Wine sales prediction

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1. Introduction

A large wine manufacturer is studying data collected on 12,000 commercially available wines, with a goal to predict the number of cases ordered based upon the characteristics. The manufacturer intends to adjust the winde offerings based on the findings. The data collected is related to chemical properties of wine with response variable being the number of sample cases sold to distribution companies. the data also includes features like review stars provided by the tasters and label appeal.

2. Exploratory Data analysis

The below table shows the summary statistics of the data. It is seen that there are missing data. "Stars" has the most missing values. The missing values mostly correspond to NO (0) cases sold. Which is most likely due to lack of opportunity to sample because of none sold.

Table 1: Summary Stats and missing values

	min	Q1	median	Q3	max	mean	sd	n	missing
INDEX	1.00	4037.50	8110.00	12106.50	16129.00	8069.98	4656.91	12795	0
TARGET	0.00	2.00	3.00	4.00	8.00	3.03	1.93	12795	0
FixedAcidity	-18.10	5.20	6.90	9.50	34.40	7.08	6.32	12795	0
VolatileAcidity	-2.79	0.13	0.28	0.64	3.68	0.32	0.78	12795	0
CitricAcid	-3.24	0.03	0.31	0.58	3.86	0.31	0.86	12795	0
ResidualSugar	-127.80	-2.00	3.90	15.90	141.15	5.42	33.75	12179	616
Chlorides	-1.17	-0.03	0.05	0.15	1.35	0.05	0.32	12157	638
${\bf Free Sulfur Dioxide}$	-555.00	0.00	30.00	70.00	623.00	30.85	148.71	12148	647
${\bf Total Sulfur Dioxide}$	-823.00	27.00	123.00	208.00	1057.00	120.71	231.91	12113	682
Density	0.89	0.99	0.99	1.00	1.10	0.99	0.03	12795	0
рН	0.48	2.96	3.20	3.47	6.13	3.21	0.68	12400	395
Sulphates	-3.13	0.28	0.50	0.86	4.24	0.53	0.93	11585	1210
Alcohol	-4.70	9.00	10.40	12.40	26.50	10.49	3.73	12142	653
LabelAppeal	-2.00	-1.00	0.00	1.00	2.00	-0.01	0.89	12795	0
AcidIndex	4.00	7.00	8.00	8.00	17.00	7.77	1.32	12795	0
STARS	1.00	1.00	2.00	3.00	4.00	2.04	0.90	9436	3359

Figure 2 shows the historgram of features in the data. The chemical properties of wines appear to share an identical distribution with peaks closer to zero. This mau be likely to some standardization done to the day. The variable "TARGET" looks to be poisson or negative biniomially distributed with inflation at 0.

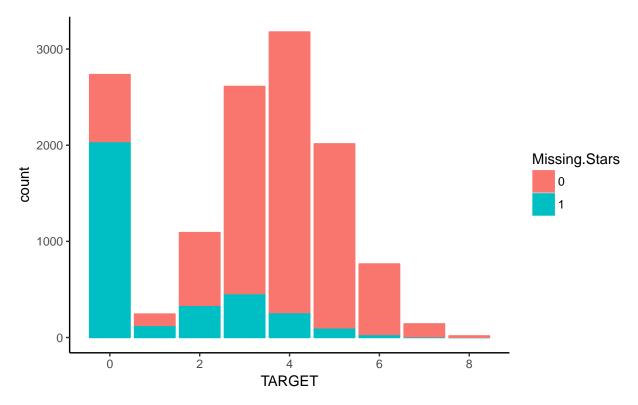


Figure 1: Missing STARS values' association with Number of cases sold

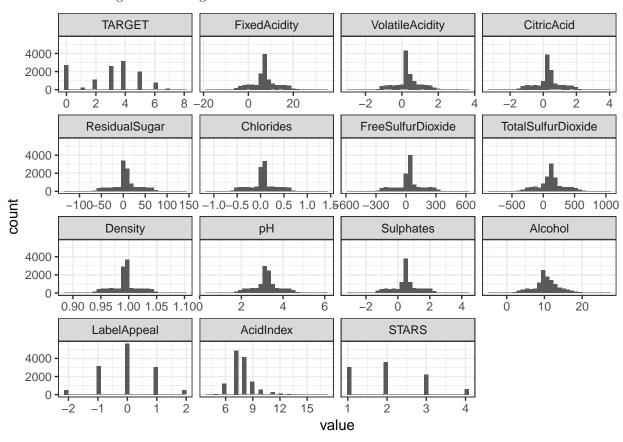


Figure 2: Histograms of features

3. Feature selection

In this section we'll attempt to select important features that explain the target variable. We'll explore the correlations that might exist in the data. There is positive correlations between TARGET and STARS and LabelAppeal.

