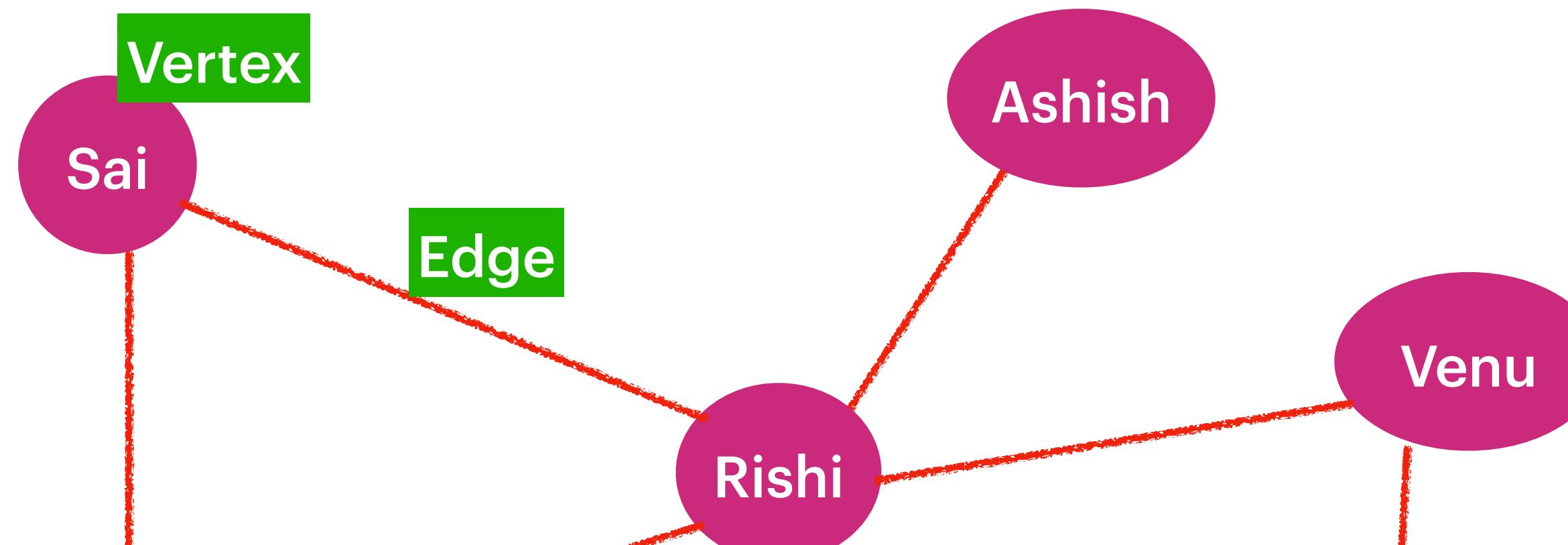


Graph Terminology

Graph

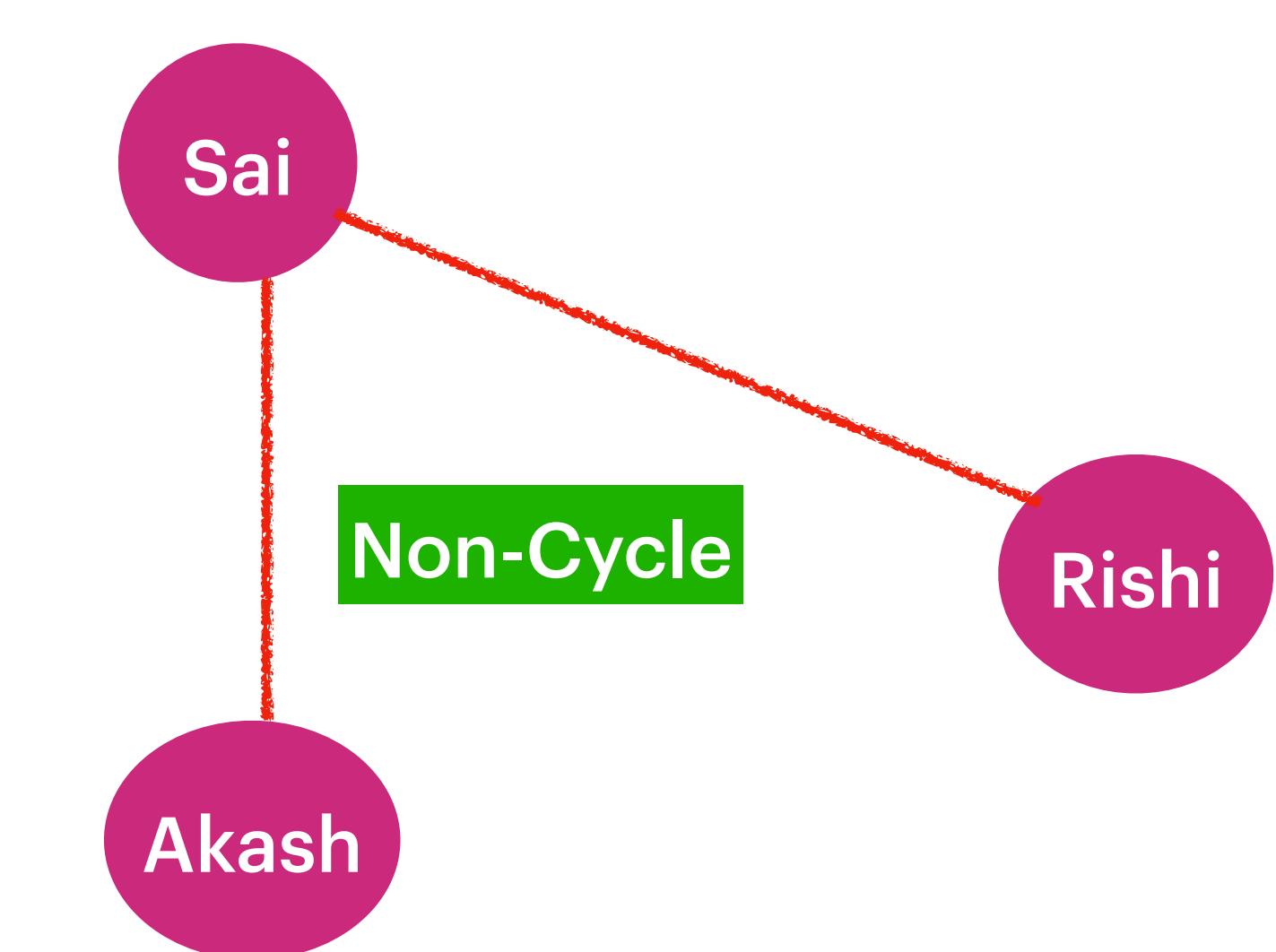
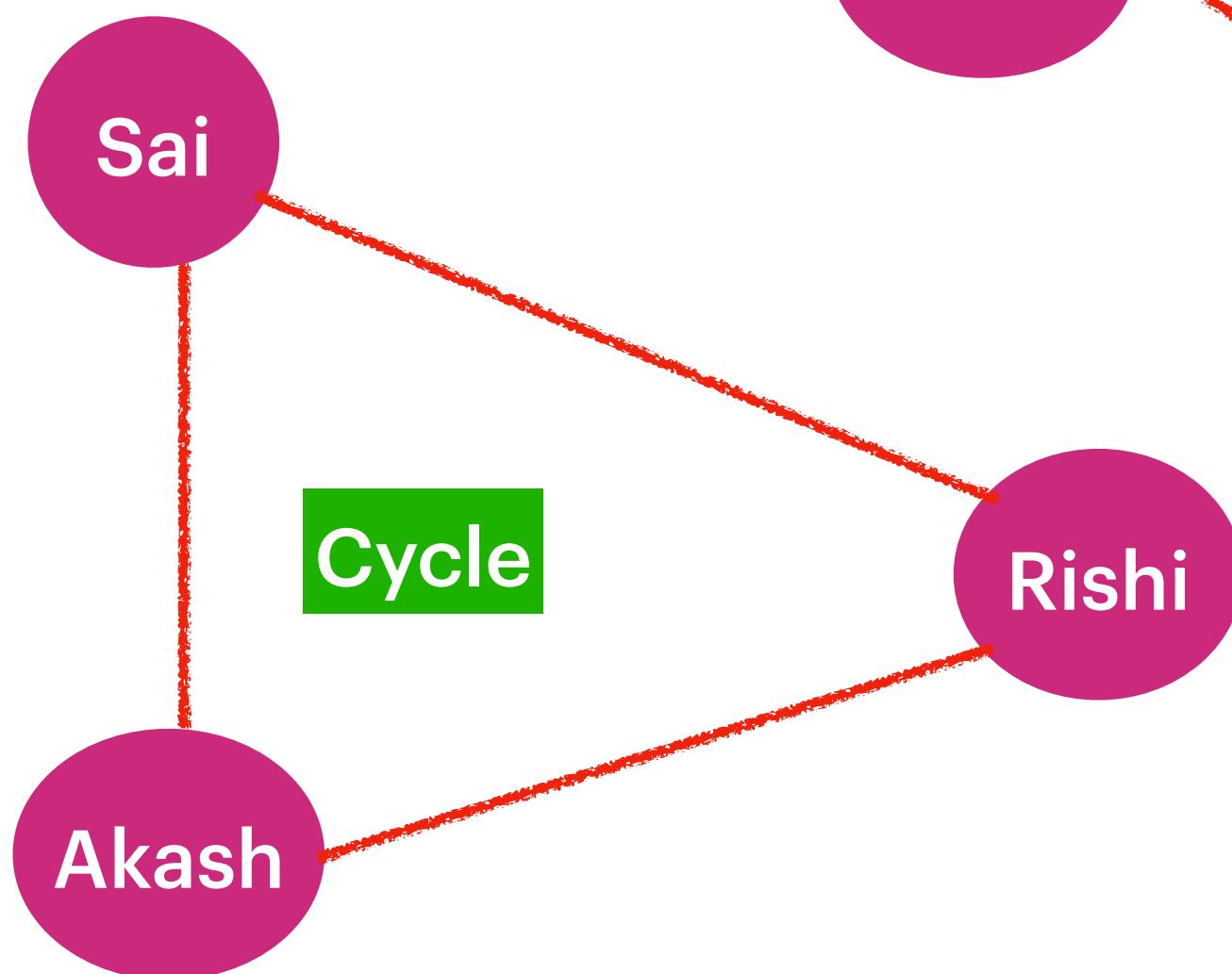
It's a way of connecting dot's.

Path



Connectivity

Degree of a Vertex

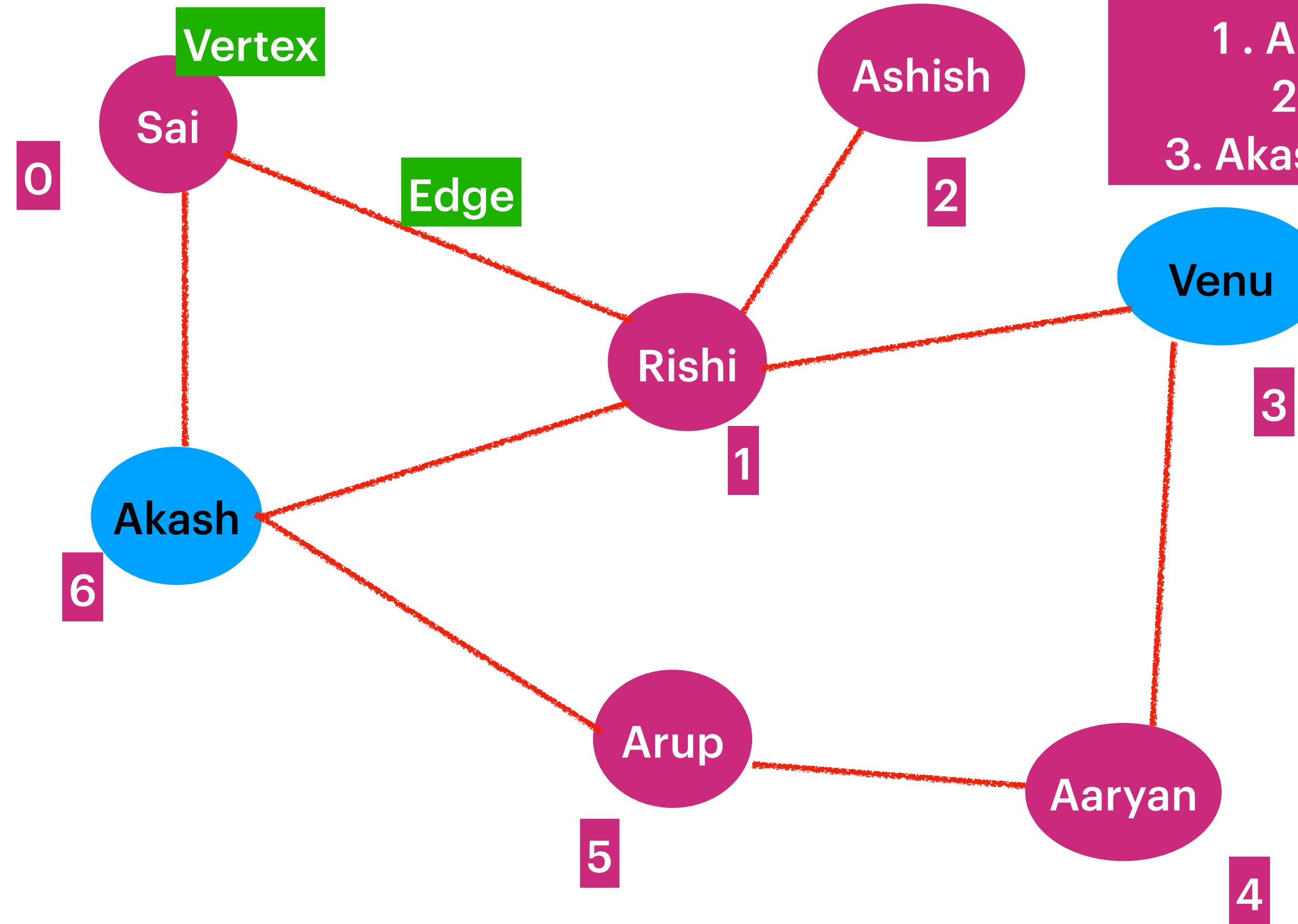


Path :

If there is connection exists,
Path just talks about no.of between Source
& Destination vertices.

Graph

It's a way of connecting dot's.



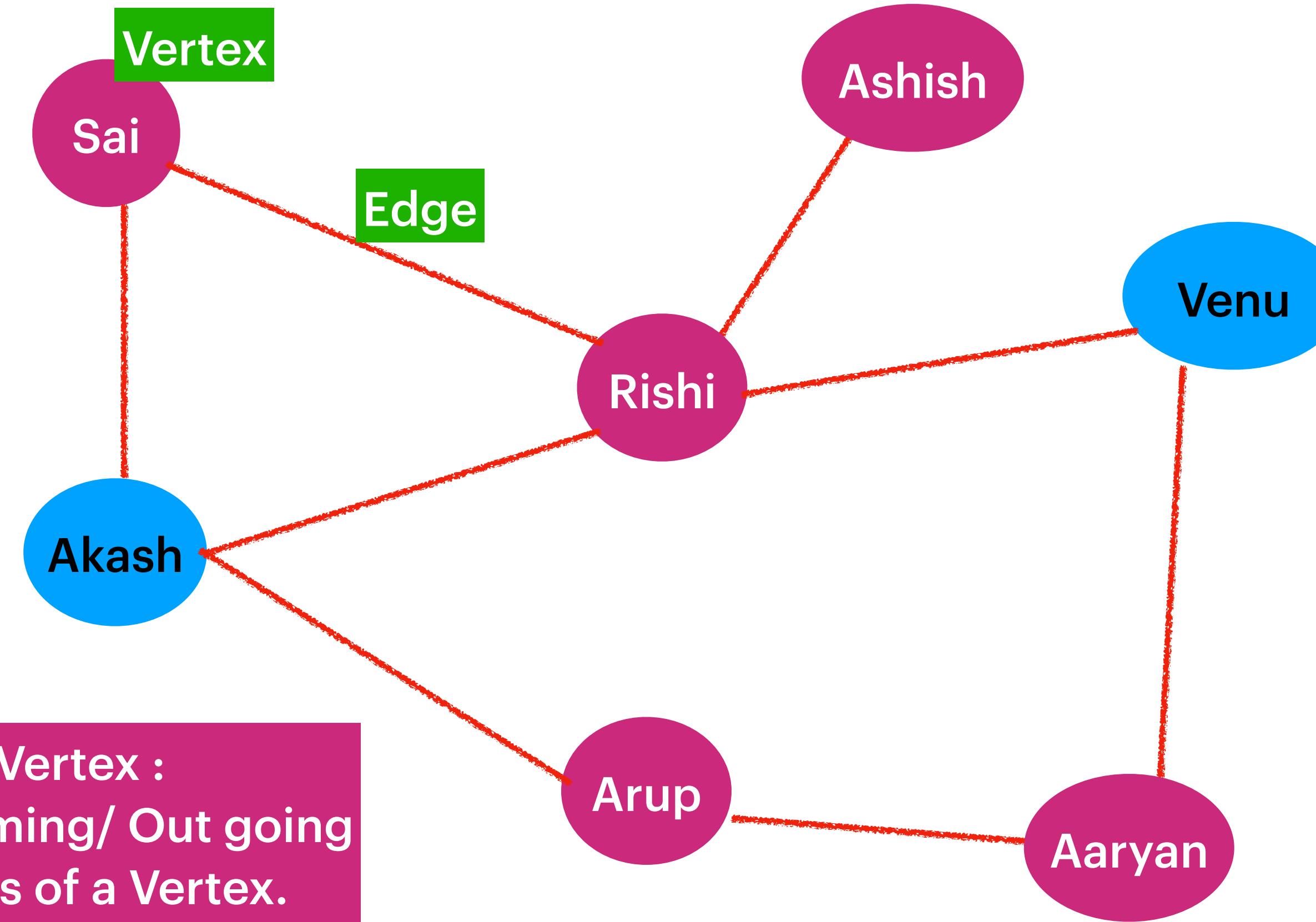
Path between Akash <-> Venu

Does path exists ? Yes

1. Akash — Sai — Rishi — Venu (3)
2. Akash — Rishi — Venu (2)
3. Akash — Arup — Aaryan — Venu (3)

Bidirectional Graph

Here the connection exists in Both the ways.
Source \longleftrightarrow Destination



Degree Of Vertex :
Talks about Incoming/ Out going
Connections of a Vertex.

DegreeOf(Aakash) :
In-Degree =>3
Out-Degree =>3

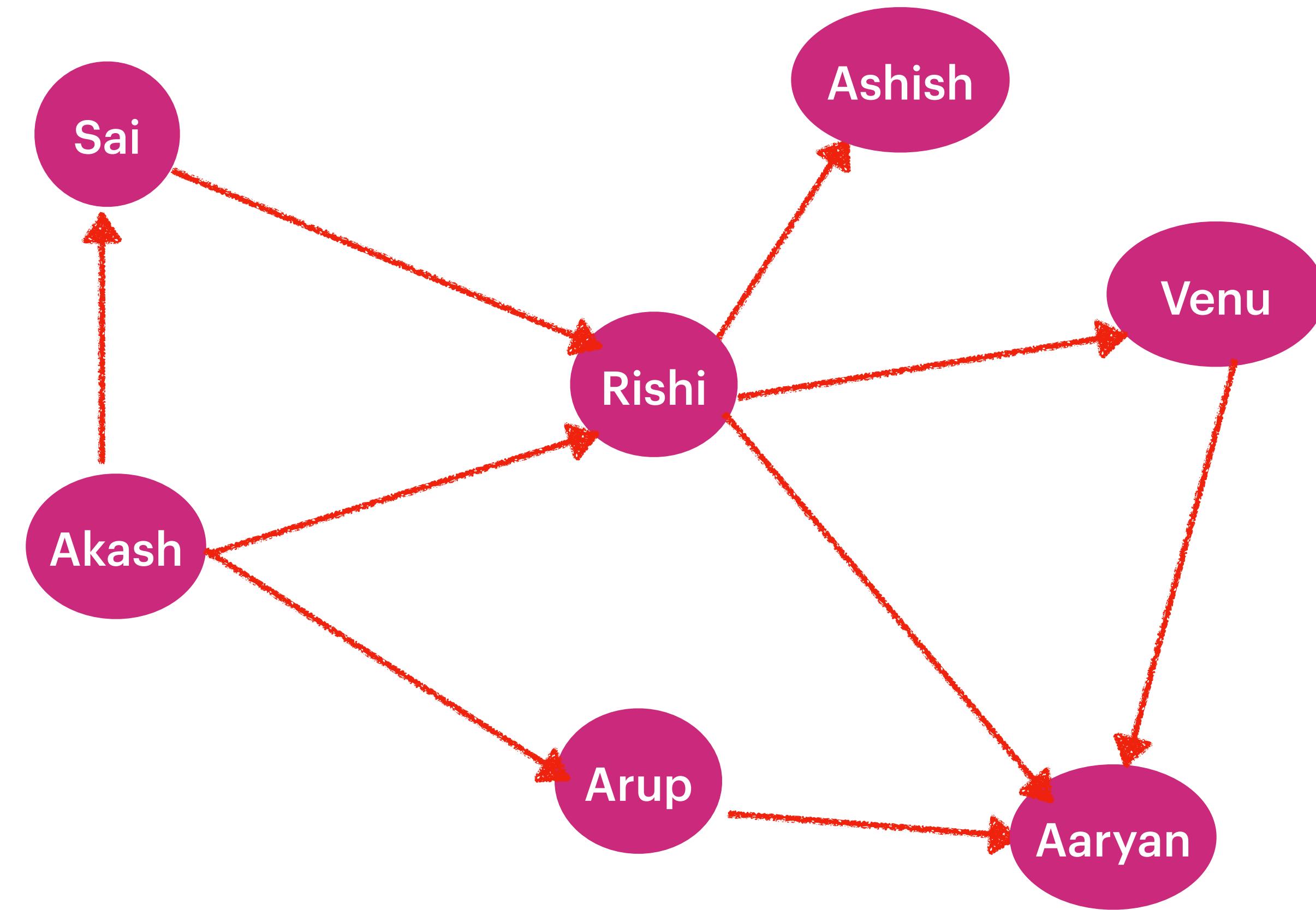
Directed Graph

In-Degree (Sai) : 1

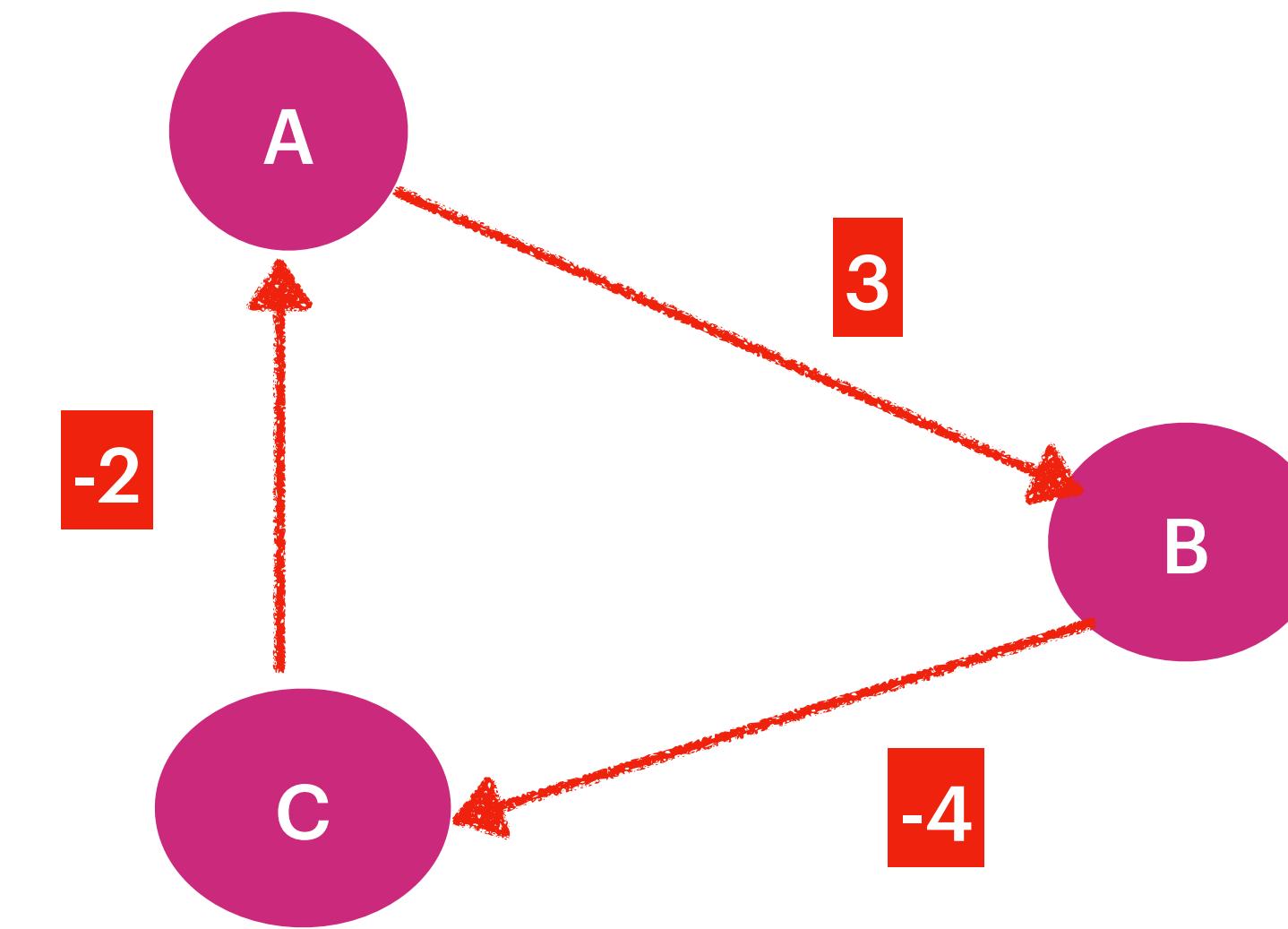
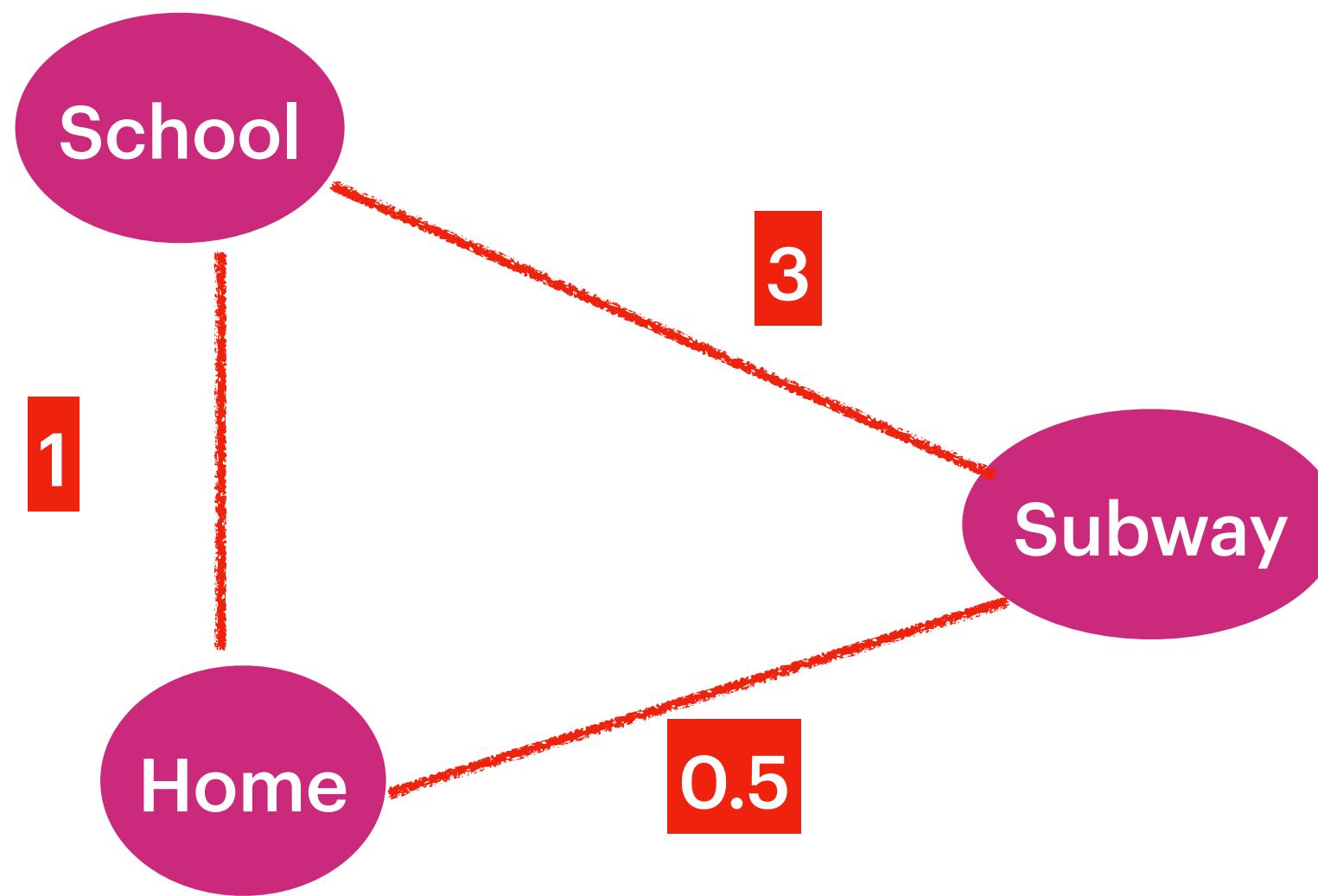
Out-Degree (Sai) : 1

In-Degree (Rishi) : 2

Out-Degree (Rishi) : 3

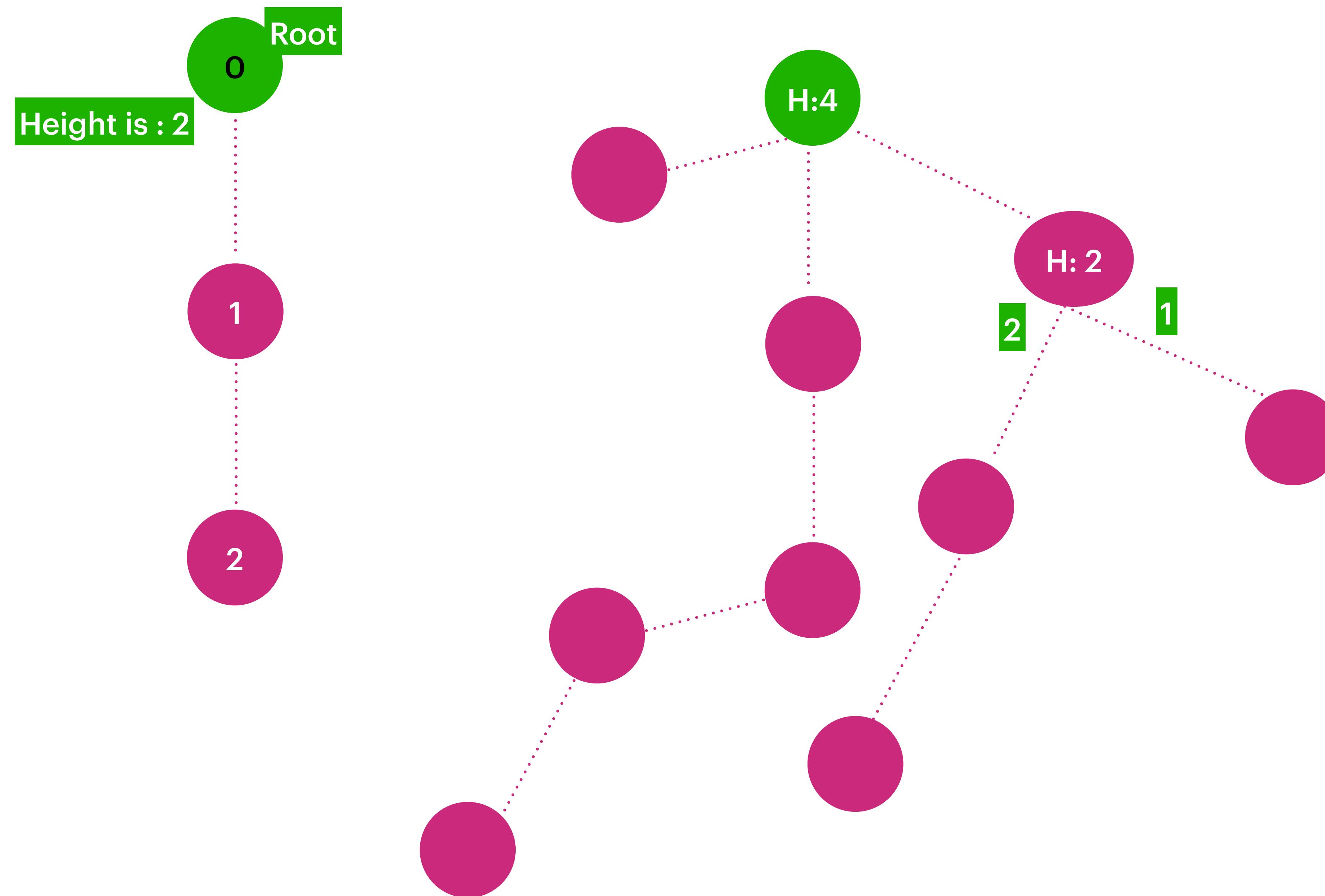


Weighted Graph

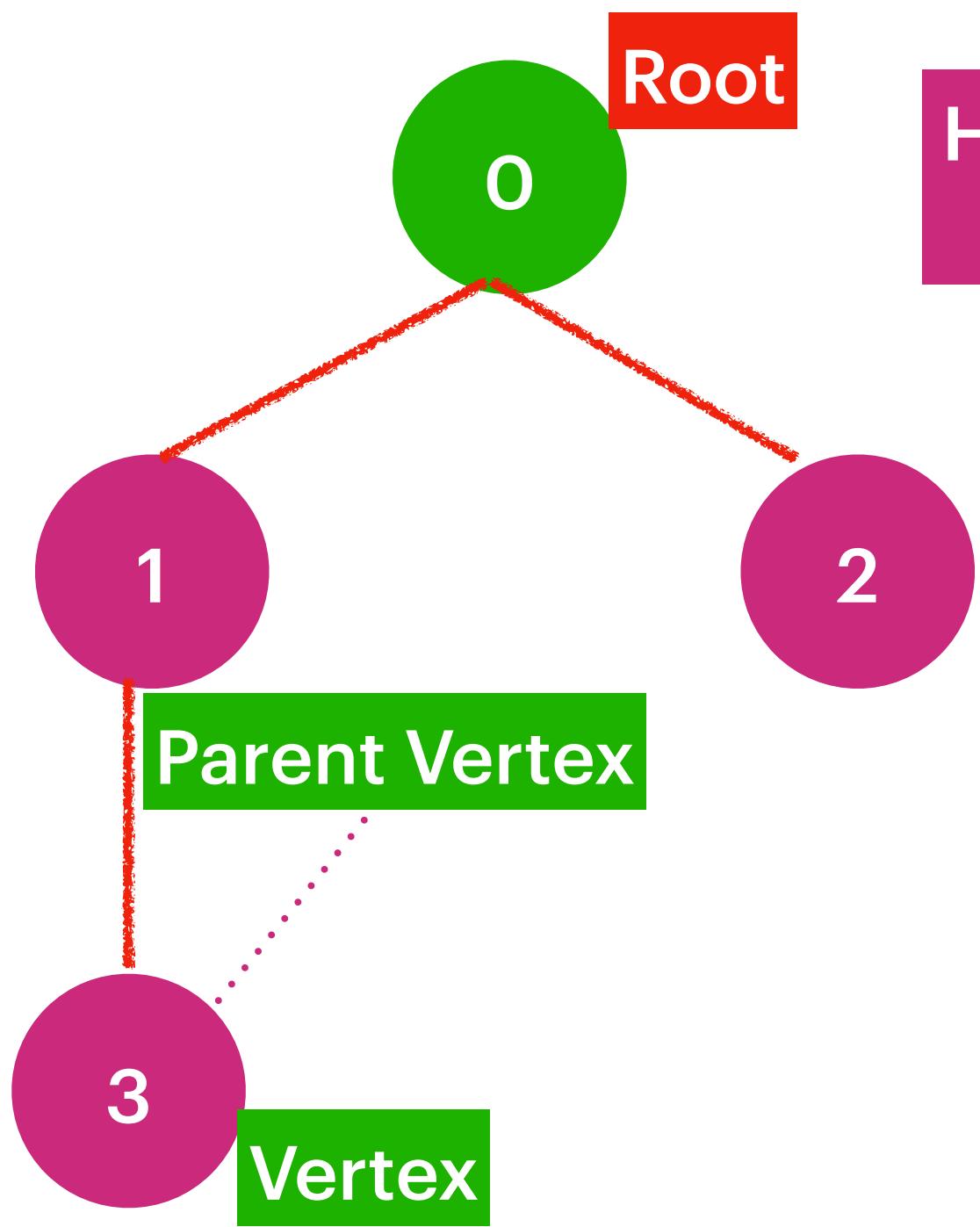


**Negative Weight Cycle =
 $A \rightarrow B \rightarrow C = 3 + (-4) + (-2) = -3$**

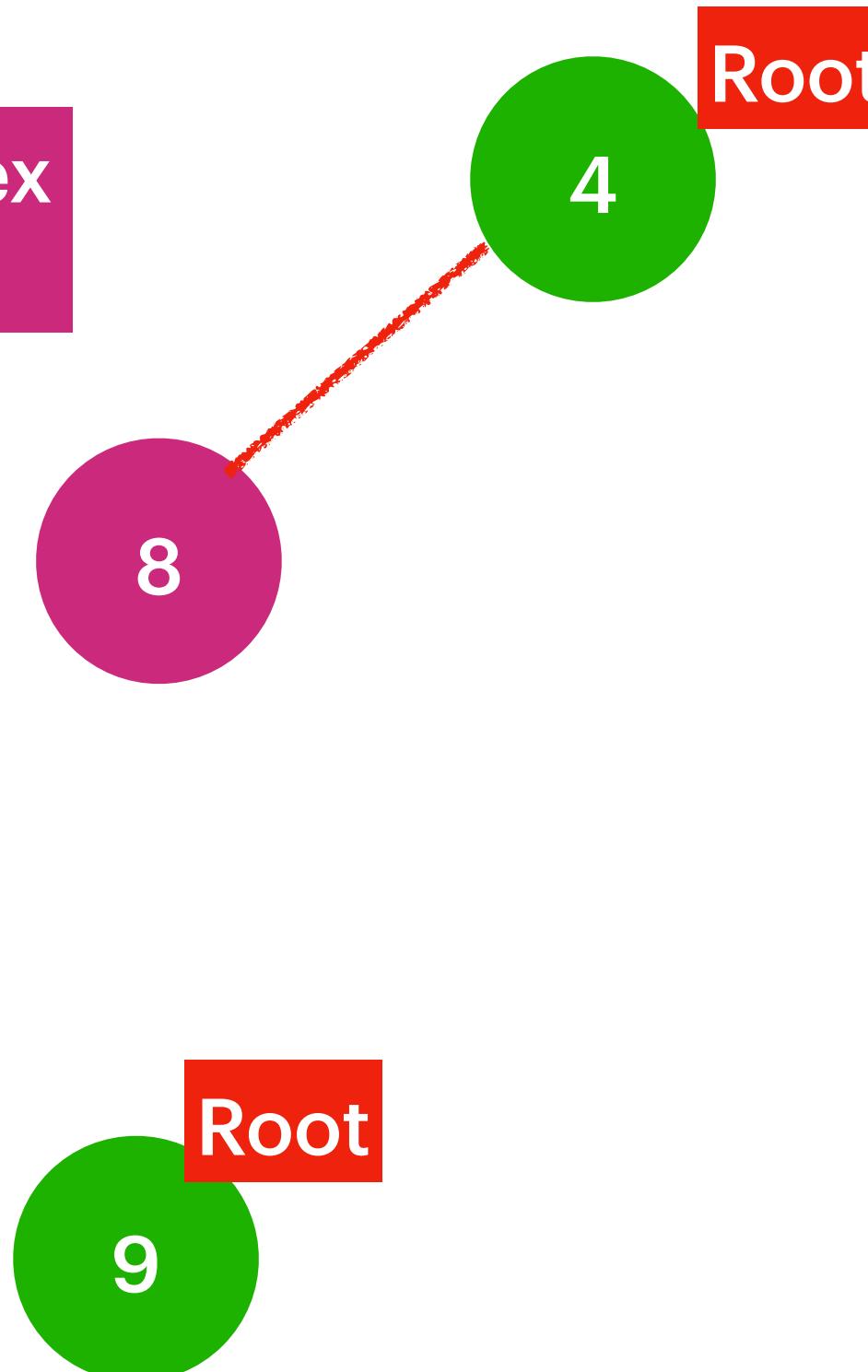
Height Of The Graph



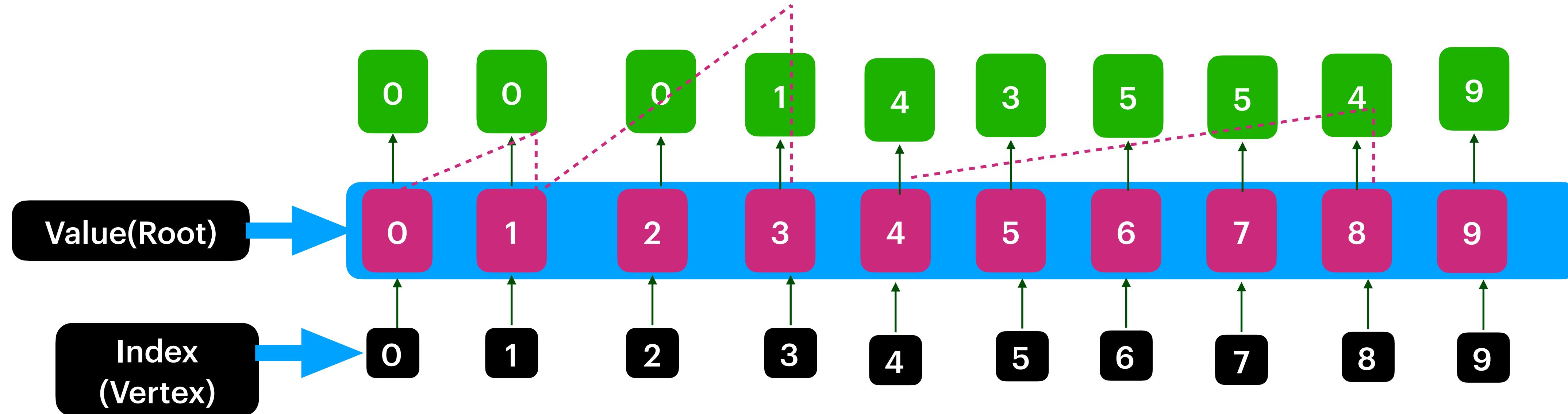
Disjoint Set



How do we say that vertex
are connected ?



