

AI1103 : Assignment 5

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Download latex codes from

<https://github.com/srivatsav01/Assignment-5/blob/main/Assignment-5.tex>

STATISTICS-1 2016 QUESTION 3

If in 6 trials, X is a binomial variate which follows the relation $9 \Pr(X = 4) = \Pr(X = 2)$, then what is the probability of success?

SOLUTION

Let probability of success be p .

Binomial variate X follows following distribution.

$$\Pr(X = k) = \binom{n}{k} \times (p)^k \times (1 - p)^{n-k}$$

Given

$$9 \Pr(X = 4) = \Pr(X = 2), n = 6$$

$$\Pr(X = 4) = \binom{6}{4} \times (p)^4 \times (1 - p)^2 \quad (1)$$

$$\Pr(X = 2) = \binom{6}{2} \times (p)^2 \times (1 - p)^4 \quad (2)$$

$$\frac{\Pr(X = 2)}{\Pr(X = 4)} = 9 \quad (3)$$

$$\frac{(1 - p)^2}{p^2} = 9 \quad (4)$$

$$8p^2 + 2p - 1 = 0 \quad (5)$$

$$p = \frac{1}{4} \quad (6)$$