REPORT-4

cfunHDDC with Fourier Basis

| Initializer | Threshold | Alphamin | Eta1 | Eta2 | CCR | Class 1 Outliers | Class 2 Outliers |
|-------------|-----------|----------|----------|----------|-------|---------------------|--|
| | 0.001 | 0.5 | 4.851801 | 12.54592 | 0.76 | 27/67 | 106/133 |
| | | 0.6 | 4.851801 | 12.54592 | 0.76 | 27/67 | 106/133 |
| | | 0.7 | 4.881624 | 12.56158 | 0.76 | 27/67 | 106/133 |
| | | 0.8 | 5.192161 | 12.9742 | 0.76 | 28/67 | 110/133 |
| | | 0.85 | 5.634242 | 12.22906 | 0.76 | 29/67 | 113/133 |
| | | 0.9 | 5.775491 | 12.1989 | 0.76 | 33/67 | 113/133 |
| | | 0.95 | 7.390356 | 12.47509 | 0.755 | 39/67 | 113/133 |
| | 0.01 | 0.5 | 4.916504 | 12.98552 | 0.745 | 26/67 | 107/133 |
| | | 0.6 | 4.916504 | 12.98552 | 0.745 | 26/67 | 107/133 |
| | | 0.7 | 4.941505 | 13.02134 | 0.745 | 26/67 | 107/133 |
| kmeans | | 0.8 | 5.099383 | 13.04572 | 0.745 | 27/67 | 107/133 |
| | | 0.85 | 5.117947 | 12.64636 | 0.745 | 29/67 | 110/133 |
| | | 0.9 | 6.287614 | 11.33169 | 0.75 | 31/67 | 106/133 106/133 110/133 113/133 113/133 107/133 107/133 107/133 |
| | | 0.95 | 5.20952 | 13.98913 | 0.765 | 48/67 | 130/133 |
| | | 0.5 | 3.660024 | 15.92869 | 0.74 | 19/67 | 108/133 |
| | | 0.6 | 3.714448 | 15.7564 | 0.74 | 19/67 | 108/133 |
| | | 0.7 | 3.807025 | 15.36336 | 0.74 | 21/67 | 110/133 |
| | 0.05 | 0.8 | 4.336278 | 14.6707 | 0.745 | 28/67 | 113/133 |
| | | 0.85 | 4.698932 | 14.18823 | 0.735 | 23/67 | 110/133 |
| | | 0.9 | 4.896812 | 13.49985 | 0.735 | 27/67 | 111/133 |
| | | 0.95 | 12.96076 | 14.18095 | 0.75 | 38/67 | 117/133 |