$0,1,2,3 : A$
 $5,6,7 : B$
 $A \cup B : 0,1,2,3,5,6,7$



(0,1) , (0,2) , (1,3) , (4,8), (5,6), (5,7)

Connected(1,3)=
root(1) == root(3)
0 == 0 = true

connected(1,8)
root(1) == root(8)
0 == 4 (false)

connected(5,7)
5 == 5 : true

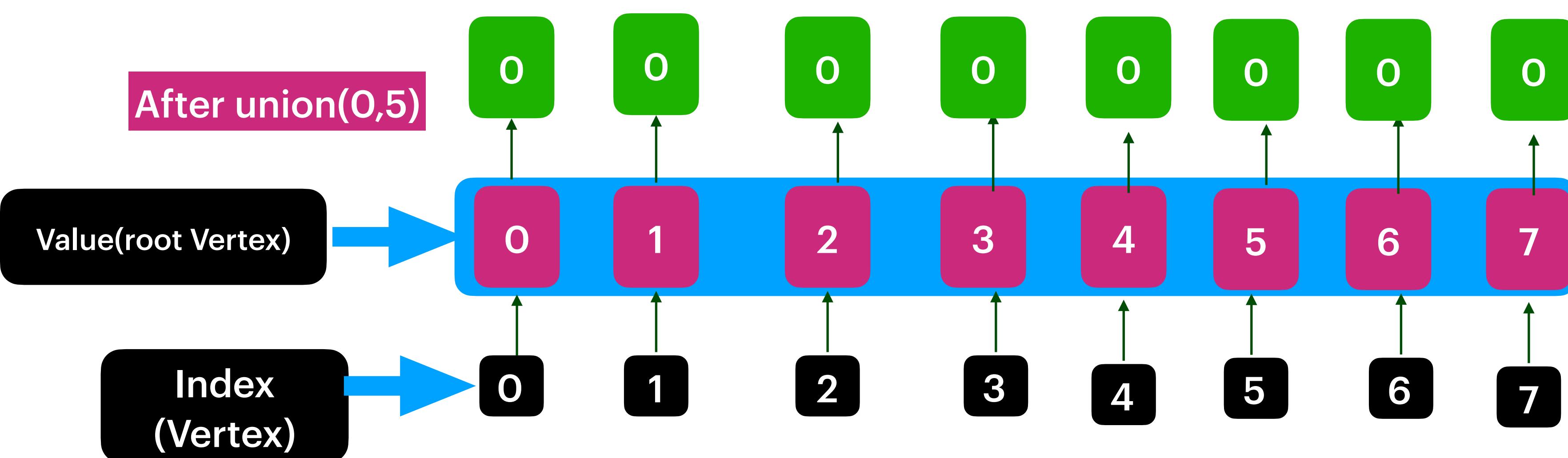
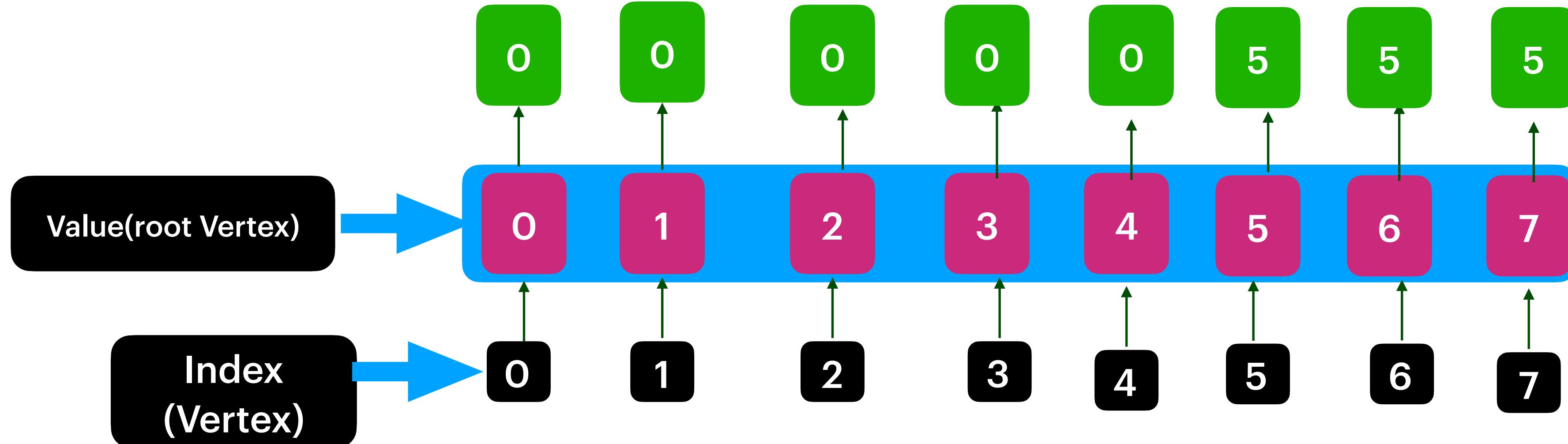
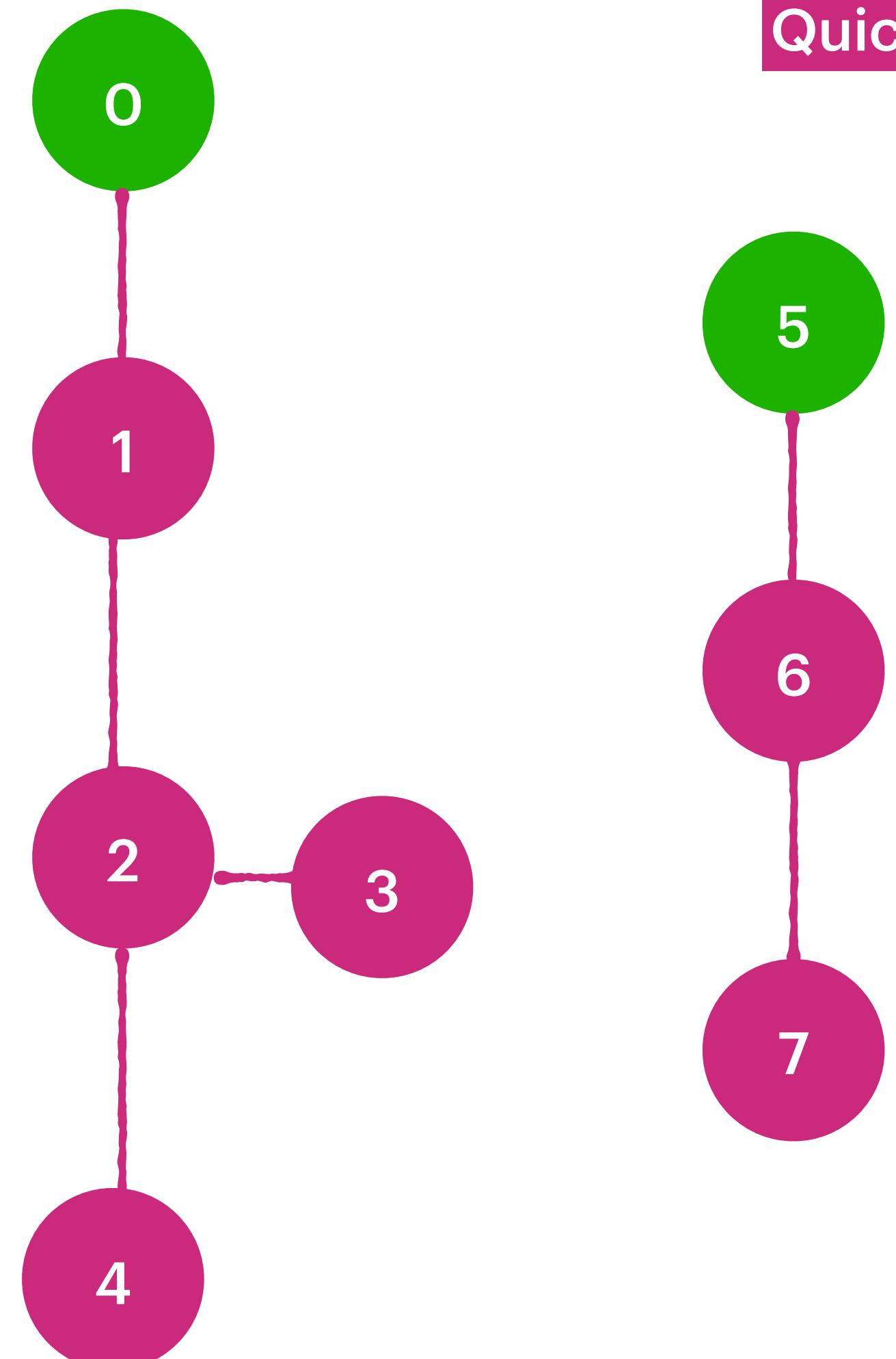
Quick Union:

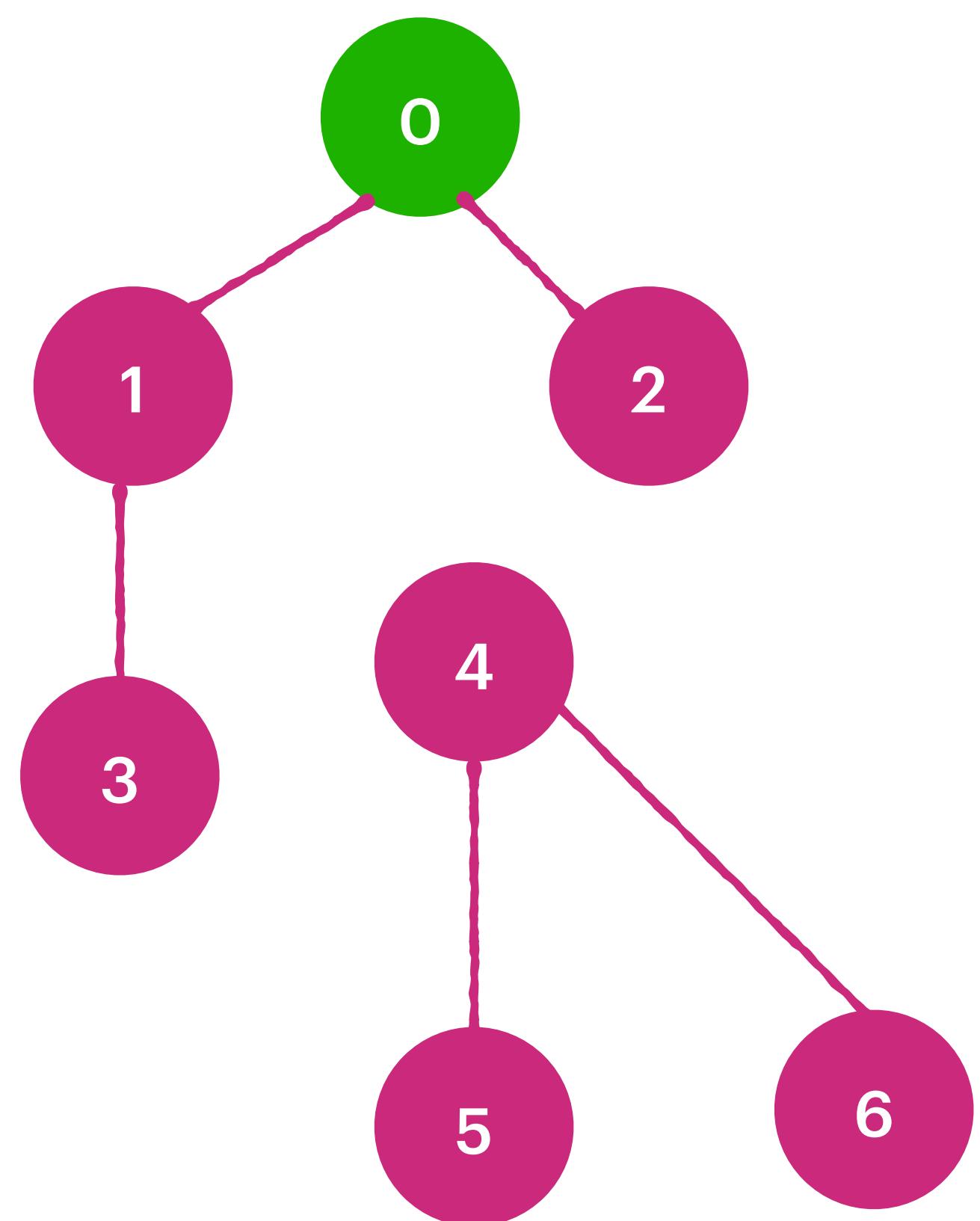
union(vx, vy) => TimeComplexity : O(1)

connection(vx, vy) => TimeComplexity : O(n) + O(n) = O(2n) = O(n)

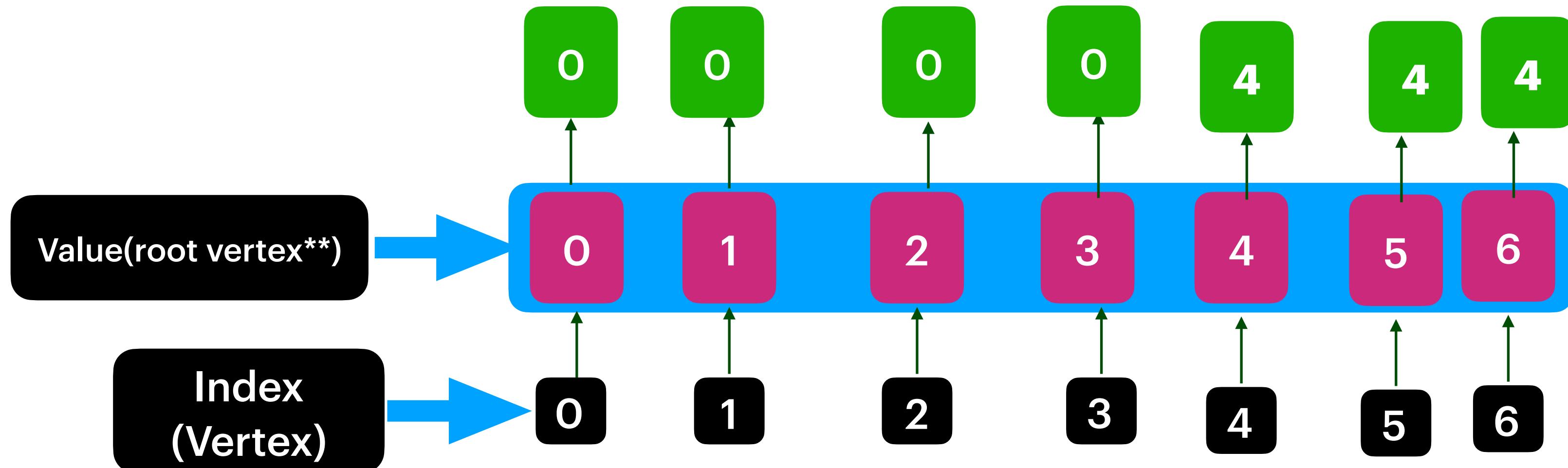
find(vertex) => Time Complexity : O(n)

Quick Find :





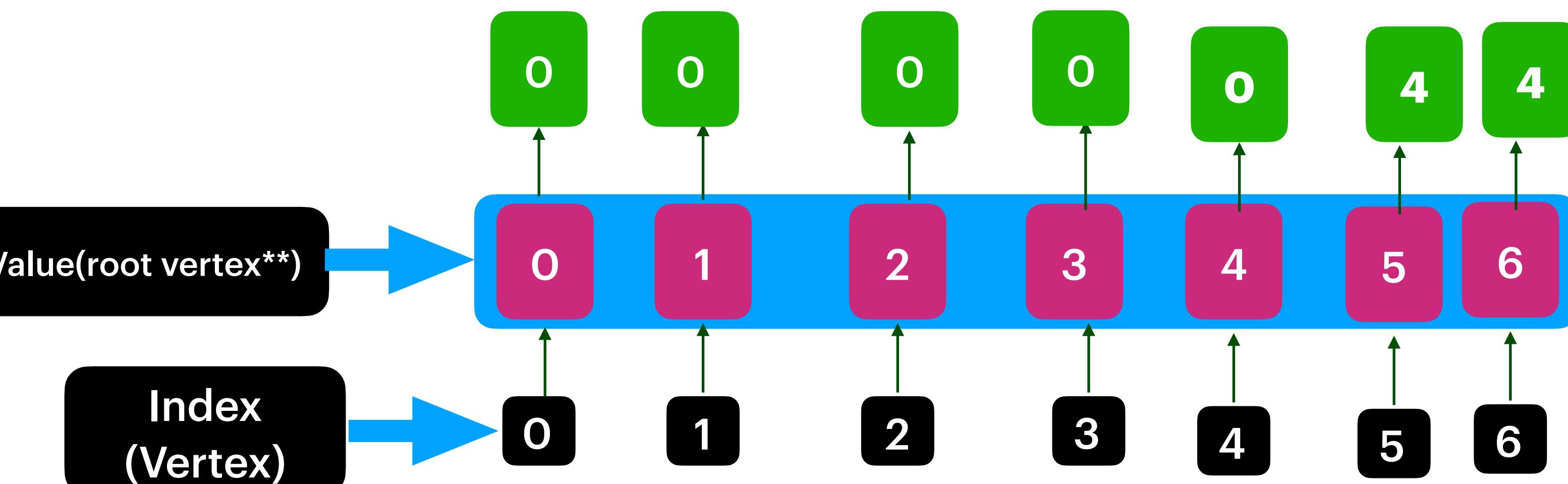
Quick Union :

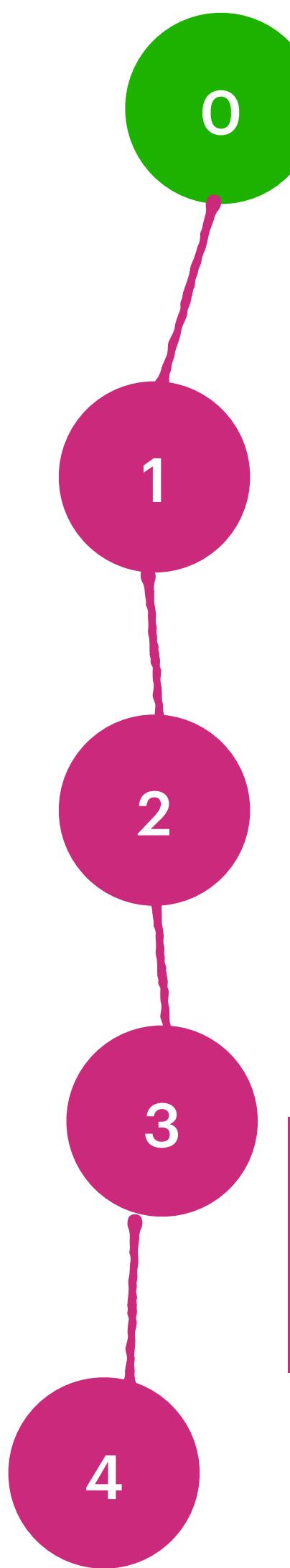


union(0,1)
union(0,2)
union(1,3)
union(4,5)
union(4,6)

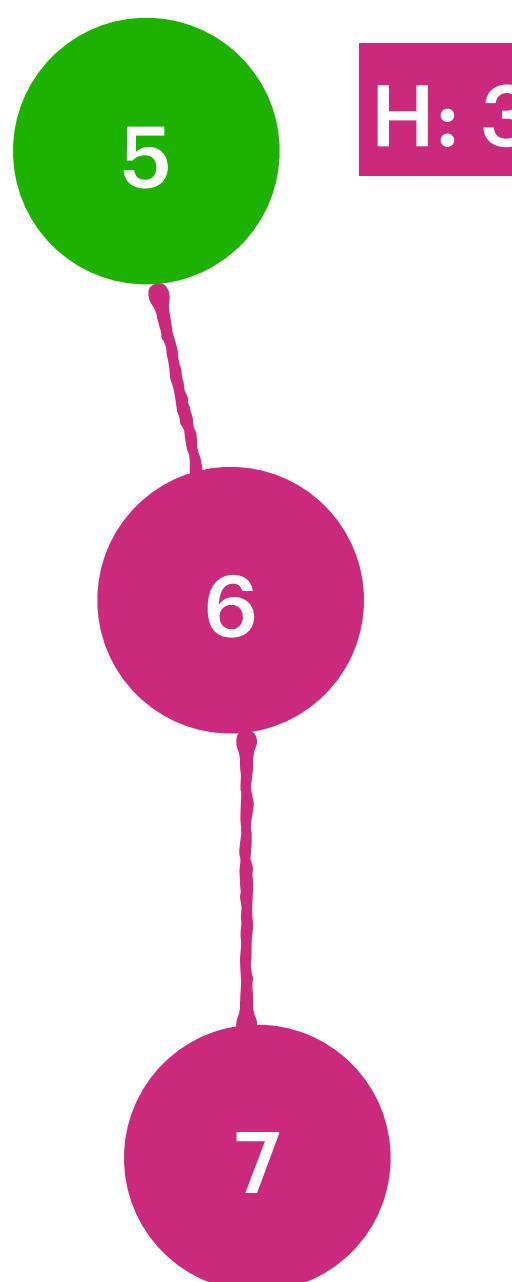
union(0, 1)
Int rootX = find(x); // 0
Int rootY = find(y); // 1
root[rootY] = rootX; //

After union(3,5)
Int rootX = find(3) = 0
Int rootY = find(5) = 4
root[rootY] = rootX
root[4] = 0

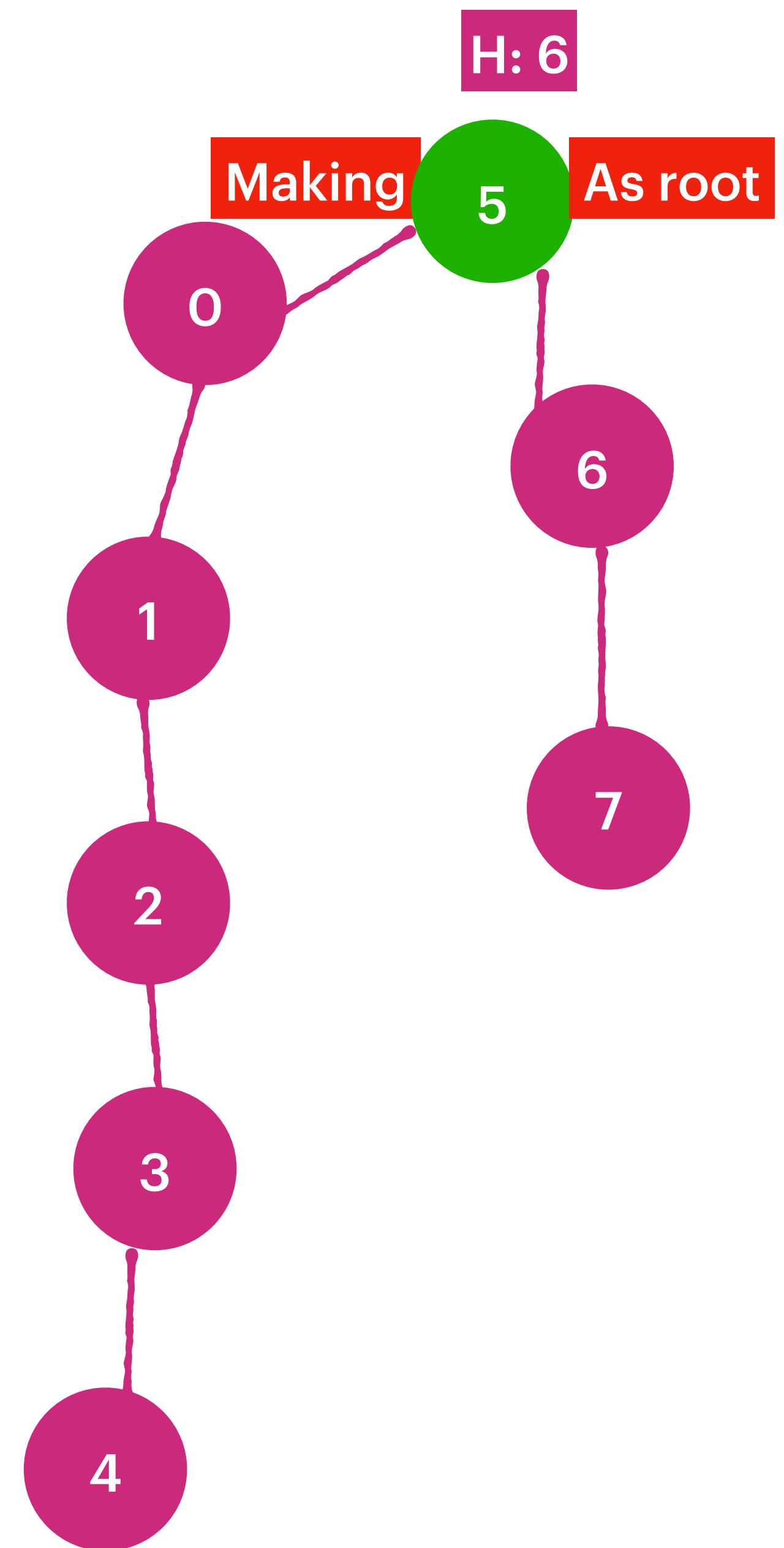




H: 5



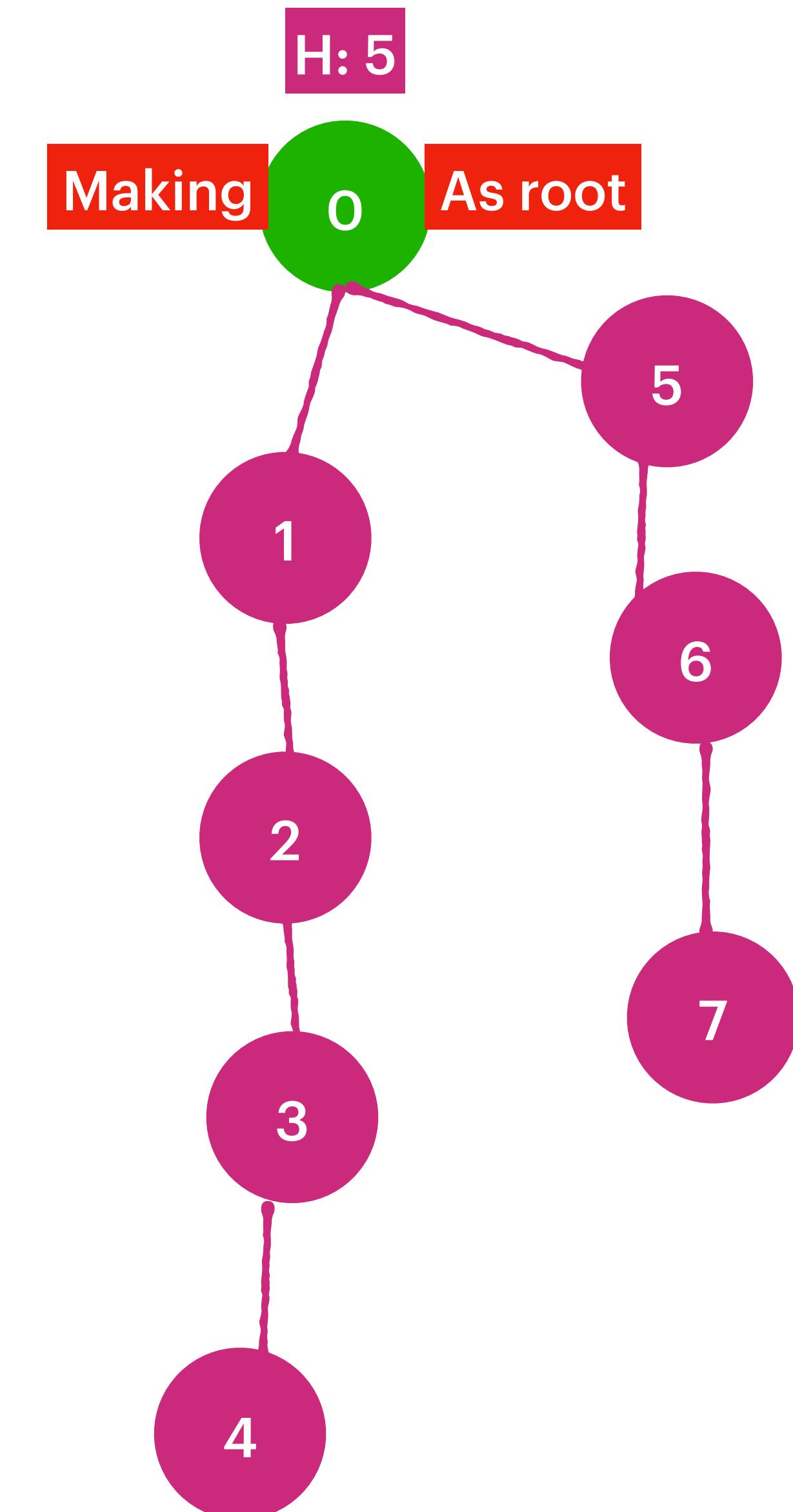
H: 3



H: 6

Making

As root

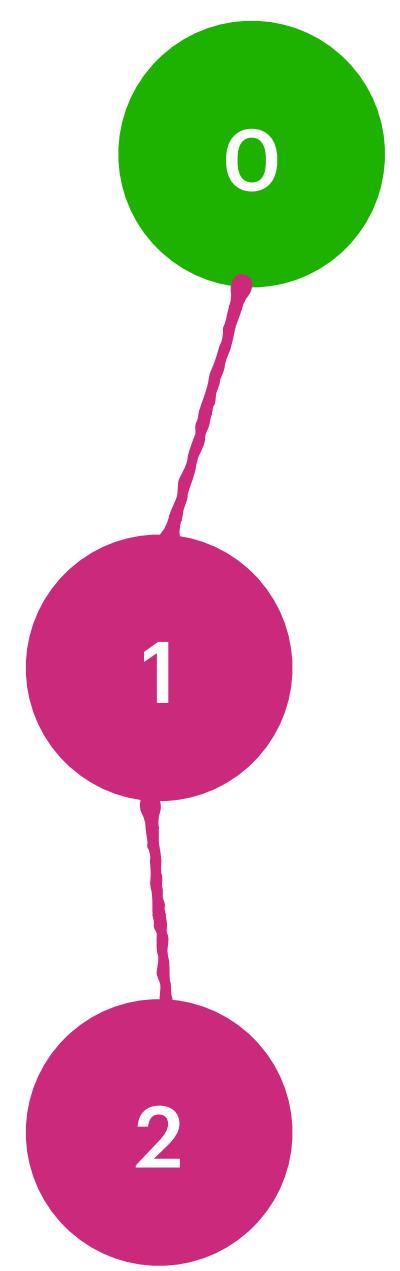


H: 5

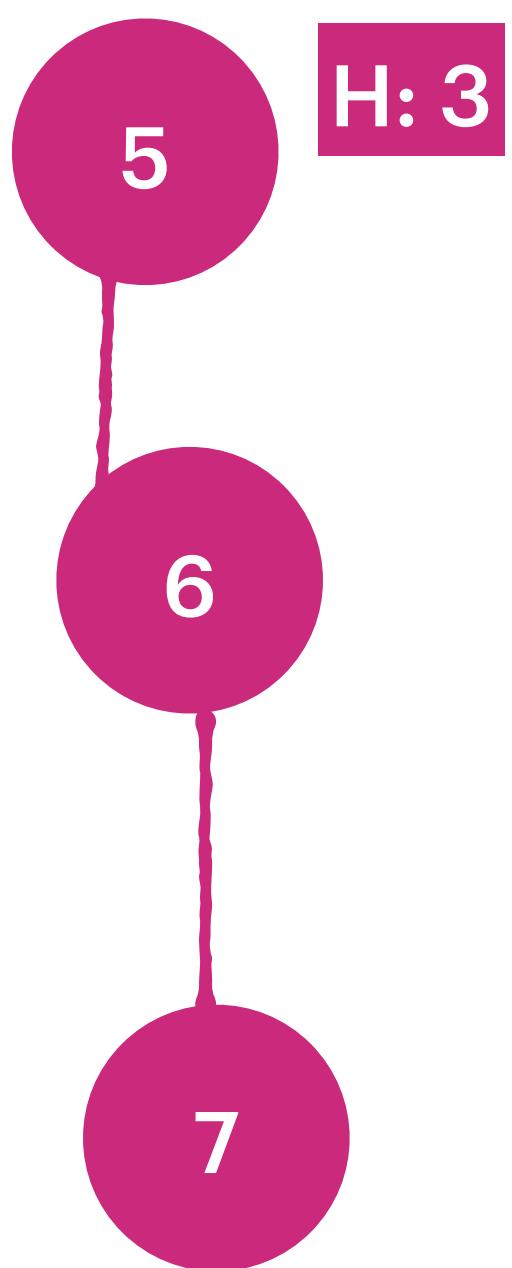
Making

As root

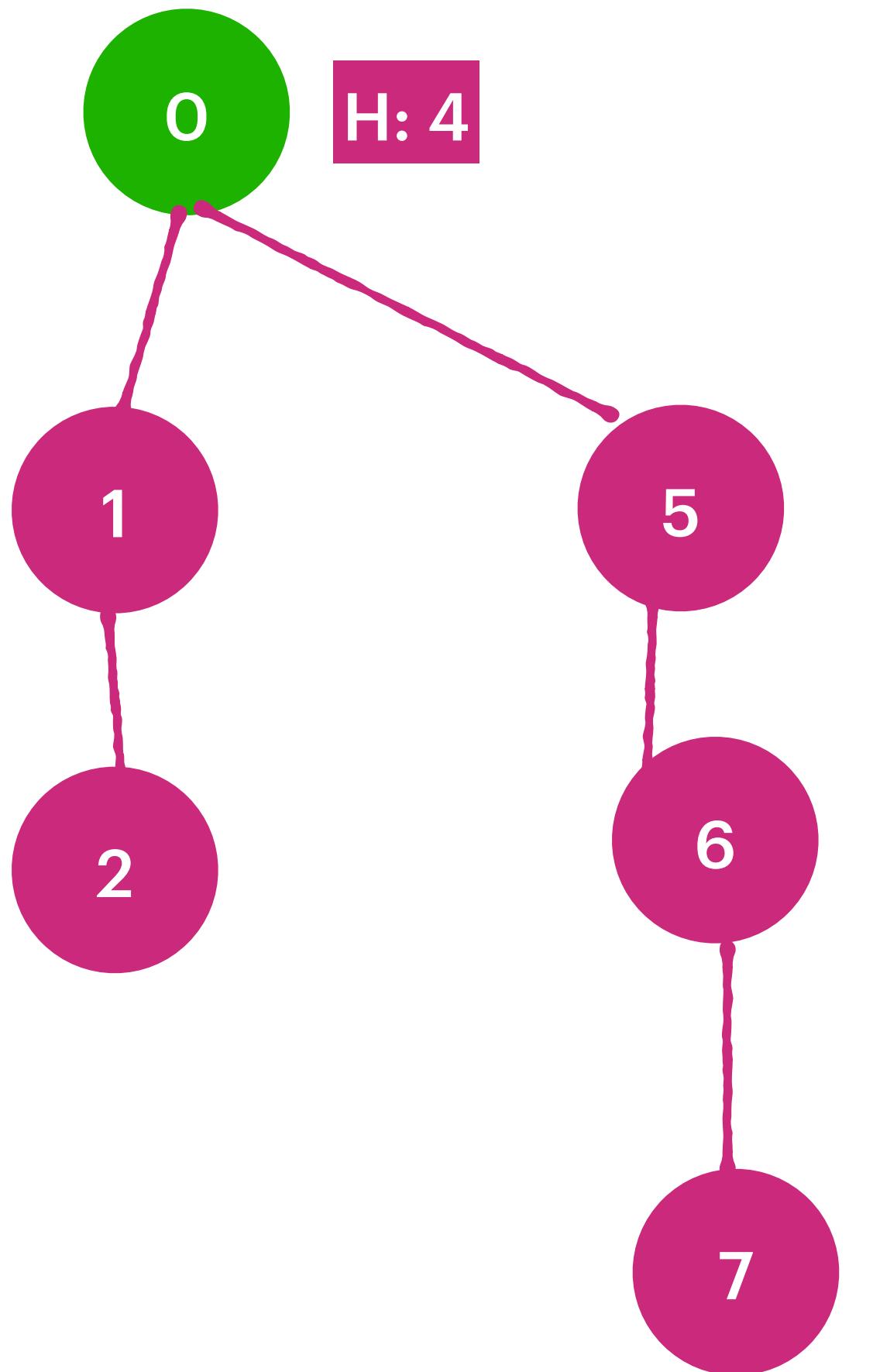
Ranking :
While Joining always assign
Mak Height Root node as Parent.



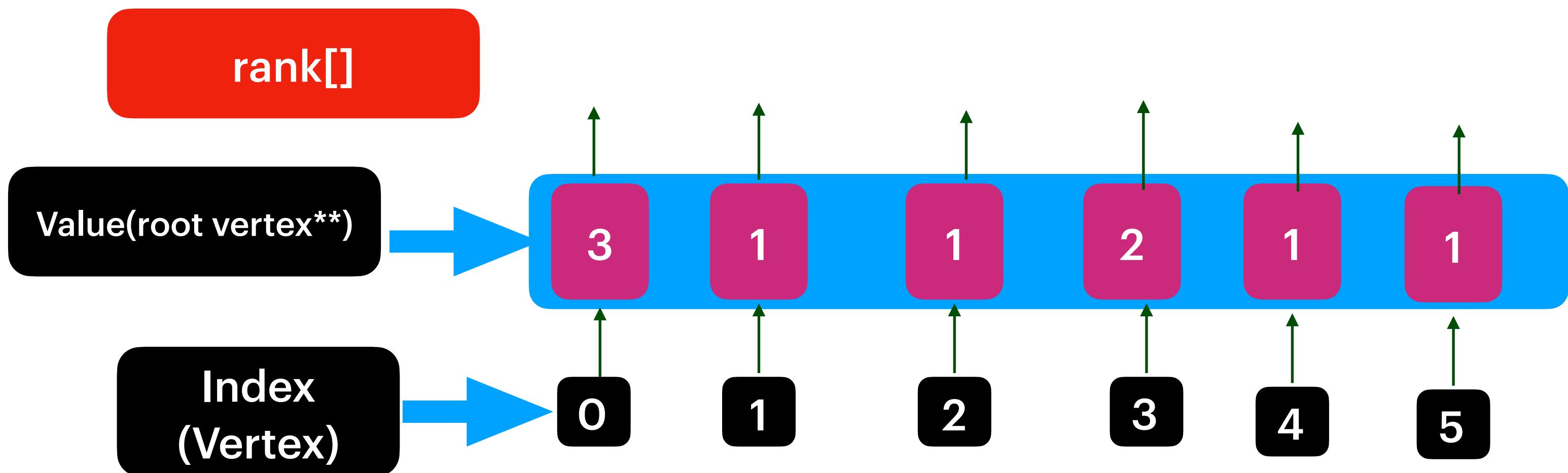
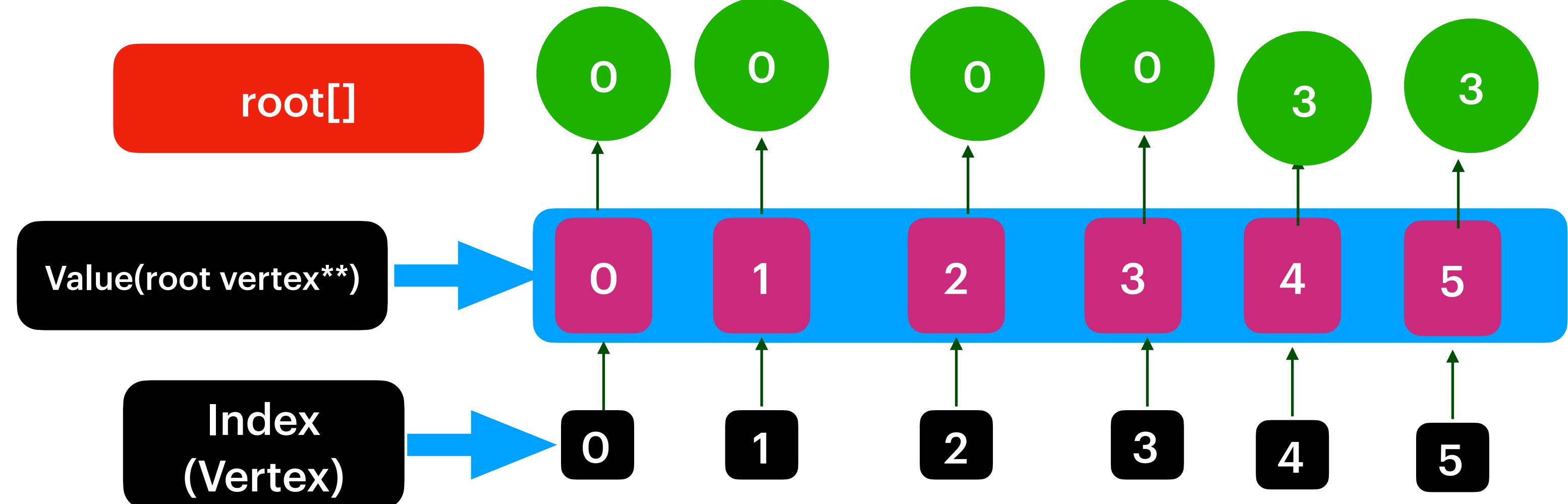
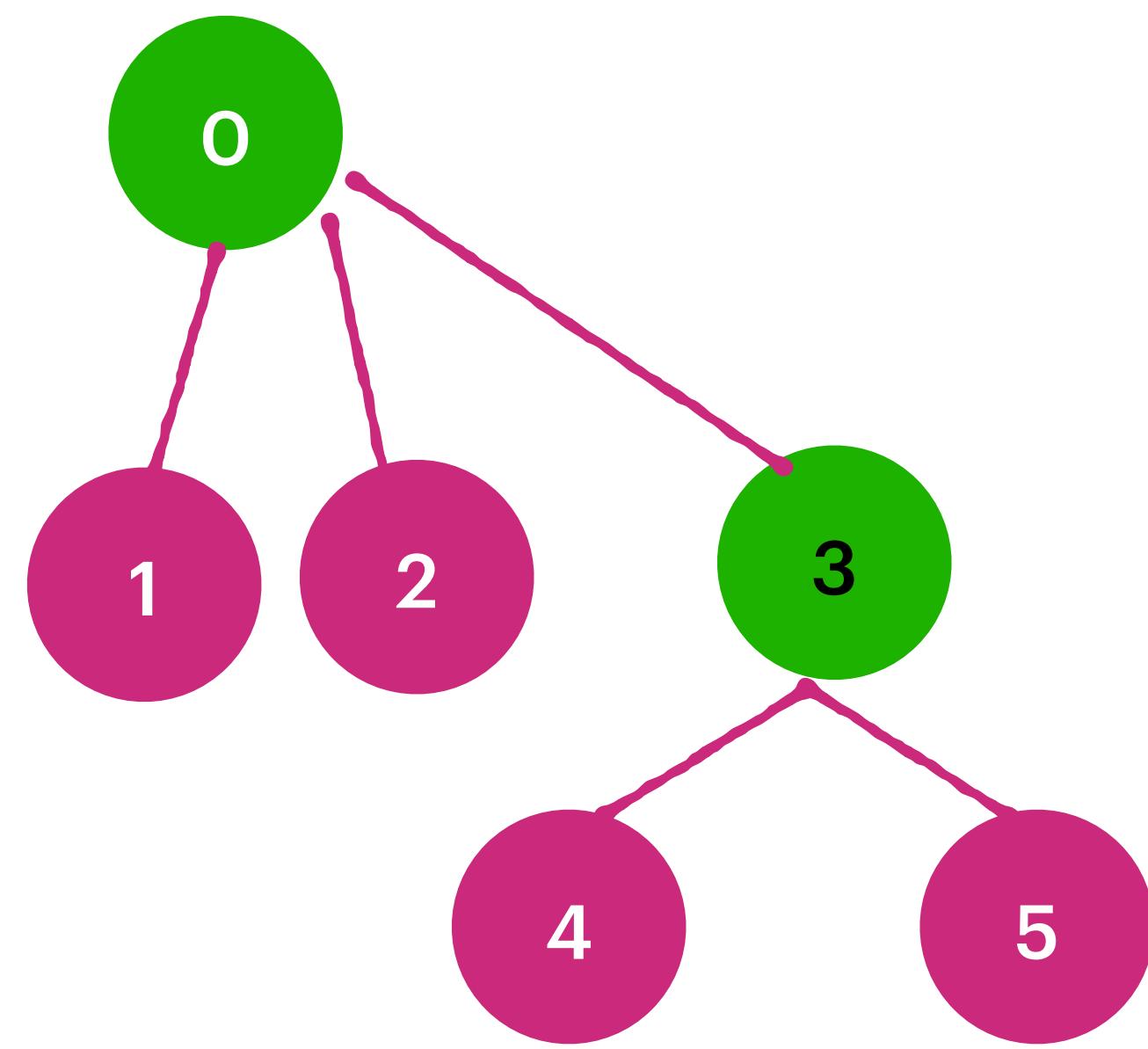
H: 3