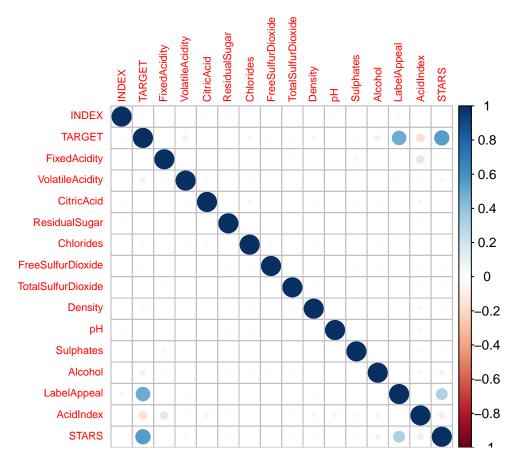


Figure 3: Correlation plot

It'll be useful to identify what contributes to the zero inflation in the TARGET variable. For which let's create an indicator variable "TARGET0" to equal 1 when TARGET is 0 and 0 otherwise.

3.1 Decision Trees

3.1.1 Predictors for zero cases sold (No sale)

Figure 4 shows the decision tree for TARGET0. Where 1 is no sale (cases sold = 0) and 0 is sale (cases sold > 0). Figure 5 shows the variable importance plot after a random forest bootstrap. While LabelAppeal did not contribute to node purity (Decrease in Gini index), it did affect accuracy on out of bag (OOB) samples.

3.1.2 Predictors for cases sold; when successfuly sold (cases > 0)

Figure 6 shows the decision tree of cases sold when they are greater than 0. It can be seen that the LabelAppeal and STARS are the top hitters. Figure 7 shows the variable importance plot when a random forest method is employed, where a random set of predictors are chosen at each iteration to fit a decision tree. Variables

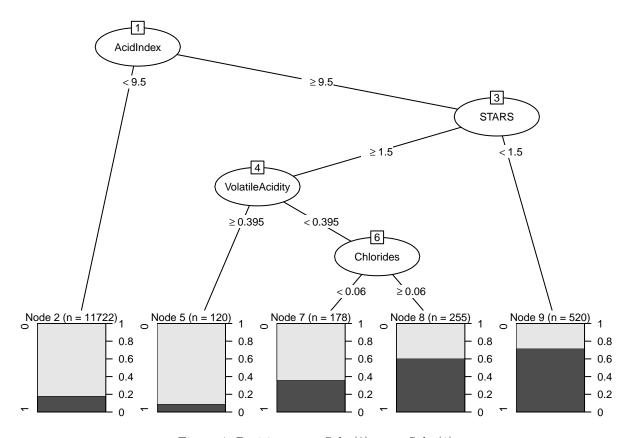


Figure 4: Decision tree - Sale (0) or no Sale (1)

whose exclusion contributes to higher Mean Squared Error (MSE) is deemed important. LabelApeal, STARS and Alcohol are top 3 variables that are important.