| | | 1 | | | | | |
|--|-----|------|----------|----------|-------|-------|---------|
| | 0.1 | 0.5 | 13.83218 | 4.715653 | 0.735 | 20/67 | 108/133 |
| | | 0.6 | 13.77458 | 4.755339 | 0.735 | 20/67 | 108/133 |
| | | 0.7 | 13.73522 | 4.932894 | 0.725 | 24/67 | 110/133 |
| | | 0.8 | 9.991508 | 14.6662 | 0.745 | 36/67 | 117/133 |
| | | 0.85 | 9.959099 | 14.62584 | 0.745 | 36/67 | 117/133 |
| | | 0.9 | 9.880587 | 14.43394 | 0.745 | 38/67 | 117/133 |
| | | 0.95 | 14.60717 | 3.738225 | 0.735 | 36/67 | 117/133 |
| | | 0.5 | 12.09131 | 5.371083 | 0.755 | 25/67 | 108/133 |
| | | 0.6 | 12.10309 | 5.376286 | 0.755 | 25/67 | 108/133 |
| | | 0.7 | 12.14522 | 5.319775 | 0.755 | 25/67 | 108/133 |
| | 0.2 | 0.8 | 12.09836 | 4.748381 | 0.755 | 30/67 | 113/133 |
| | | 0.85 | 4.780299 | 13.42369 | 0.75 | 27/67 | 111/133 |
| | | 0.9 | 4.10241 | 19.68735 | 0.76 | 46/67 | 129/133 |
| | | 0.95 | 4.615807 | 19.27739 | 0.765 | 50/67 | 132/133 |
| | 0.3 | 0.5 | 5.417174 | 21.87661 | 0.74 | 19/67 | 101/133 |
| | | 0.6 | 4.373444 | 24.07831 | 0.735 | 23/67 | 104/133 |
| | | 0.7 | 4.403296 | 23.9974 | 0.735 | 23/67 | 104/133 |
| | | 0.8 | 4.392968 | 23.83858 | 0.74 | 23/67 | 105/133 |
| | | 0.85 | 3.829425 | 23.60799 | 0.74 | 27/67 | 110/133 |
| | | 0.9 | 4.80912 | 22.14721 | 0.75 | 29/67 | 113/133 |
| | | 0.95 | 5.93394 | 3.494555 | 0.55 | 48/67 | 127/133 |
| | 0.4 | 0.5 | 5.417174 | 21.87661 | 0.74 | 19/67 | 101/133 |
| | | 0.6 | 4.373444 | 24.07831 | 0.735 | 23/67 | 104/133 |
| | | 0.7 | 4.403296 | 23.9974 | 0.735 | 23/67 | 104/133 |
| | | 0.8 | 4.392968 | 23.83858 | 0.74 | 23/67 | 105/133 |

| | | 0.95 | 2 920425 | 22 (0700 | 0.74 | 27/67 | 110/122 |
|--------|-------|------|----------|----------|-------|-------|---------|
| | | 0.85 | 3.829425 | 23.60799 | 0.74 | 27/67 | 110/133 |
| | | 0.9 | 4.80912 | 22.14721 | 0.75 | 29/67 | 113/133 |
| | | 0.95 | 9.864785 | 5.109795 | 0.75 | 36/67 | 123/133 |
| | | 0.5 | 7.340147 | 8.721371 | 0.77 | 26/67 | 105/133 |
| | | 0.6 | 7.340147 | 8.721371 | 0.77 | 26/67 | 105/133 |
| | | 0.7 | 7.360263 | 8.758391 | 0.77 | 26/67 | 105/133 |
| | 0.001 | 0.8 | 8.944482 | 7.134026 | 0.78 | 50/67 | 123/133 |
| | | 0.85 | 5.628841 | 6.529131 | 0.79 | 47/67 | 120/133 |
| | | 0.9 | 7.463936 | 4.749399 | 0.795 | 54/67 | 122/133 |
| | | 0.95 | 4.902774 | 7.874592 | 0.795 | 54/67 | 125/133 |
| | | 0.5 | 8.915587 | 6.530792 | 0.77 | 26/67 | 105/133 |
| random | 0.01 | 0.6 | 5.981619 | 9.654887 | 0.765 | 23/67 | 105/133 |
| | | 0.7 | 7.085553 | 7.762559 | 0.84 | 48/67 | 111/133 |
| | | 0.8 | 7.076365 | 7.861789 | 0.84 | 48/67 | 113/133 |
| | | 0.85 | 7.059114 | 7.93761 | 0.84 | 48/67 | 113/133 |
| | | 0.9 | 7.092878 | 8.034011 | 0.835 | 48/67 | 114/133 |
| | | 0.95 | 6.553035 | 6.591264 | 0.795 | 58/67 | 125/133 |
| | | 0.5 | 9.821098 | 6.041657 | 0.775 | 23/67 | 104/133 |
| | | 0.6 | 9.820287 | 6.045162 | 0.775 | 23/67 | 104/133 |
| | 0.05 | 0.7 | 9.803387 | 6.197766 | 0.77 | 23/67 | 106/133 |
| | | 0.8 | 10.99151 | 4.193703 | 0.79 | 29/67 | 103/133 |
| | | 0.85 | 10.94827 | 4.229101 | 0.79 | 30/67 | 103/133 |
| | | 0.9 | 72.10354 | 2.316662 | 0.765 | 51/67 | 132/133 |
| | | 0.95 | 3.489963 | 31.59507 | 0.745 | 54/67 | 131/133 |
| | 0.1 | 0.5 | 2.941184 | 151.8979 | 0.77 | 27/67 | 115/133 |