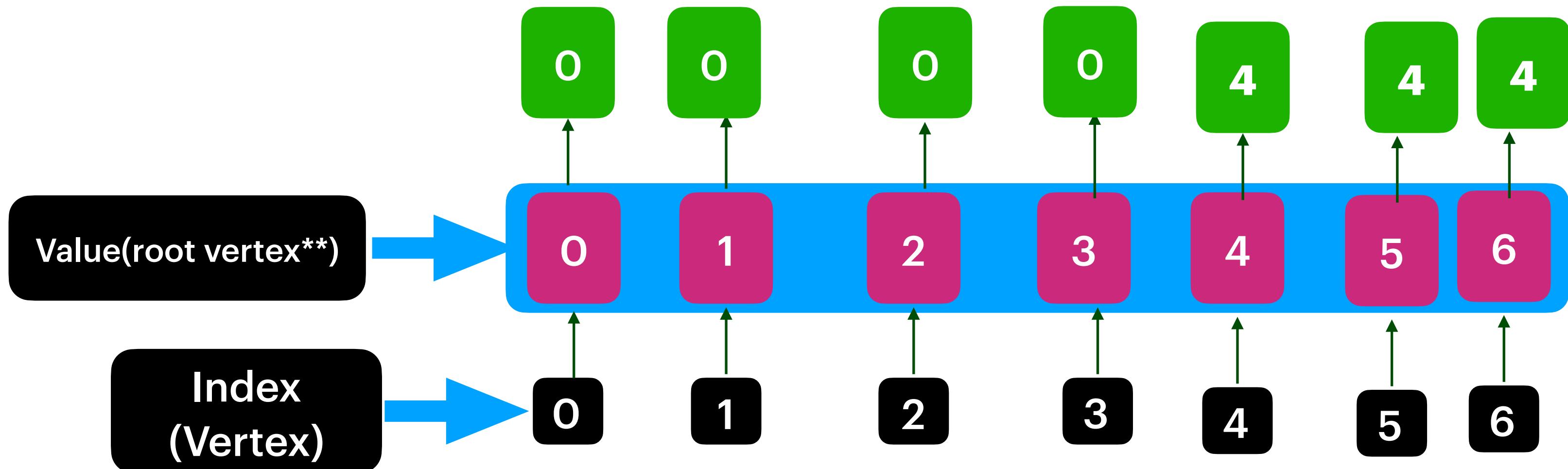
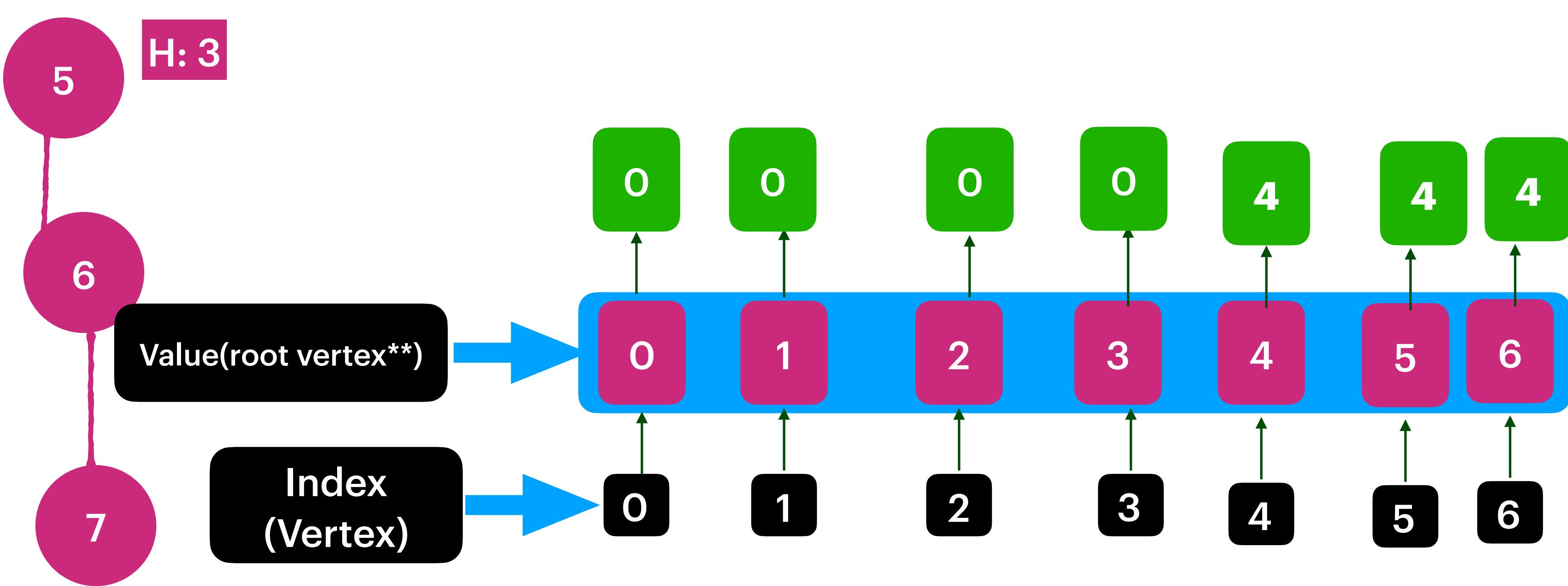
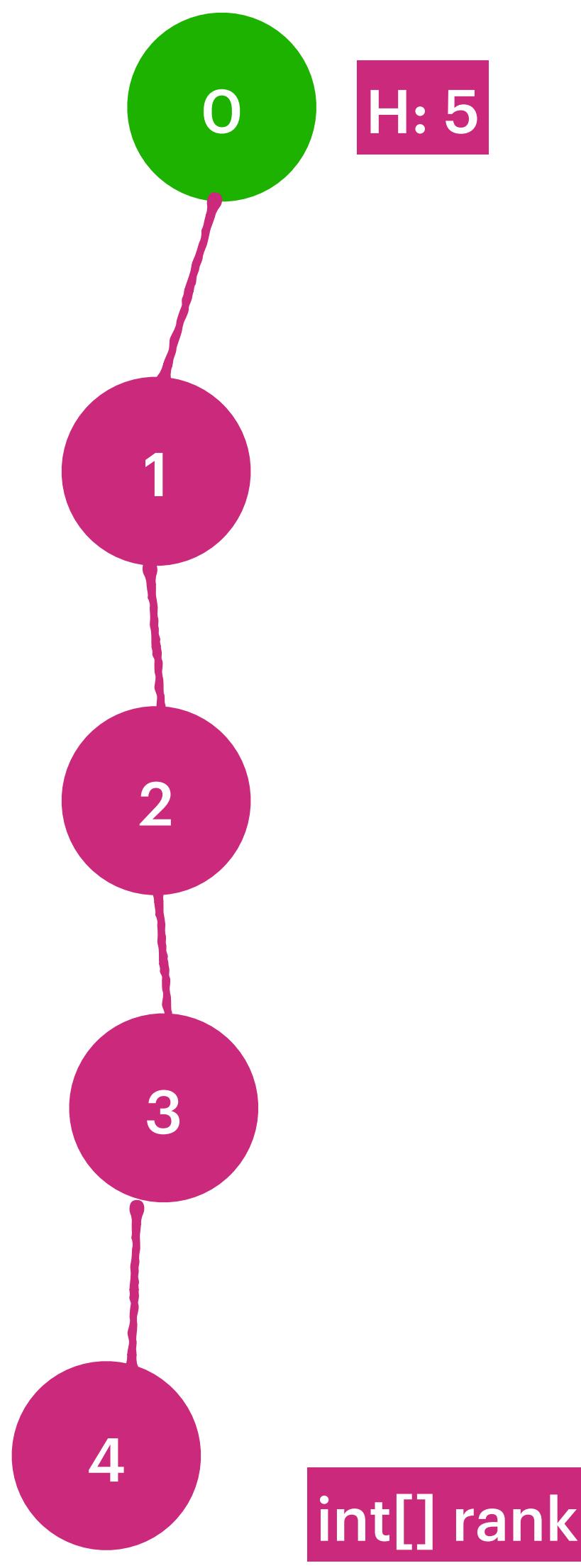


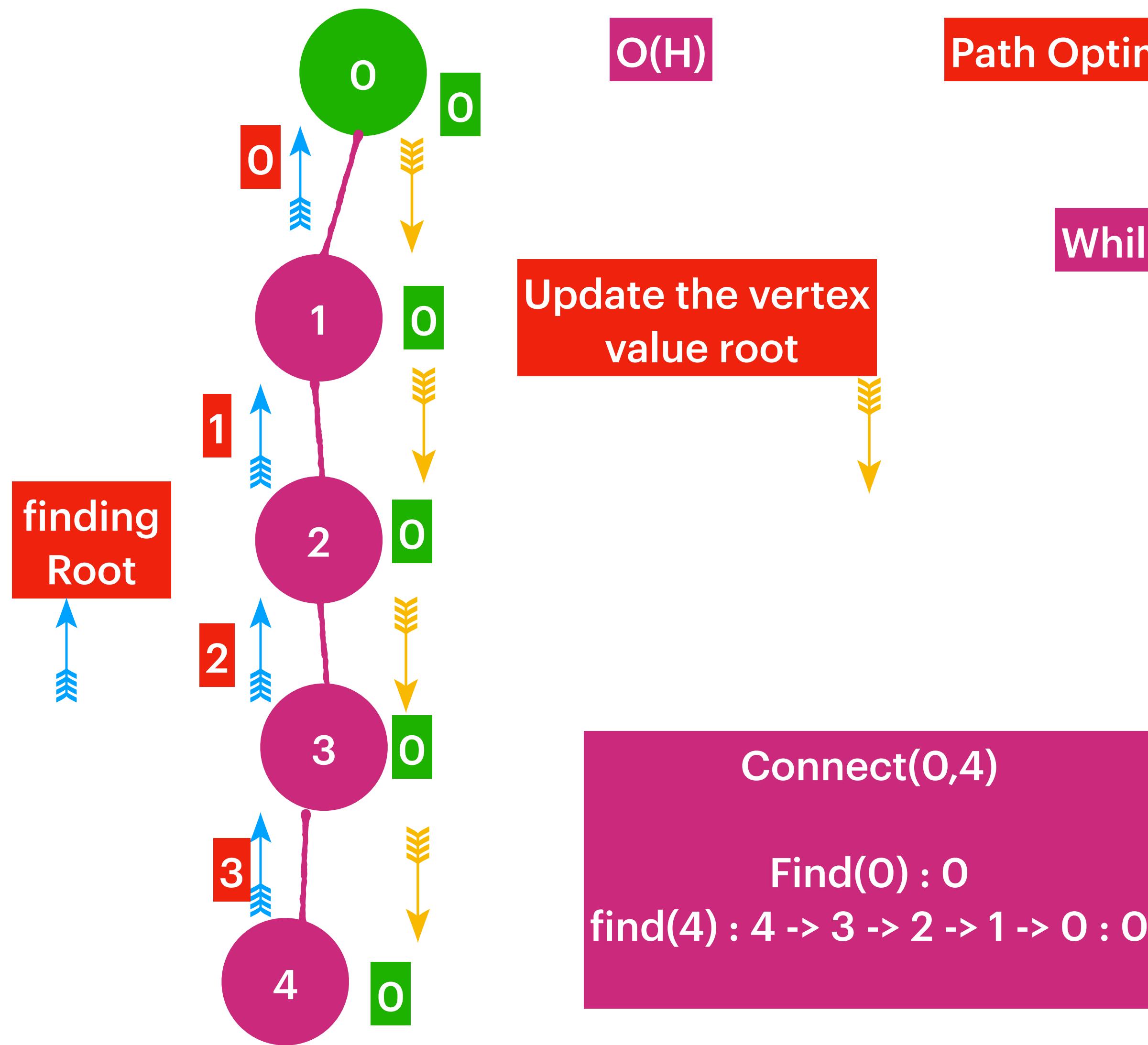
H: 3

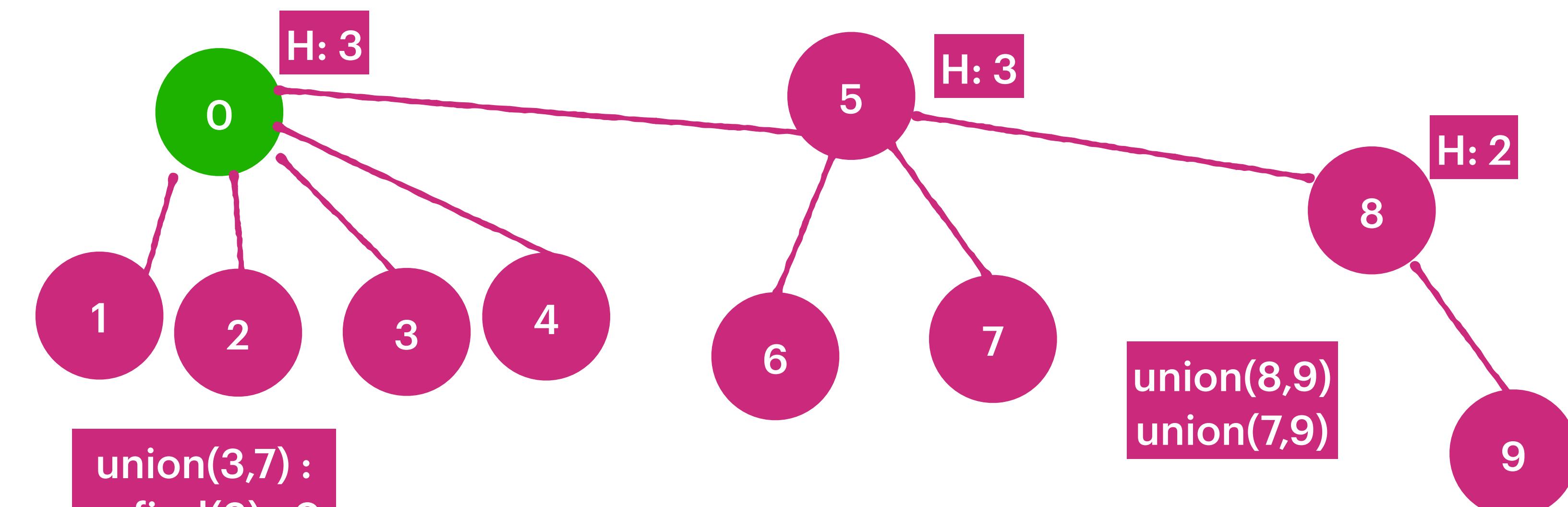


H: 4

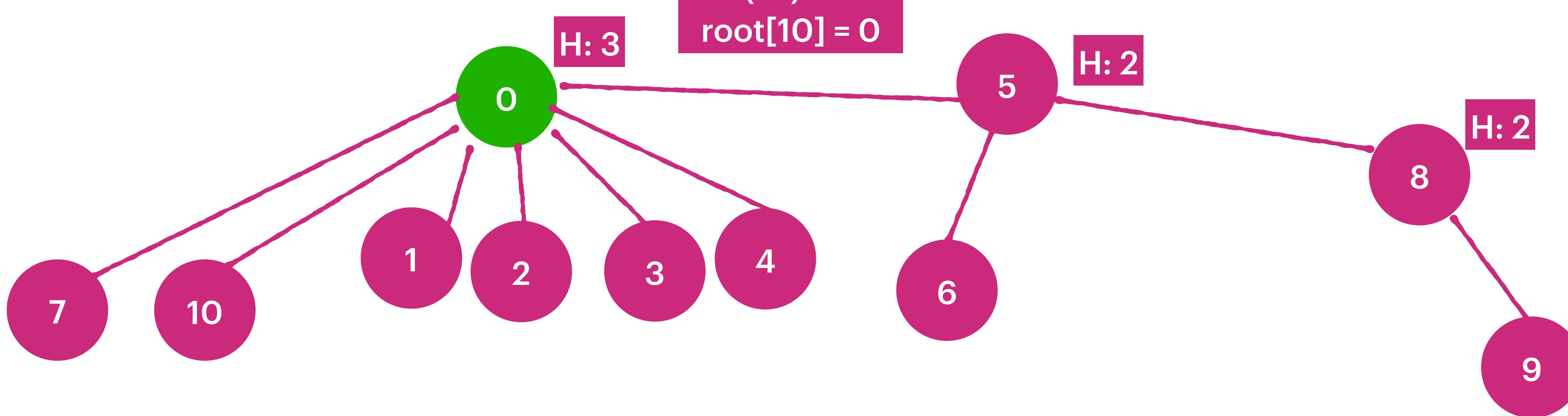


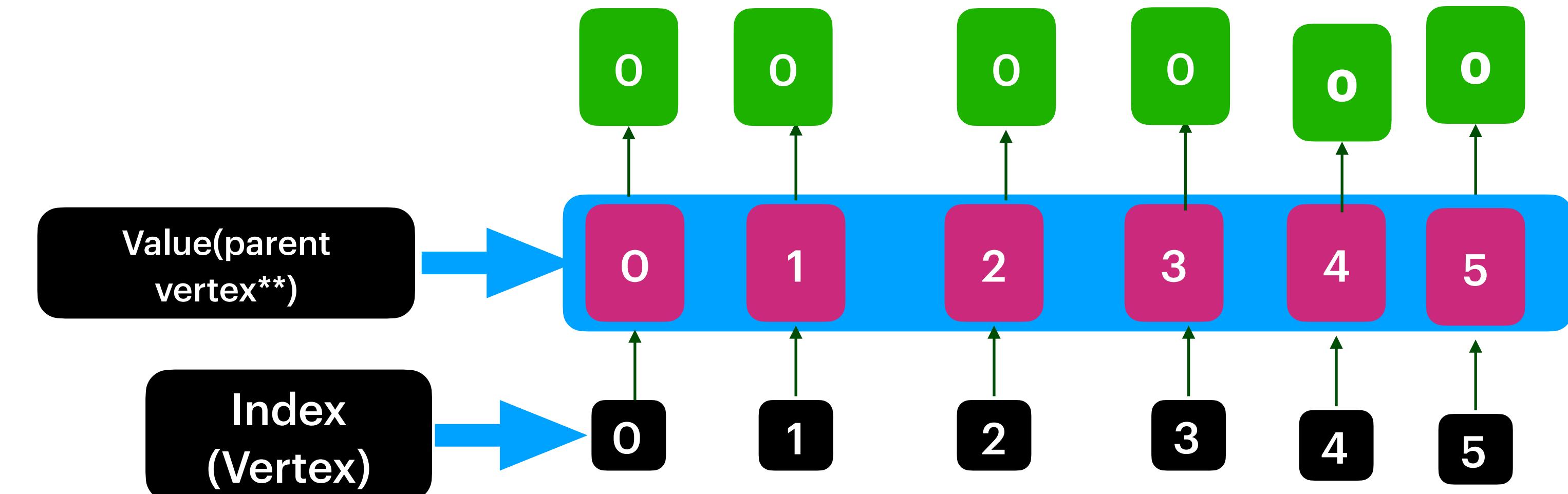
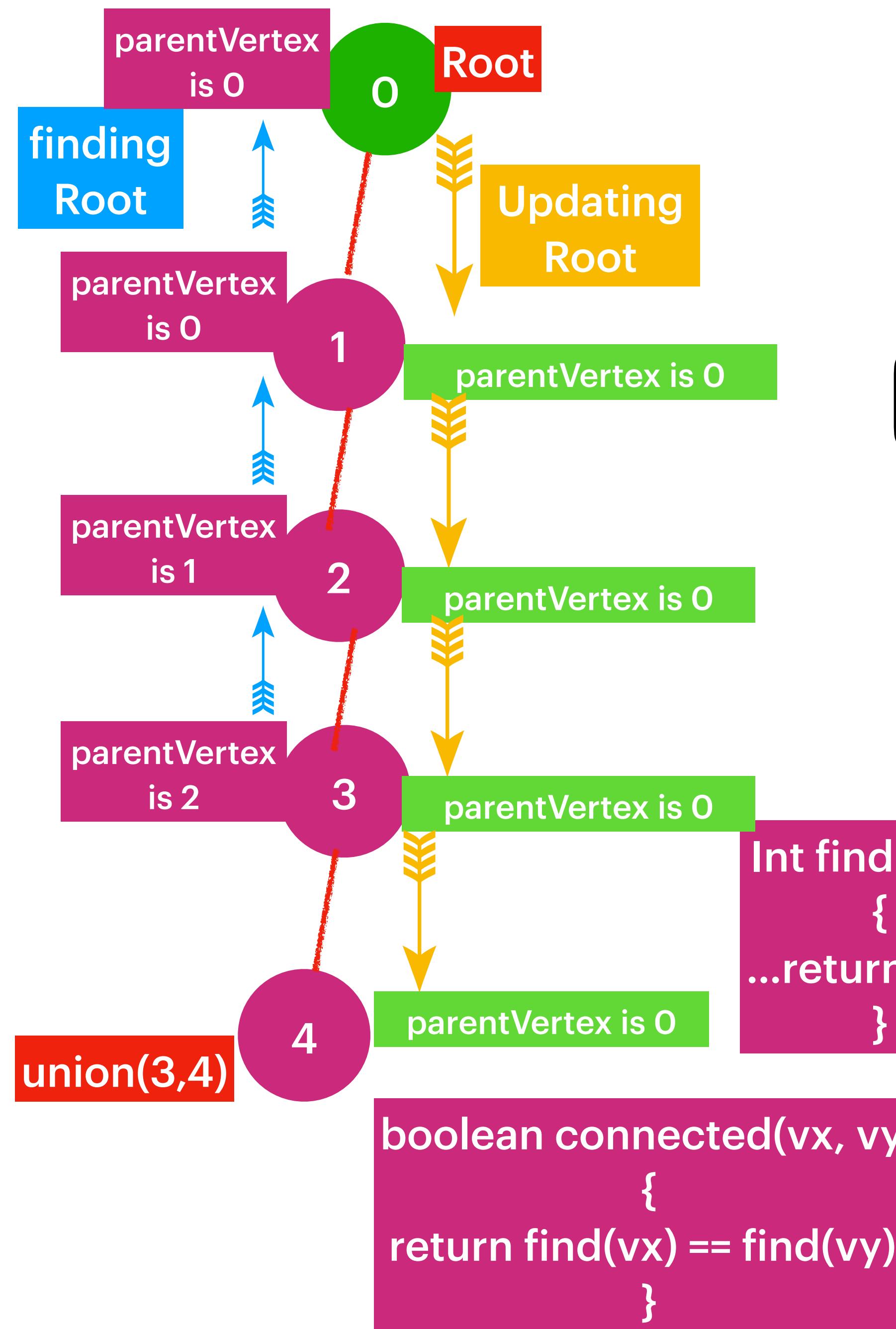






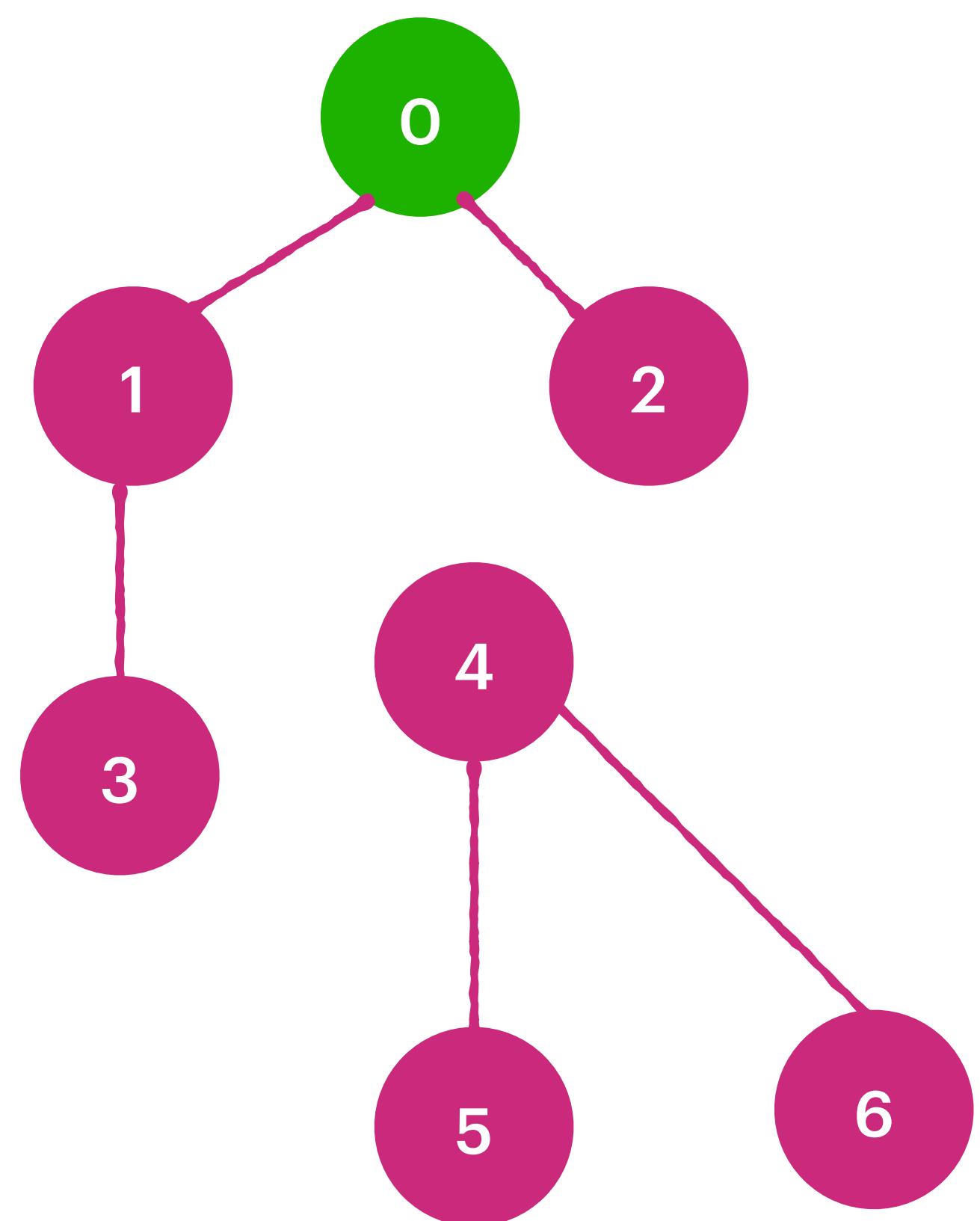
isConnected(1,9) :
 $\text{find}(1) : 0 // 1\text{step}$
 $\text{find}(9) : 8 \rightarrow 5 \rightarrow 0 : 0 // 3\text{steps}$
 returns true.



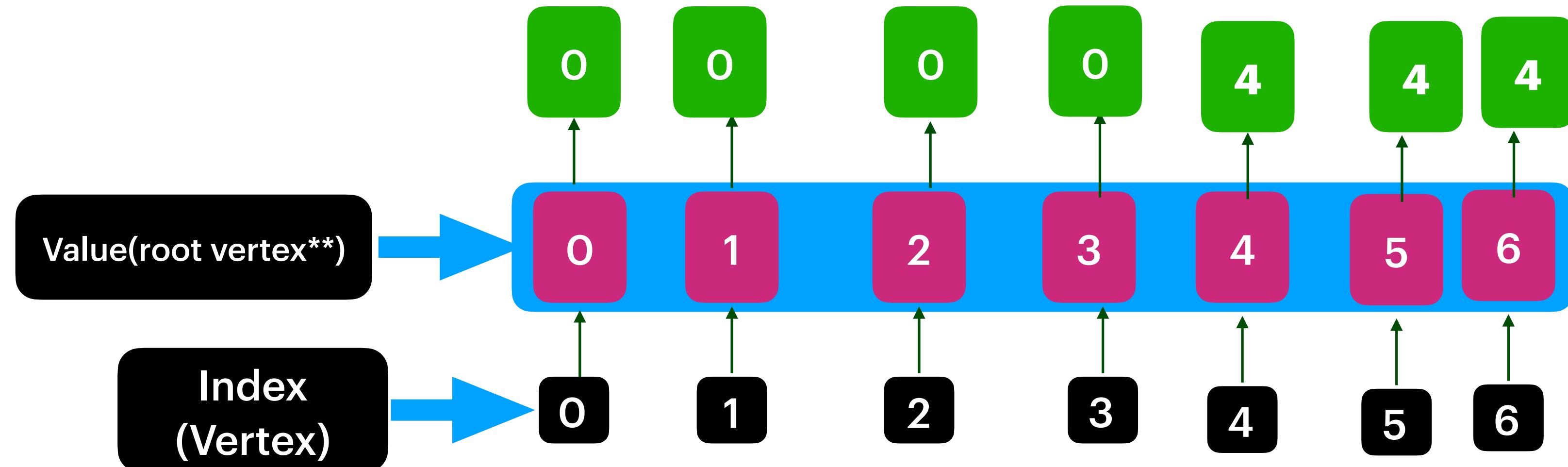


0,4 are Connected ?
 $\text{root}(0) = 0 :// 1 \text{ step}$
 $\text{root}(4) = 0 // 4 \text{ steps } \sim n$

```
union(int vx, vy)  
{  
    ...  
    ...  
}  
}
```



Quick Union :



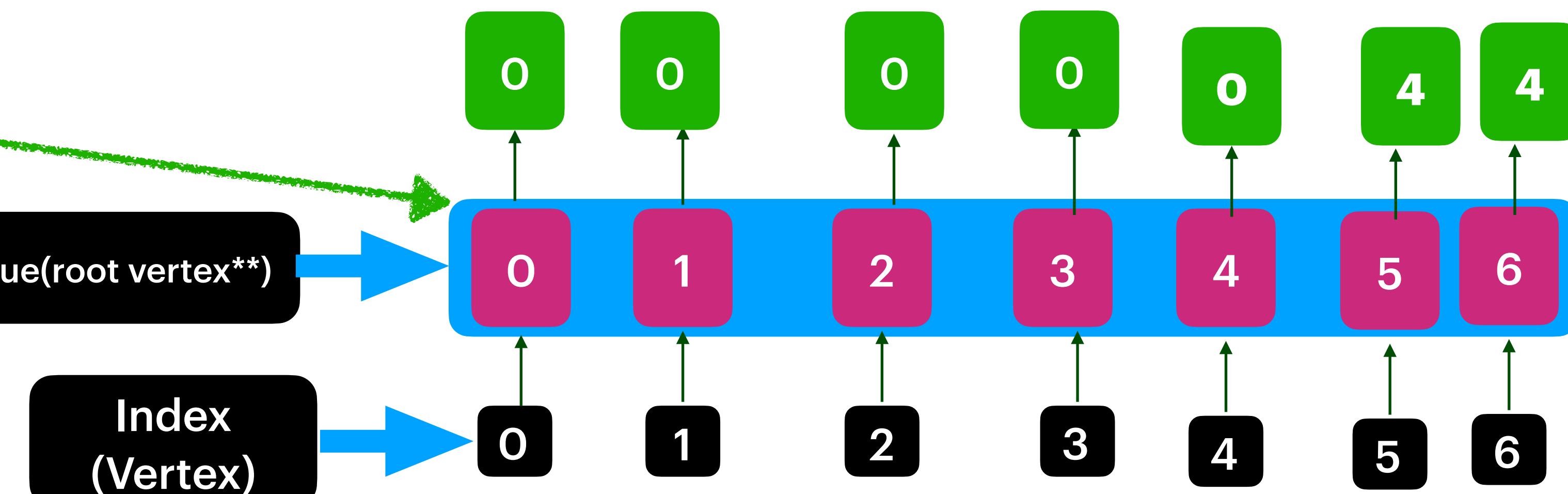
**union(0,1)
union(0,2)
union(1,3)
union(4,5)
union(4,6)**

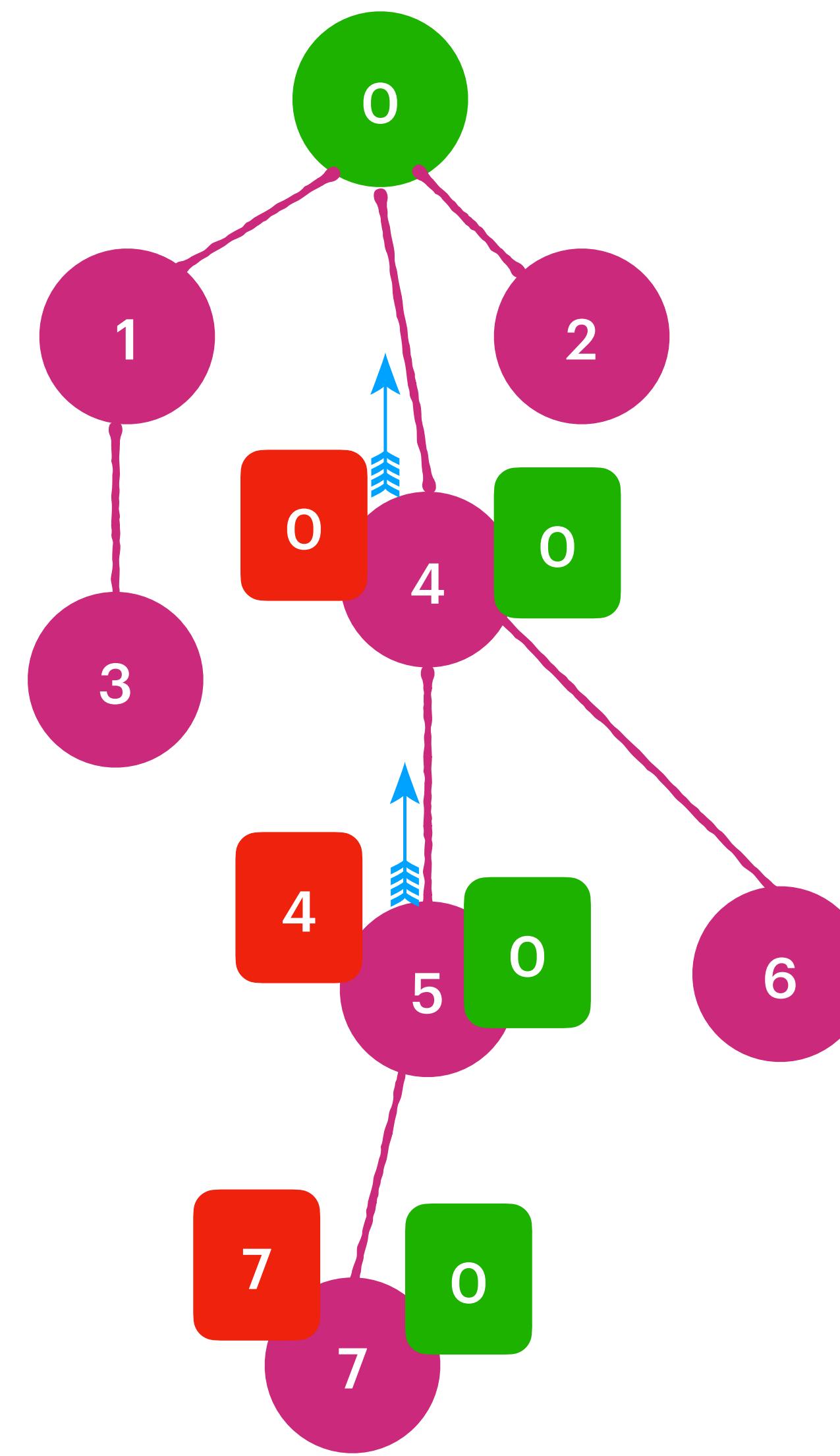
```

union(0, 1)
Int rootX = find(x); // 0
Int rootY = find(y); // 1
root[rootY] = rootX; //

```

After union(3,5)
Int rootX = find(3) = 0
Int rootY = find(5) = 4
root[rootY] = rootX
root[4] = 0

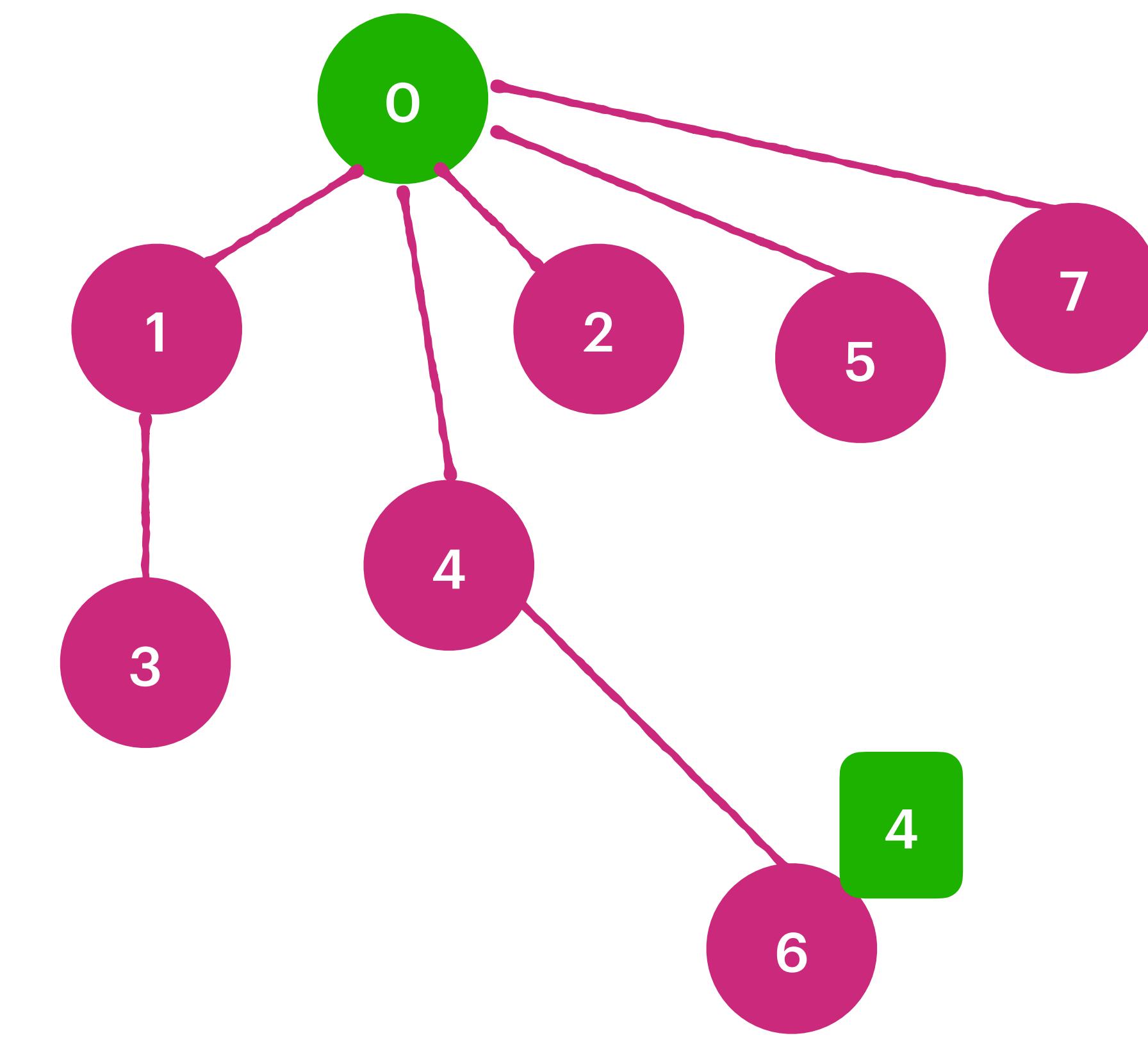




Quick Union :

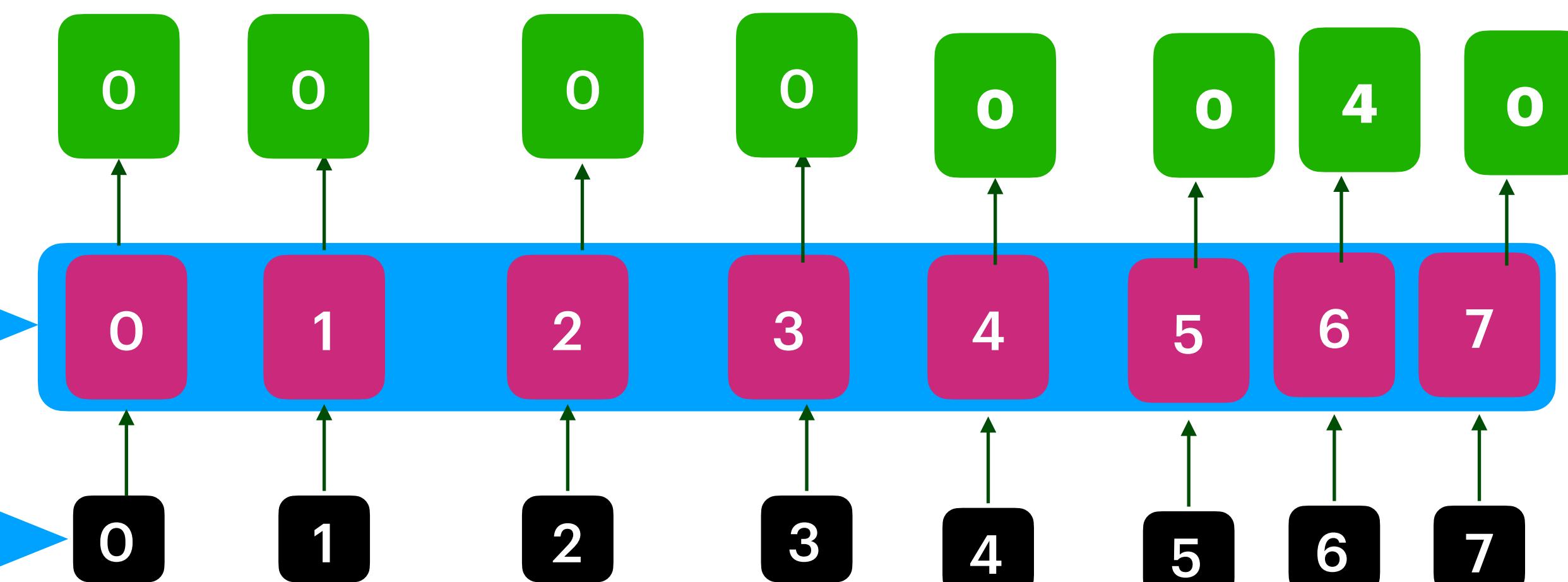


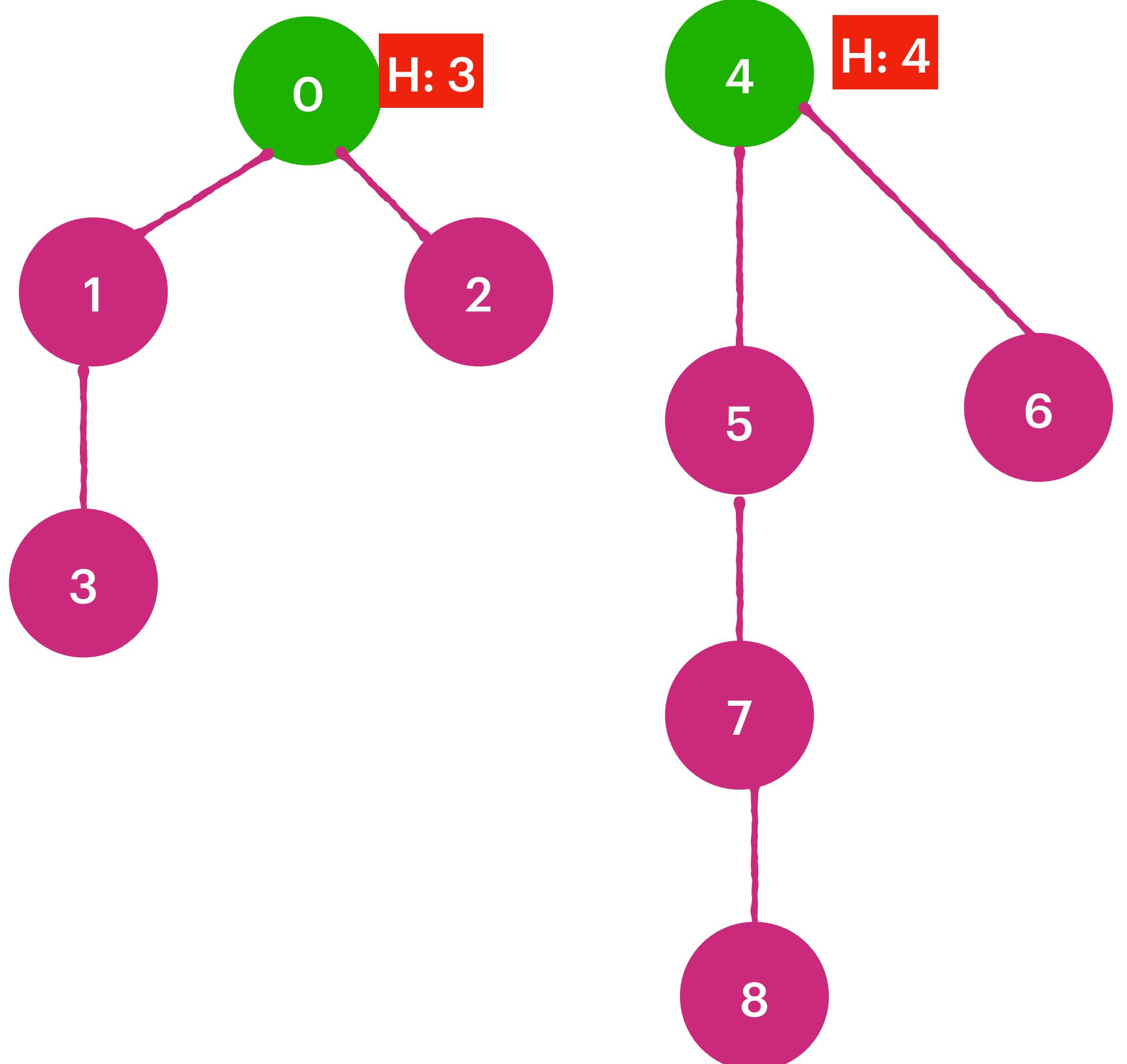
`union(5,7)`



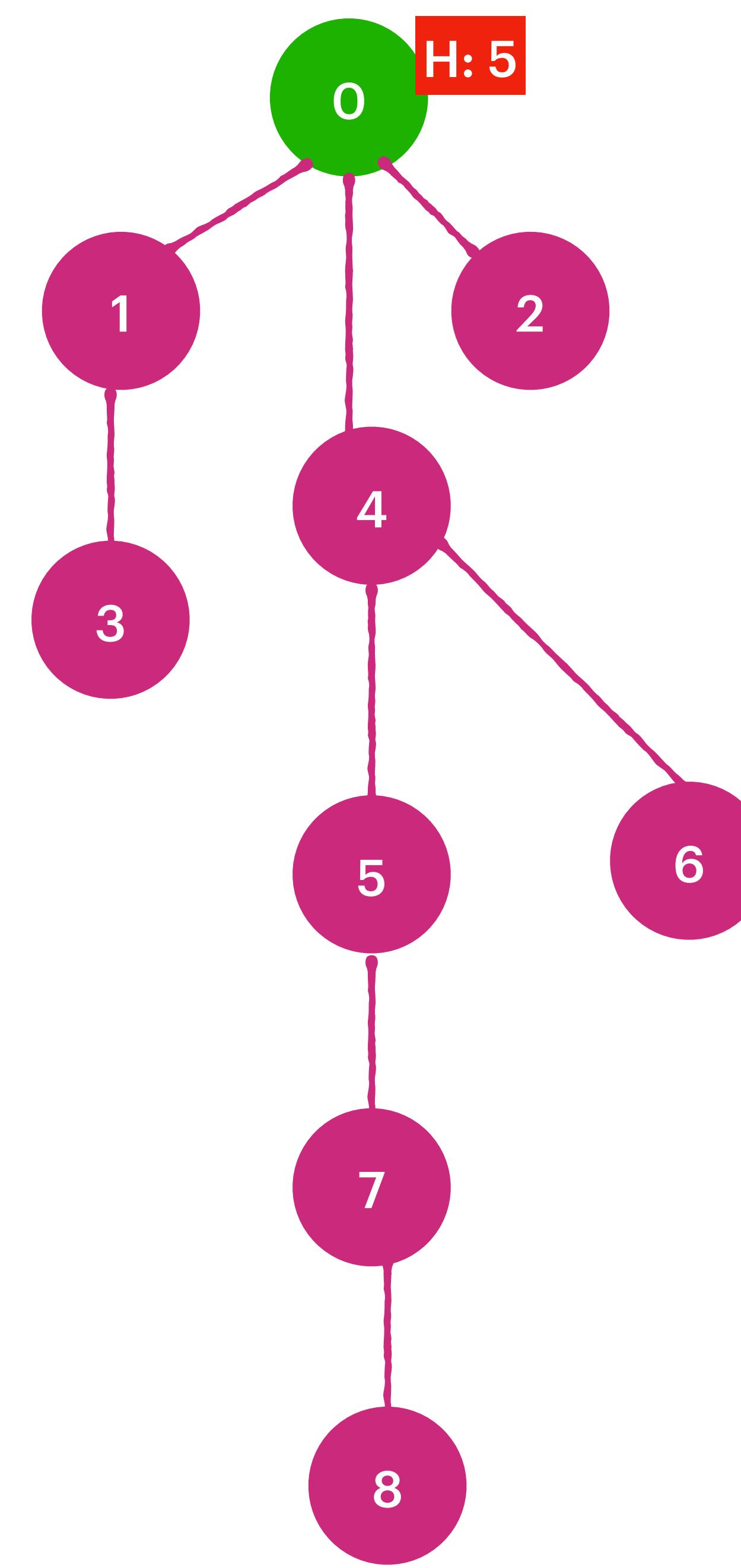
Value(root vertex**)