Variable Importance plot - Random forest

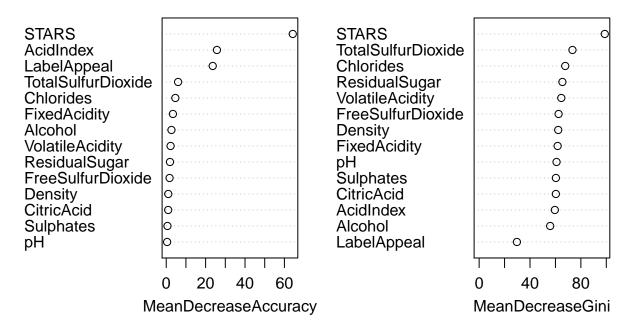


Figure 5: Variable Importance - Randomforest

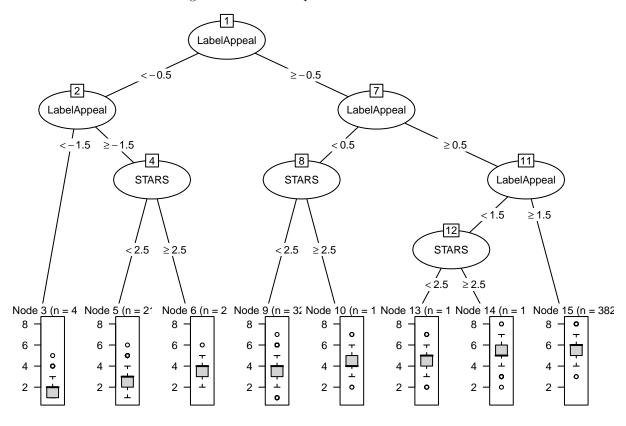


Figure 6: Simple tree for TARGET

Variable importance plot from random forest – TARGET

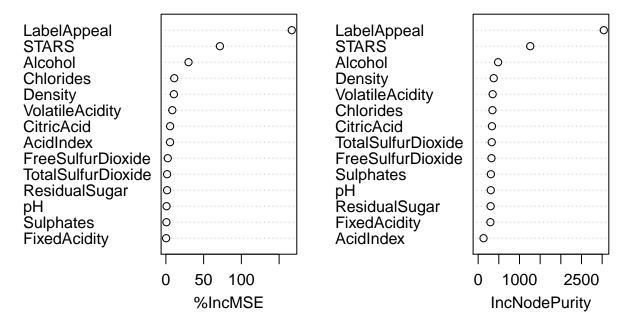


Figure 7: Variable importance plot - TARGET

4. Training and validation samples

The data is split into training and validation sample for evaluating models for final selection. The 75% of the data is sampled as training sample and the rest is set aside as validation set. Figure 8 shows that the TARGET variable is identically distributed for both training and validation samples.

5. Modeling

The following modeling approaches will be tried for predicting the number of cases sold.

- Poisson regression
- Negative binomial regression
- Zero infalted Poisson regression
- Zero inflated Negative binomial regression
- OLS regression

5.1 Poisson regression.

As seen in table 1, the mean and standard deviation of TARGET are not too far apart. Poisson model is a good candidate for regression modeling.

TARGET from training sample

TARGET from test sample

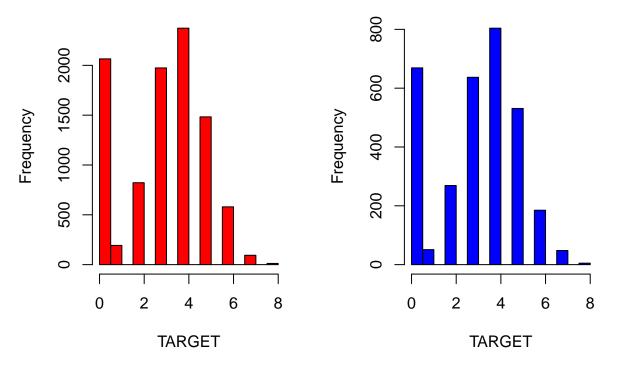


Figure 8: TARGET distribution for training and validation samples

5.1.1 Simple model with Label appeal as the predictor.

While we know that the TARGET variable is zero inflated and there are at least more than one important predictor from the section above, we'll attempt to build the model ground up with LabelAppeal as the single predictor.

```
##
   glm(formula = TARGET ~ LabelAppeal, family = poisson(link = "log"),
##
       data = train)
##
  Deviance Residuals:
##
       Min
                 1Q
                      Median
                                   3Q
                                           Max
## -3.1342
           -0.4281
                      0.1717
                               0.5821
                                        2.0412
##
  Coefficients:
##
               Estimate Std. Error z value Pr(>|z|)
##
                          0.006012
## (Intercept) 1.080397
                                    179.70
                                             <2e-16 ***
## LabelAppeal 0.255594
                          0.006623
                                     38.59
                                              <2e-16 ***
##
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
   (Dispersion parameter for poisson family taken to be 1)
##
##
       Null deviance: 17183
                             on 9595 degrees of freedom
## Residual deviance: 15689
                             on 9594 degrees of freedom
## AIC: 39571
```

```
##
## Number of Fisher Scoring iterations: 5
## Likelihood ratio test
##
## Model 1: TARGET ~ LabelAppeal
## Model 2: TARGET ~ 1
## #Df LogLik Df Chisq Pr(>Chisq)
## 1 2 -19783
## 2 1 -20530 -1 1494.4 < 2.2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1</pre>
```

Table 2: Simple Poisson model statistics

null.deviance	df.null	logLik	AIC	BIC	deviance	df.residual	pseudoR.Sq	MAE
17182.9	9595	-19783.35	39570.7	39585.04	15688.51	9594	0.09	1.39

5.1.1.1 Model interpretation

It can be seen from the Likelihood ratio test above, that the slope of LabelAppeal is NOT zero and an unit increase in label appeal increases by 1. However the model is not an adequate fit with residual deviance over degrees of freedom being much higher than 1 (in comparison to a saturated model). This is also reflected in the Pseudo R Squared value.

