2
q_3	q_1	q_4
q_4	q_1	q_2

$$\pi_0 = \{q_0, q_1, q_2, q_3\} \{q_4\}$$

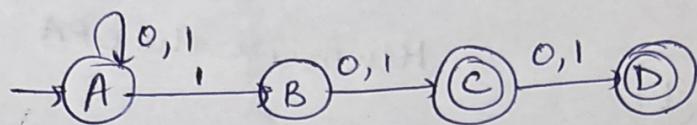
$$\pi_1 = \{q_0, q_1, q_2\} \{q_3\} \{q_4\}$$

$$\pi_2 = \{q_0, q_2\} \{q_1\} \{q_3\} \{q_4\}$$



Q2

Ans 2. NFA to RE



$$A = \epsilon + A \cdot 0 + A \cdot 1$$

$$B = A \cdot 1$$

$$C = B \cdot 0 + B \cdot 1$$

$$D = C \cdot 0 + C \cdot 1$$

By using arden's theorem ,

$$R = Q + RP \\ \text{so, } R = QP^*$$

$$A = \epsilon + (0+1)A$$

$$A = (0+1)^*$$

put in B

$$B = (0+1)^* \cdot 1$$

put in C

$$C = (0+1)^* \cdot 1(0+1)$$

$$D = (0+1)^* \cdot 1(0+1) \cdot (0+1)$$

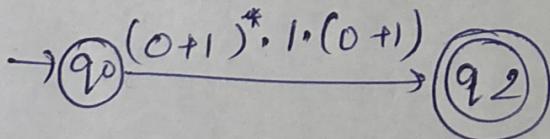
So, final regular expression will be $C + D$

$$(0+1)^* \cdot 1(0+1) + (0+1)^* \cdot 1 \cdot (0+1) \cdot (0+1)$$

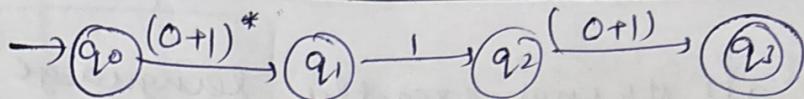
$$((0+1)^* \cdot 1 \cdot (0+1)) \cdot (\epsilon + (0+1))$$

Q3.

$$\text{Ans 3. } (0+1)^* \cdot 1 \cdot (0+1)$$

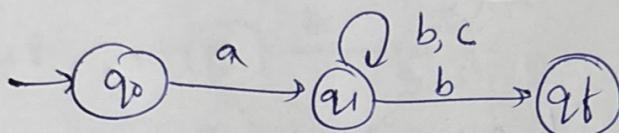
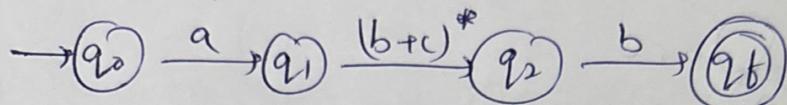
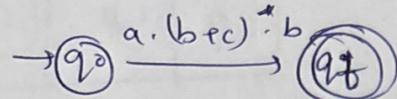


As there are two multiplication there will be
two states,



Q4.

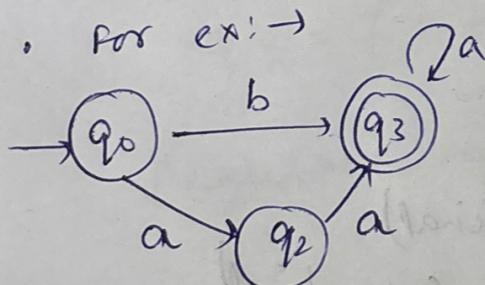
Ans 4. $a \cdot (b+c)^* \cdot b$



Q5.