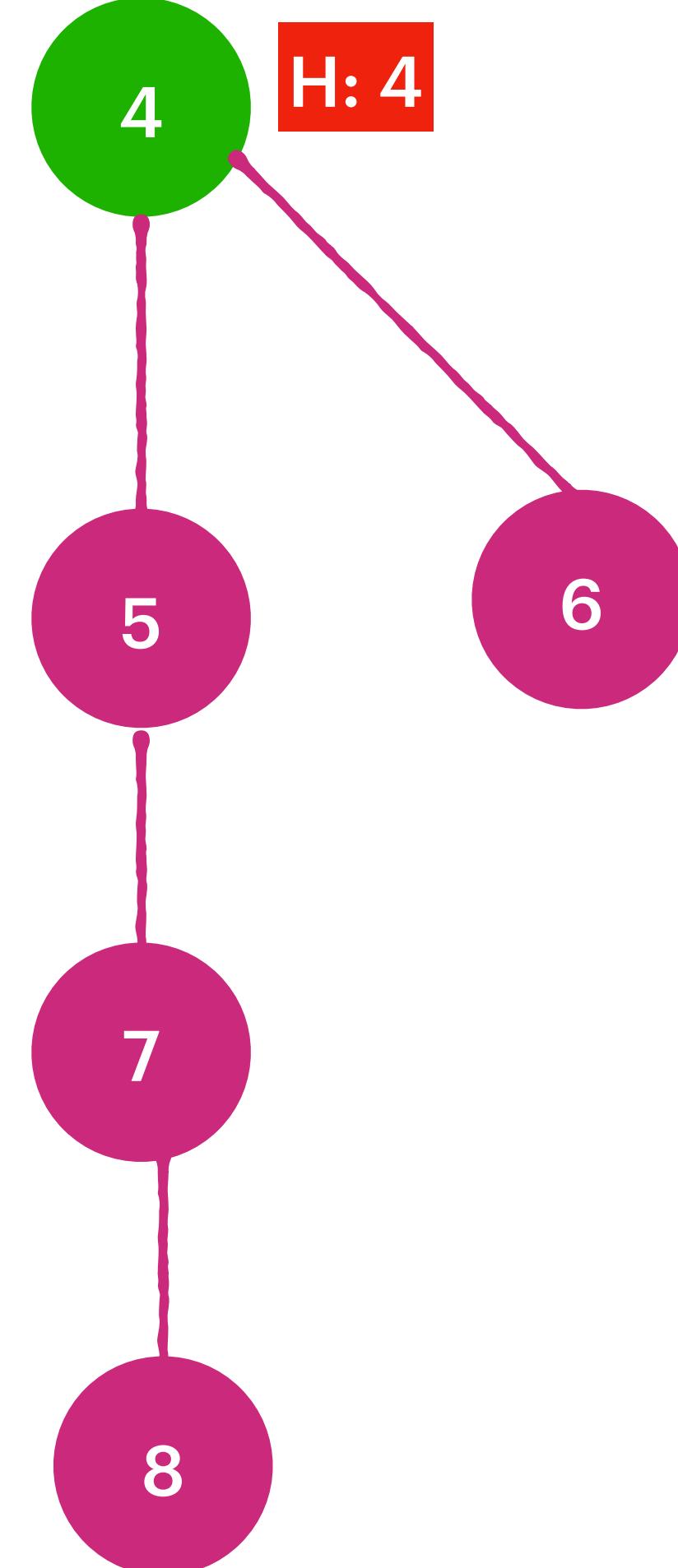
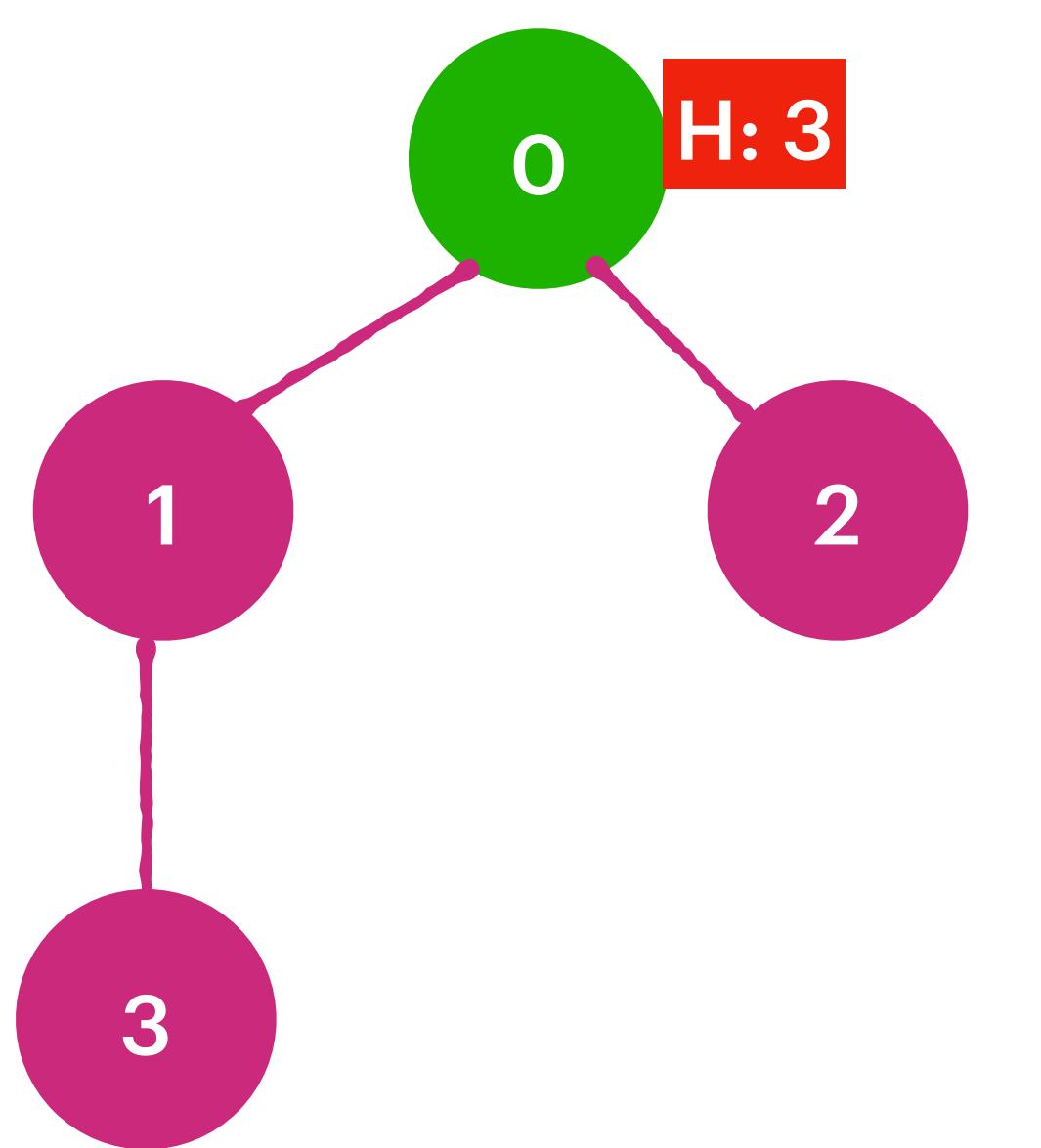
Index
(Vertex)





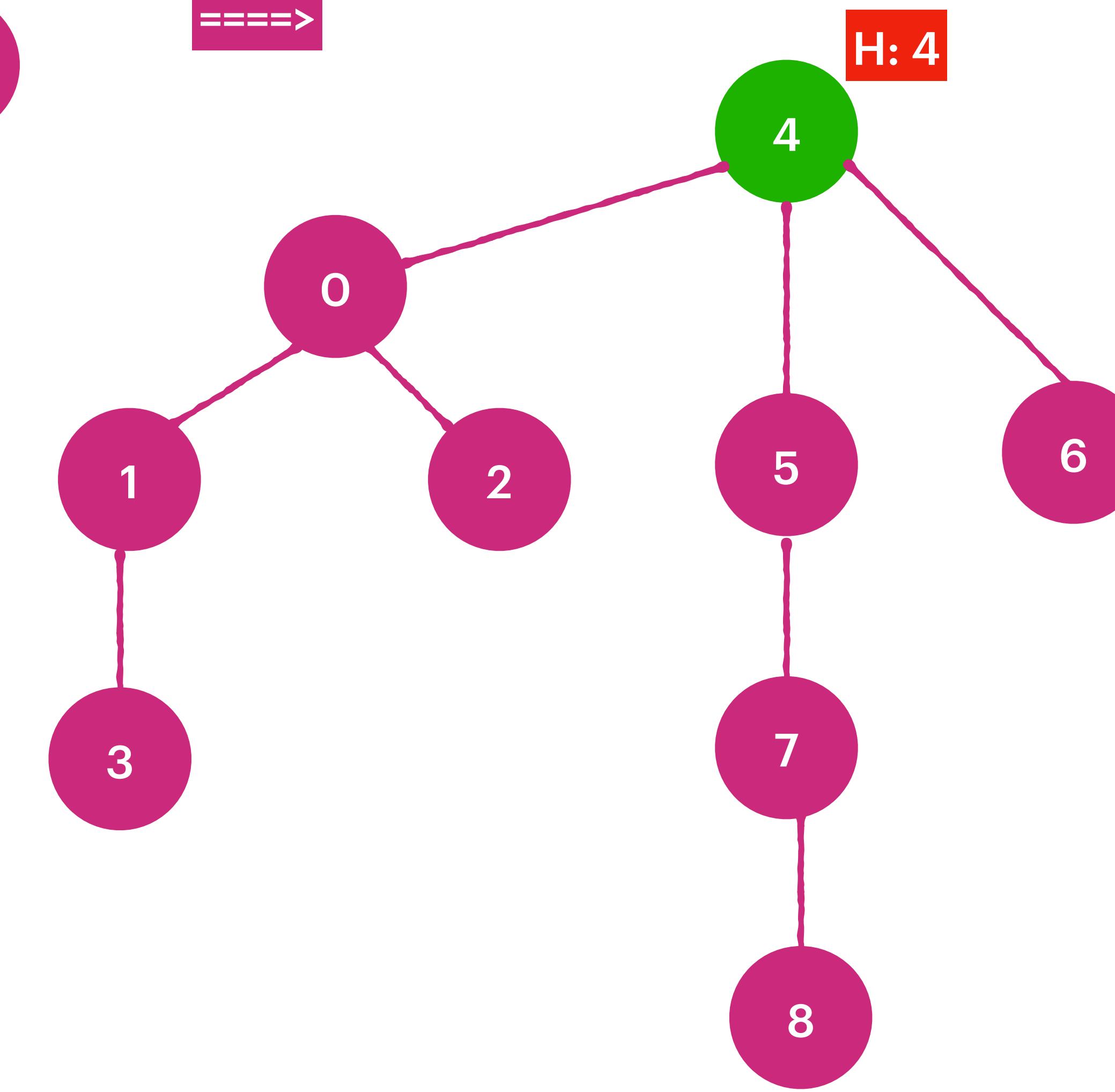
union(3,8)
find(3) = 0
find(8) = 4
vetexs[4] = 0
=====>

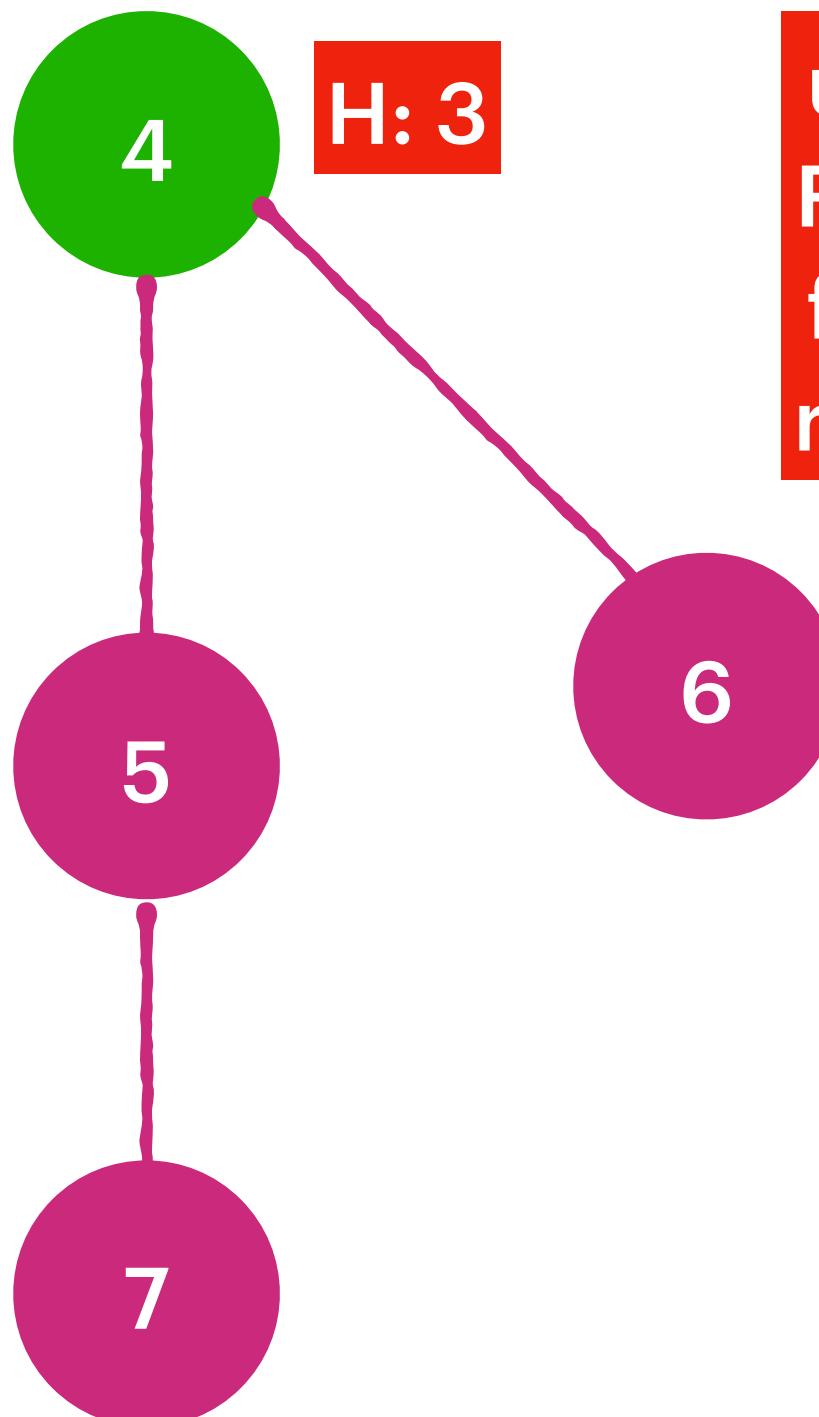
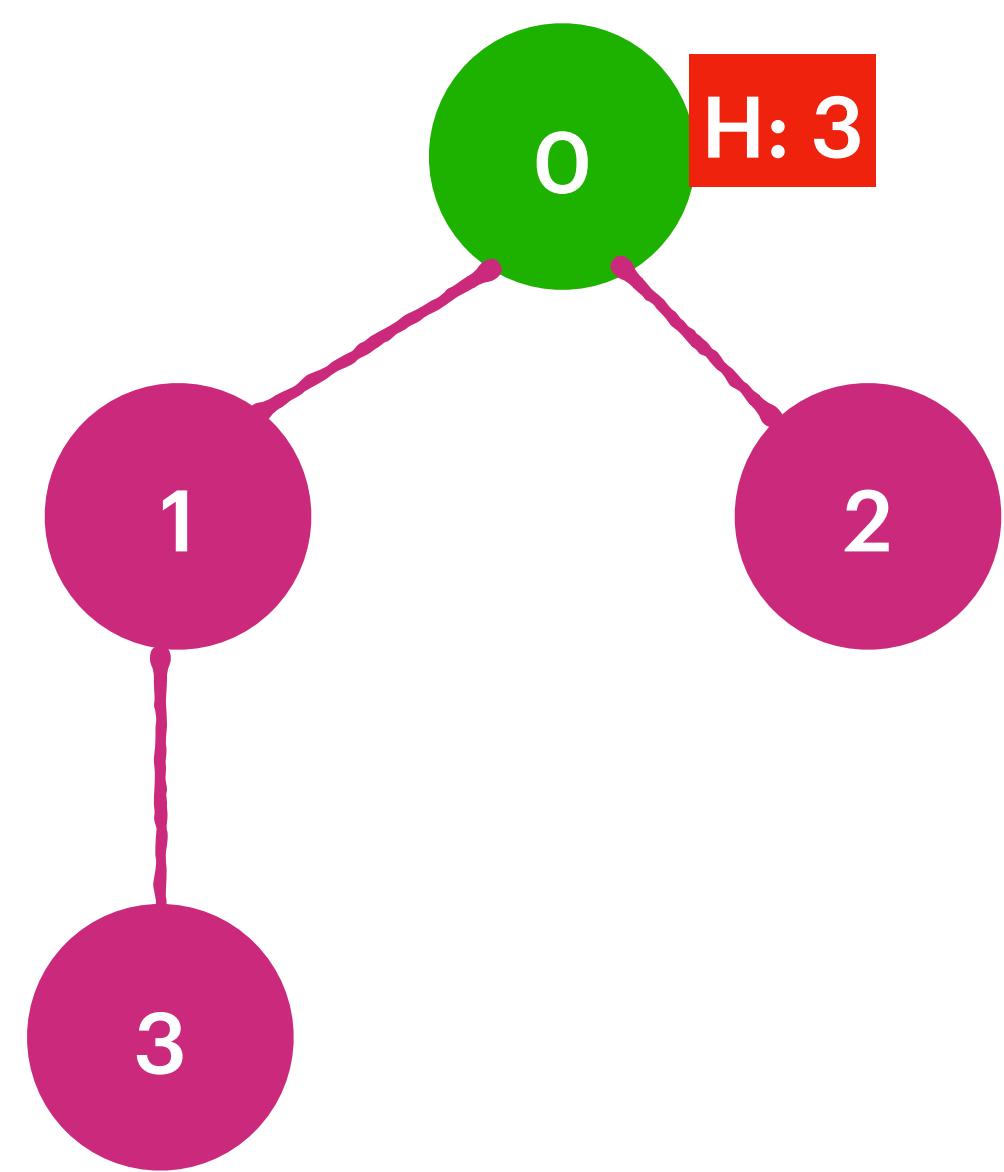




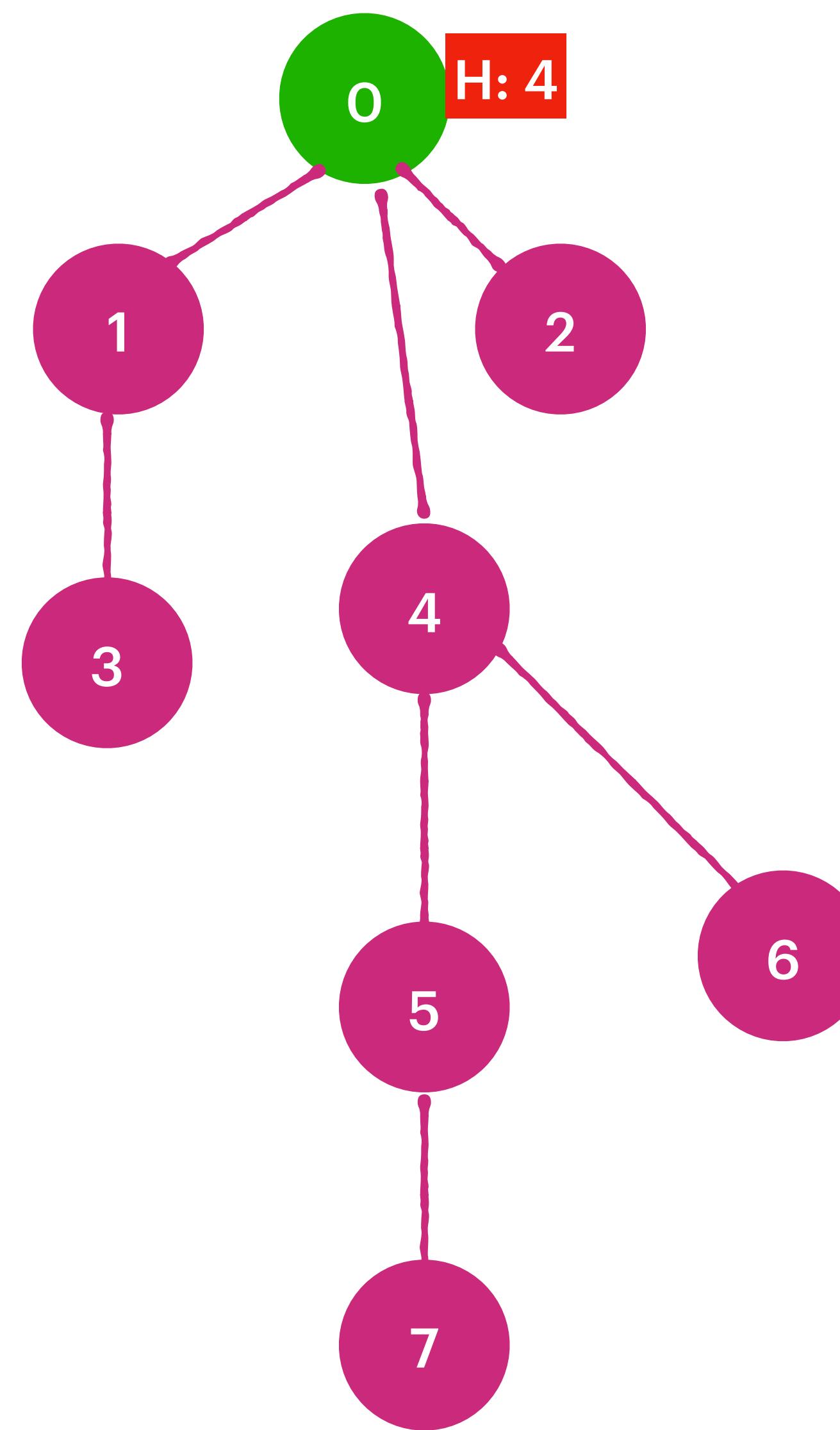
union(3,8)
find(3) = 0
find(8) = 4
vetexs[0] = 4

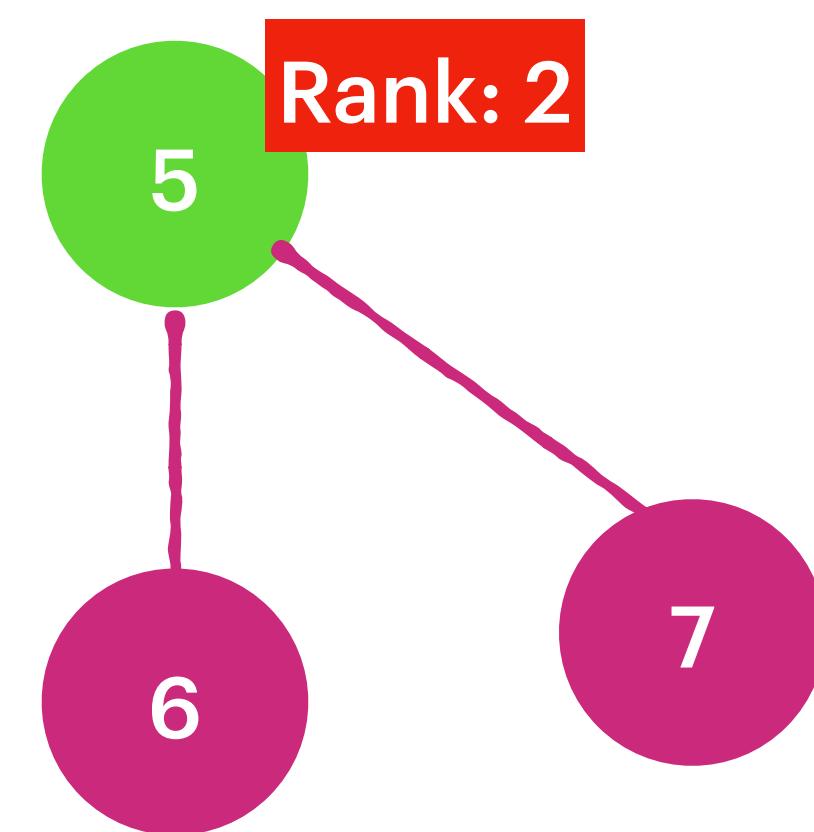
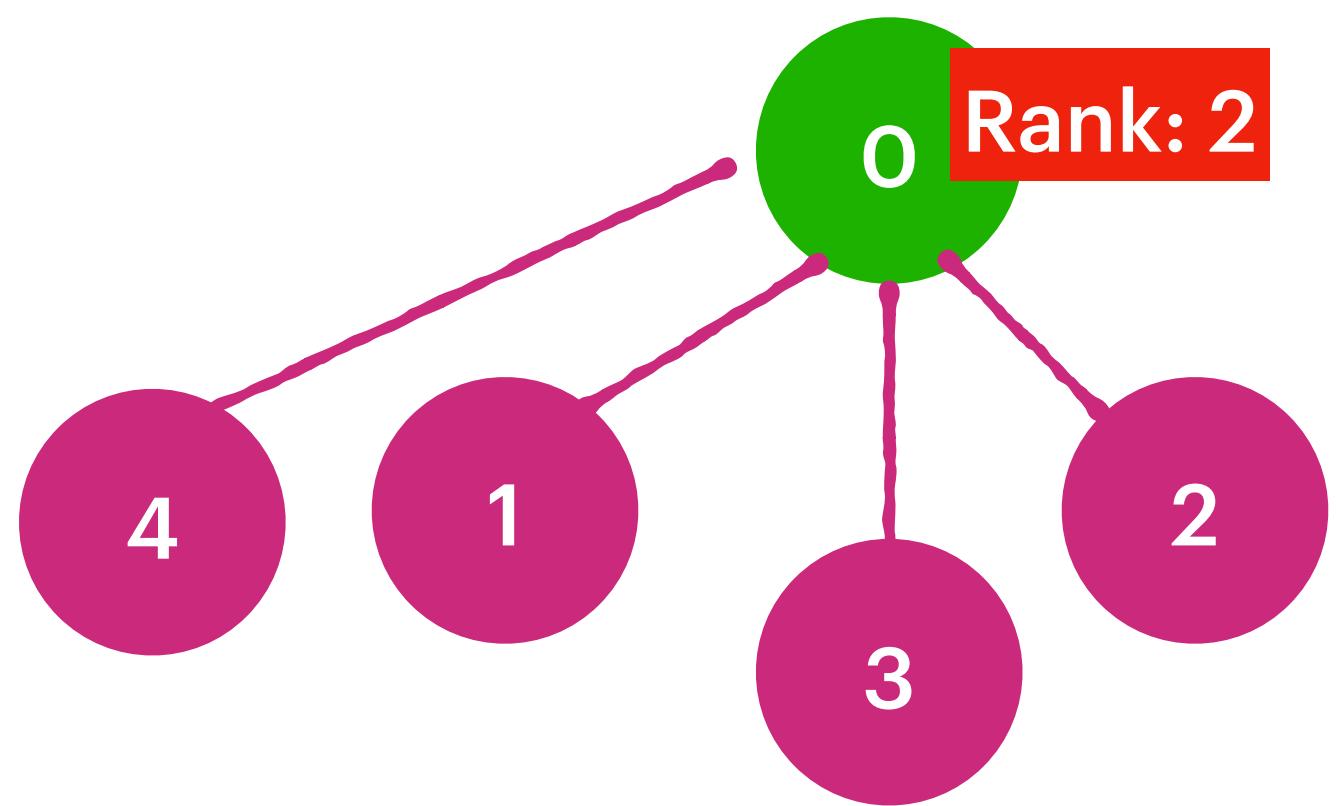
=====>



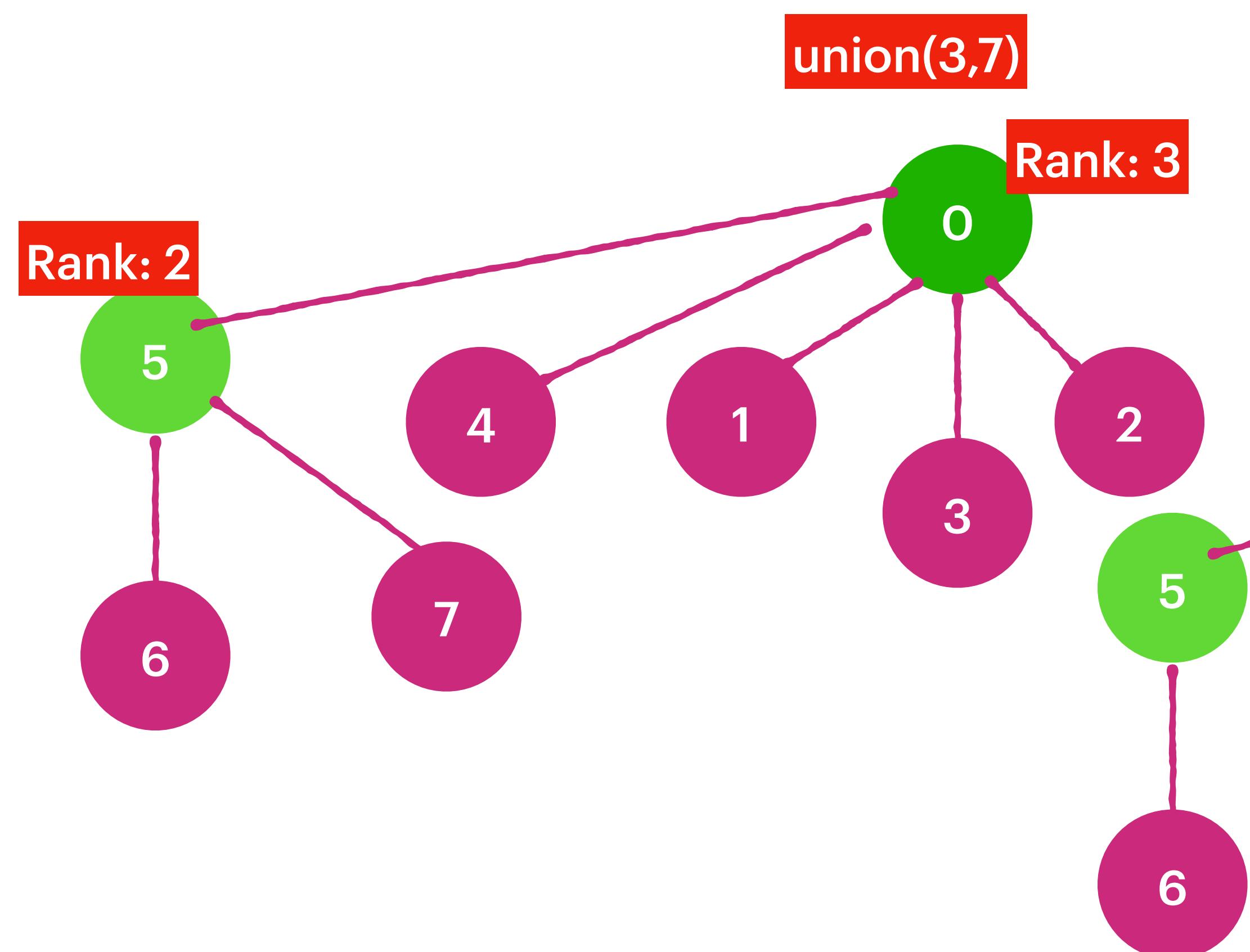


union(2,7)
Find(2) = 0
find(7) = 4
root[4] = 0
=====>



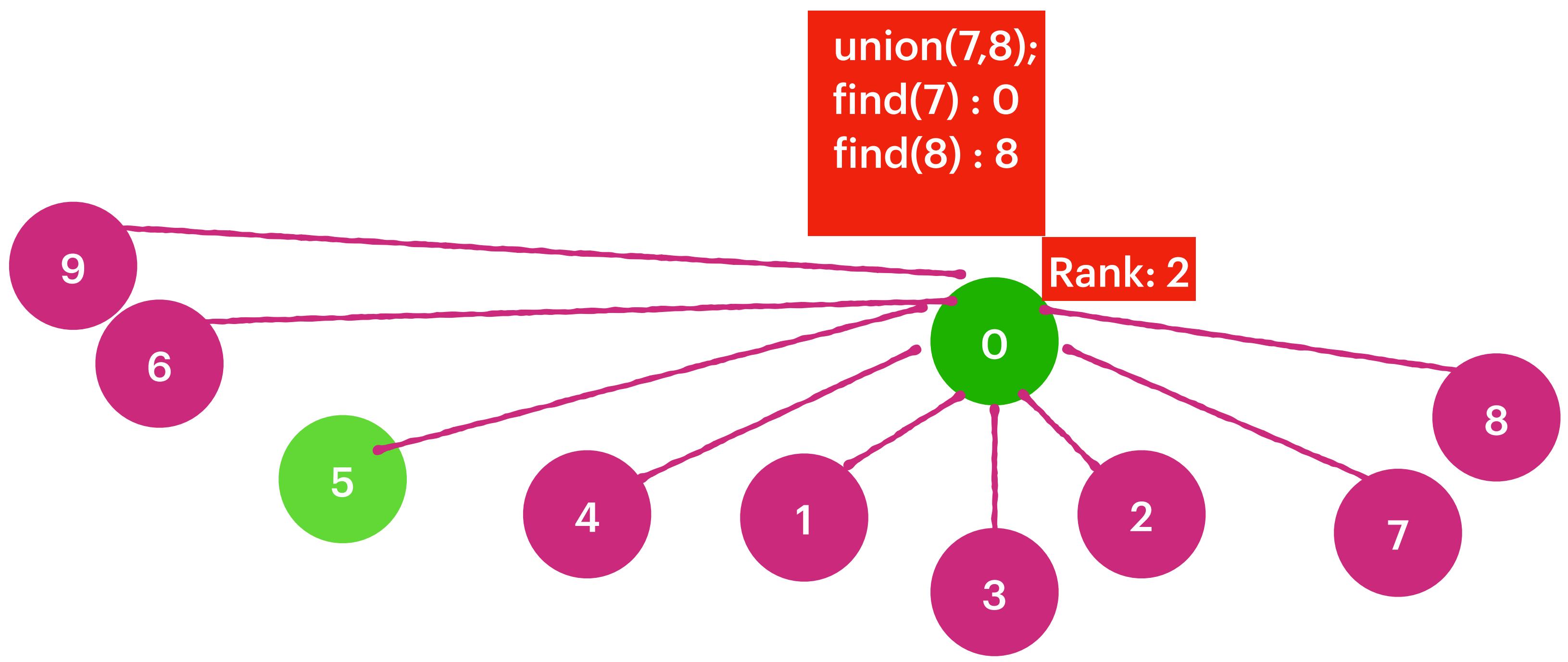


// 0-1-2-3-4 :: 5-6-7 :: 8



union(7,8);
find(7) : 0
find(8) : 8

```
union(7,8);  
find(7) : 0  
find(8) : 8
```



```
union(6,9)  
Find(6) : 0  
Find(9) : 9
```

Graph Valid Tree

You have a graph of n nodes labeled from 0 to $n - 1$. You are given an integer n and a list of edges where $\text{edges}[i] = [a_i, b_i]$ indicates that there is an undirected edge between nodes a_i and b_i in the graph.
Return true if the edges of the given graph make up a valid tree, and false otherwise.

