

National Institute of Technology, Delhi
Name of the Examination: B. Tech. (Makeup Exam)

Branch : CSE Semester : III
Title of the Course : Probability and Statistics Course Code : MAL241

Time: 3 Hours

Maximum Marks: 50

Note1: Attempt all the question is section A, any four questions in section-B and any two questions in Section C. Attempt all the question in increasing order from Q1 to Q9

Section A

- Q1. (a)** A coin is biased so that a head is twice as likely to occur as a tail. If the coin is tossed 3 times, what is the probability of getting 2 tail and 1 head?
(b) What is Bay's Rule in probability?
(c) Define the Hypergeometric distribution and its density function.
(d) Define continuous and discrete probability distribution.
(e) What is the main difference between Type-I and Type-II error?
(f) State the Gamma distribution with density function.
(g) How to define Jacobian transformation for a continuous random variable X and Y with pdf $f(x)$ and $g(y)$ respectively.
(h) State the central limit theorem.
(i) What is Null and Alternate hypothesis?
(j) State the theorem based on the difference of two sample distribution is approximated by standard normal distribution.

Section B

- Q2.** In a certain industry, accidents occur frequently. It is known that the probability of any accident on a given day is 0.005 and accidents area independent of each other.
(a) What is the probability that in any day of 400 days there will be an accident on one day?
(b) What is the probability that there are at most 3 days with an accident? [3+2]
- Q3.** Suppose that the probability is 0.8 that any given person will believe a tale about transgression of a famous actress. What is the probability that
(a) the sixth person to hear this tale is the fourth one to believe it?
(b) the third person to hear this tale is the first one to believe it? [3+2]
- Q4.** Suppose that two dimensional continuous random variable (X, Y) has joint p.d.f. is given by:

$$f(x, y) = 6x^2y \quad 0 < x < 1, 0 < y < 1$$

 Find
 I. $P(X+Y < 1)$ II. $P(X > Y)$ III. $P(X < 1/Y < 2)$ [2+1+2]
- Q5.** The joint p.d.f. of two random variables X and Y is given by: $f(x, y) = \frac{9(1+x+y)}{2(1+x)^4(1+y)^4}$,
 $0 \leq x < \infty, 0 \leq y < \infty$
 Find
 i. The marginal distribution of X and Y .
 ii. The conditional distribution of Y for $X=x$. [3+2]
- Q6.** A multiple choice quiz has 200 questions each with 4 possible answers of which one is correct answer. What is the probability that sheer guesswork yields from 25 to 30 correct answer for 80 of 200 problems about which the student has no knowledge? [5]

Section C

- Q7. (a)** In a binomial distribution consisting of 5 independent trials, probability of 1 and 2 successes are 0.4096 and 0.2048, respectively. Find the parameter ' p ' of the distribution?
Q7. (b) A manufacturer of cotter pins knows that 5% of his product is defective. If he sells cotter pins in boxes of 100 and guarantees that not more than 10 pins will be defective, what is the approximation probability that a box will fail to meet the guaranteed quality? [5+5]
- Q8. (a)** An insurance company insures 4,000 people against loss of both eyes in a car accident. Based on previous data, the rates were computed on the assumption that on the average 10 person in 100,000 will have car accident each year that result in this type of injury. What is the probability that more than 3 of the insured will correct on their policy in a given year?