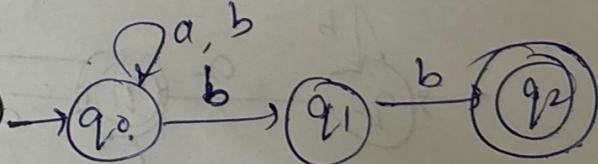
Ans 5. DFA

- DFA stands for Deterministic Finite Automata.
- For each symbolic representation of the alphabet, there is only one transition in DFA
- DFA cannot use ϵ -transition
- All DFA are NFA



NFA

- NFA stands for Non-deterministic FA
- No need to specify how does the NFA react acc. to some symbol
- NFA can use ϵ -transition
- Not all NFA are DFA
- For ex: $\xrightarrow{\quad} q_0 \xrightarrow{a,b} q_1 \xrightarrow{b} q_2$



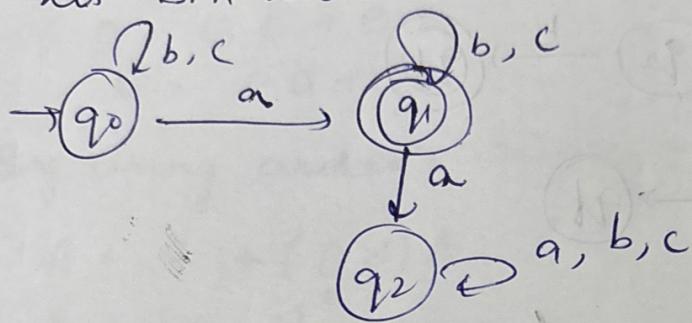
Q6-

Ans 6 It accepts all strings exactly language

$\Rightarrow \{ a, ab, abc, cab, cba, ccbba, \dots \}$

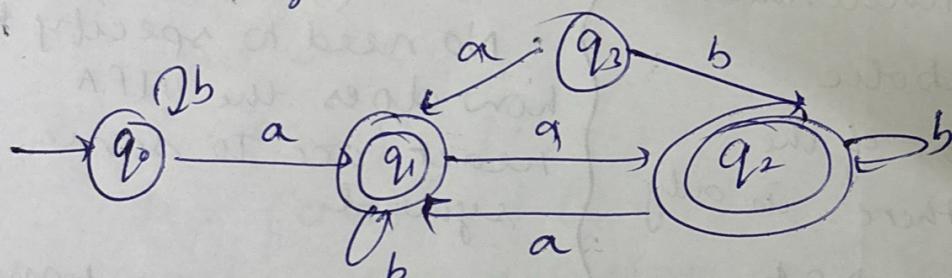
$$RE = (b+c)^* a (b+c)^*$$

its DFA will be:-

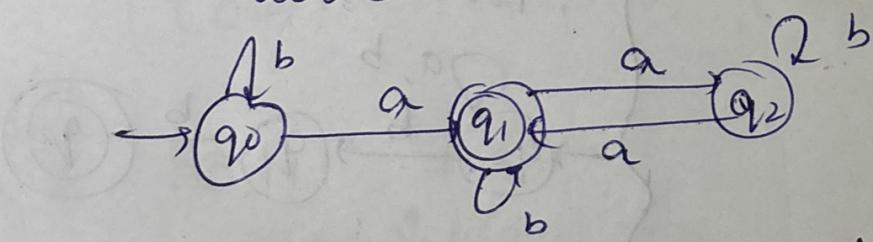


Q7

Ans 7 Minimize the DFA.

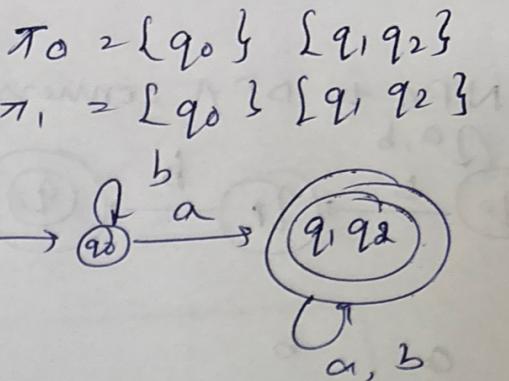


S1 \rightarrow remove unreachable state q_3 is
unreachable state.



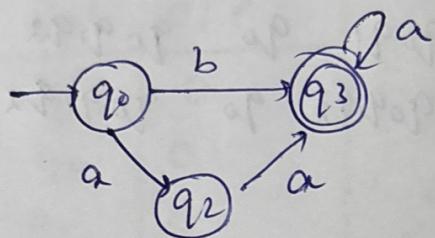
S2 \rightarrow classes \rightarrow 1) Accepting (final)
2) Non Accepting (Non-final)

δ	a	b
q_0	q_1	q_0
q_1	q_2	q_1
q_2	q_1	q_2



Q8.