Input: $n = 5$, $\text{edges} = [[0,1],[0,2],[0,3],[1,4]]$

Output: true

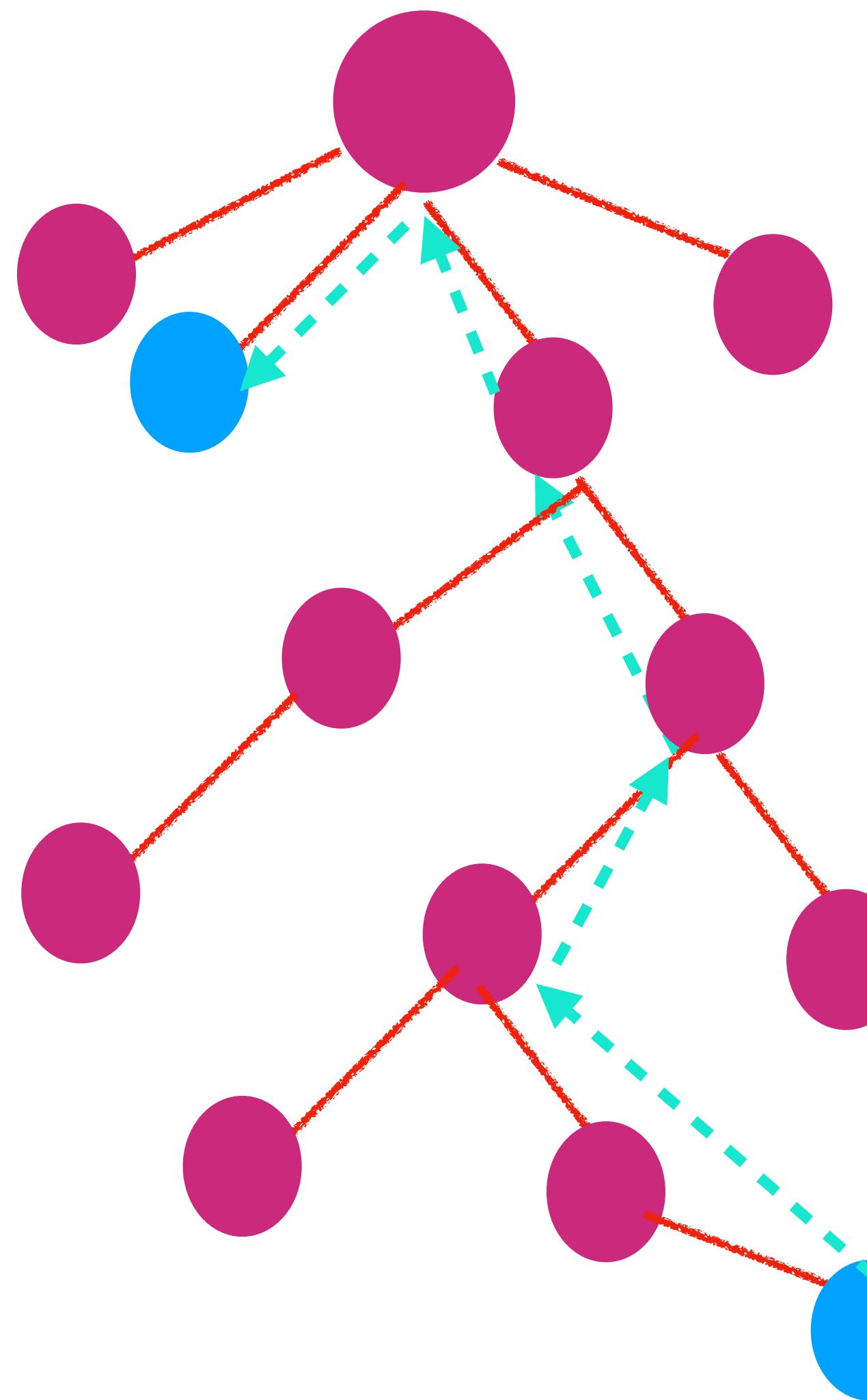
Input: $n = 5$,
 $\text{edges} = [[0,1],[0,4],[1,4],[2,3]]$
Output: false

Input: $n = 5$, $\text{edges} = [[0,1],[1,2],[2,3],[1,3],[1,4]]$

Output: false

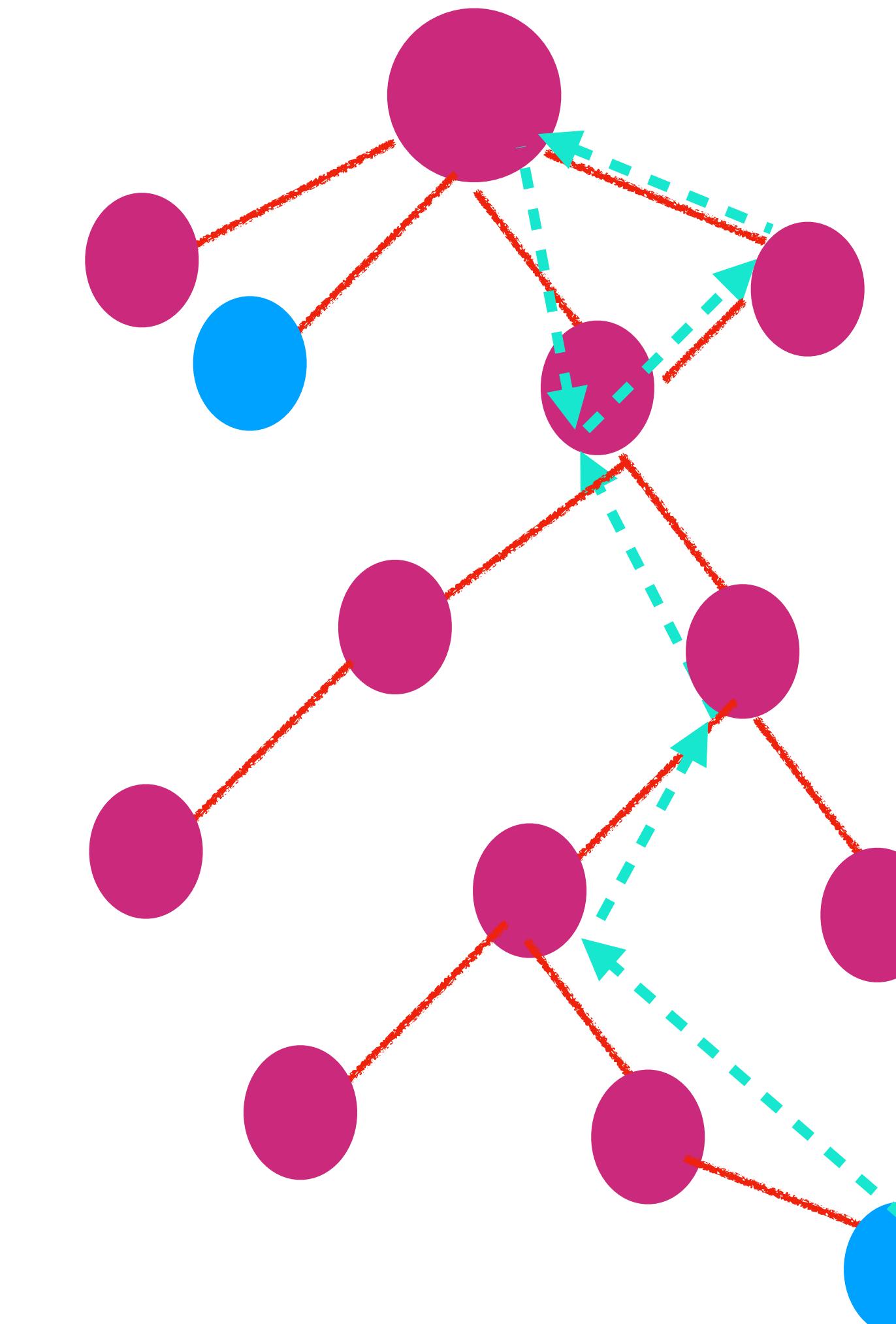
Constraints :
 $1 \leq n \leq 2000$
 $0 \leq \text{edges.length} \leq 5000$
 $\text{edges}[i].length == 2$
 $0 \leq a_i, b_i < n$
 $a_i \neq b_i$ (No Self loop)

Graph with Valid Tree



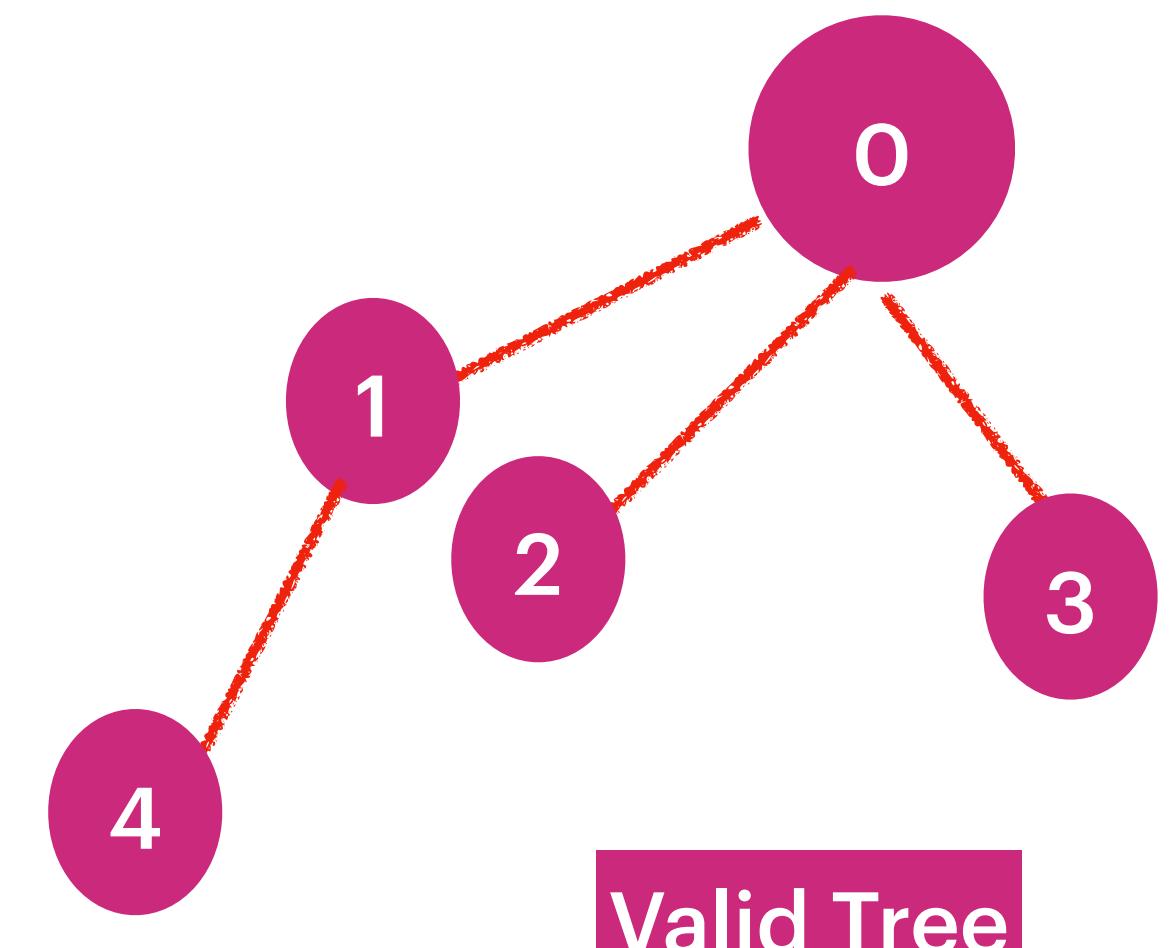
Its a valid tree because
From one branch we can move to another branch

Graph with Invalid Tree

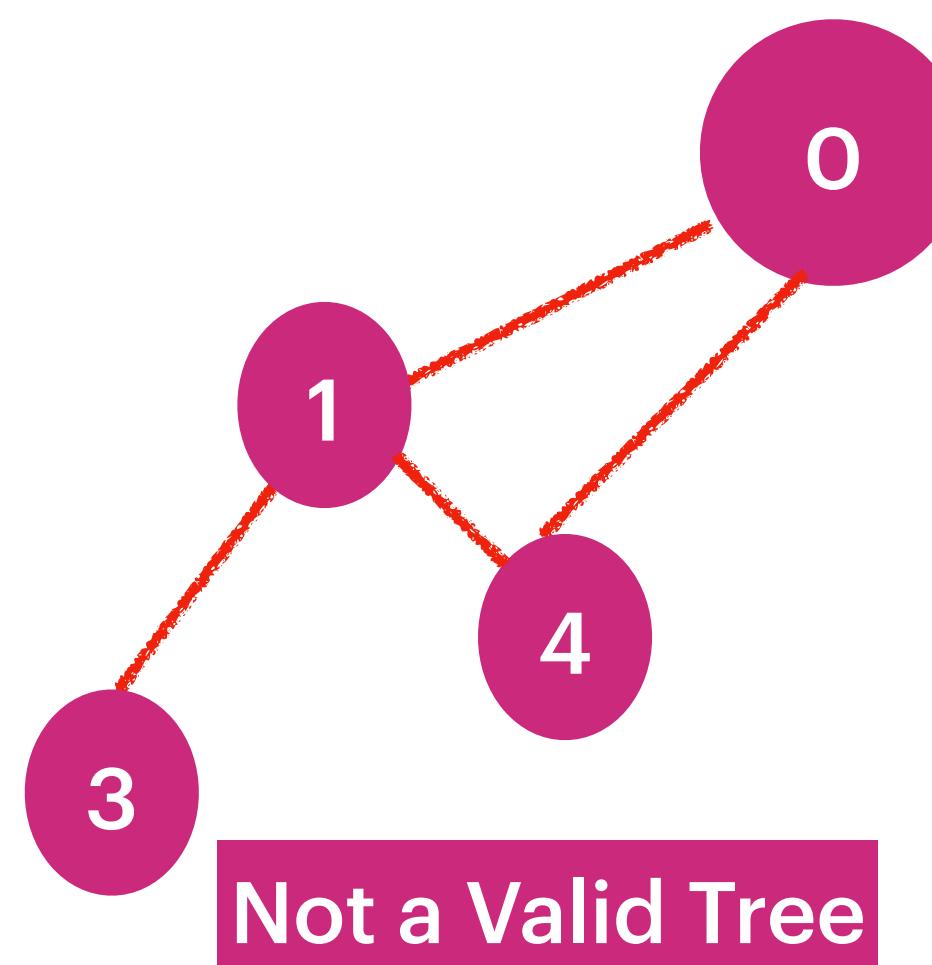


Its not a valid tree because
, a child node has more than one immediate parent so it causes cycle.

Input: $n = 5$, edges = [[0,1],[0,2],[0,3],[1,4]]
Output: true



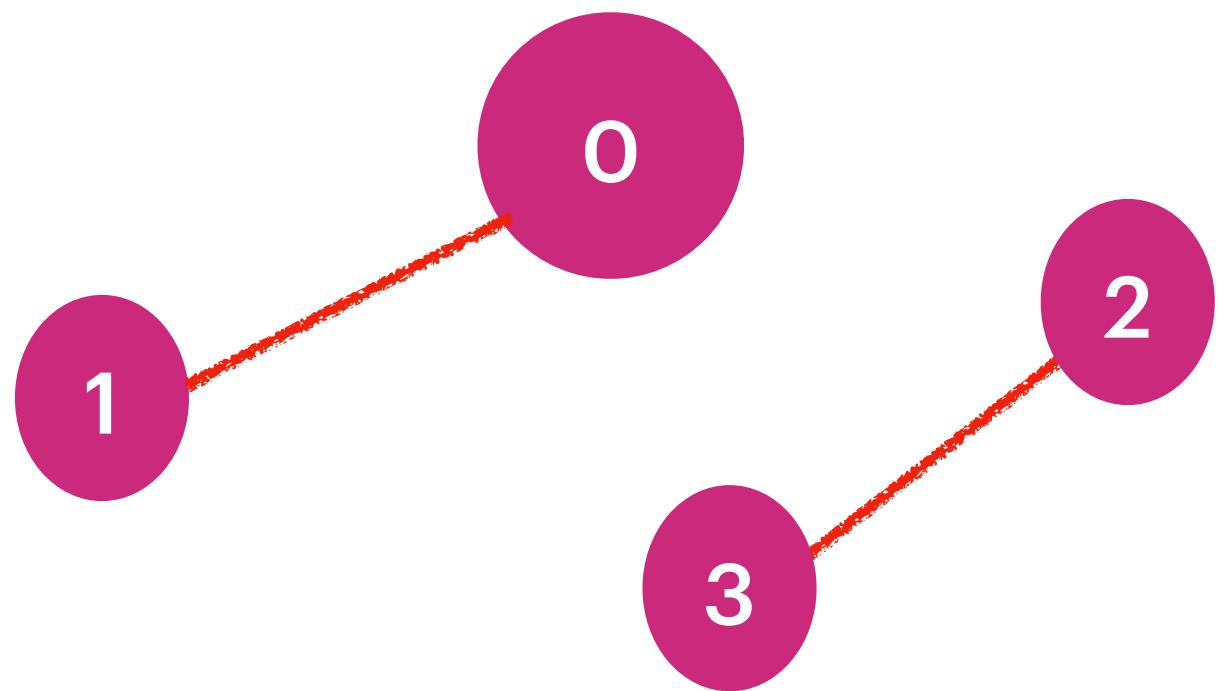
Input: $n = 5$,
edges = [[0,1],[0,4],[1,4],[1,3]]
Output: false



Input: $n = 5$, edges = [[0,1],[1,2],[2,3],[1,3],[1,4]]
Output: false

For n vertexes we can have at max $n-1$ edges.
Here $n = 5$ and edges = 5 so Not a Valid Tree.

n=4 [[0,1], [2,3]]



Its not a Valid Tree because

[[0,1],[0,4],[1,4],[1,3]] n = 5

0[0]
1[1]
2[2]
3[3]
4[4]

[0,1] => 0[0]-1[0]

[0,4] => 0[0]-1[0]-4[0]

[1,4] => 1[0] - 4[0] They are already connected : Its a loop return false

Input: n = 5, edges = [[0,1],[0,2],[0,3],[1,4]]

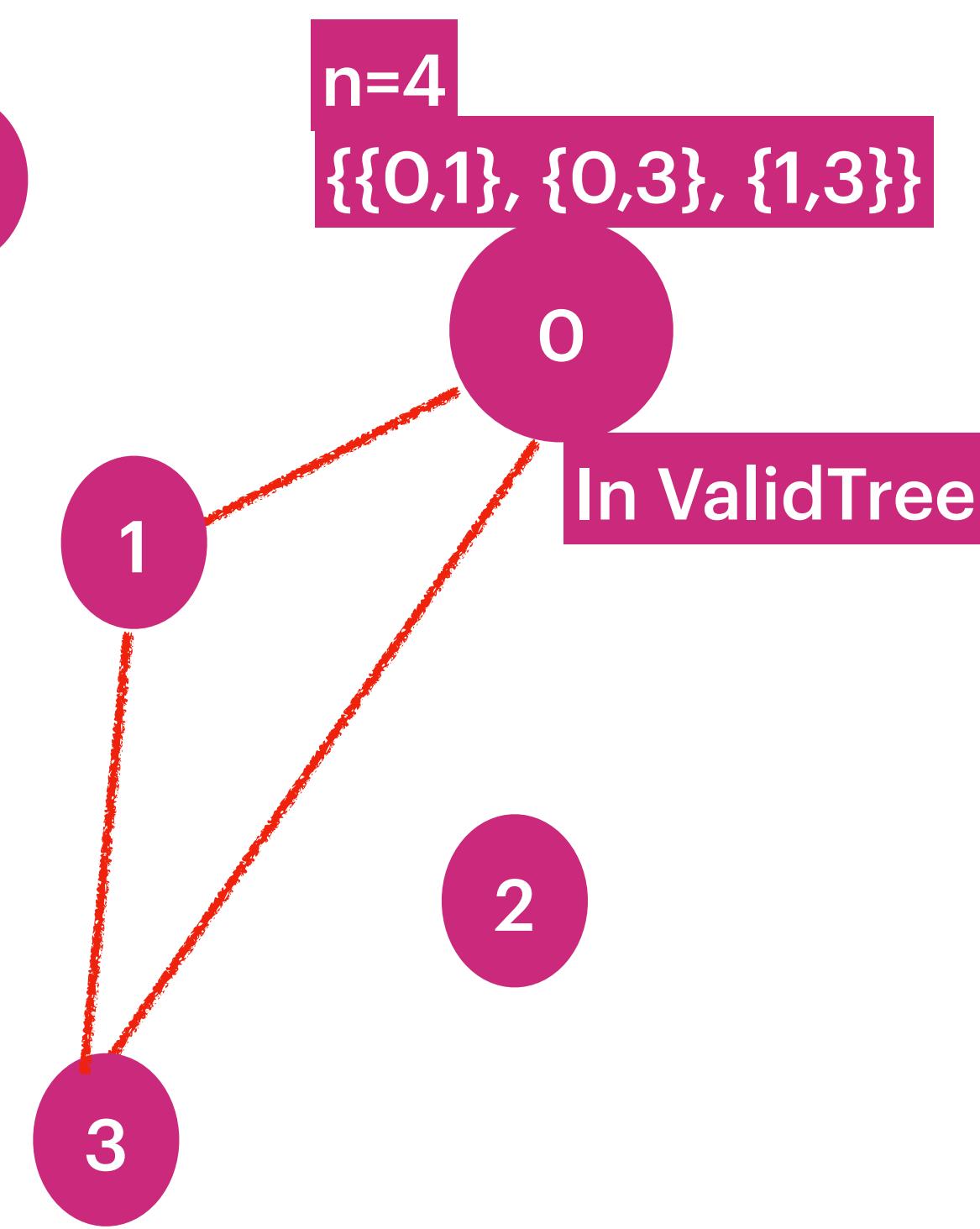
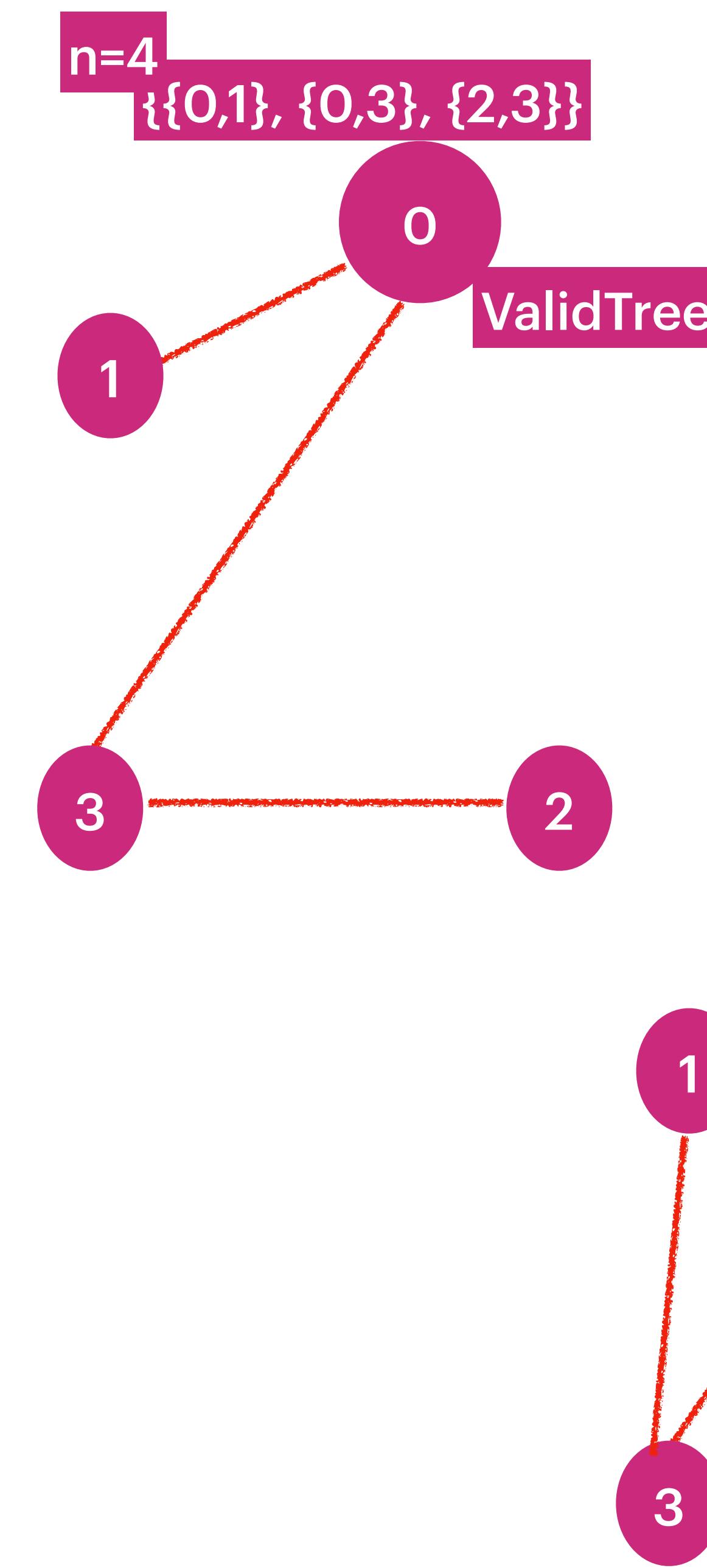
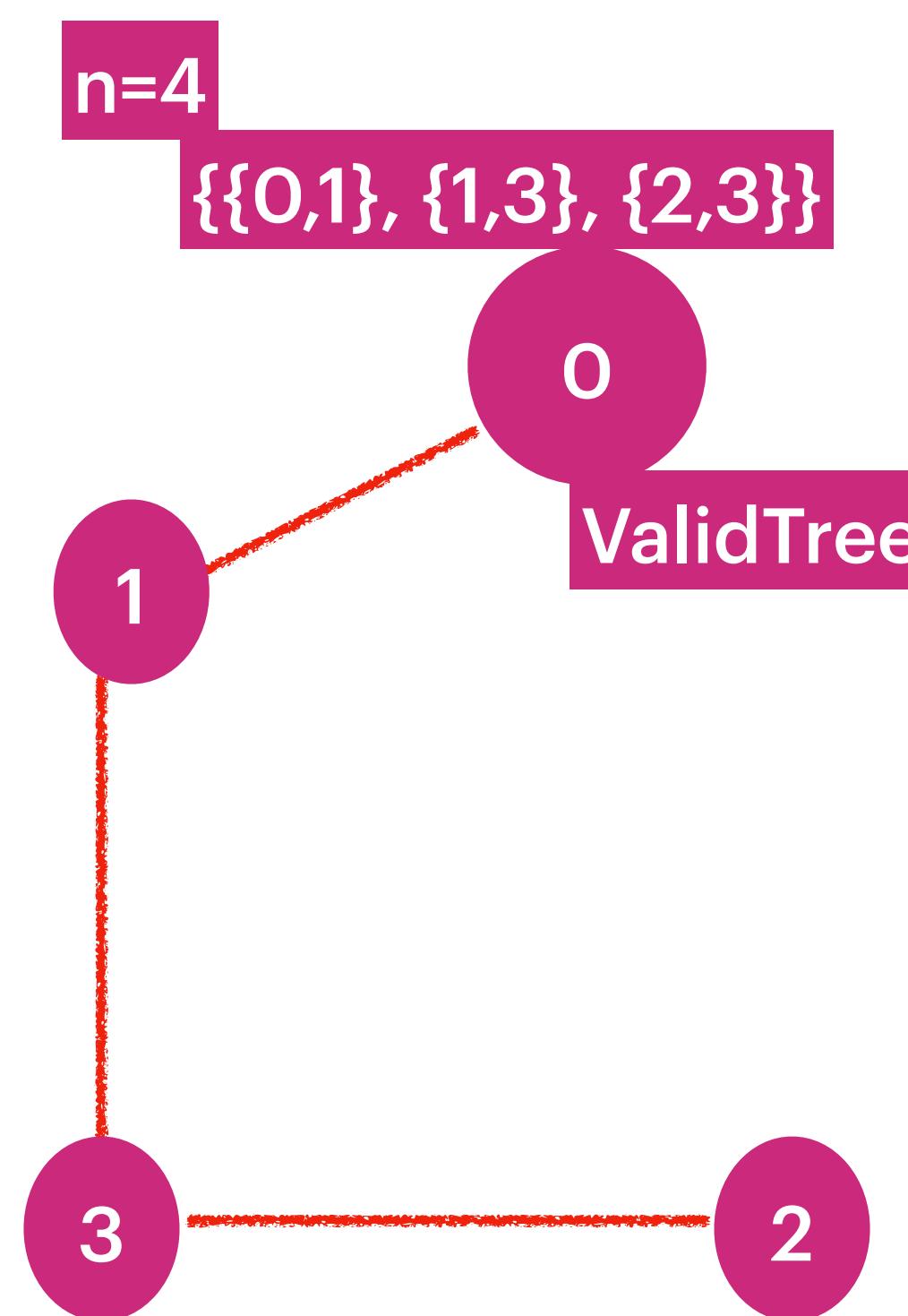
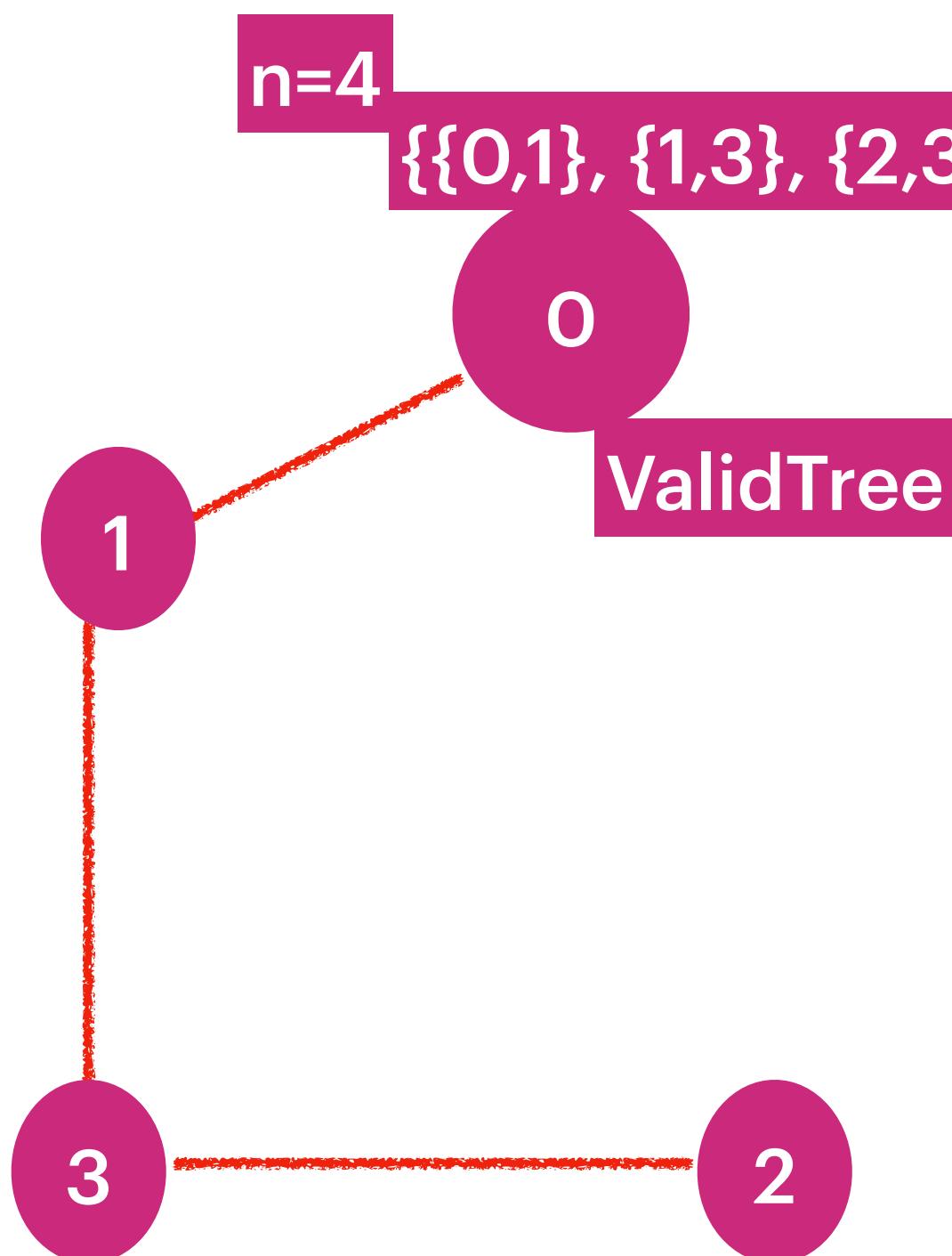
0[0]
1[1]
2[2]
3[3]
4[4]

[0,1] => 0[0]-1[0]

[0-2] => 0[0]-1[0]- 2[0]

[0-3] => 0[0]-1[0]- 2[0]-3[0]

[1-4] =>0[0]-1[0]- 2[0]-3[0]-4[0] Its a valid Tree : return true



Number of Connected Components in an Undirected Graph

You have a graph of n nodes. You are given an integer n and an array edges where edges[i] = [ai, bi] indicates that there is an edge between ai and bi in the graph.

Return the number of connected components in the graph.

Input: n = 5, edges = [[0,1],[1,2],[3,4]]

Output: 2

Input: n = 5, edges = [[0,1],[1,2],[2,3],[3,4]]

Output: 1

Constraints : 1 <= n <= 2000

1 <= edges.length <= 5000

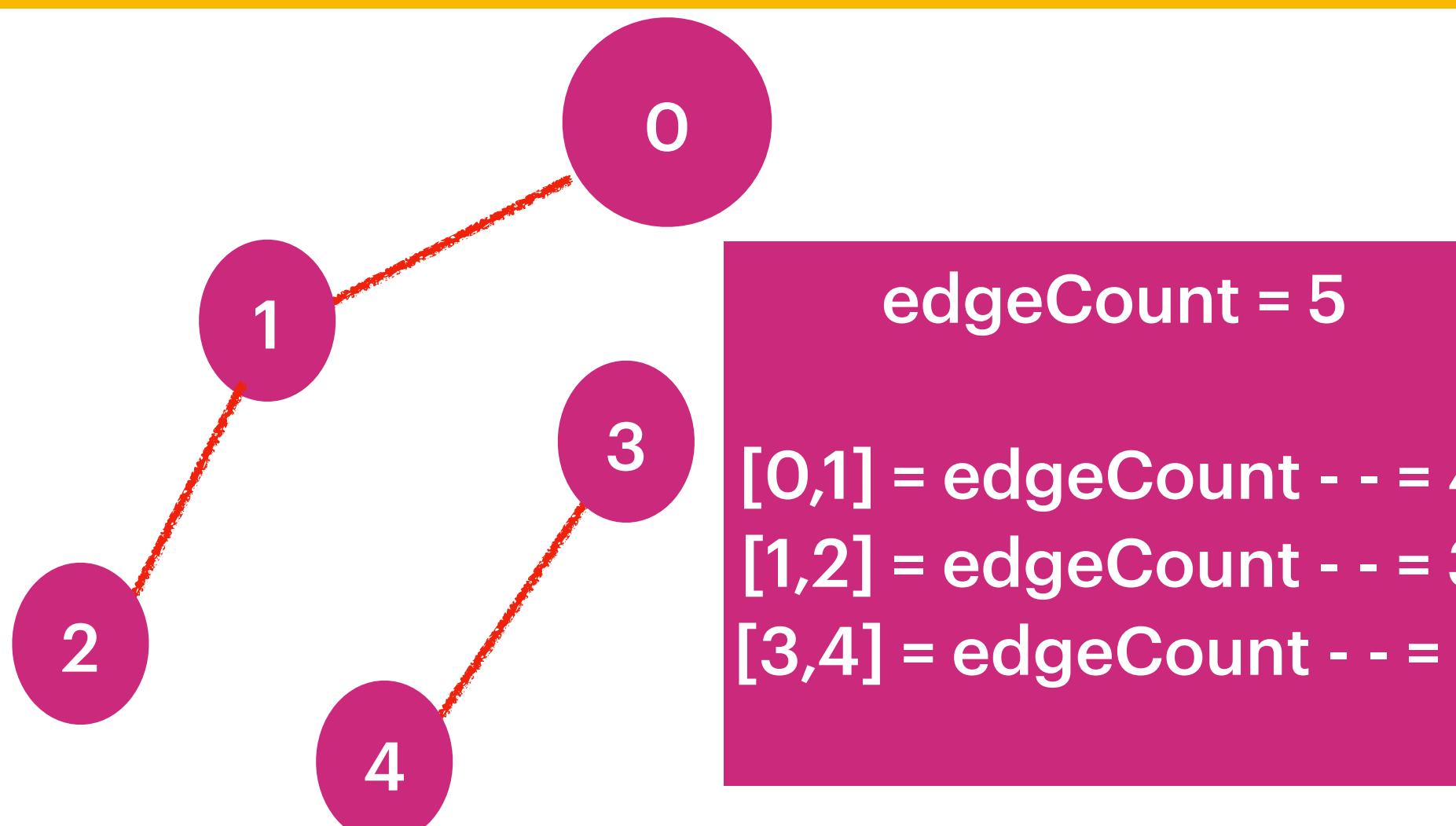
edges[i].length == 2

0 <= ai <= bi < n

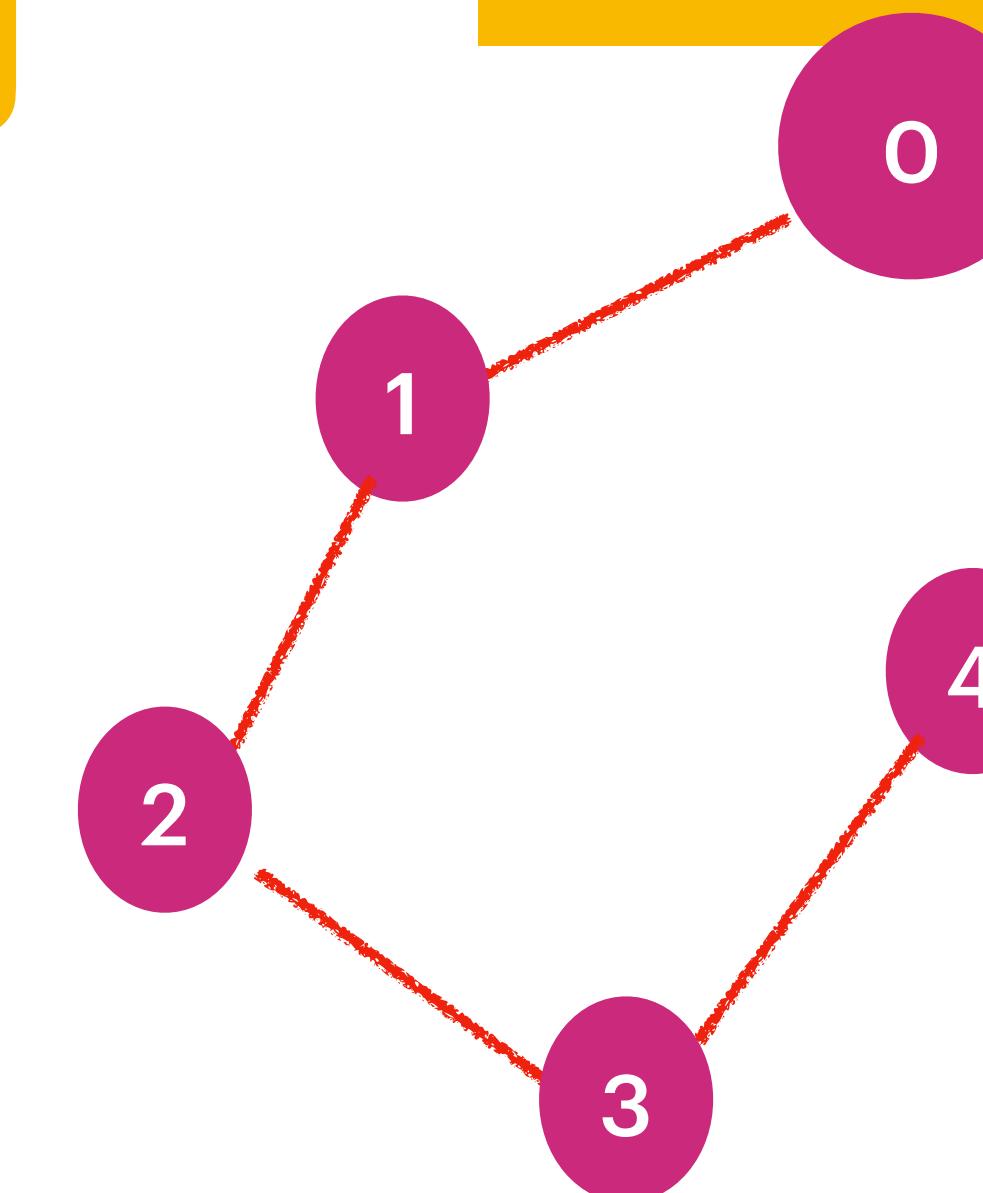
ai != bi

There are no repeated edges.

Input: n = 5, edges = [[0,1],[1,2],[3,4]]
Output: 2

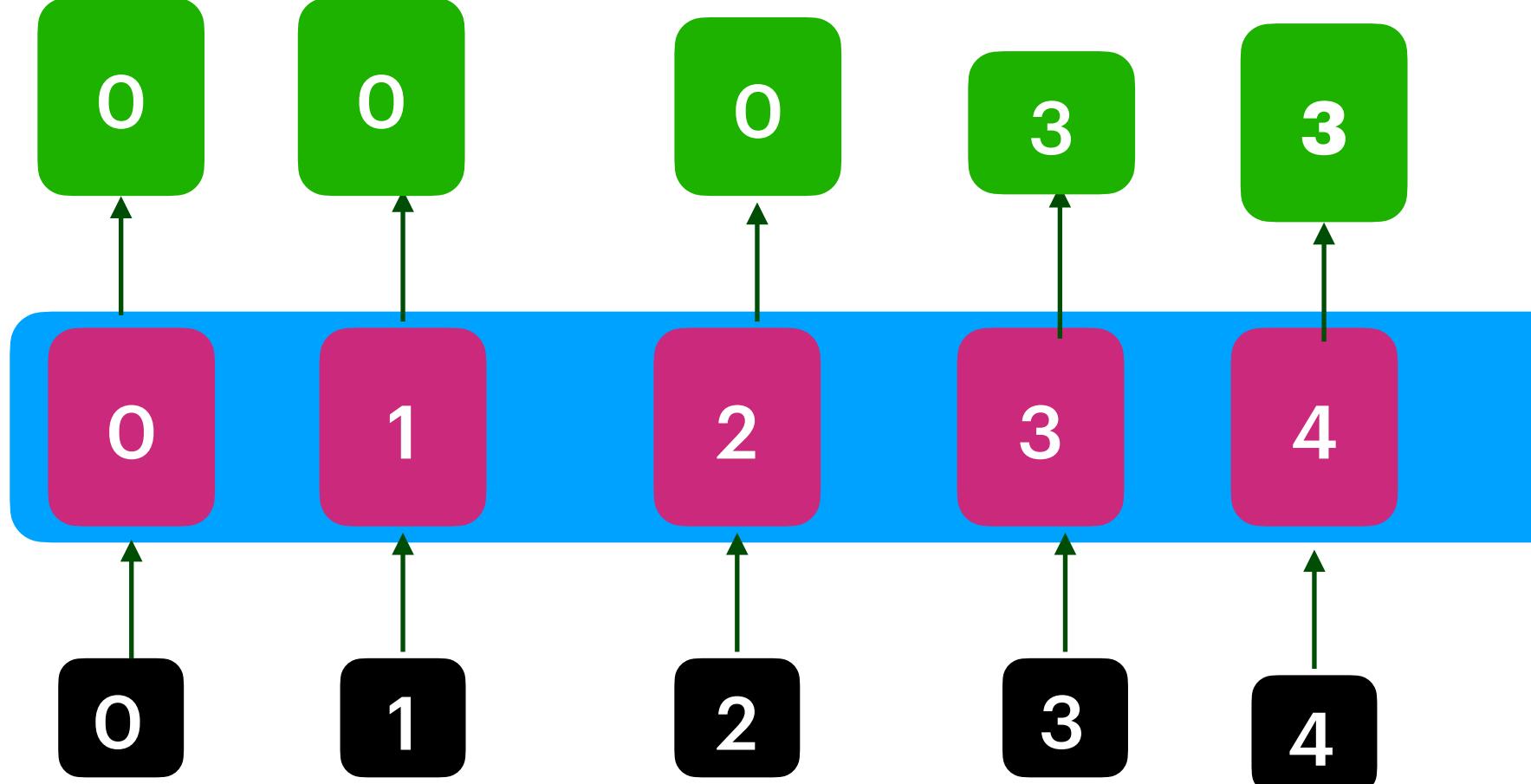


Input: n = 5, edges = [[0,1],[1,2],[2,3],[3,4]]
Output: 1

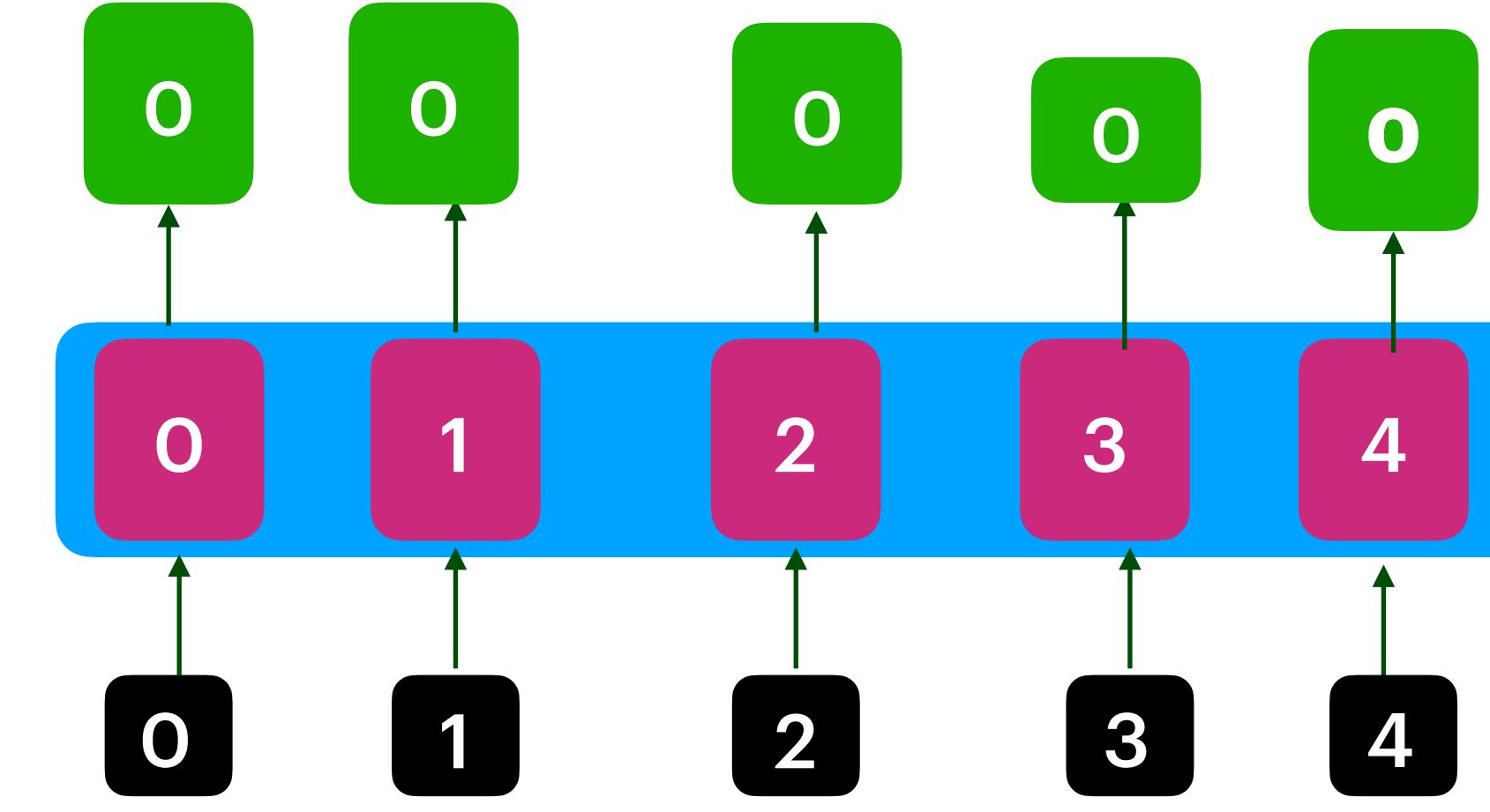


edgeCount = n = 5
edgeCount
[0,1] = edgeCount- - = 4
[1,2] = edgeCount- - = 3
[2,3] = edgeCount- - = 2
[3,4] = edgeCount- - = 1

Connected Components / Paths. = 2



Connected Components / Paths. = 1



Number of Provinces

There are n cities. Some of them are connected, while some are not. If city a is connected directly to city b, and city b is connected directly with city c, then city a is connected indirectly with city c. A province is a group of directly or indirectly connected cities and no other cities outside of the group.

You are given an $n \times n$ matrix isConnected where $\text{isConnected}[i][j] = 1$ if the ith city and the jth city are directly connected, and $\text{isConnected}[i][j] = 0$ otherwise.

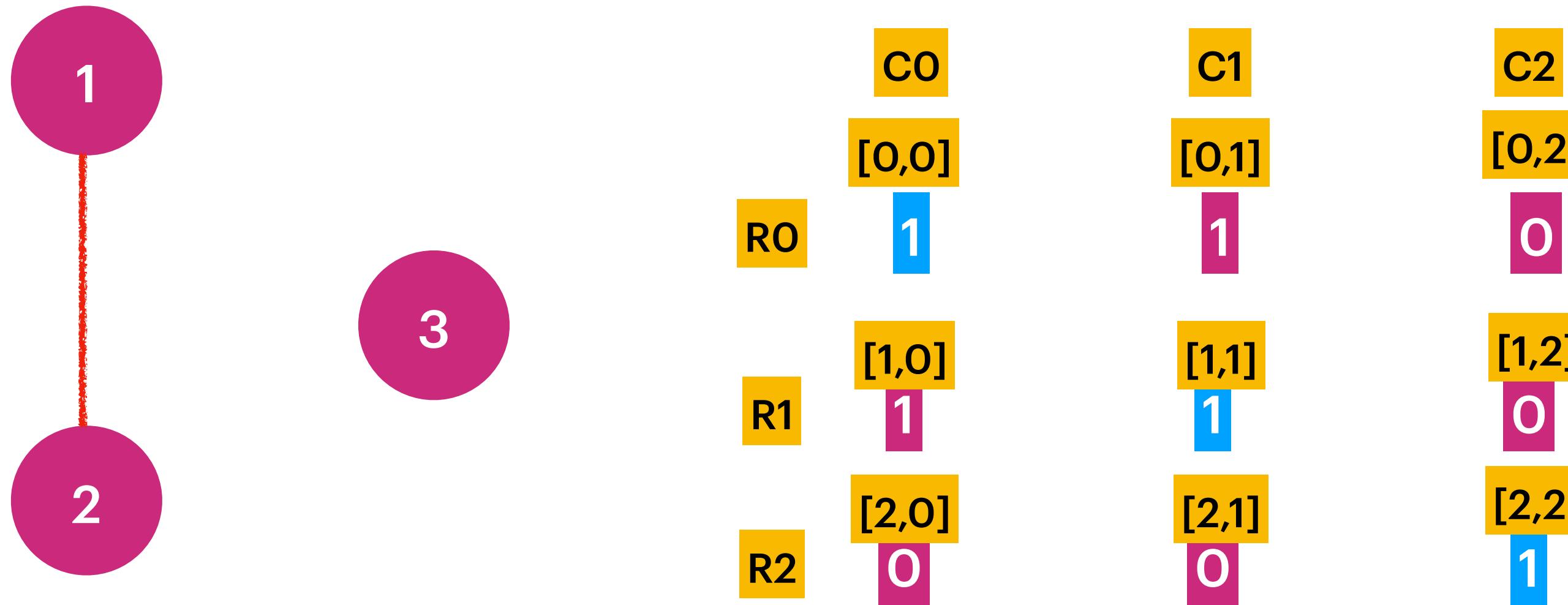
Return the total number of provinces.

