

DERIVATION OF CENTROID OF A RECTANGLE

Let us consider a rectangular lamina of area $b*d$ as shown in the figure. Now consider a horizontal elementary strip of area $b*dy$, which is at a distance y from the reference axis AB.

Moment of area of elementary strip about AB

$$=b*dy*y$$

Sum of moments of such elementary strips about AB is given by

$$= \int_0^d b*dy*y$$

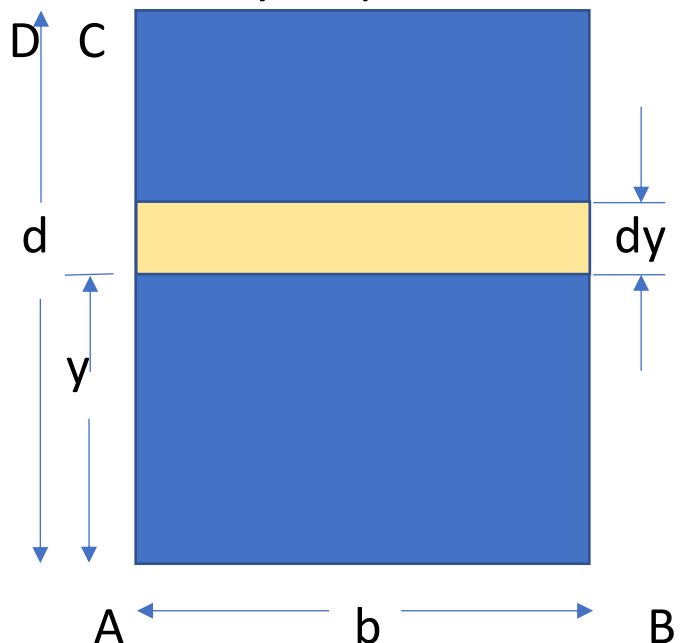
$$= b \int_0^d y*dy$$

$$= b*[y^2/2]_0^d$$

$$= bd^2/2$$

Moment of total

$$\text{area about AB} = bd*\bar{y}$$



Applying the principle of moments about AB,

$$bd^2/2 = bd*\bar{y}$$

$$\text{Or } \bar{y} = d/2$$

By considering a vertical strip, similarly, we can prove that $\bar{x} = b/2$