The model does not predict 0s. As can be see from figure 9.

5.1.2 Poisson model with Label appeal & Stars as predictors

Now, we'll use Label appeal and stars as predictors and compare the model with the simple model in the above section.

```
##
## Call:
## glm(formula = TARGET ~ LabelAppeal + STARS, family = poisson(link = "log"),
##
       data = train[!is.na(train$LabelAppeal), ])
##
  Deviance Residuals:
##
##
                                        3Q
        Min
                   10
                         Median
                                                 Max
   -3.16162 -0.26871
                        0.04889
##
                                  0.36797
                                             1.65061
##
## Coefficients:
##
               Estimate Std. Error z value Pr(>|z|)
## (Intercept) 0.869060
                          0.016581
                                     52.41
                                              <2e-16 ***
                                     23.65
## LabelAppeal 0.179589
                          0.007595
                                              <2e-16 ***
## STARS
               0.190392
                          0.007074
                                     26.92
                                              <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for poisson family taken to be 1)
##
##
       Null deviance: 6398.3 on 7057
                                       degrees of freedom
## Residual deviance: 4457.8 on 7055
                                       degrees of freedom
     (2538 observations deleted due to missingness)
##
```

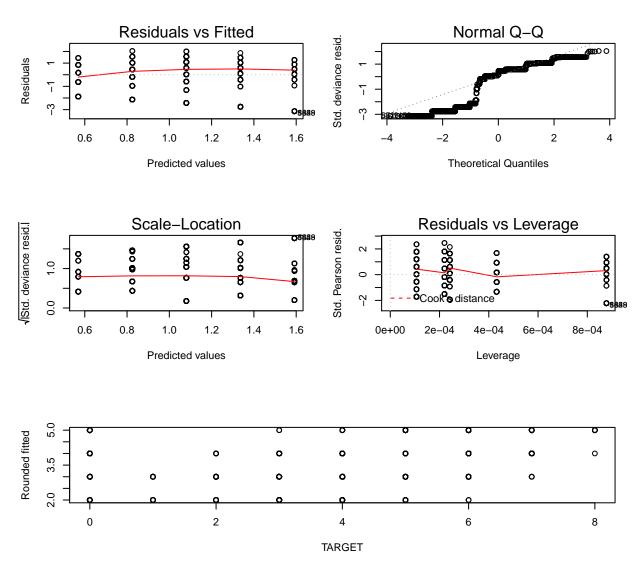


Figure 9: Simple poisson regression diagnostics

```
## AIC: 25458
##
## Number of Fisher Scoring iterations: 4
## Likelihood ratio test
##
## Model 1: TARGET ~ LabelAppeal + STARS
## Model 2: TARGET ~ 1
##
     #Df LogLik Df
                   Chisq Pr(>Chisq)
       3 -12726
## 1
## 2
       1 -13696 -2 1940.5 < 2.2e-16 ***
##
                     '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
```

Table 3: Poisson model statistics with STARS & Label Appeal as predictors

null.deviance	df.null	logLik	AIC	BIC	deviance	df.residual	pseudoR.Sq	MAE
6398.3	7057	-12726.13	25458.26	25478.85	4457.75	7055	0.3	0.88

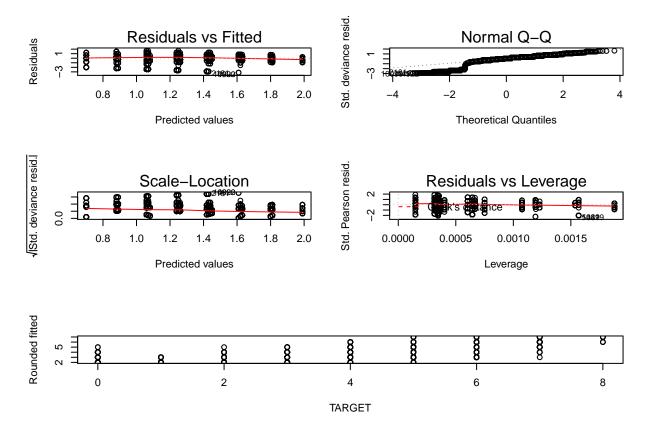


Figure 10: Model diagnostics TARGET ~ Label Appeal + STARS

5.1.2.1 Model interpretation.

It is seen that the regression model is statistically significant from the Likelihood Ratio Test (LRT) and the regression coefficents are also significant. The MAE is 1.5 which is a marginally higher than the simple

model with LabelAppeal as predictor. However the ratio of residual deviance to its degrees of freedom is significantly less than 1, which can be interpreted as better model fit to the data. This model also does not fit the zero counts.