Input: isConnected = [[1,1,0],[1,1,0],[0,0,1]]
Output: 2

Input: isConnected = [[1,0,0],[0,1,0],[0,0,1]]
Output: 3

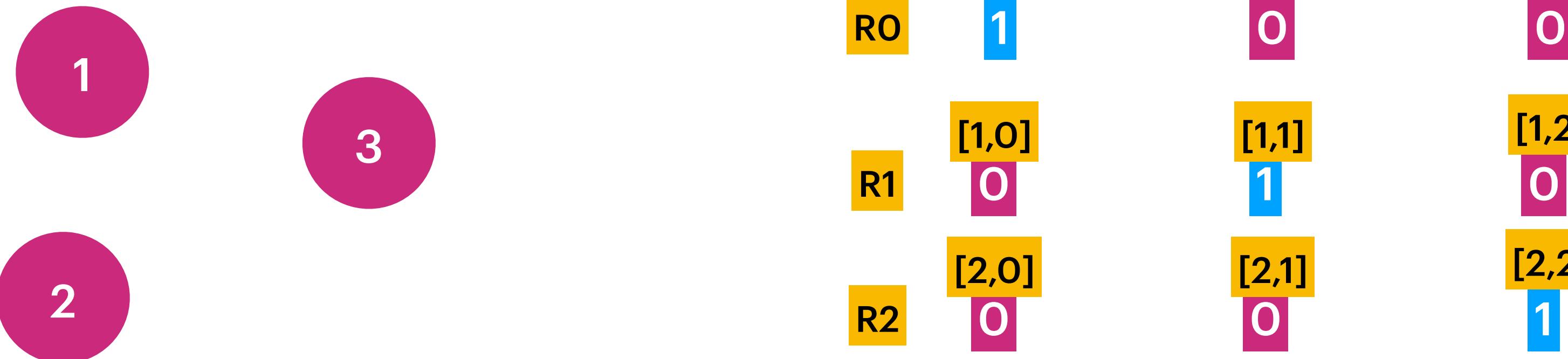
Input: isConnected = [[1,1,0],[1,1,0],[0,0,1]]
Output: 2

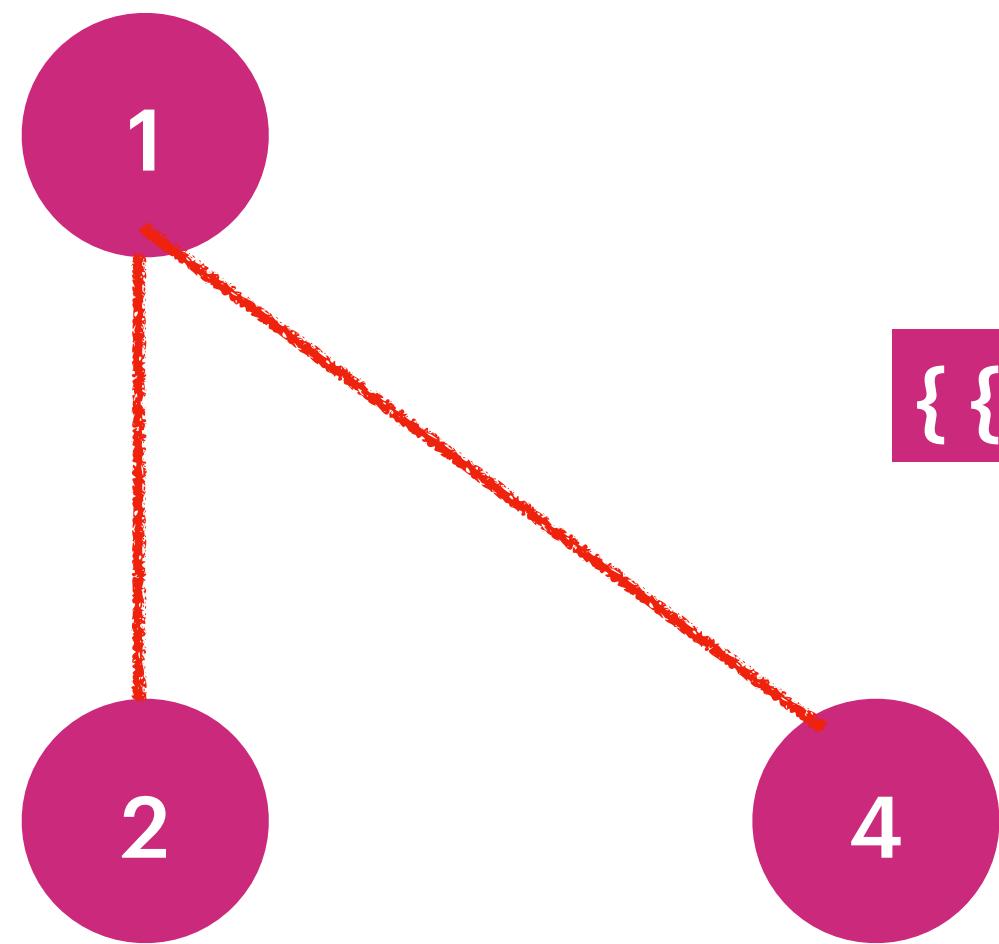
Count = 3
Count - - = 2



Input: isConnected = [[1,0,0],[0,1,0],[0,0,1]]
Output: 3

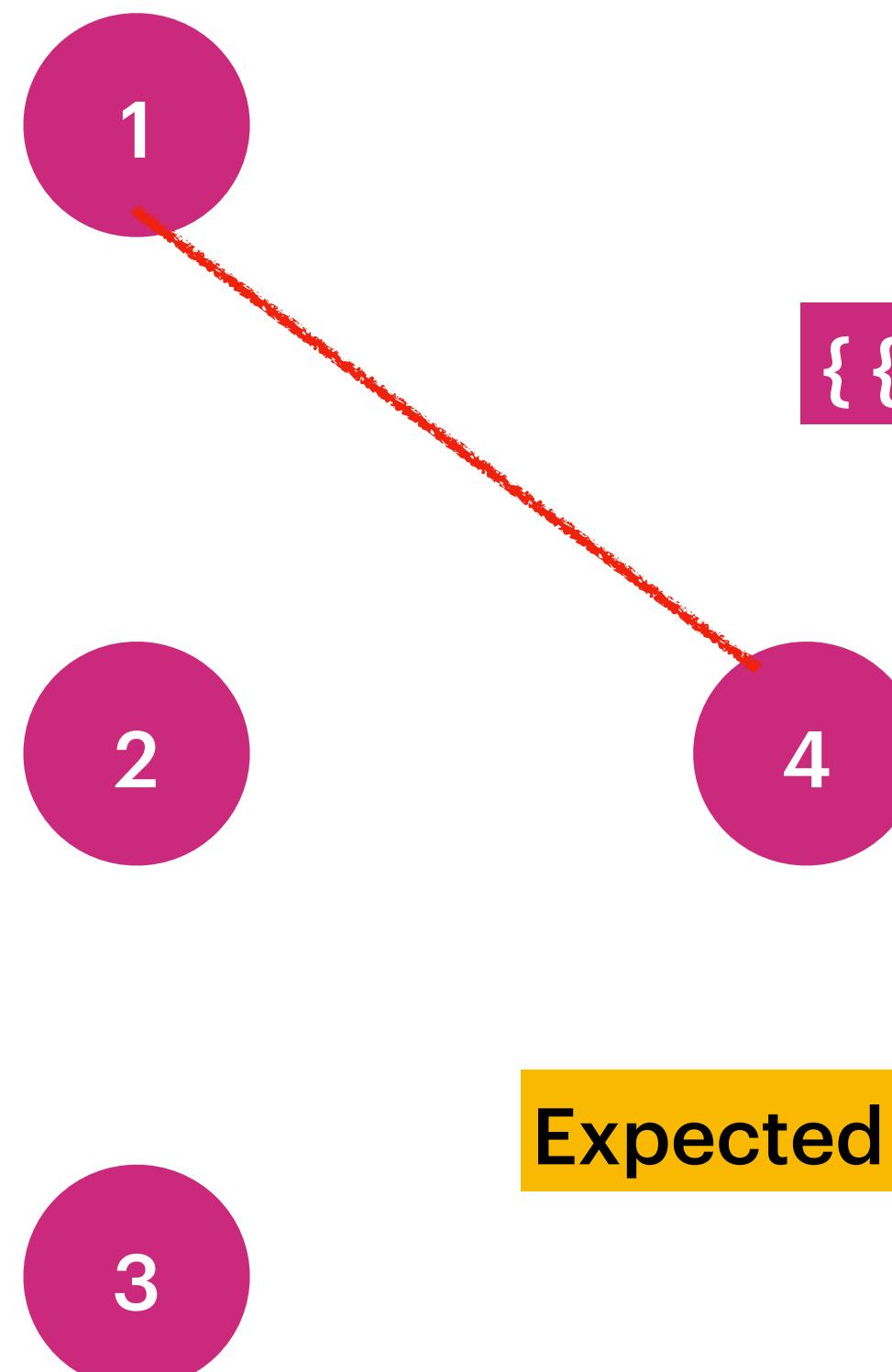
Count = 3
Count - - = 2





{ {1,1,0,1}, {1,1,0,0},{0,0,1,0},{1,0,0,1} }

Expected Output : 2



{ {1,0,0,1}, {0,1,0,0},{0,0,1,0},{1,0,0,1} }

Expected Output : 3

The Earliest Moment When Everyone Become Friends in Instagram

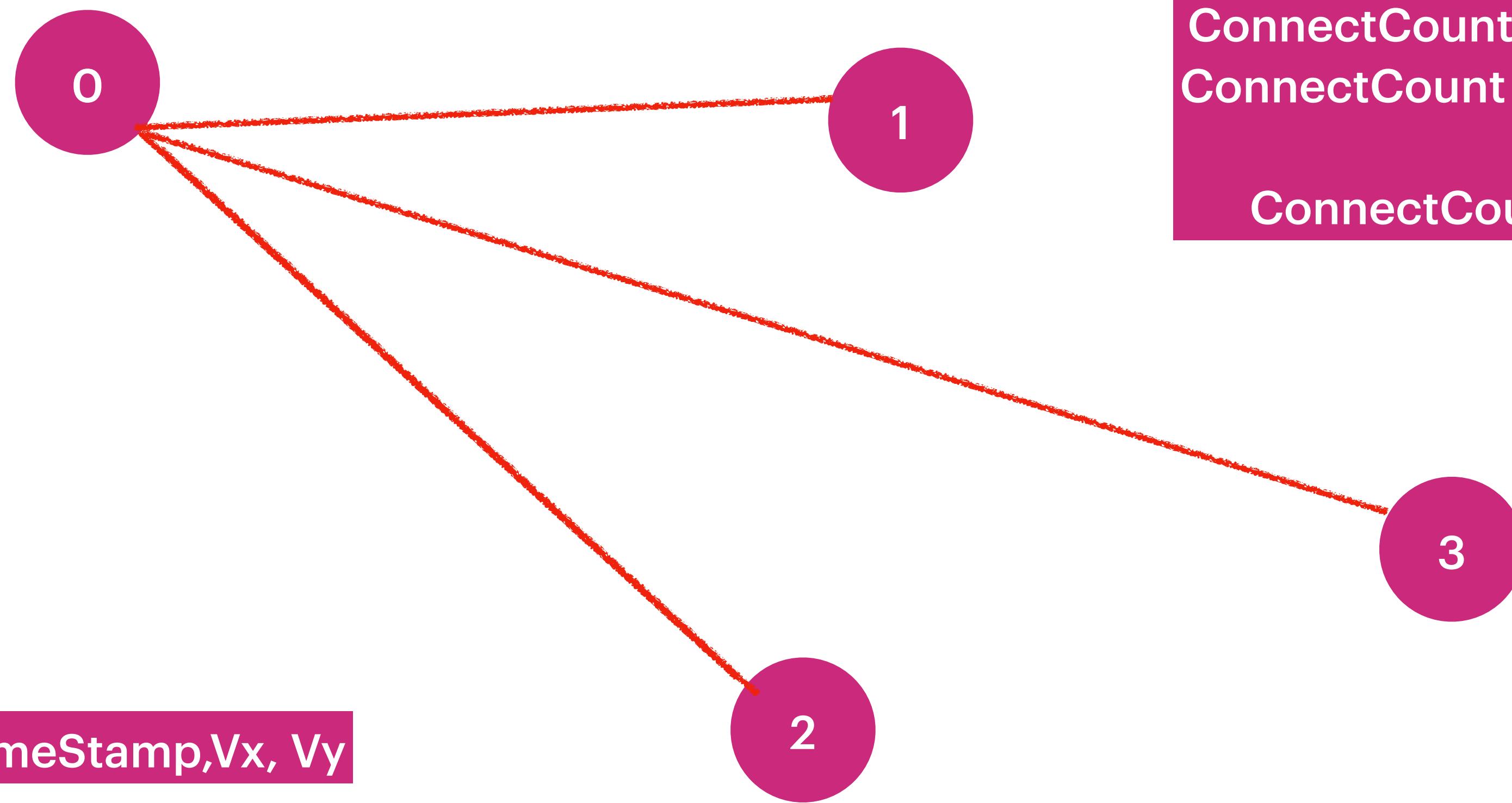
There are n people in a social group labeled from 0 to $n - 1$. You are given an array logs where $\text{logs}[i] = [\text{timestamp}_i, x_i, y_i]$ indicates that x_i and y_i will be friends at the time timestamp_i .

Friendship is symmetric. That means if a is friends with b , then b is friends with a . Also, person a is acquainted with a person b if a is friends with b , or a is a friend of someone acquainted with b . Return the earliest time for which every person became acquainted with every other person. If there is no such earliest time, return -1.

Input: $\text{logs} = [[20190101,0,1],[20190104,3,4],[20190107,2,3],[20190211,1,5],[20190224,2,4],[20190301,0,3],[20190312,1,2],[20190322,4,5]]$, $n = 6$
Output: 20190301

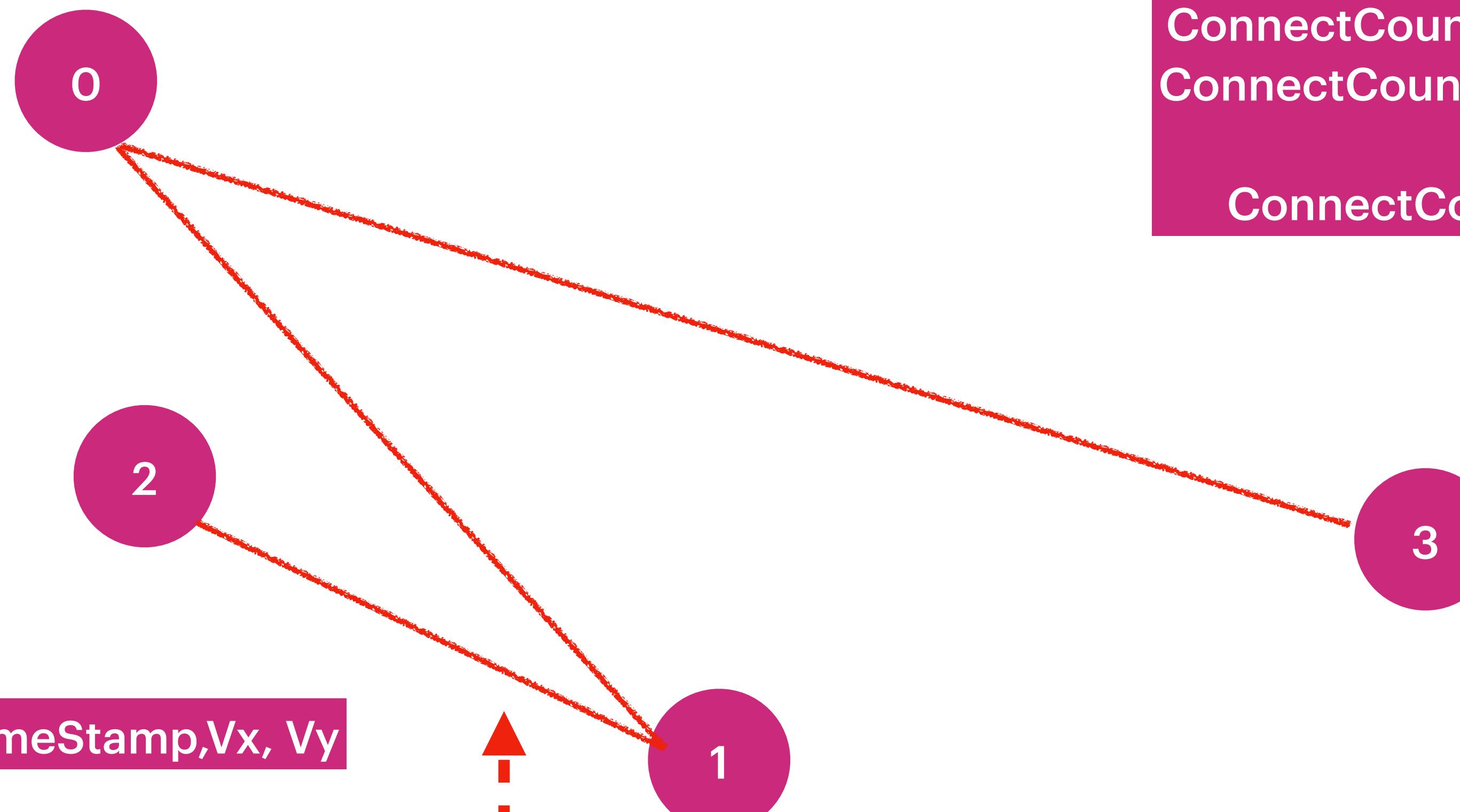
Input: $\text{logs} = [[0,2,0],[1,0,1],[3,0,3],[4,1,2],[7,3,1]]$, $n = 4$
Output: 3

$[[9,3,0],[0,2,1],[8,0,1],[1,3,2],[2,2,0],[3,3,1]]$



ConnectCount = n=4 = 3
ConnectCount = n-1 stop
ConnectCount = 0

Input: logs = [[0,2,0],[1,0,1],[3,0,3],[4,1,2],[7,3,1]], n = 4
Output: 3



Not Expected Result : 8

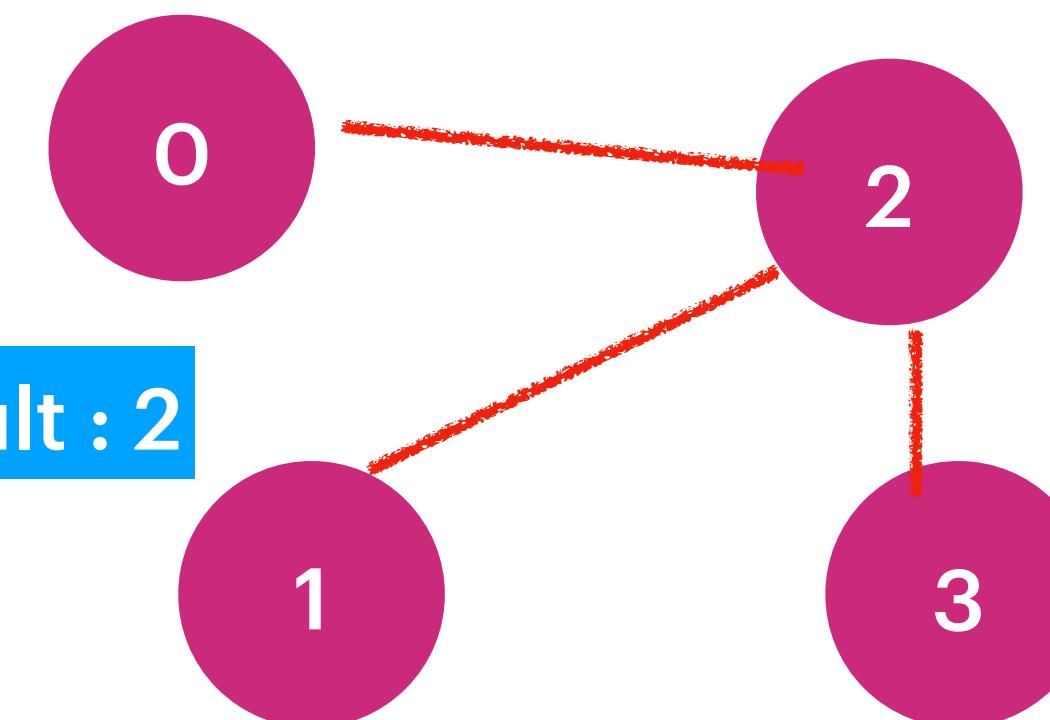
[[9,3,0],[0,2,1],[8,0,1],[1,3,2],[2,2,0],[3,3,1]]
n=4 output : 2

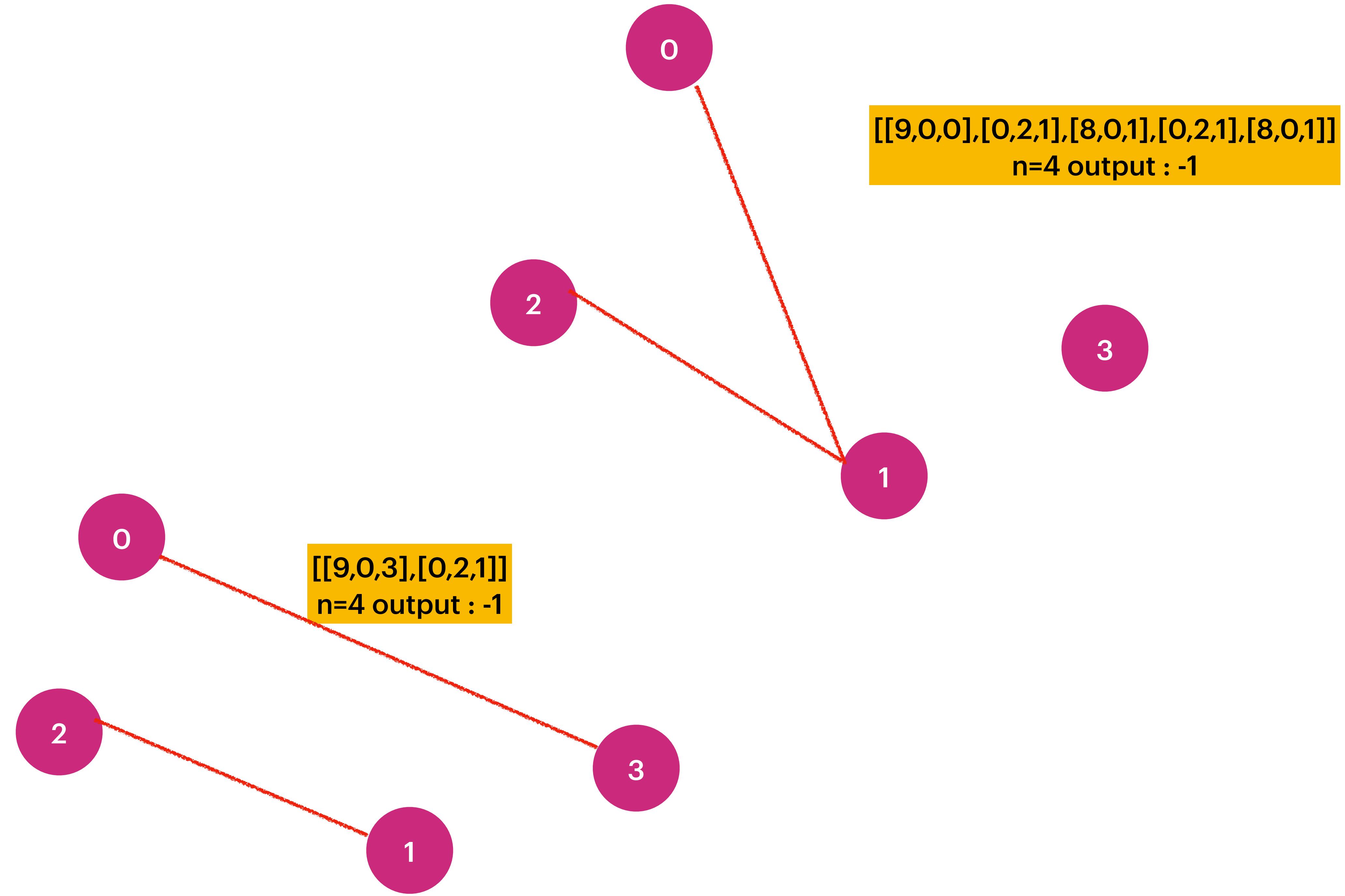
TreeMap<Key(timeStamp),value[array]>

ConnectCount = n=4 = 3
ConnectCount = n-1 stop
ConnectCount = 0

[[0,2,1],[1,3,2],[2,2,0],[3,3,1],[8,0,1],[9,3,0]]
Output : 2

True Expected Result : 2





Design Graph

AddVertex

AddEdge

RemoveEdge

Remove Vertex

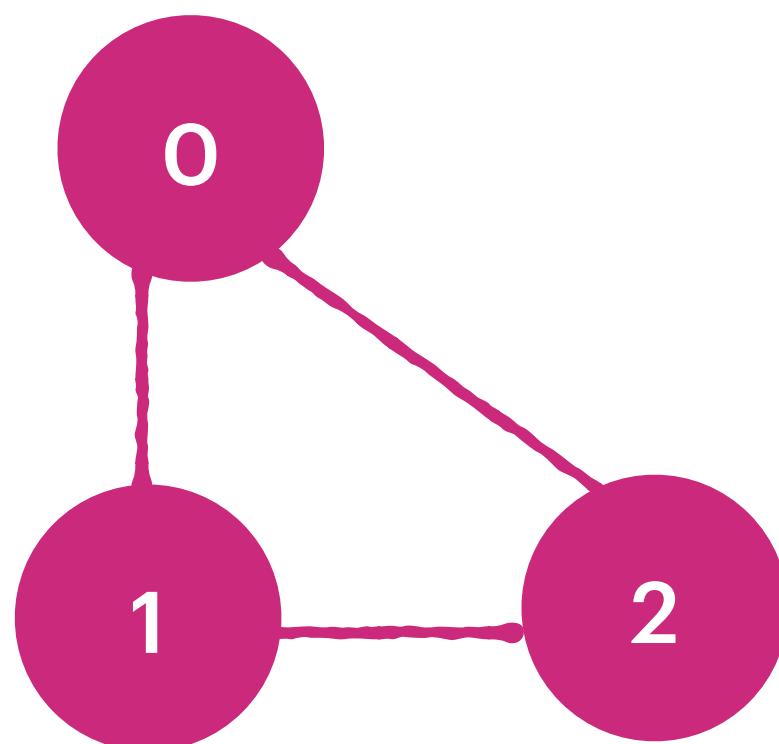
Print

$n = 3$, edges = [[0,1],[0,2],[1,2],[2,1],[2,0],[1,0]]

$O(1)$

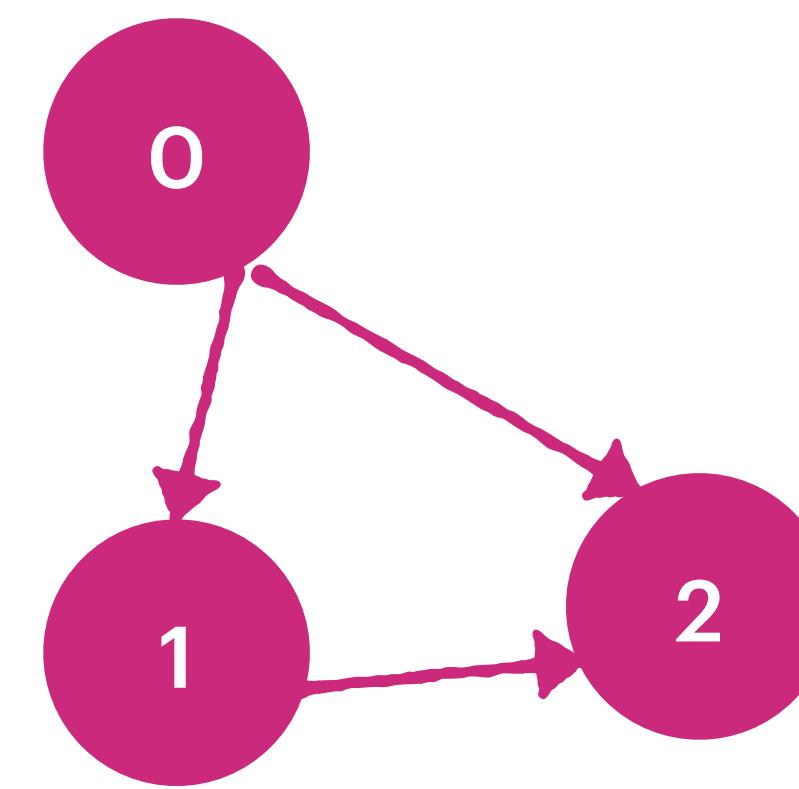
$O(V)$

$O(V+E)$

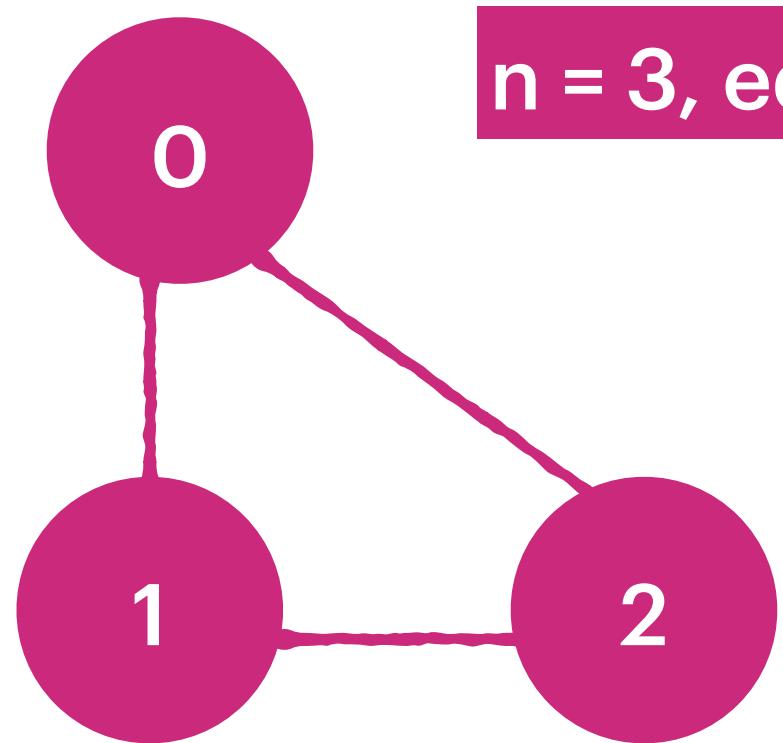


UnDirected Graph

$n = 3$, edges = [[0,1],[1,2],[0,2]]



Directed Graph

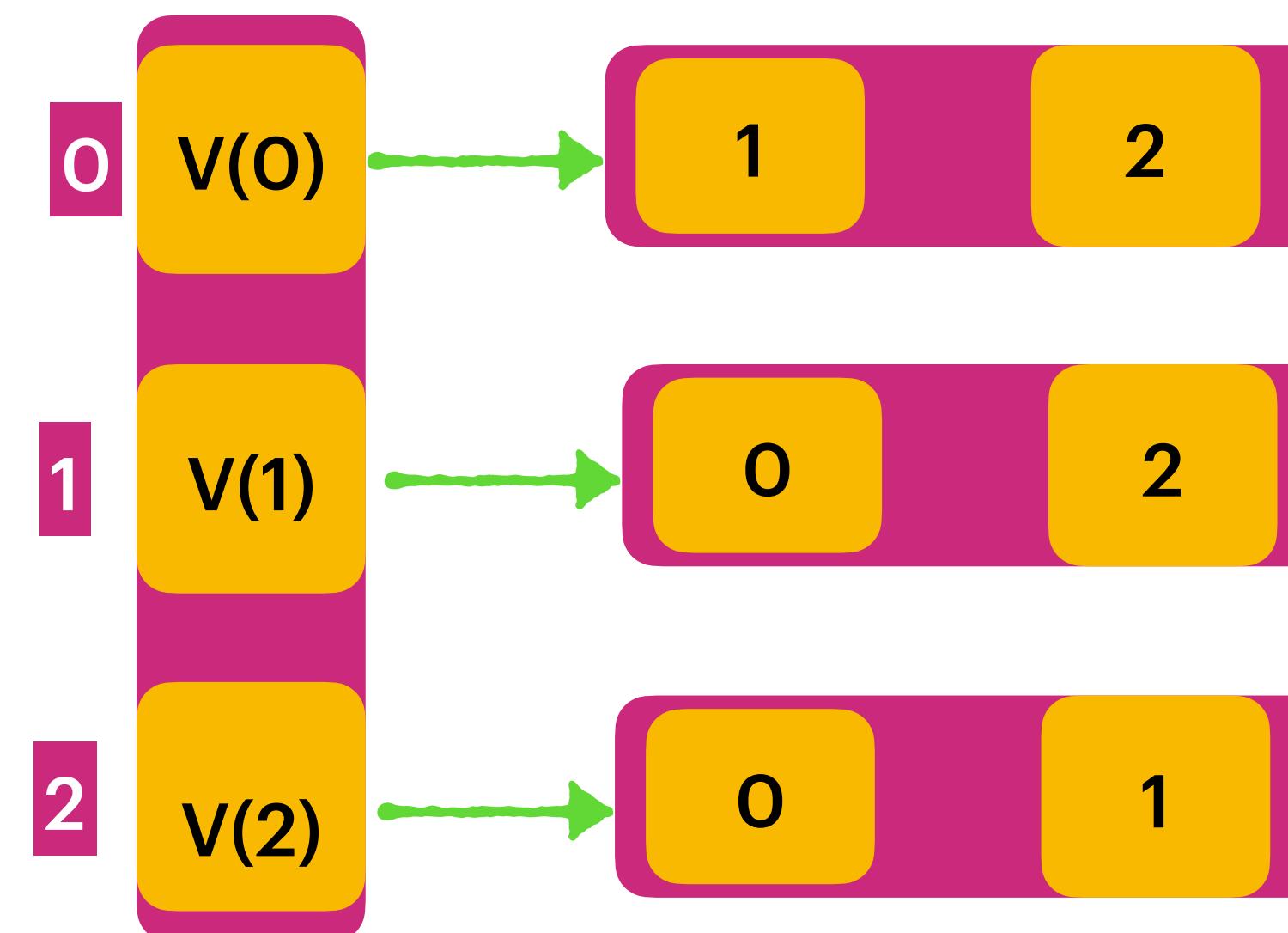


$n = 3$, edges = [[0,1],[0,2],[1,2],[2,1],[2,0],[1,0]]

UnDirected Graph

List< List<Integer> >

Adjacent List ::



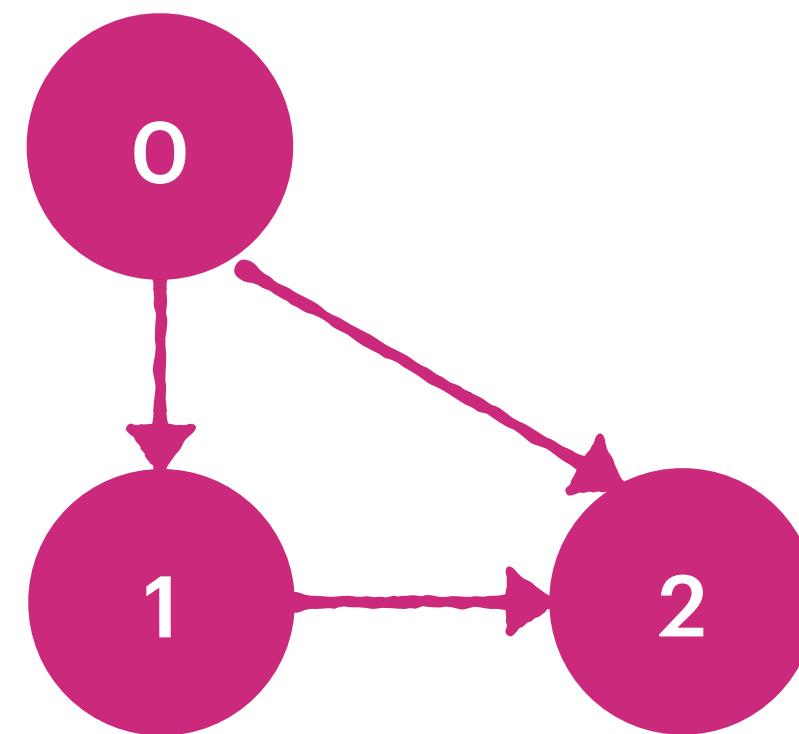
Matrix Row represents vertex

Matrix Column represents connections to the vertexes

Adjacent Matrix:
 $n \times n$

0	1	2
0	0	1
1	1	0
2	1	0

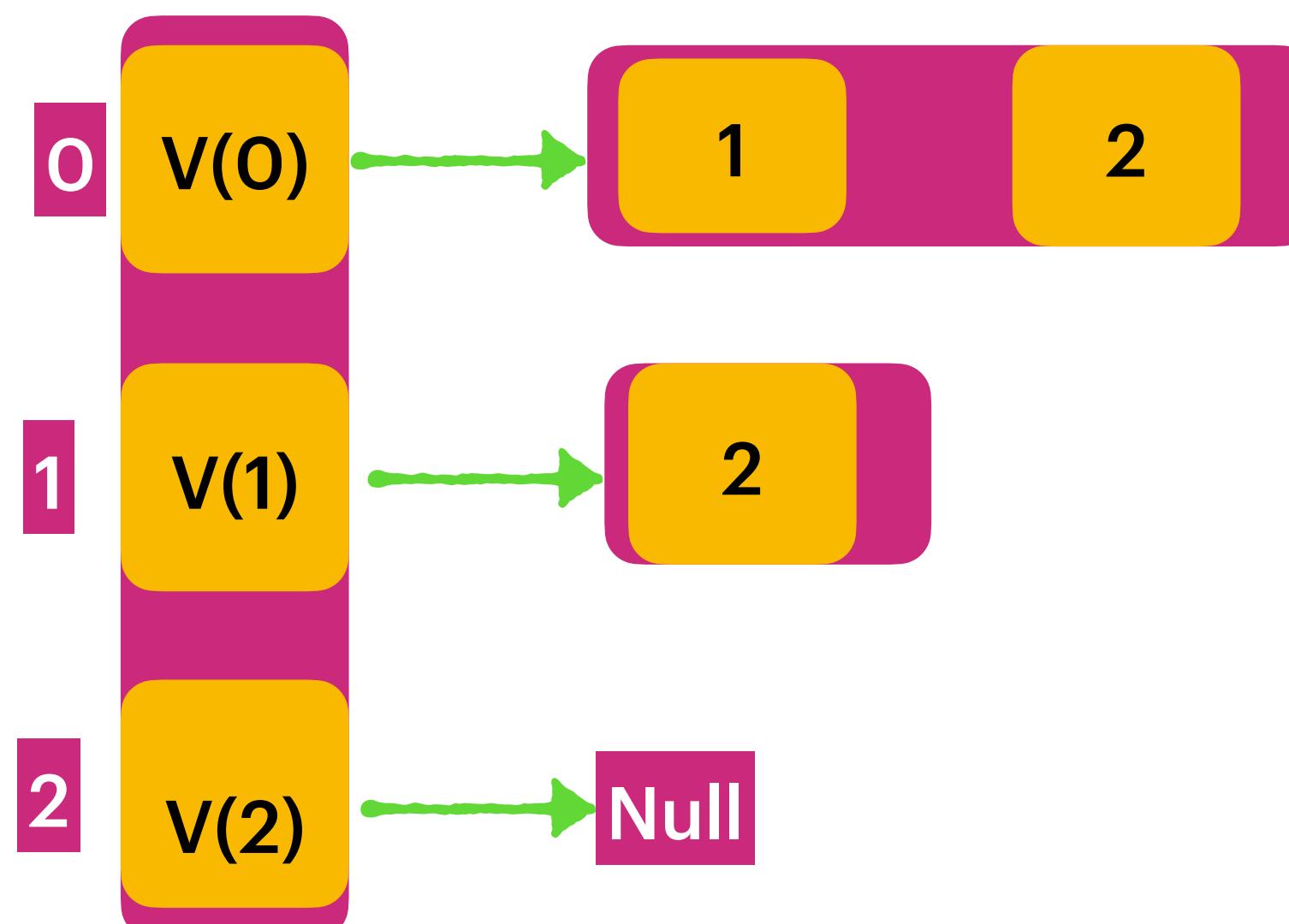
$n = 3$, edges = [[0,1],[1,2],[0,2]]



Directed Graph

List< List<Integer> >

Adjacent List ::



Matrix Row represents vertex

Matrix Column represents connections to the vertexes

Adjacent Matrix:
 $n \times n$

0	1	2
0	1	1
0	0	1
0	0	0

Adjacent List

Add Vertex

$O(1)$

Remove Vertex

$O(V+E)$

Add Edge

$O(1)$

Remove Edge

$O(E)$

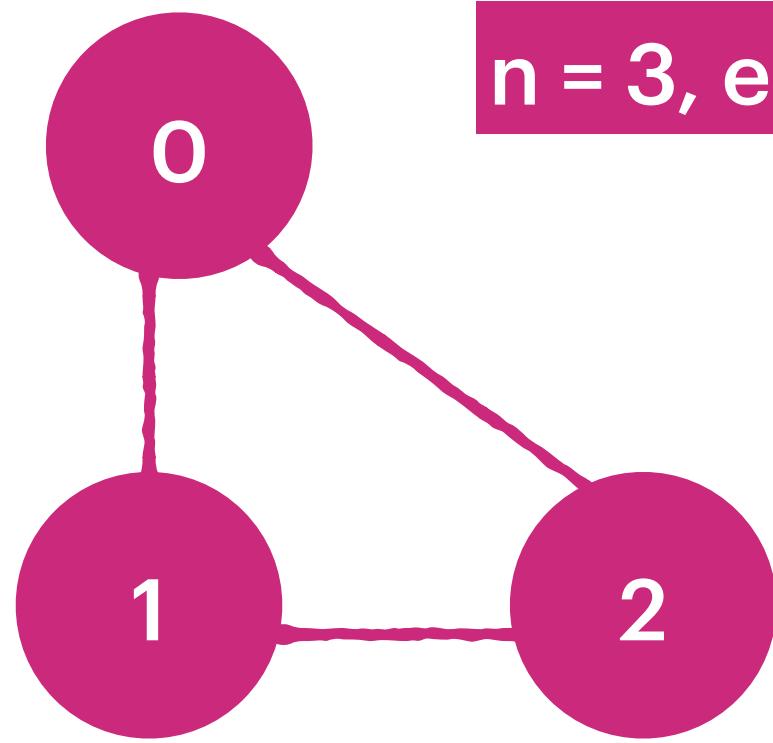
Adjacent Matrix

$O(n^2)$

$O(n^2)$

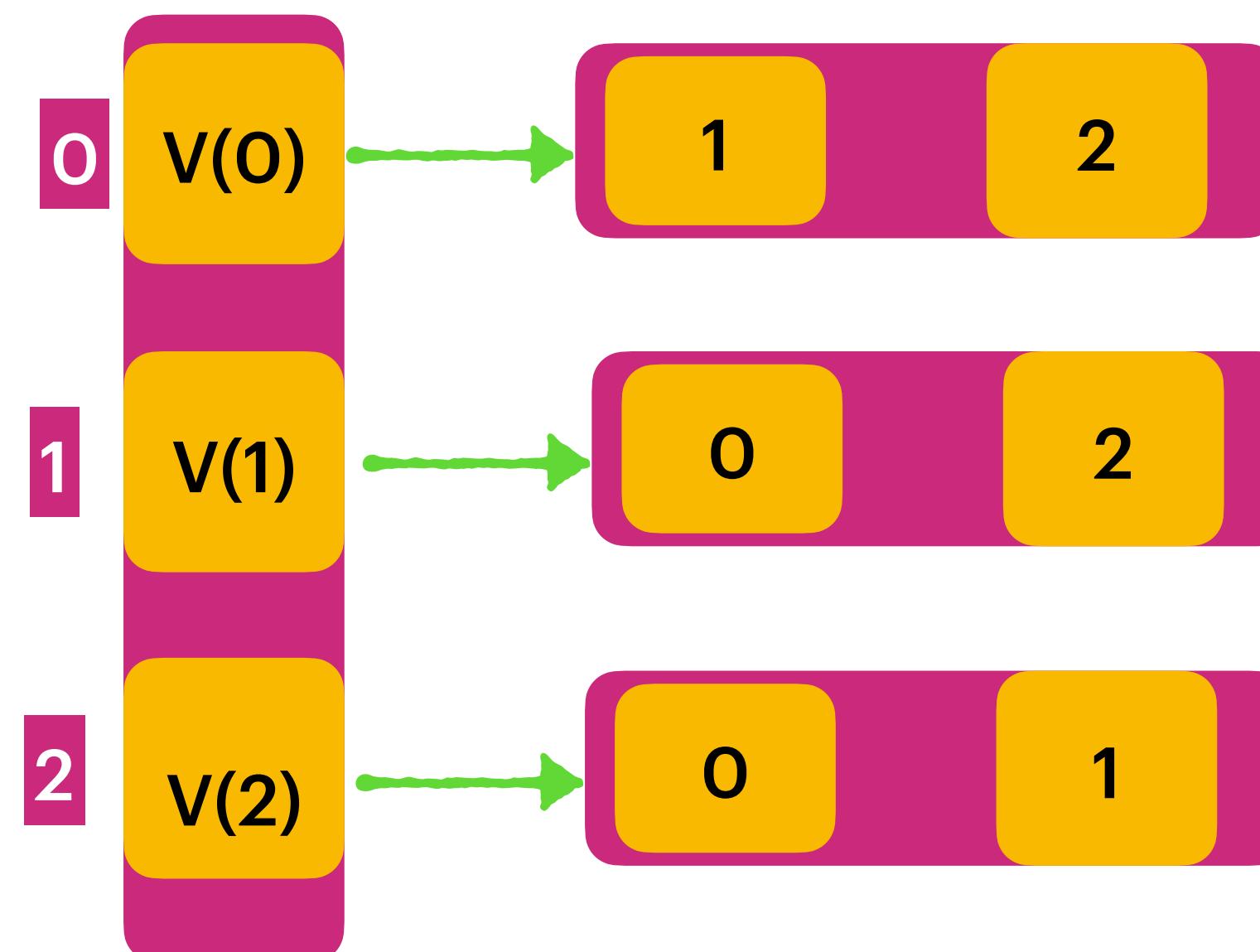
$O(1)$

$O(1)$



$n = 3$, edges = $[[0,1], [0,2], [1,2], [2,1], [2,0], [1,0]]$

```
removeVertex(2) :  
    for(v:o to Vn )  
    {  
        if(list.get(v).contains(2))  
        {  
            list.get(v).remove(2)  
        }  
    }  
    list.remove(2);
```