Ans 8.



Using Arden's theorem

$$q_1 \rightarrow \epsilon$$

$$q_2 = q_1 \cdot a$$

$$q_3 = q_1 b + q_2 a + q_3 a$$

Put values of q_1 & q_2 in q_3

$$q_3 \rightarrow b + a a + q_3 a$$

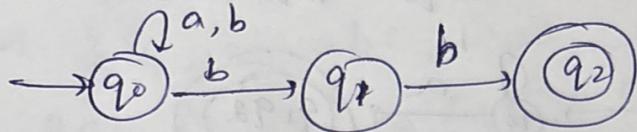
by using $R = Q + RP$
 $R = QP^*$

$$q_3 = (b + aa) + q_3 a$$

$$\text{Regular exp.} = (b + aa) \cdot a^*$$

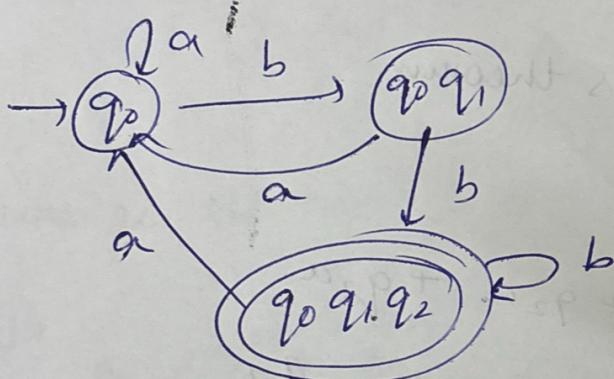
Q9.

Ans 9. NFA to DFA conversion



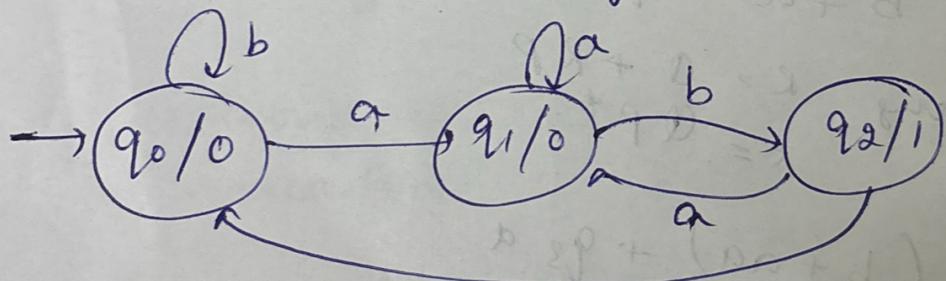
δ	a	b
q_0	q_0	$q_0 q_1$
q_1	-	q_2
q_2	-	-

δ	a	b
q_0	q_0	$q_0 q_1$
$q_0 q_1$	q_0	$q_0 q_1 q_2$
$q_0 q_1 q_2$	q_0	$q_0 q_1 q_2$

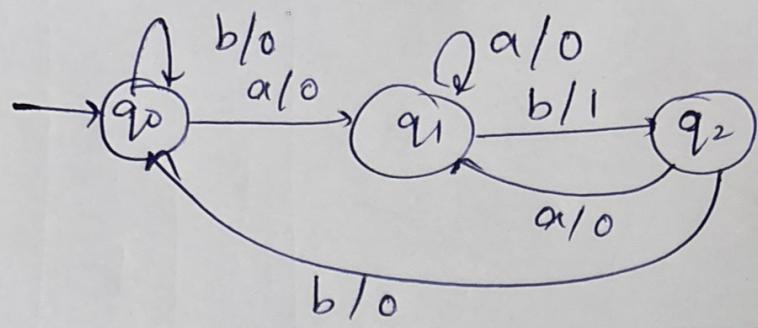


Q10.

Ans 10. Moore to Mealy Conversion :-



δ	New state		O/P
	a	b	
q_0	q_1	q_0	0
q_1	q_1	q_2	1
q_2	q_1	q_0	



δ	a		b	
	state	O/P	state	O/P
q_0	q_1	0	q_0	0
q_1	q_1	0	q_2	1
q_2	q_1	0	q_0	0