5.1.3 Dropping one predcitor from model.

It'll be interesting to see if there is value in dropping one of the regressors from the model. Below, LRT is performed by dropping one regressor at a time from the model.

```
## Single term deletions
##
## Model:
## TARGET ~ LabelAppeal + STARS
##
               Df Deviance
                            AIC
                                   LRT Pr(>Chi)
## <none>
                    4457.8 25458
                   5017.2 26016 559.40 < 2.2e-16 ***
## LabelAppeal
               1
## STARS
                1
                   5174.8 26173 717.07 < 2.2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

From LRT, both Label Appeal and STARS appear significant. Dropping Label Appeal (kepping STARS as the only predictor) providing a marginal increase in model fit compared to dropping STARS (keeping Label Appeal as the only predictor). This interpretation is onsistent with the decision tree interpretation in the section 3.1.2.

The LRT test for model comparison may be biased, since the models may have different samples sizes due to missing data. However, LRT can be used as a guidance for model selection. It is examined in the below section just to be sure

5.1.3.1 Two models - A. STARS as predictor B. LabelAppeal and Interpretation.

Verifying the results in the above section to make sure the drop1 test is providing us the expected results. It can be seen that when the data is kept contant between the models, the results are as expected. The result for model B is different from that of in section 5.1.1, this is because the data used to fit the model is different. Based on AIC and MAE comparison Label Appeal seems to be a better predcitor so far, when using a Poisson model.

```
##
  glm(formula = TARGET ~ STARS, family = poisson(link = "log"),
##
       data = train)
##
## Deviance Residuals:
##
       Min
                 1Q
                      Median
                                    30
                                            Max
## -2.6632
           -0.2980
                      0.1404
                               0.2361
                                         1.6824
##
## Coefficients:
               Estimate Std. Error z value Pr(>|z|)
##
## (Intercept) 0.766962
                          0.016161
                                      47.46
                                              <2e-16 ***
## STARS
                                      37.58
                                              <2e-16 ***
               0.249465
                          0.006639
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for poisson family taken to be 1)
##
```

```
## Null deviance: 6398.3 on 7057 degrees of freedom
## Residual deviance: 5017.2 on 7056 degrees of freedom
## (2538 observations deleted due to missingness)
## AIC: 26016
##
## Number of Fisher Scoring iterations: 5
## Likelihood ratio test
##
## Model 1: TARGET ~ STARS
## Model 2: TARGET ~ 1
## #Df LogLik Df Chisq Pr(>Chisq)
## 1 2 -13006
## 2 1 -13696 -1 1381.1 < 2.2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1</pre>
```

Table 4: Simple Poisson model statistics with STARTS as regressor

null.deviance	df.null	logLik	AIC	BIC	deviance	df.residual	pseudoR.Sq	MAE
6398.3	7057	-13005.83	26015.66	26029.39	5017.16	7056	0.22	0.97

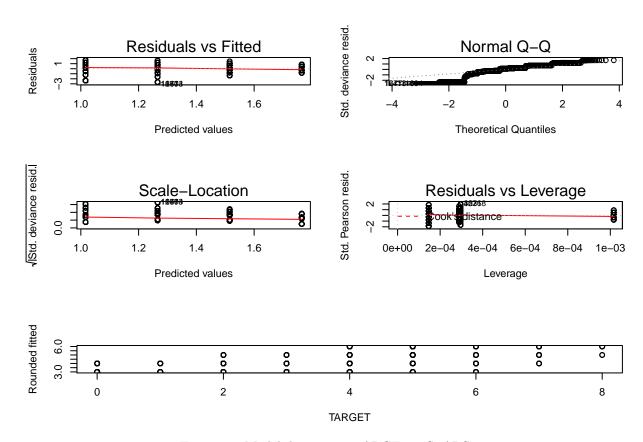


Figure 11: Model diagnostics TARGET \sim STARS

```
##
## Call:
## glm(formula = TARGET ~ LabelAppeal, family = poisson(link = "log"),
```