List< LinkedHashSet >

Add Vertex

O(1)

Adjecent Hashing

Remove Vertex

O(V)

Add Edge

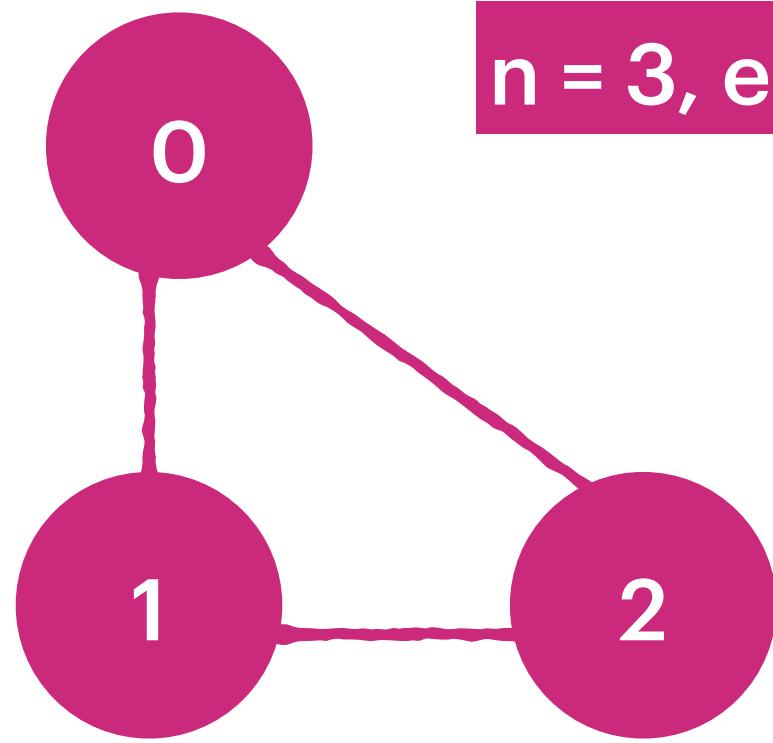
O(1)

Remove Edge

O(1)

Print O(V+E)

Hashing



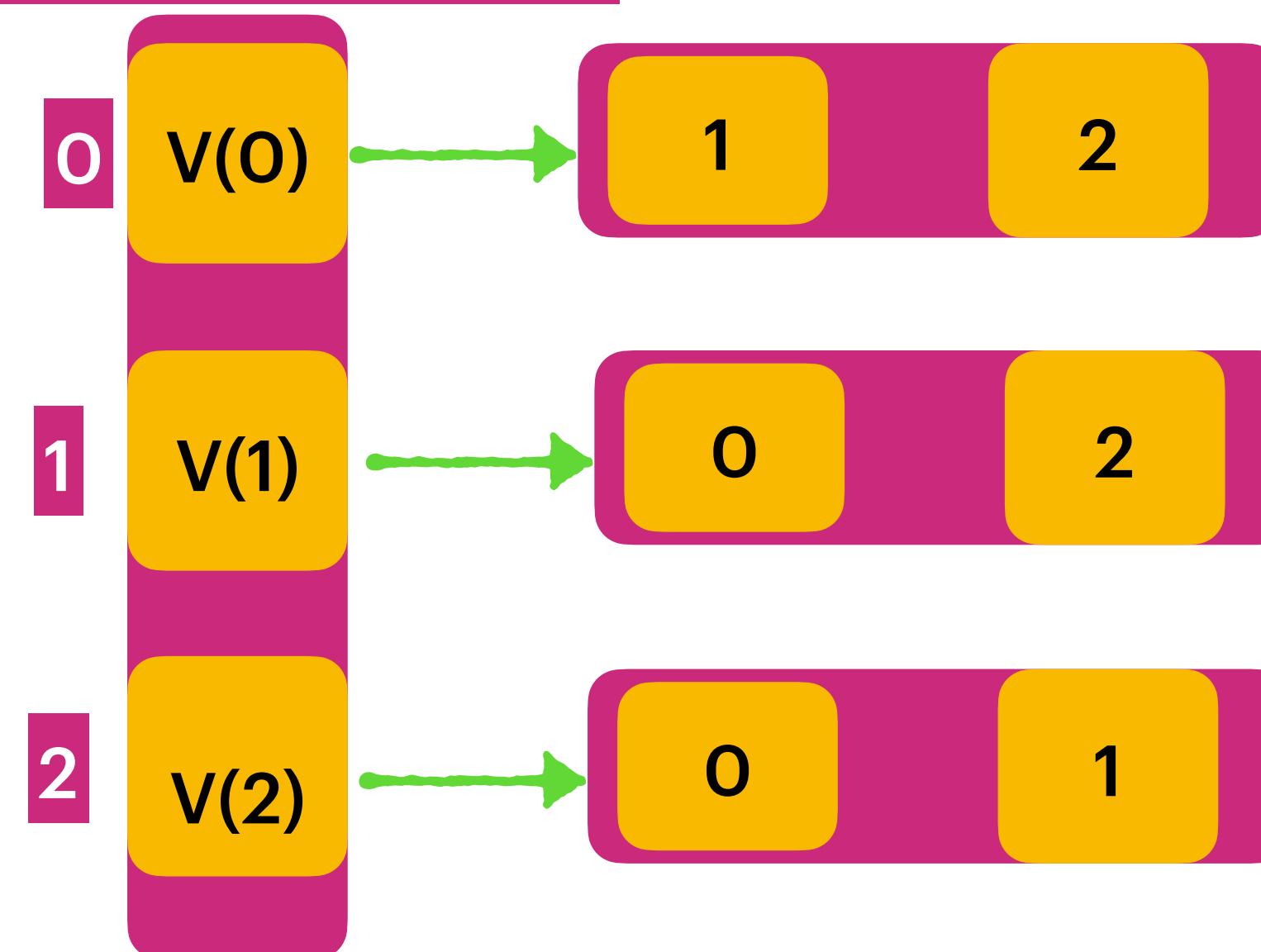
$n = 3$, edges = $[[0,1], [0,2], [1,2], [2,1], [2,0], [1,0]]$

List< LinkedHashSet >

Is this can be applied in
RealWorld ?

Limitations ***

1. Graph should be fixed .
2. Demands vertexes must
Be in the range of 0 to n-1
3. Occupy the fixed
memory.



Hashing

Add Vertex

O(1)

Remove Vertex

O(V)

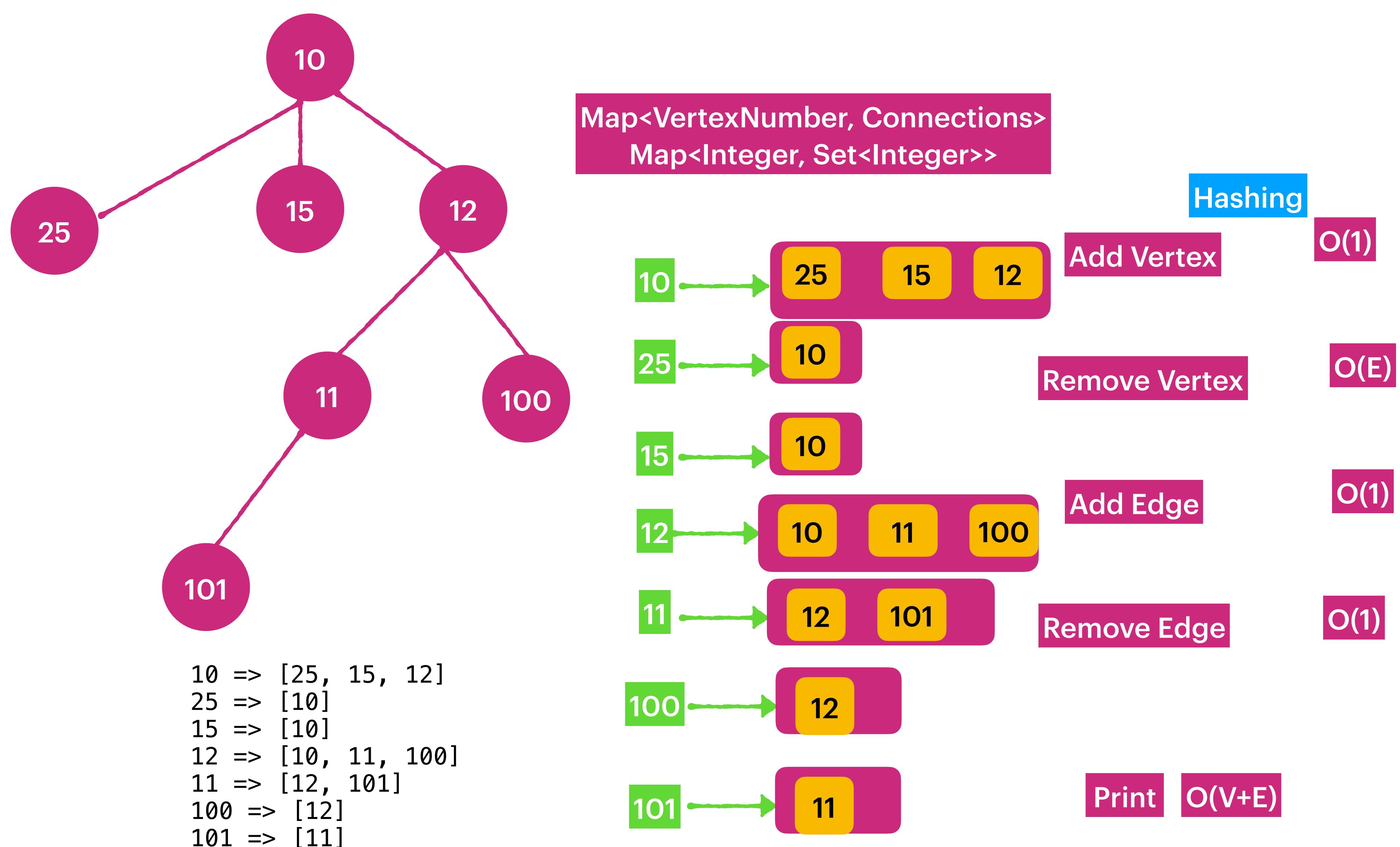
Add Edge

O(1)

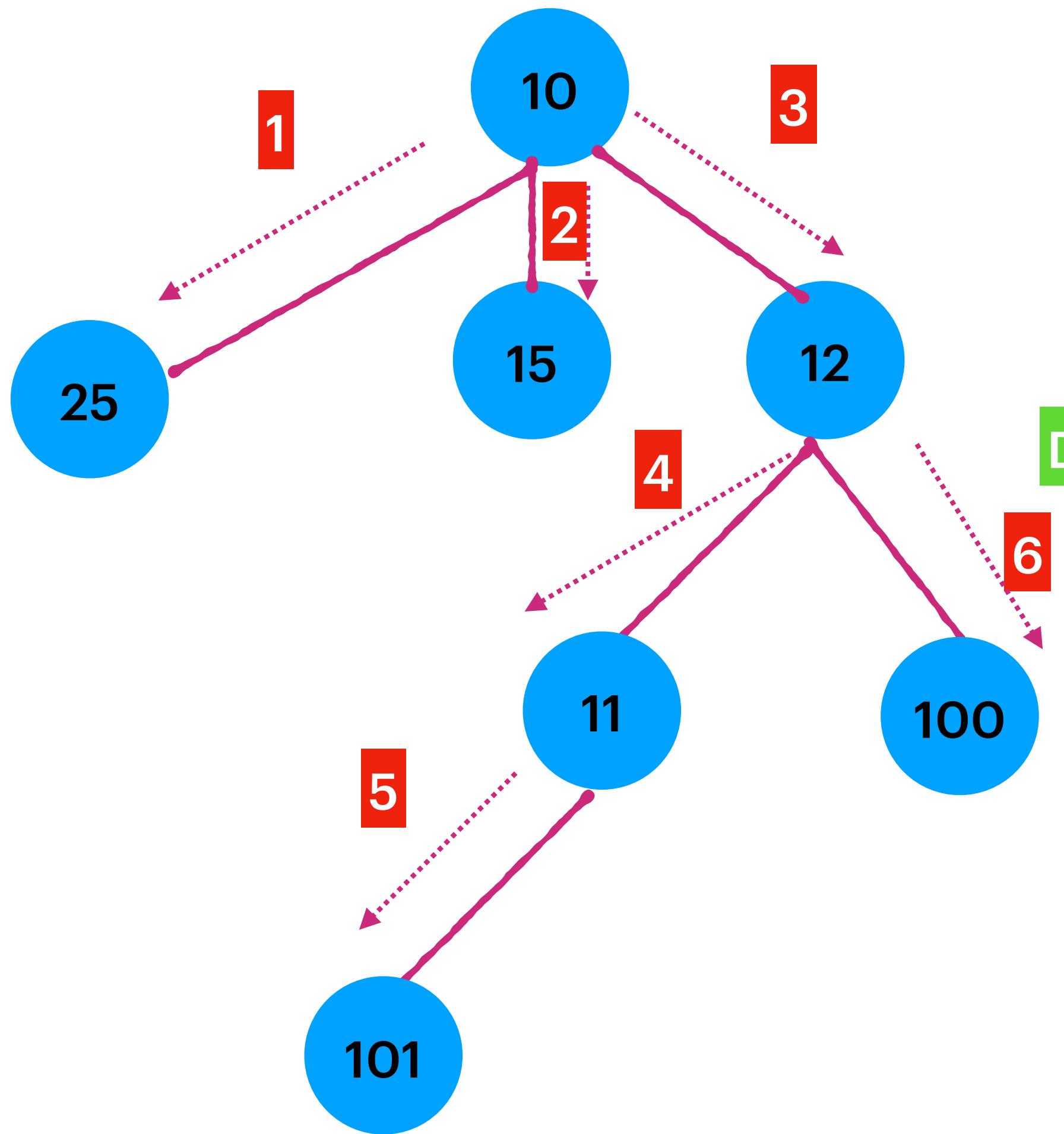
Remove Edge

O(1)

Print O(V+E)



Undirected Graph



Depth First Search

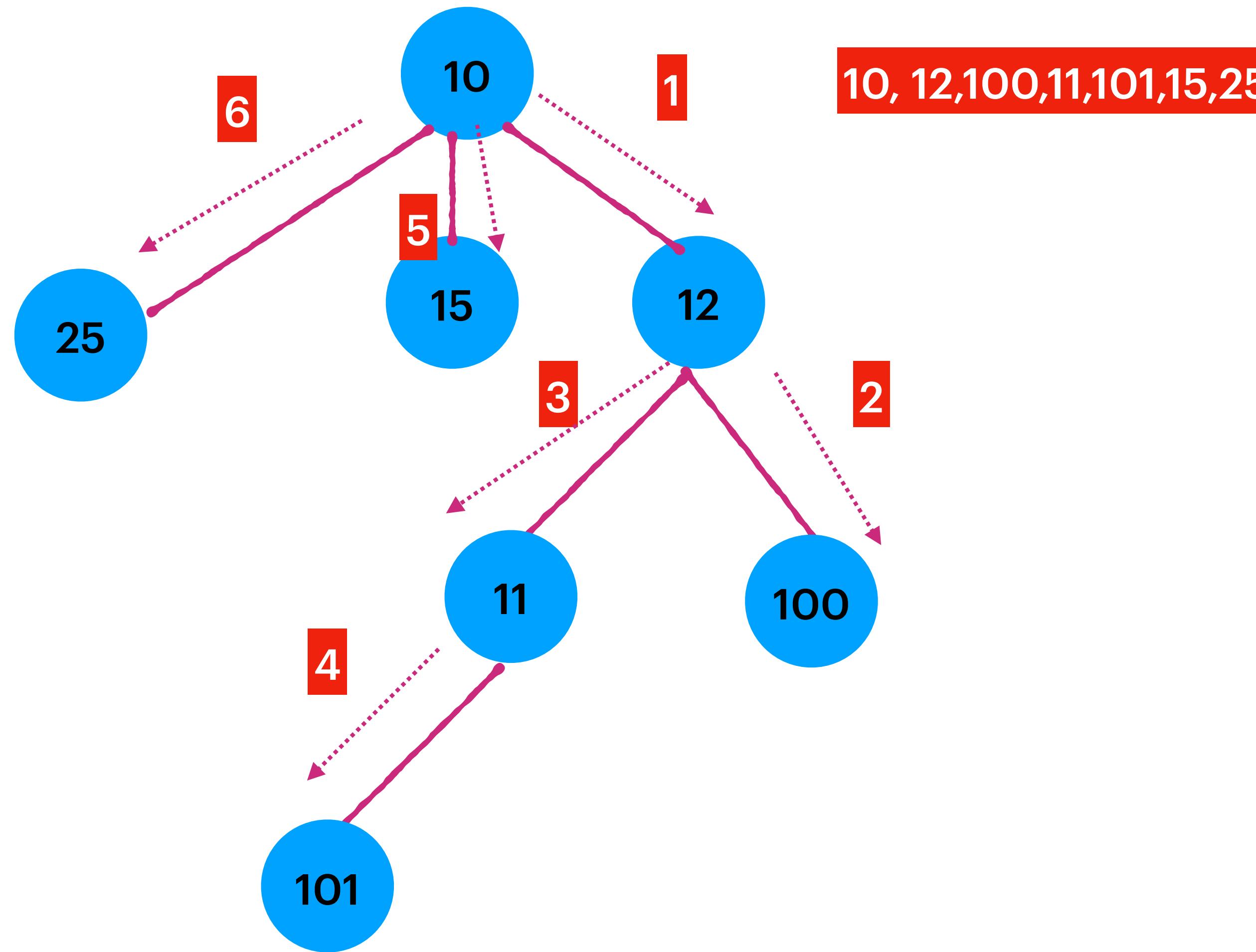
Moving => from root- left to right

10,25,15,12,11,101,100

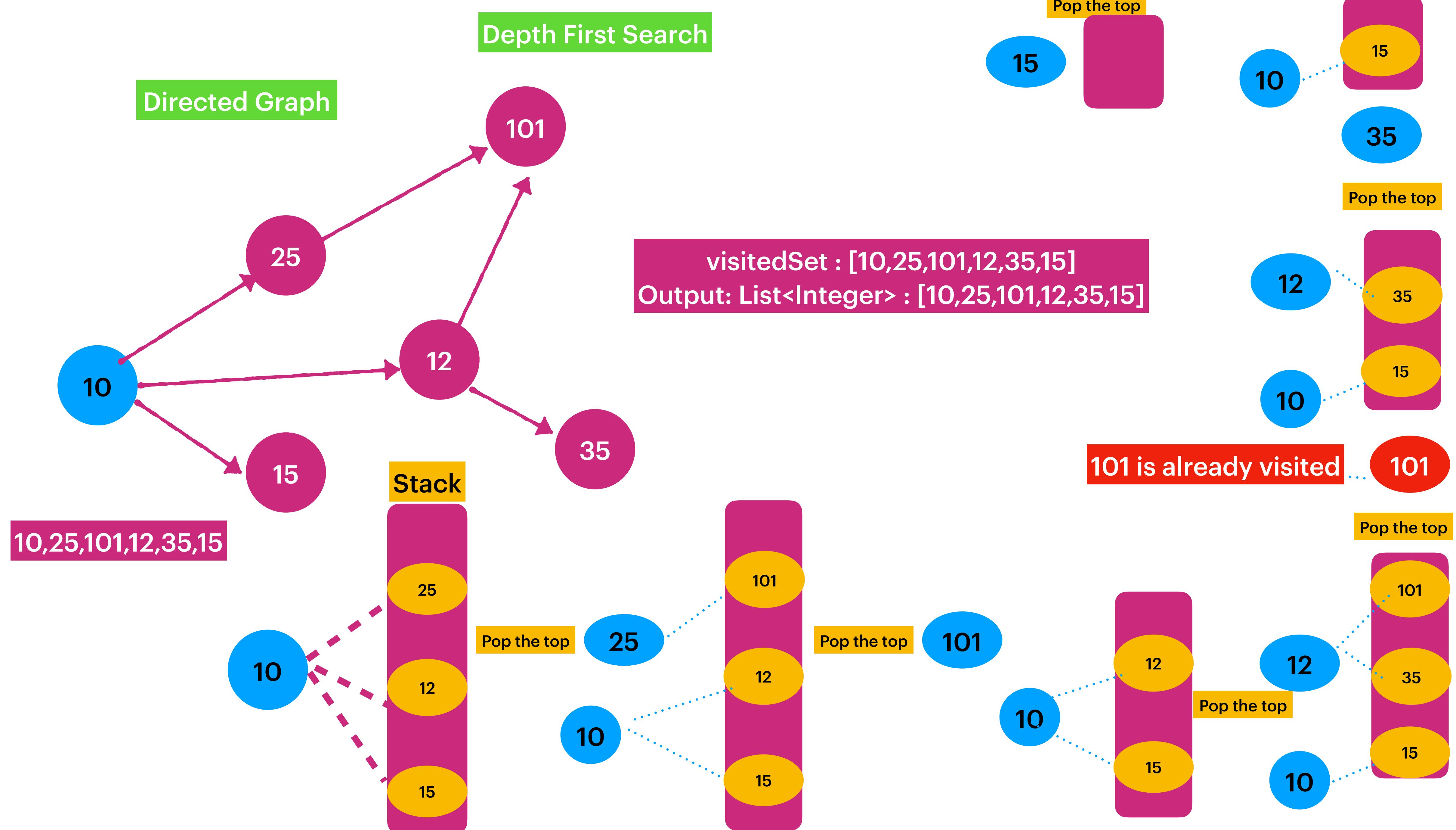
Undirected Graph

Depth First Search

Moving => from root - right to left

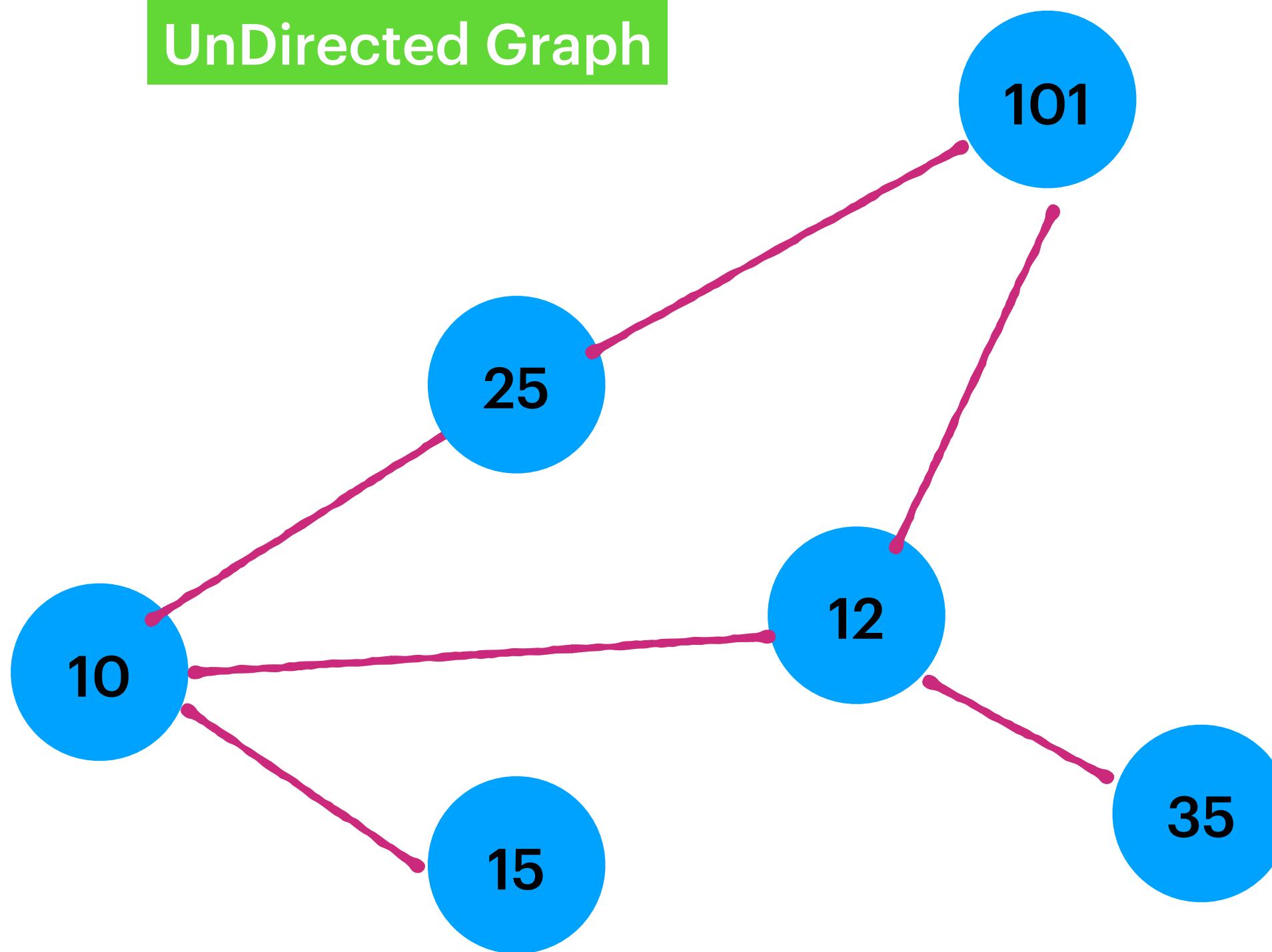


10, 12, 100, 11, 101, 15, 25



Depth First Search

UnDirected Graph



10 => [15, 12, 25] 15 => [10]
12 => [10, 101, 35]
25 => [10, 101]
101 => [25, 12]
35 => [12]

Stack []

Set [10,25,101,12,35,15]

OutputList[10,25,101,12,35,15]

DFS [10, 25, 101, 12, 35, 15]

Traverse All the Vertexes + Visit the unique Edges
Time Complexity : O(V+E)

$V(10) \Rightarrow [15,12,25]$
 $V(25) \Rightarrow [10,101]$
 $V(101) \Rightarrow [25,12]$
 $V(12) \Rightarrow [10,101,35]$
 $V(35) \Rightarrow [12]$
 $V(15) \Rightarrow [10]$

start : 10
stack($v(10)$) : 1

$v(10) \Rightarrow$ stack ([15,12,25]) = 3 : visited : [$v(10)$]
 $v(25) \Rightarrow$ stack ([15,12,10,101]) = 2: visited : [$v(10), v(25)$]
 $v(101) \Rightarrow$ stack ([15,12,10,25,12]) = 2 visited : [$v(10), v(25), v(101)$]
 $v(12) \Rightarrow$ stack ([15,12,10,25,10,101,35]) = 3
visited : [$v(10), v(25), v(101), v(12)$]
 $V(35) \Rightarrow$ stack ([15,12,10,25,10,101,12]) = 1
visited : [$v(10), v(25), v(101), v(12), v(35)$]

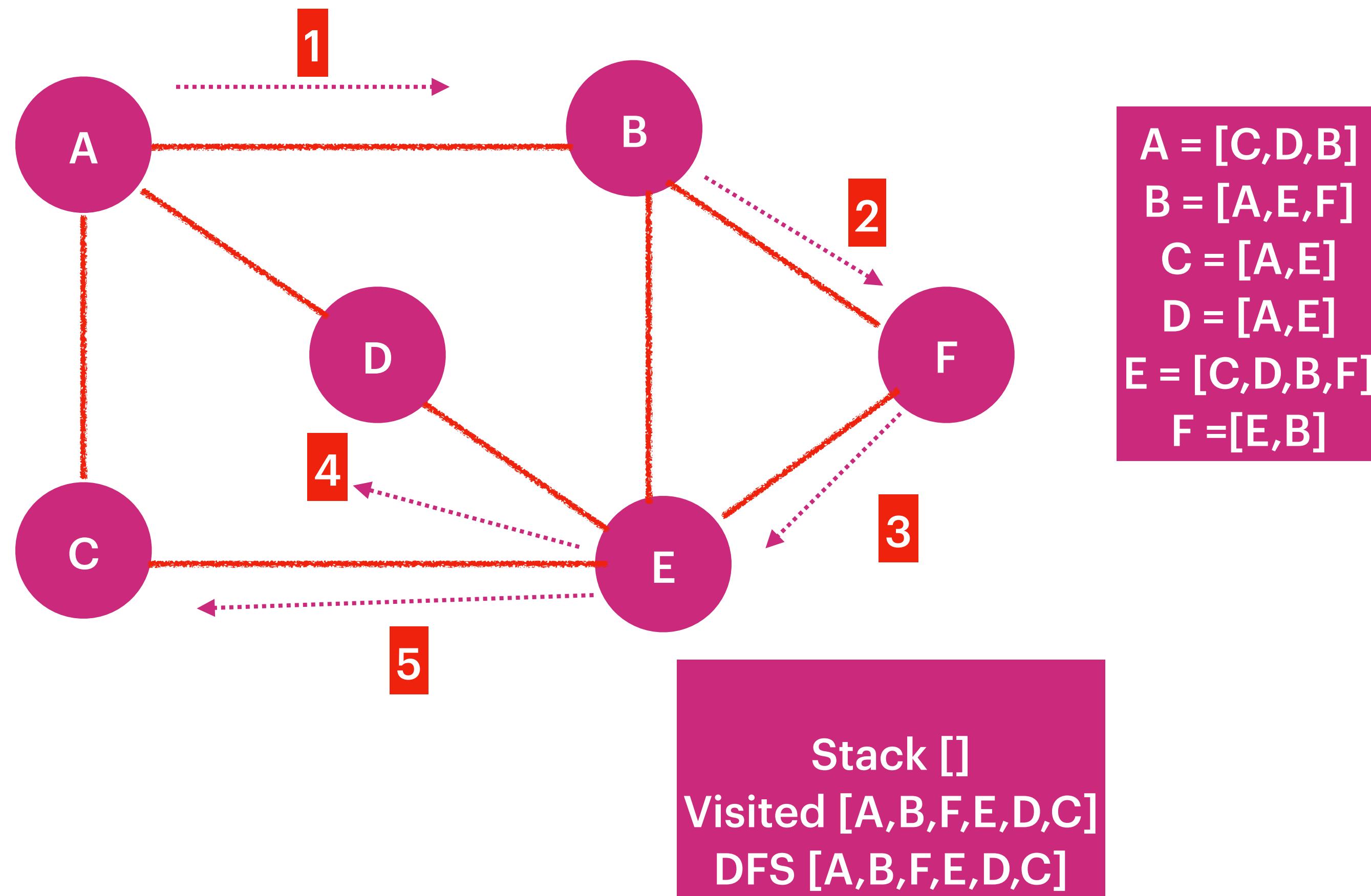
$v(12) = 0$ stack ([15,12,10,25,10,101])
 $v(101) = 0$ stack ([15,12,10,25,10])
 $v(10) = 0$ stack ([15,12,10,25])
 $v(25) = 0$ stack ([15,12,10])
 $v(10) = 0$ stack ([15,12])
 $v(12) = 0$ stack ([15])
 $v(15) = 1$ stack ([10]) visited : [$v(10), v(25), v(101), v(12), v(35), v(15)$]
 $v(10) = Ostac([])$ visited : [$v(10), v(25), v(101), v(12), v(35), v(15)$]

numberOf.Connections(V) + Unique[Edges]

$$13V + 12(E) = V + E$$

Analysis's Of DFS Time Complexity : $O(V+E)$

Depth First Search

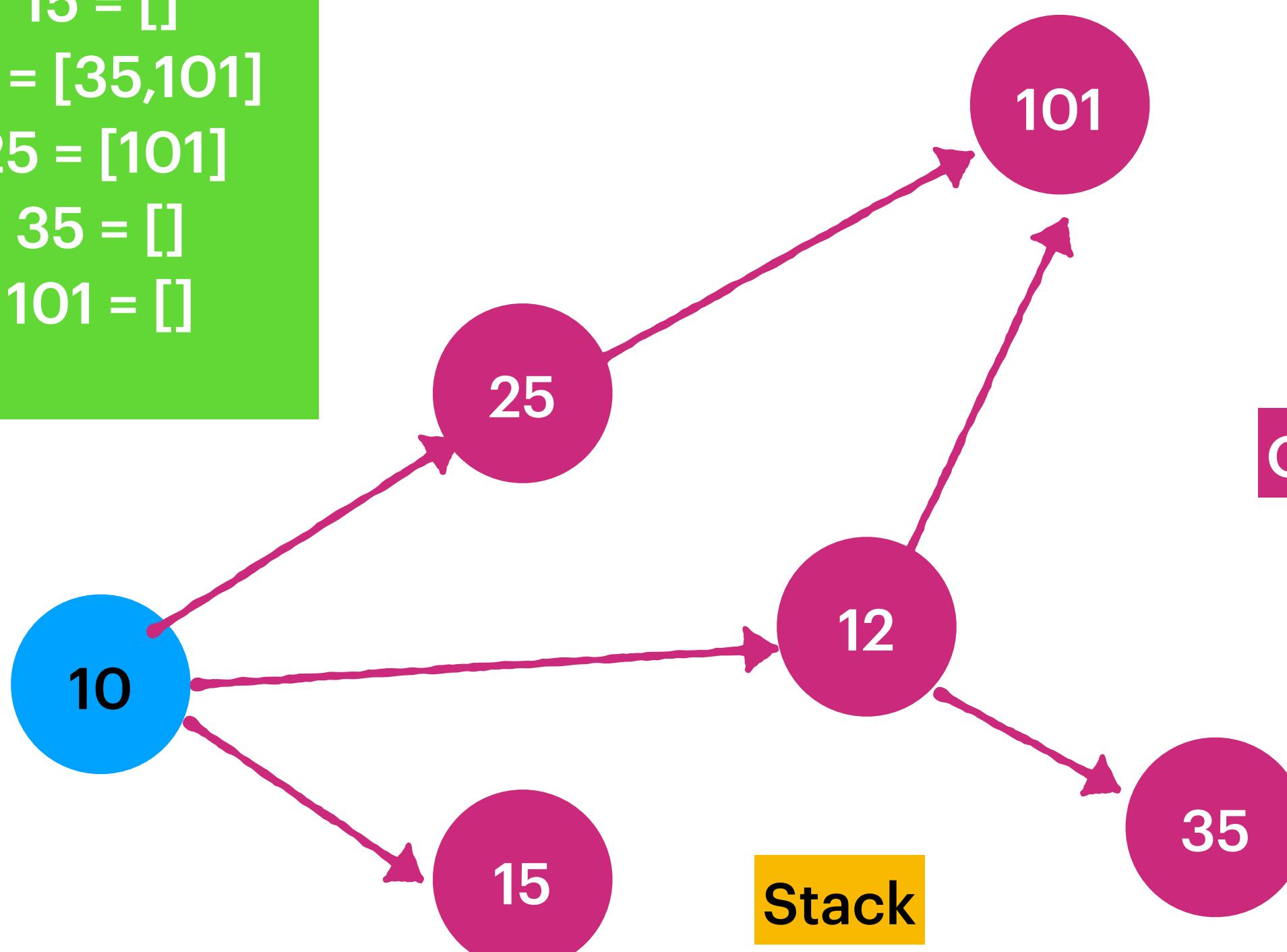


Directed Graph

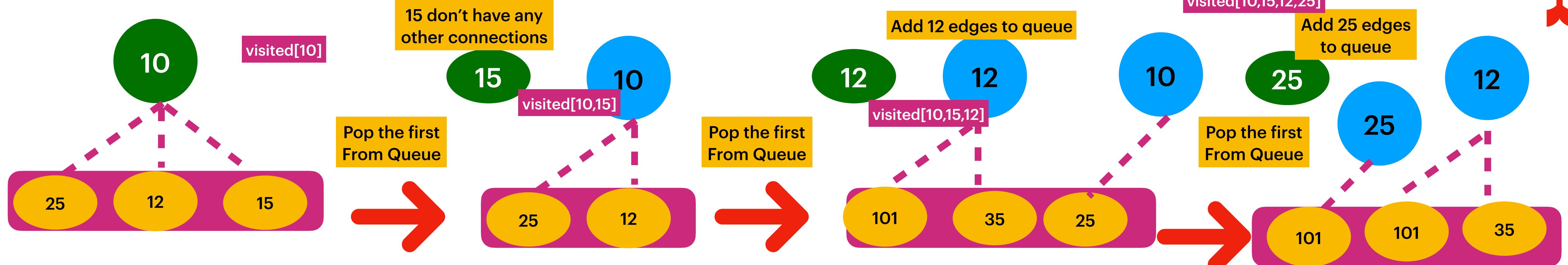
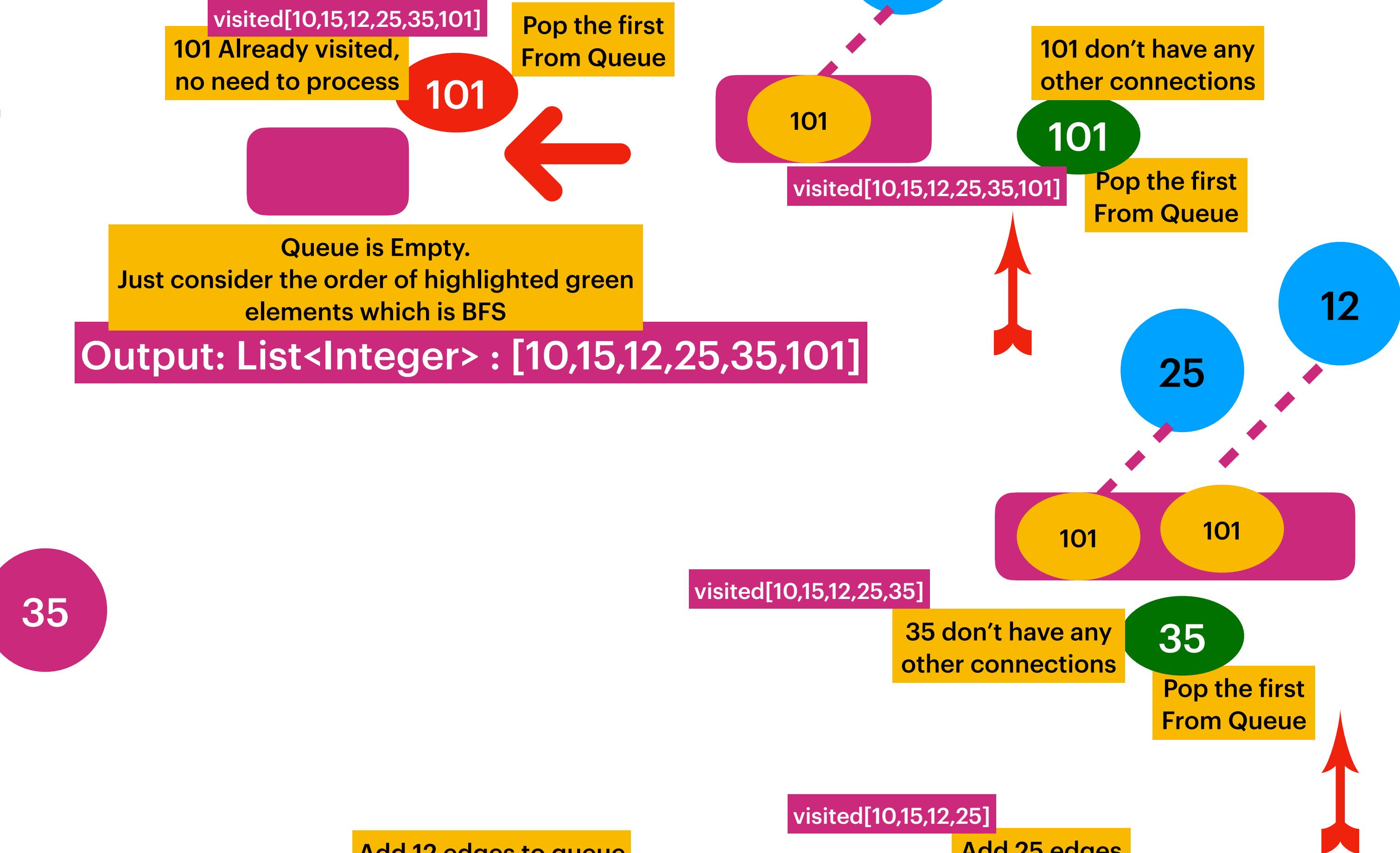
```

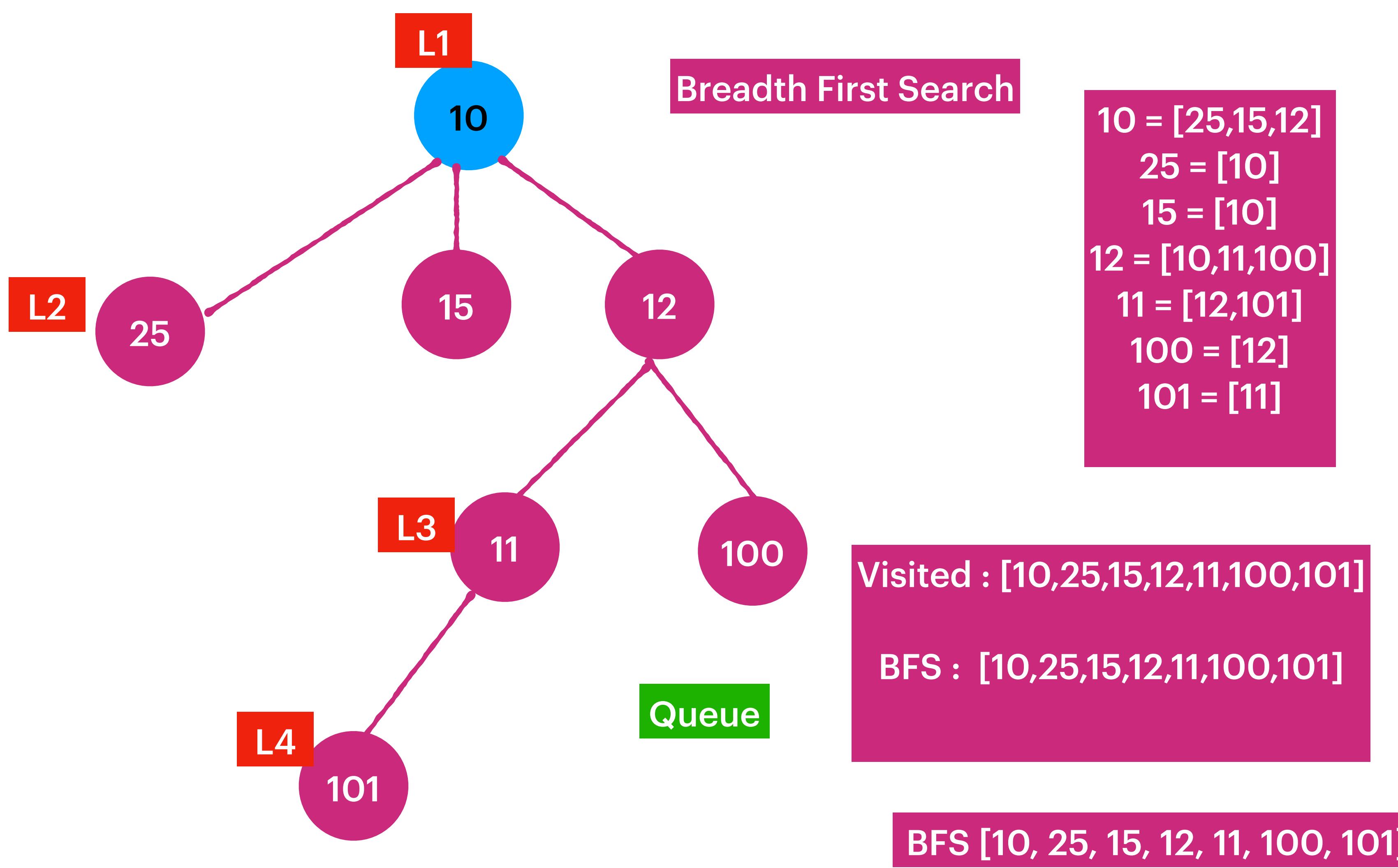
10 = [15,12,25]
15 = []
12 = [35,101]
25 = [101]
35 = []
101 = []

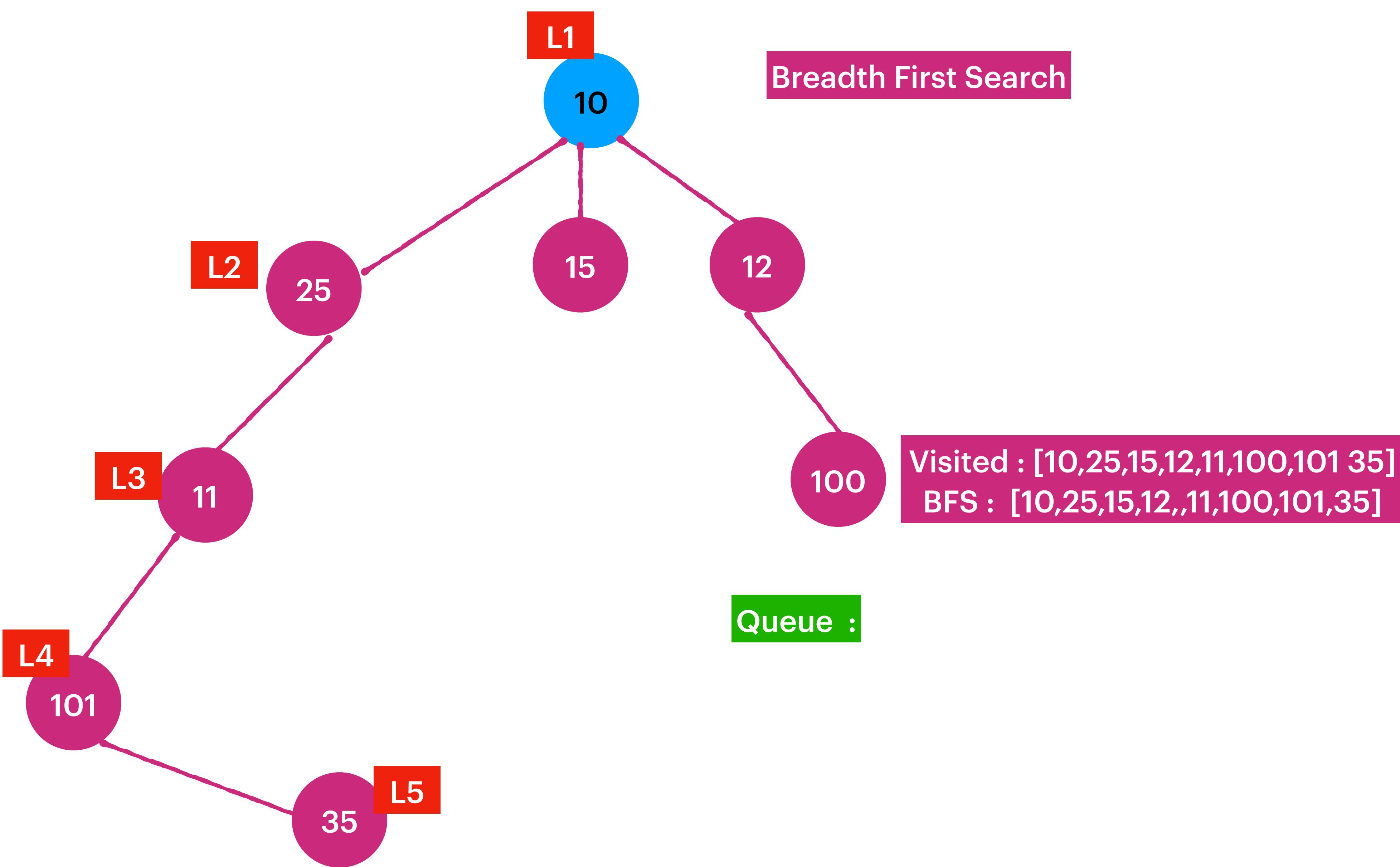
```