| | | 0.6 | 2.755144 | 151.9469 | 0.77 | 29/67 | 118/133 |
|--|-----|------|----------|----------|-------|-------|---------|
| | | 0.7 | 2.641318 | 152.7392 | 0.77 | 37/67 | 123/133 |
| | | 0.8 | 2.605505 | 154.0694 | 0.775 | 43/67 | 128/133 |
| | | 0.85 | 2.569878 | 154.3025 | 0.775 | 47/67 | 129/133 |
| | | 0.9 | 2.688531 | 155.0571 | 0.775 | 54/67 | 132/133 |
| | | 0.95 | 10.40805 | 49.47463 | 0.805 | 60/67 | 133/133 |
| | | 0.5 | 15.09518 | 6.592133 | 0.72 | 12/67 | 96/133 |
| | | 0.6 | 14.96766 | 6.472133 | 0.72 | 12/67 | 96/133 |
| | | 0.7 | 3.668319 | 13.75549 | 0.745 | 23/67 | 107/133 |
| | 0.2 | 0.8 | 13.87498 | 3.839593 | 0.71 | 27/67 | 106/133 |
| | | 0.85 | 2.994477 | 13.73651 | 0.77 | 40/67 | 120/133 |
| | | 0.9 | 14.22036 | 3.03651 | 0.765 | 43/67 | 122/133 |
| | | 0.95 | 8.767399 | 7.056145 | 0.785 | 51/67 | 126/133 |
| | 0.3 | 0.5 | 13.9963 | 3.80061 | 0.745 | 21/67 | 105/133 |
| | | 0.6 | 13.86783 | 3.733776 | 0.745 | 22/67 | 107/133 |
| | | 0.7 | 13.75549 | 3.668306 | 0.745 | 23/67 | 107/133 |
| | | 0.8 | 13.00803 | 3.010589 | 0.785 | 35/67 | 116/133 |
| | | 0.85 | 13.73653 | 2.994478 | 0.77 | 40/67 | 120/133 |
| | | 0.9 | 14.22041 | 3.036501 | 0.765 | 43/67 | 122/133 |
| | | 0.95 | 7.056141 | 8.767435 | 0.785 | 51/67 | 126/133 |
| | 0.4 | 0.5 | 7.261258 | 6.068487 | 0.785 | 24/67 | 90/133 |
| | | 0.6 | 7.275038 | 6.075912 | 0.785 | 24/67 | 91/133 |
| | | 0.7 | 7.31652 | 6.065175 | 0.785 | 24/67 | 92/133 |
| | | 0.8 | 7.339745 | 5.971047 | 0.785 | 24/67 | 98/133 |
| | | 0.85 | 6.244864 | 6.961841 | 0.825 | 54/67 | 109/133 |
| | | | | | | | |

| 0.9 | 6.280434 | 6.949104 | 0.815 | 54/67 | 111/133 |
|------|----------|----------|-------|-------|---------|
| 0.95 | 6.304806 | 7.143745 | 0.8 | 54/67 | 116/133 |

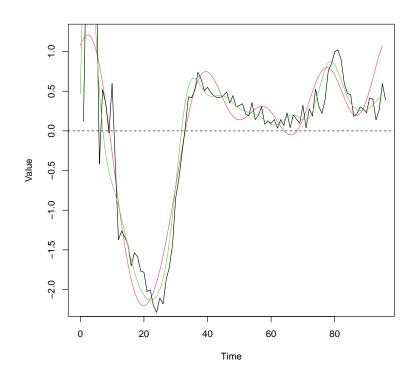
The cfunHDDC algorithm was run on the ECG data converted into a functional data object using a Fourier basis. The parameters were varied according to the table and the CCR for each configuration was recorded. The best model was chosen automatically using the BIC metric. The highest CCR was obtained with the "Threshold" set to 0.01, the "Initializer" set to "random", the "Alphamin" set to 0.7, 0.8 or 0.85. This configuration was able to achieve a CCR of 0.84 on the data. The total number of misclassified labels are 32. This data has a total of 22 outliers from both classes. The number of outliers that are misclassified is 4.