```
##
       data = train[complete.cases(train[, c(14, 16)]), ])
##
##
  Deviance Residuals:
##
      Min
                 1Q
                     Median
                                   3Q
                                           Max
##
   -3.4169
           -0.3004
                      0.2063
                               0.2336
                                        1.6783
##
## Coefficients:
##
              Estimate Std. Error z value Pr(>|z|)
## (Intercept) 1.267168
                          0.006425
                                    197.24
                                             <2e-16 ***
                                             <2e-16 ***
## LabelAppeal 0.248567
                          0.007119
                                     34.92
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
##
  (Dispersion parameter for poisson family taken to be 1)
##
##
       Null deviance: 6398.3 on 7057 degrees of freedom
## Residual deviance: 5174.8 on 7056 degrees of freedom
## AIC: 26173
## Number of Fisher Scoring iterations: 4
## Likelihood ratio test
## Model 1: TARGET ~ LabelAppeal
## Model 2: TARGET ~ 1
     #Df LogLik Df Chisq Pr(>Chisq)
## 1
      2 -13085
## 2
      1 -13696 -1 1223.5 < 2.2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

Table 5: Simple Poisson model statistics with LabelAppeal as regressor; non missing cases for STARS and LabelAppeal

null.deviance	df.null	logLik	AIC	BIC	deviance	df.residual	pseudoR.Sq	MAE
6398.3	7057	-13084.67	26173.33	26187.06	5174.83	7056	0.19	0.85

5.1.4 Poisson regression with LabelAppeal, STARS and Alcohol as predictors

In this section Alcohol is added as a preditor to the model in 5.1.2. Then LRT is performed by dropping one variable from the predictor. Though Alcohol is statistically significant, it does not add significant predictive power to the model. There is no significant reduction in MAE. Also we see that there is pattern in residuals based on the levels of the TARGET variable. It is to be noted that the predicted values are in log scale.

```
##
## Call:
## glm(formula = TARGET ~ LabelAppeal + STARS + Alcohol, family = poisson(link = "log"),
##
       data = train[complete.cases(train[, c(13, 14, 16)]), ])
##
## Deviance Residuals:
##
       Min
                 10
                      Median
                                    3Q
                                            Max
## -3.2162 -0.2634
                      0.0512
                                0.3702
                                         1.6226
```