Function Approximation: Fourier vs Bspline (old values)

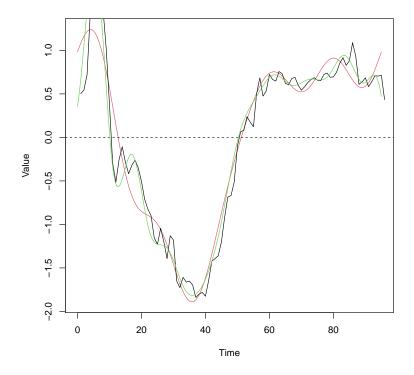
Original data => **BLACK**

Fourier basis => **RED**

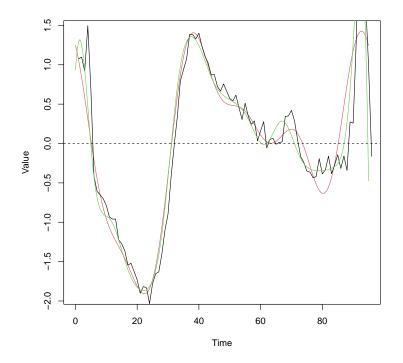
Bspline basis => **GREEN**



Feature Vector 1



Feature Vector 50



Feature Vector 150

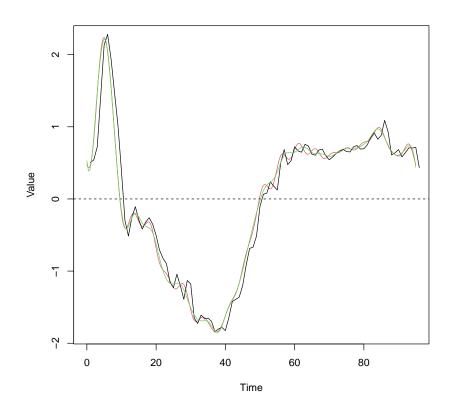
From the example plots we can see that the Bspline basis (20 splines) does a better job of approximation of the original data than the Fourier basis. However, it is interesting to note that even though Fourier basis (11 splines) does not approximate well, it consistently provides the better results while clustering.

Function Approximation: Fourier vs Bspline (new values)

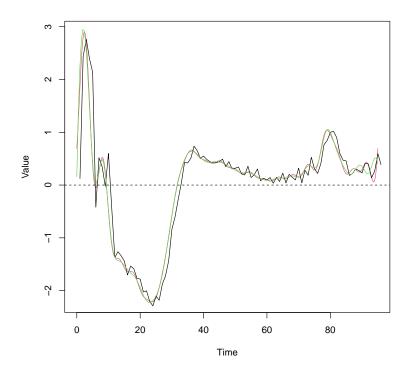
Original data => **BLACK**

Fourier basis => **RED**

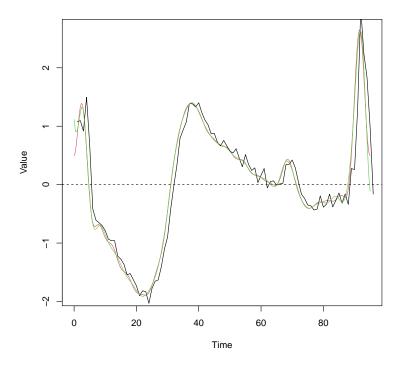
Bspline basis => **GREEN**



Feature Vector 1



Feature Vector 50



Feature Vector 150

From the example plots we can see that both the Bspline basis (38 splines) and Fourier basis (41 splines) do a similar job of approximation of the original data. It can be noted that for both basis the new values perform a lot better than the old values.