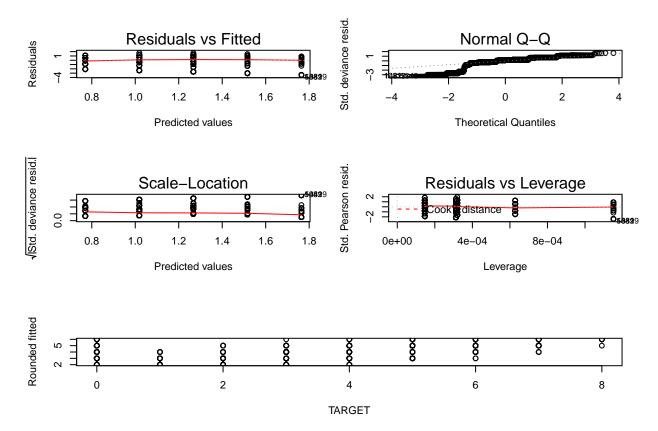


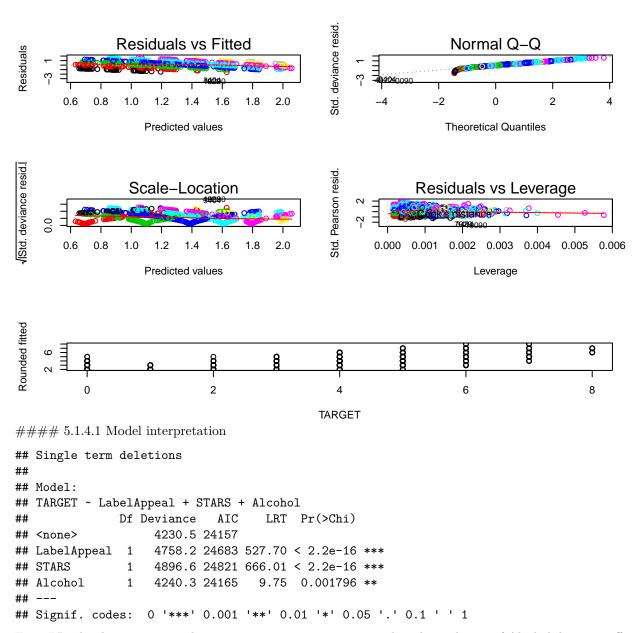
Figure 12: Model diagnostics TARGET ~ LABEL APPEAL non missing data for STARS and LabelAppeal

```
##
## Coefficients:
##
               Estimate Std. Error z value Pr(>|z|)
## (Intercept) 0.812942
                          0.024086
                                    33.751
                                              <2e-16 ***
## LabelAppeal 0.179440
                                    22.967
                          0.007813
                                              <2e-16 ***
## STARS
               0.189742
                          0.007316
                                     25.934
                                              <2e-16 ***
## Alcohol
               0.005377
                          0.001722
                                      3.122
                                              0.0018 **
  Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
##
   (Dispersion parameter for poisson family taken to be 1)
##
##
       Null deviance: 6076.9 on 6697
                                        degrees of freedom
##
## Residual deviance: 4230.5 on 6694
                                        degrees of freedom
## AIC: 24157
##
## Number of Fisher Scoring iterations: 4
## Likelihood ratio test
## Model 1: TARGET ~ LabelAppeal + STARS + Alcohol
## Model 2: TARGET ~ 1
     #Df LogLik Df Chisq Pr(>Chisq)
       4 -12074
## 2
       1 -12998 -3 1846.4 < 2.2e-16 ***
## ---
```

```
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

Table 6: Poisson model statistics with LabelAppeal, STARS, ALCOHOL as regressors

null.deviance	df.null	logLik	AIC	BIC	deviance	df.residual	pseudoR.Sq	MAE
6076.92	6697	-12074.49	24156.99	24184.22	4230.55	6694	0.3	0.83



From LRT by droping one predictor at every iteration, it is seen that the exclusion of Alcohol does not affect the fit considerably. Hence it is best to drop Alcohol from the model.

5.1.5 Addition of AcidIndex as predictor

One of the other predictors that was found key in section 3.1.2 is AcidIndex. It is seen below that though Acidindex's coefficient is statistically significant, it does not improve prediction. Alcohol's coefficient is marginally significant.

```
##
## Call:
##
  glm(formula = TARGET ~ LabelAppeal + STARS + Alcohol + AcidIndex,
       family = poisson(link = "log"), data = train[complete.cases(train[,
          c(13, 14, 15, 16)]), ])
##
##
## Deviance Residuals:
##
      Min
                 1Q
                     Median
                                   3Q
                                           Max
  -3.2171 -0.2763
                     0.0566
                               0.3687
                                        1.6568
##
## Coefficients:
##
               Estimate Std. Error z value Pr(>|z|)
                           0.052053 23.070
## (Intercept) 1.200847
                                              <2e-16 ***
## LabelAppeal 0.181869
                          0.007820
                                    23.257
                                              <2e-16 ***
                                    25.017
## STARS
               0.183927
                           0.007352
                                              <2e-16 ***
## Alcohol
               0.004418
                           0.001725
                                     2.560
                                              0.0105 *
## AcidIndex
              -0.048170
                                    -8.359
                           0.005763
                                              <2e-16 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for poisson family taken to be 1)
##
##
       Null deviance: 6076.9 on 6697
                                      degrees of freedom
## Residual deviance: 4158.8 on 6693
                                      degrees of freedom
## AIC: 24087
## Number of Fisher Scoring iterations: 5
## Likelihood ratio test
## Model 1: TARGET ~ LabelAppeal + STARS + Alcohol + AcidIndex
## Model 2: TARGET ~ 1
     #Df LogLik Df Chisq Pr(>Chisq)
## 1
      5 -12039
## 2
      1 -12998 -4 1918.2 < 2.2e-16 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

Table 7: Poisson model statistics with LabelAppeal, STARS, ALCOHOL, AcidIndex as regressors

null.deviance	df.null	logLik	AIC	BIC	deviance	df.residual	pseudoR.Sq	MAE
6076.92	6697	-12038.6	24087.2	24121.25	4158.77	6693	0.32	0.81

```
## Single term deletions
##
## Model:
## TARGET ~ LabelAppeal + STARS + Alcohol + AcidIndex
```

```
##
               Df Deviance
                             AIC
                                    LRT Pr(>Chi)
## <none>
                    4158.8 24087
## LabelAppeal
               1
                    4699.9 24626 541.13
                                        < 2e-16 ***
## STARS
                    4778.7 24705 619.93
                                        < 2e-16 ***
                1
## Alcohol
                1
                    4165.3 24092
                                   6.56
                                        0.01044 *
## AcidIndex
                    4230.5 24157
                                 71.78
                                        < 2e-16 ***
                1
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

drop1 test shows that the exclusion of Alcohol provides the best AIC. In the next section we will fit a model with LabelAppeal, AcidIndex and STARS as predictors.

5.1.5.1 Removal of Alcohol and inclusion of AcidIndex

The model with LabelAppeal, STARS and AcidIndex is fit below and it is seen that all the predictor variables' coefficients are statistically significant. However the MAE is not improved. LRT when one predictor is left out of the model at each iteration shows that inclusion of AcidIndex does NOT impact the AIC considerably.

```
##
## Call:
## glm(formula = TARGET ~ LabelAppeal + STARS + AcidIndex, family = poisson(link = "log"),
##
       data = train[complete.cases(train[, c(14, 15, 16)]), ])
##
## Deviance Residuals:
##
       Min
                      Median
                                   30
                                           Max
                 10
                      0.0445
                               0.3873
                                        1.6245
##
  -3.2163
           -0.2567
##
## Coefficients:
##
                Estimate Std. Error z value Pr(>|z|)
                                      26.71
## (Intercept)
                1.251460
                           0.046855
                                              <2e-16 ***
                           0.007602
                                      23.95
                                               <2e-16 ***
## LabelAppeal
                0.182091
                                      25.89
## STARS
                0.184124
                           0.007113
                                               <2e-16 ***
## AcidIndex
               -0.048649
                           0.005605
                                      -8.68
                                               <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
##
  (Dispersion parameter for poisson family taken to be 1)
##
       Null deviance: 6398.3 on 7057
                                       degrees of freedom
## Residual deviance: 4380.3
                             on 7054
                                       degrees of freedom
## AIC: 25383
##
## Number of Fisher Scoring iterations: 5
## Likelihood ratio test
##
## Model 1: TARGET ~ LabelAppeal + STARS + AcidIndex
## Model 2: TARGET ~ 1
     #Df LogLik Df Chisq Pr(>Chisq)
## 1
       4 -12687
## 2
       1 -13696 -3 2018 < 2.2e-16 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

Table 8: Poisson model statistics with LabelAppeal, STARS, ALCOHOL, AcidIndex as regressors

null.deviance	df.null	logLik	AIC	BIC	deviance	df.residual	pseudoR.Sq	MAE
6398.3	7057	-12687.43	25382.86	25410.3	4380.35	7054	0.32	0.82

5.1.5.1 Model interpretation

Droping one predictor and performing the LRT, it can is seen below that removing AcidIndex does NOT move the needle on AIC.

```
## Single term deletions
## Model:
## TARGET ~ LabelAppeal + STARS + AcidIndex
##
              Df Deviance
                            AIC
                                   LRT Pr(>Chi)
                   4380.3 25383
## <none>
## LabelAppeal 1
                   4954.3 25955 573.95 < 2.2e-16 ***
## STARS
               1
                   5043.8 26044 663.49 < 2.2e-16 ***
## AcidIndex
                   4457.8 25458 77.41 < 2.2e-16 ***
               1
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

5.1.6 Poisson regression summary

## ##					
##	model	null.deviance	df.null	logLik	AIC
## ##	TARGET = 1.08 + 0.256 *	17183	9595	-19783	39571
## ##	LabelAppeal				
##	TARGET = 0.869 + 0.18 *	6398	7057	-12726	25458
##	LabelAppeal + 0.19 * STARS				
## ##	TARGET = 0.767 + 0.249 * STARS	6398	7057	-13006	26016
##	2111022			2000	20010
## ##	TARGET = 1.267 + 0.249 *	6398	7057	-13085	26173
##	LabelAppeal				
##	TARGET = 0.813 + 0.179 *	6077	6697	-12074	24157
## ##	LabelAppeal + 0.19 * STARS + 0.005 * Alcohol				
##	0.005 * Alcohol				
##	TARGET = 1.201 + 0.182 *	6077	6697	-12039	24087
## ##	LabelAppeal + 0.184 * STARS + 0.004 * Alcohol - 0.048 *				
##	AcidIndex				
##	TARGET 4 054 . 0 400 .	2000	7057	10007	05000
## ##	TARGET = 1.251 + 0.182 * LabelAppeal + 0.184 * STARS -	6398	7057	-12687	25383
##	0.049 * AcidIndex				
##					

Table: Poisson fit summary (continued below)

#	#
#	#

##					
## ##	BIC	deviance	df.residual	pseudoR.Sq	MAE
##	39585	15689	9594	0.09	1
## ##	25479	4458	7055	0.3	0.9
## ##	26029	5017	7056	0.2	1
##	26187	5175	7056	0.2	0.9
##	24184	4231	6694	0.3	0.8
## ##	24121	4159	6693	0.3	0.8
## ##	25410	4380	7054	0.3	0.8