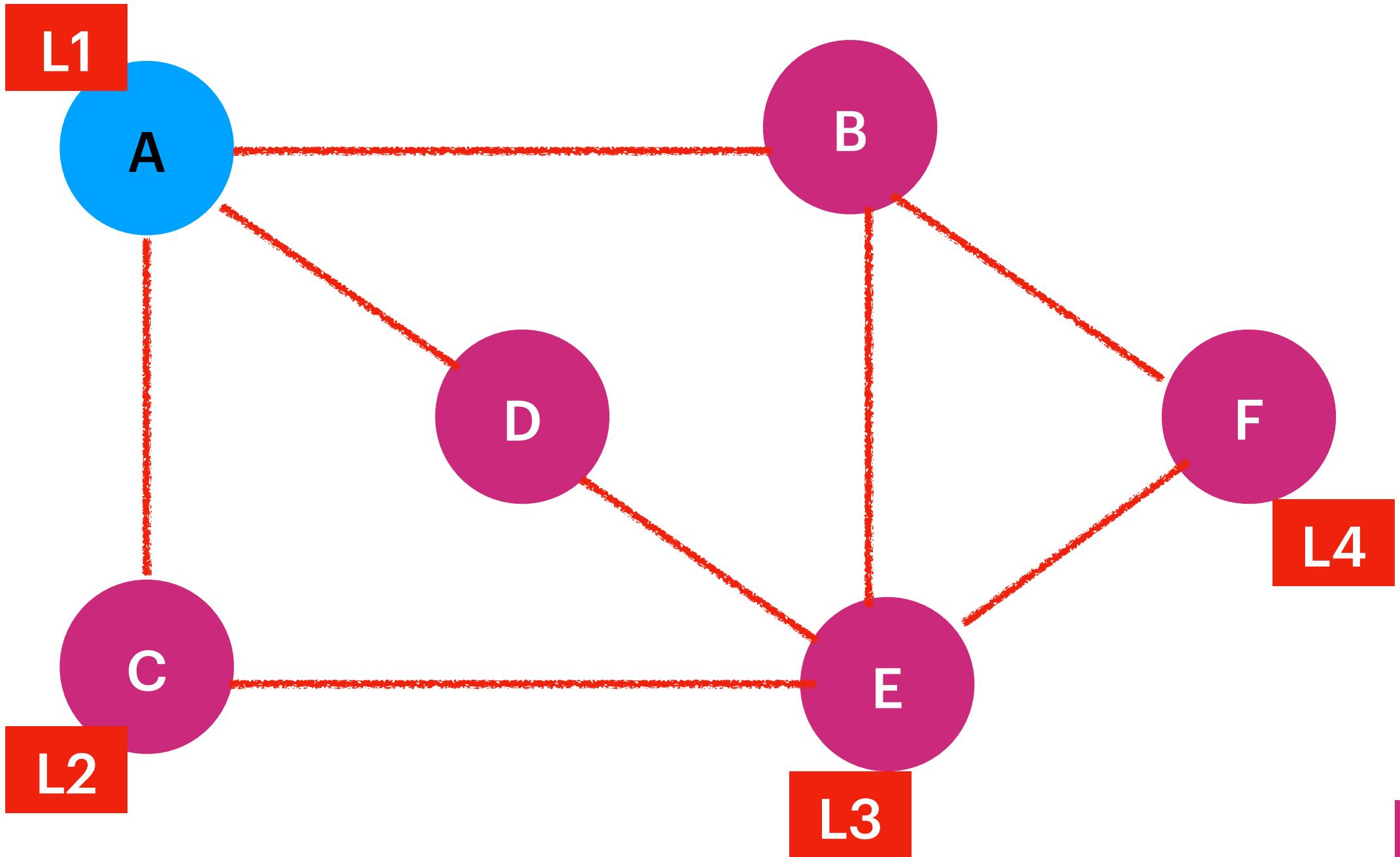
Breadth First Search







Breadth First Search



A = [C,D,B]
B = [A,E,F]
C = [A,E]
D = [A,E]
E = [C,D,B,F]
F = [E,B]

BFS : A,C,D,B,E,F

Find if Path Exists in Graph

There is a bi-directional graph with n vertices, where each vertex is labeled from 0 to $n - 1$ (inclusive). The edges in the graph are represented as a 2D integer array edges , where each $\text{edges}[i] = [\text{ui}, \text{vi}]$ denotes a bi-directional edge between vertex ui and vertex vi . Every vertex pair is connected by at most one edge, and no vertex has an edge to itself.

You want to determine if there is a valid path that exists from vertex start to vertex end .

Given edges and the integers n , start , and end , return true if there is a valid path from start to end , or false otherwise.

Input: $n = 3$, $\text{edges} = [[0,1],[1,2],[2,0]]$, $\text{start} = 0$, $\text{end} = 2$

Output: true

Explanation: There are two paths from vertex 0 to vertex 2:

- $0 \rightarrow 1 \rightarrow 2$
- $0 \rightarrow 2$

Constraints:

$1 \leq n \leq 2 * 10^5$

$0 \leq \text{edges.length} \leq 2 * 10^5$

$\text{edges}[i].length == 2$

$0 \leq u_i, v_i \leq n - 1$

$u_i \neq v_i$

$0 \leq \text{start}, \text{end} \leq n - 1$

There are no duplicate edges.

There are no self edges.

Input: $n = 6$, $\text{edges} = [[0,1],[0,2],[3,5],[5,4],[4,3]]$, $\text{start} = 0$, $\text{end} = 5$

Output: false

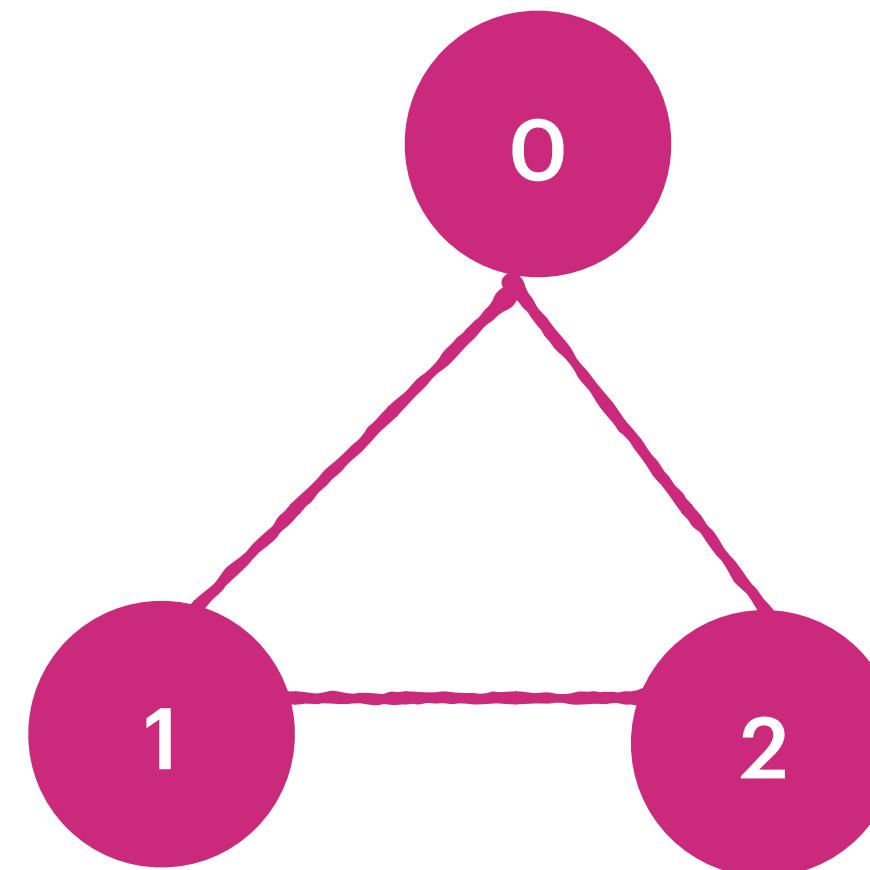
Explanation: There is no path from vertex 0 to vertex 5.

Input: n = 3, edges = [[0,1],[1,2],[2,0]], start = 0, end = 2

Output: true

Explanation: There are two paths from vertex 0 to vertex 2:

- 0 → 1 → 2
- 0 → 2



Solution 1 DisJoint Set : O(1) :

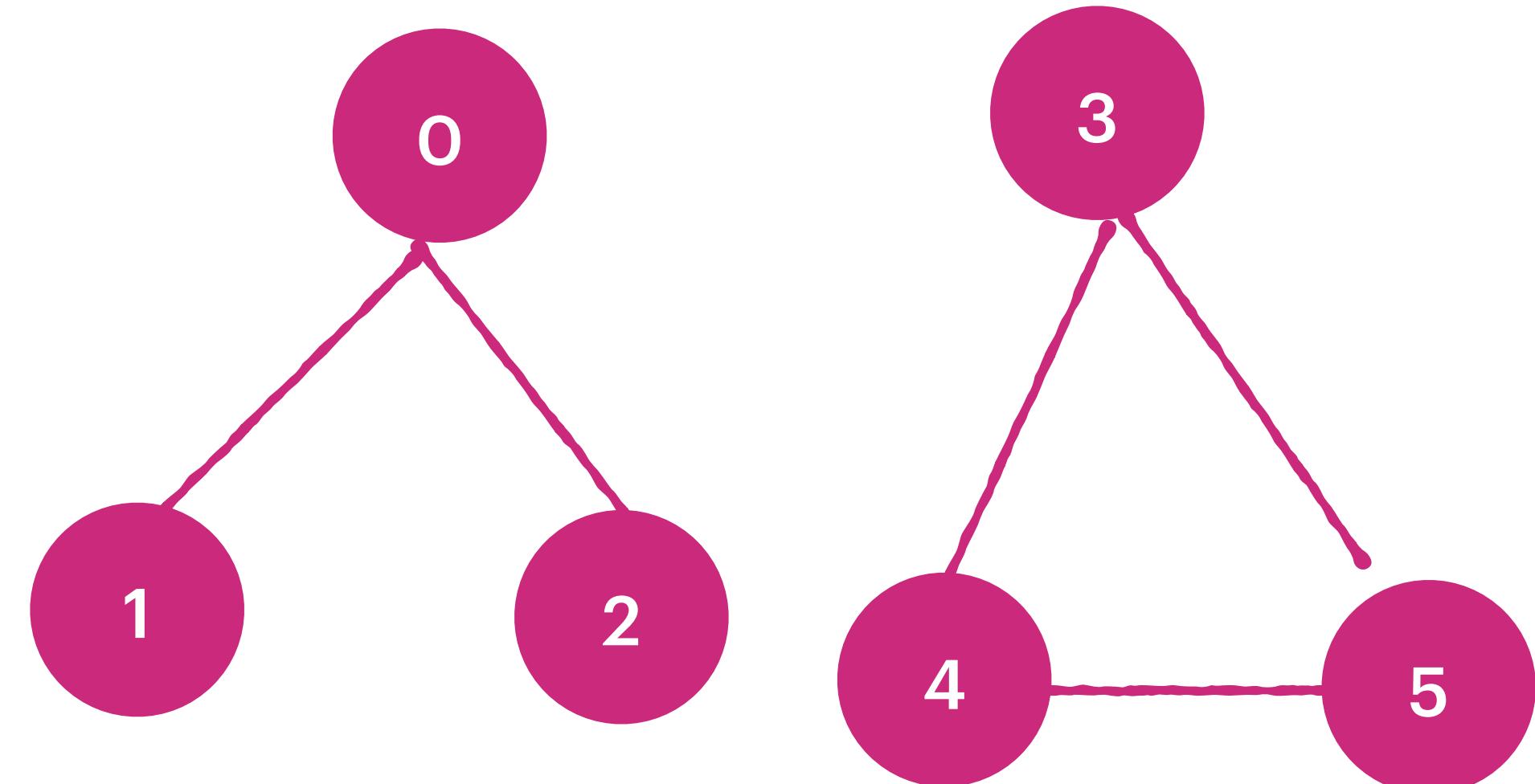
Solution 2. DFS : O(V+E)

Solution 3 BFS : O(V+E)

Input: n = 6, edges = [[0,1],[0,2],[3,5],[5,4],[4,3]], start = 0, end = 5

Output: false

Explanation: There is no path from vertex 0 to vertex 5.



All Paths From Source to Target

Given a directed acyclic graph (DAG) of n nodes labeled from 0 to $n - 1$, find all possible paths from node 0 to node $n - 1$ and return them in any order. The graph is given as follows: $\text{graph}[i]$ is a list of all nodes you can visit from node i (i.e., there is a directed edge from node i to node $\text{graph}[i][j]$).

Input: $\text{graph} = [[1,2],[3],[3],[]]$

Output: $[[0,1,3],[0,2,3]]$

Explanation: There are two paths: $0 \rightarrow 1 \rightarrow 3$ and $0 \rightarrow 2 \rightarrow 3$.

Input: $\text{graph} = [[4,3,1],[3,2,4],[3],[4],[]]$

Output: $[[0,4],[0,3,4],[0,1,3,4],[0,1,2,3,4],[0,1,4]]$

$n == \text{graph.length}$

$2 \leq n \leq 15$

$0 \leq \text{graph}[i][j] < n$

$\text{graph}[i][j] \neq i$ (i.e., there will be no self-loops).

All the elements of $\text{graph}[i]$ are unique.

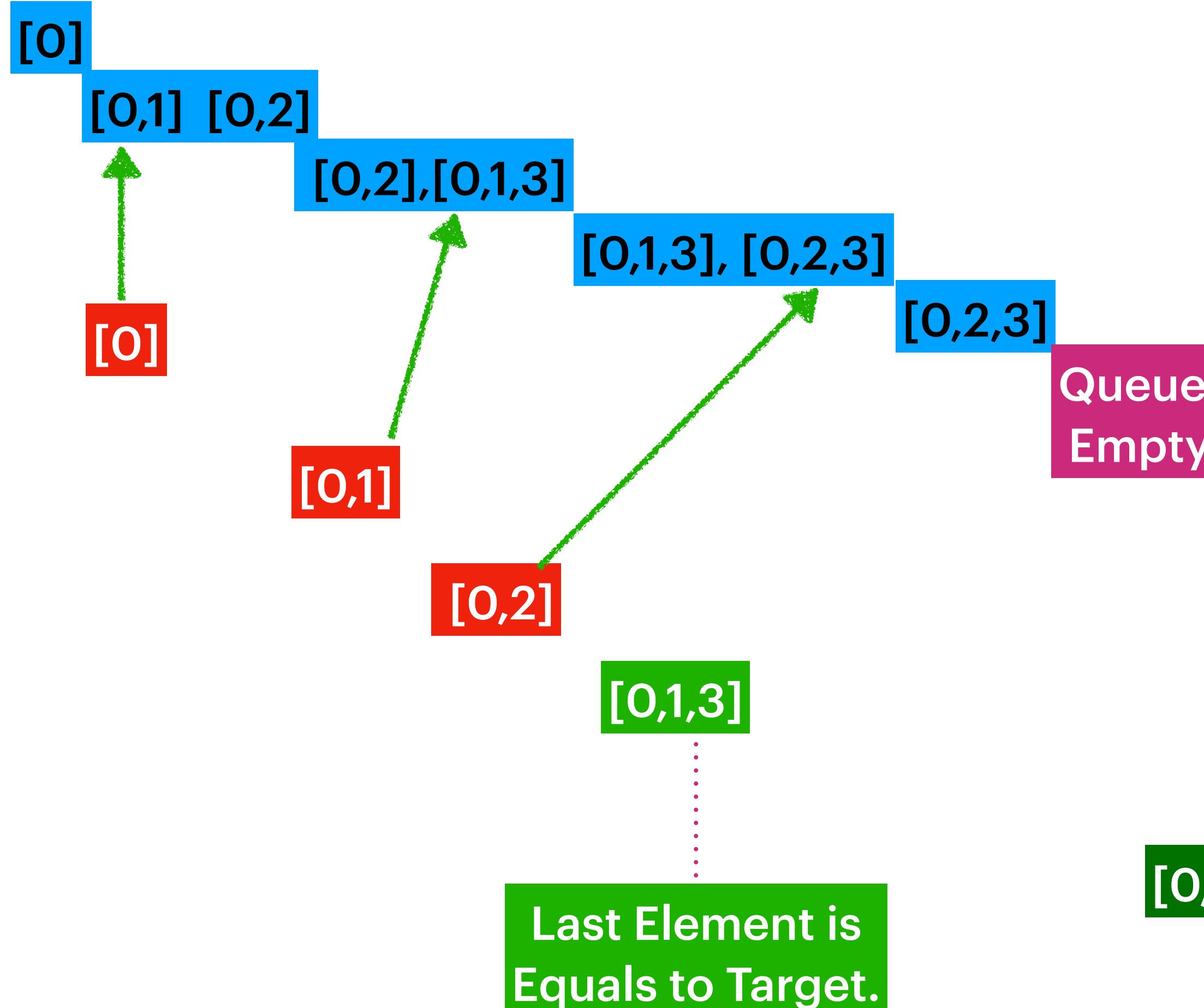
The input graph is guaranteed to be a DAG.

All Paths From Source to Target

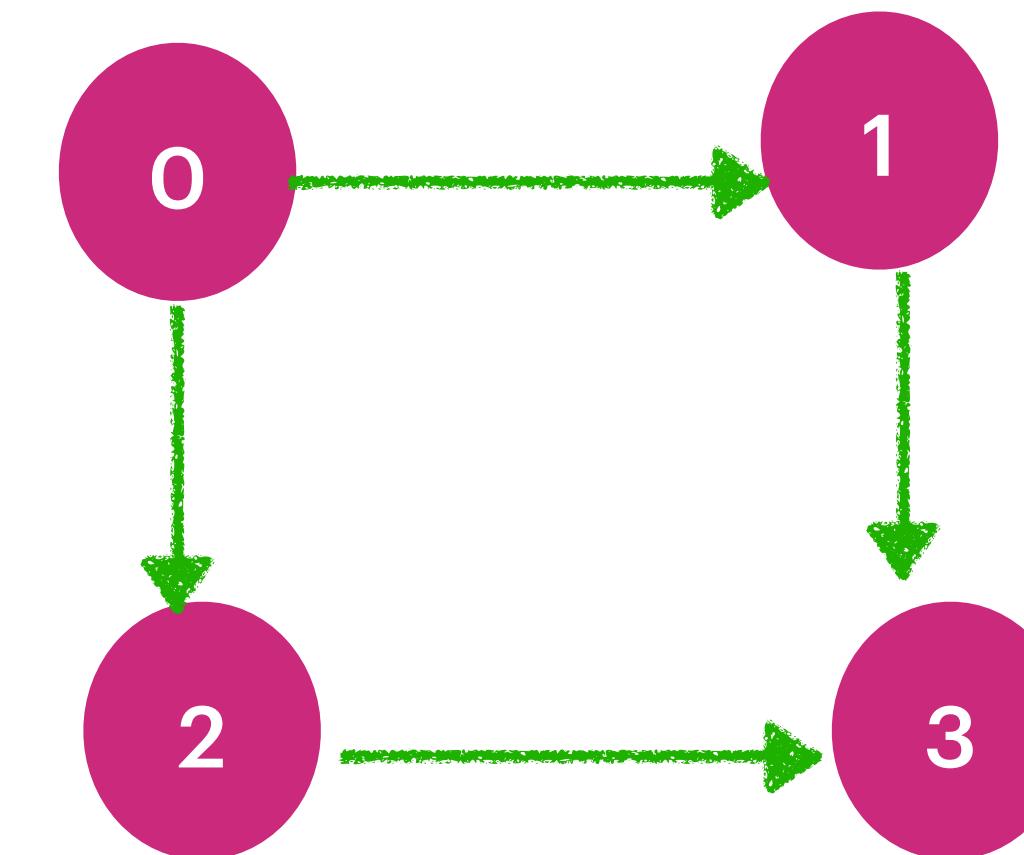
Input: graph = [[1,2],[3],[3],[]] n=4

Output: [[0,1,3],[0,2,3]]

Explanation: There are two paths: 0 -> 1 -> 3 and 0 -> 2 -> 3.



graph = [[1,2], [3], [3], []] n=4



Paths From 0 to 3

0 → 1 → 3 , 0 → 2 → 3

[0,2,3]

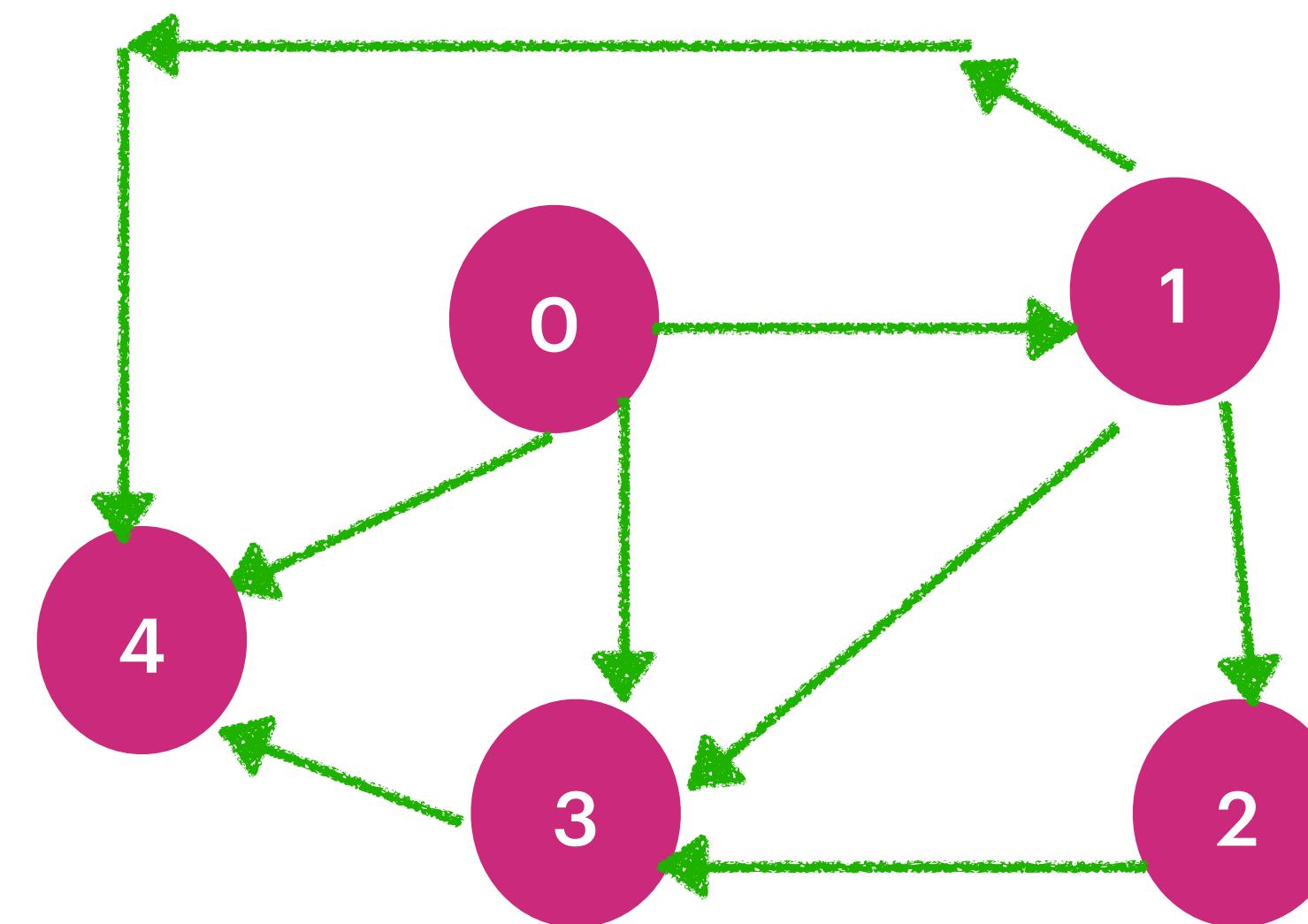
Last Element is Equals to Target.

All Paths From Source to Target

`n == graph.length`
`2 <= n <= 15`
`0 <= graph[i][j] < n`
`graph[i][j] != i` (i.e., there will be no self-loops).
All the elements of `graph[i]` are unique.
The input graph is guaranteed to be a DAG.

`graph = [[4,3,1], [3,2,4], [3], [4], []] n=5`

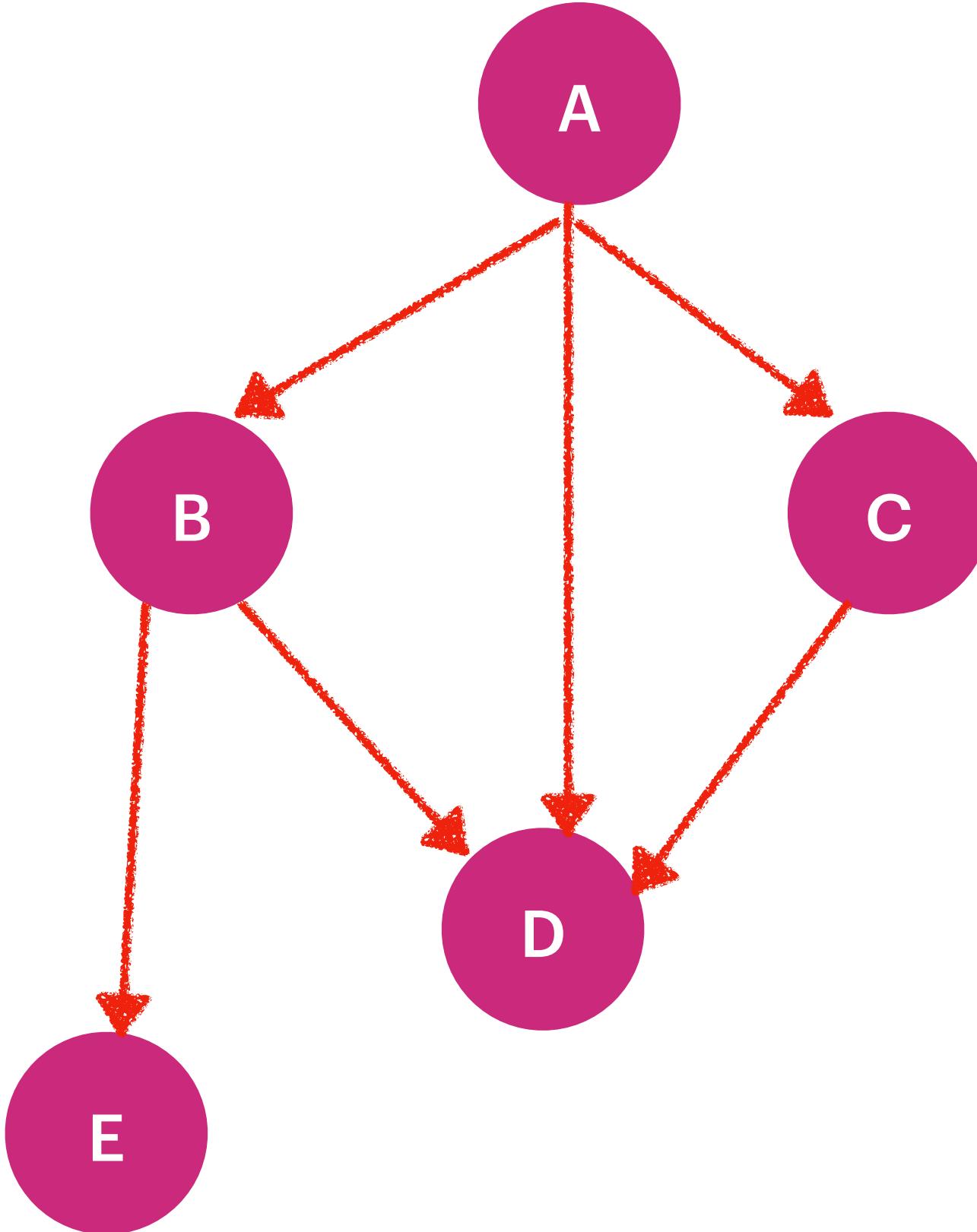
Input: `graph = [[4,3,1],[3,2,4],[3],[4],[]] n=5`
Output: `[[0,4],[0,3,4],[0,1,3,4],[0,1,2,3,4],[0,1,4]]`



Paths From 0 to 4

`0->4 , 0->3->4, 0->1->3->4, 0->1->2->3->4, 0->1->4`

BFS
Source : A
Target : D



[A]

[A,B]

[A,C]

[A,D]

Last Element is
Equals to Target.

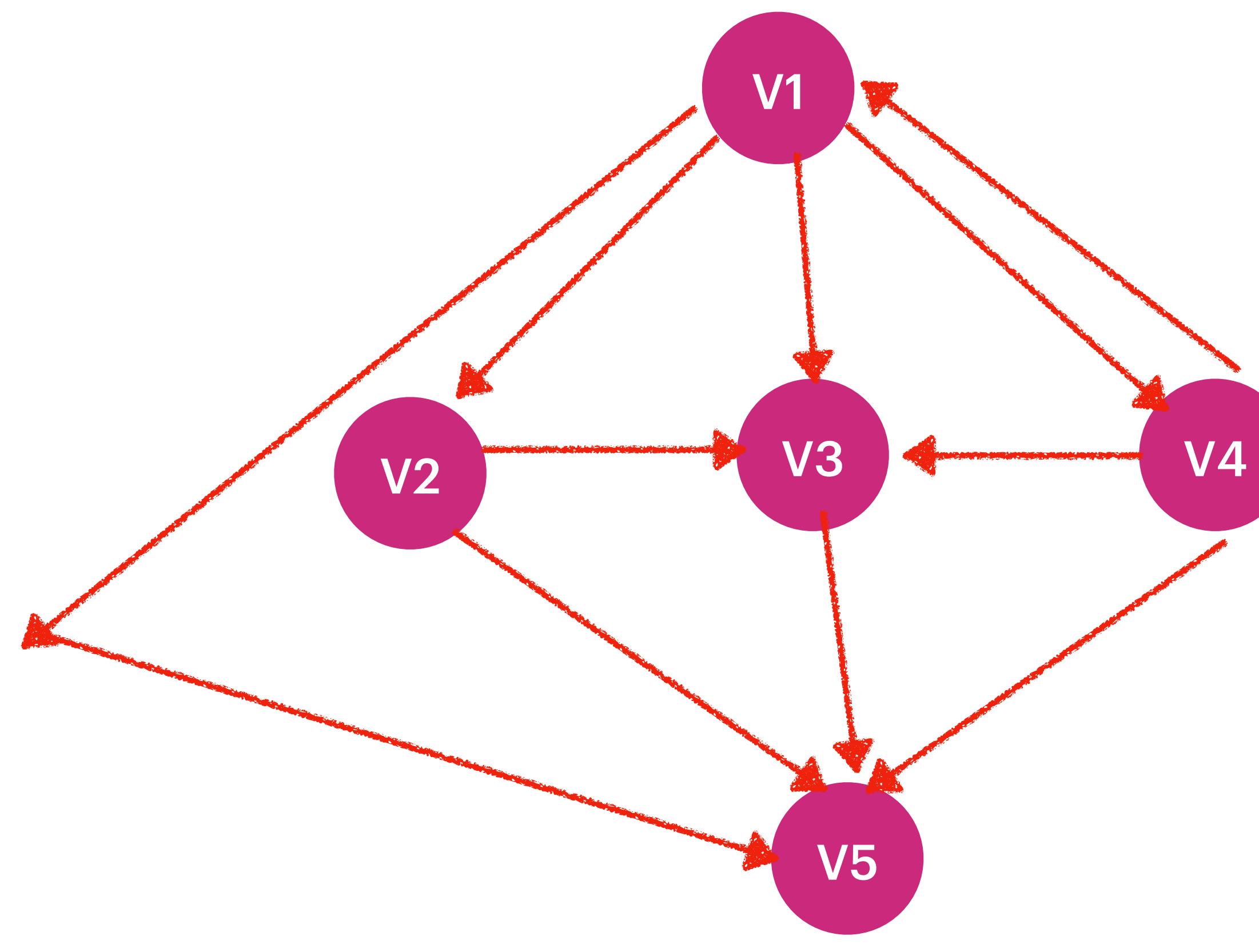
[A,B,D]

Last Element is
Equals to Target.

[A,B,E]

[A,C,D]

Last Element is
Equals to Target.



Source
(V1)
Target
(V5)

$V1 \rightarrow V5$ through $V3$ IFF $V1 \rightarrow V3$ & $V3 \rightarrow V5$

$V1 \rightarrow V5$ through $V2$ IFF $V1 \rightarrow V2$ & $V2 \rightarrow V5$

$$V * 2^V$$

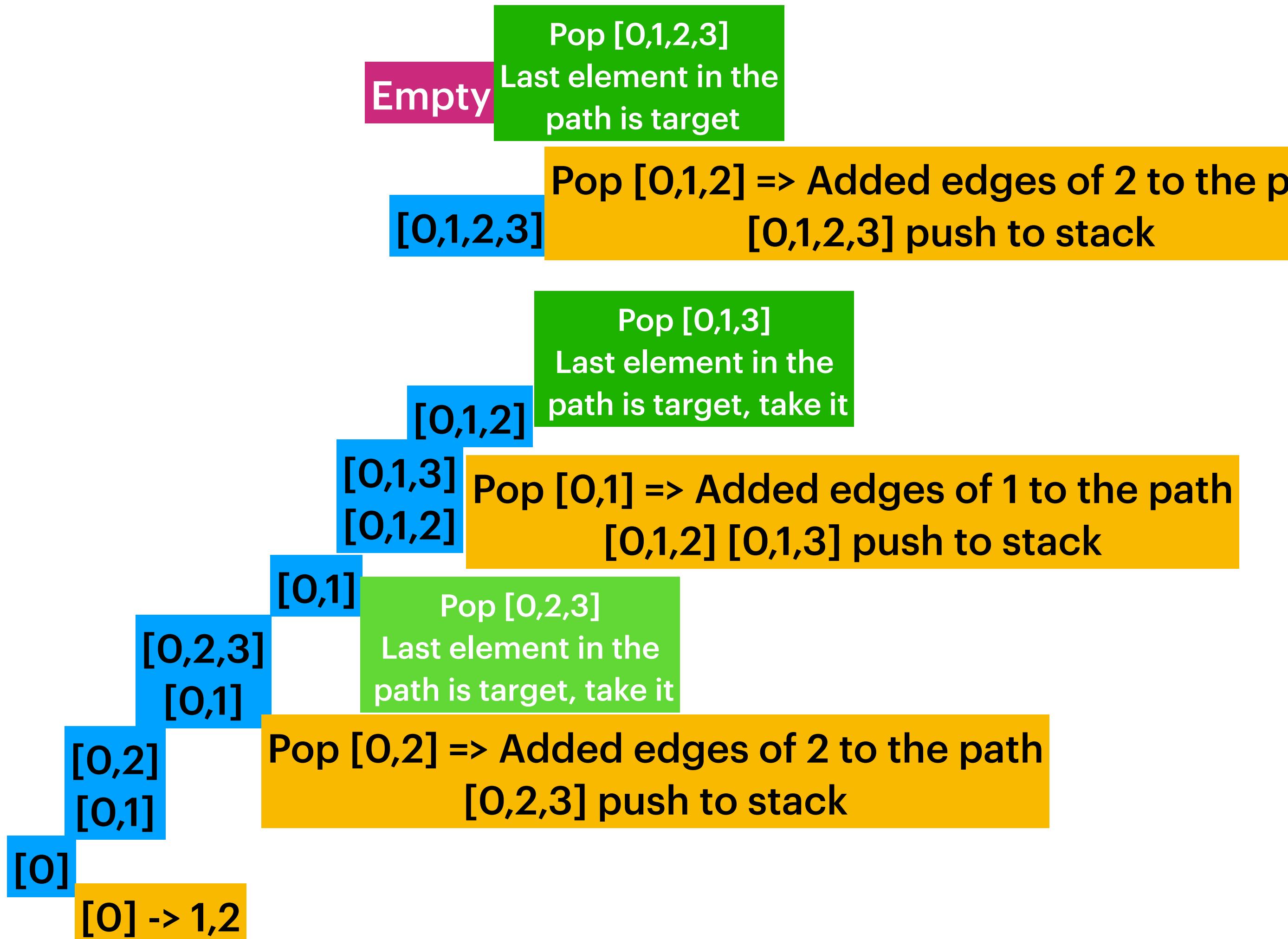
In worst case as per Graph Theory For each vertex we can make $(2^{V-1} - 1)$ unique paths. So in worst cast time complexity is $O(V * 2^V)$

All Paths From Source to Target : DFS

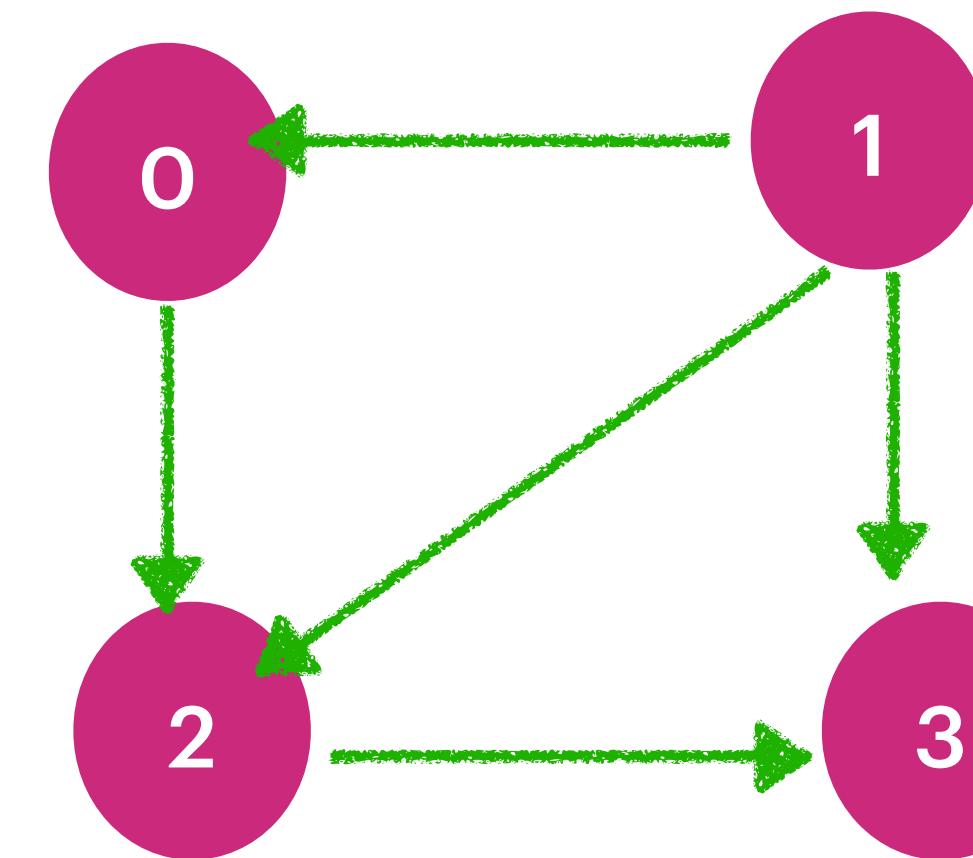
Input: graph = [[1,2],[2,3],[3],[]] n=4

Output: [[0,1,3],[0,2,3],[0,1,2,3]]

Explanation: There are two paths: 0 \rightarrow 1 \rightarrow 3 and 0 \rightarrow 2 \rightarrow 3.
0 \rightarrow 1 \rightarrow 2 \rightarrow 3

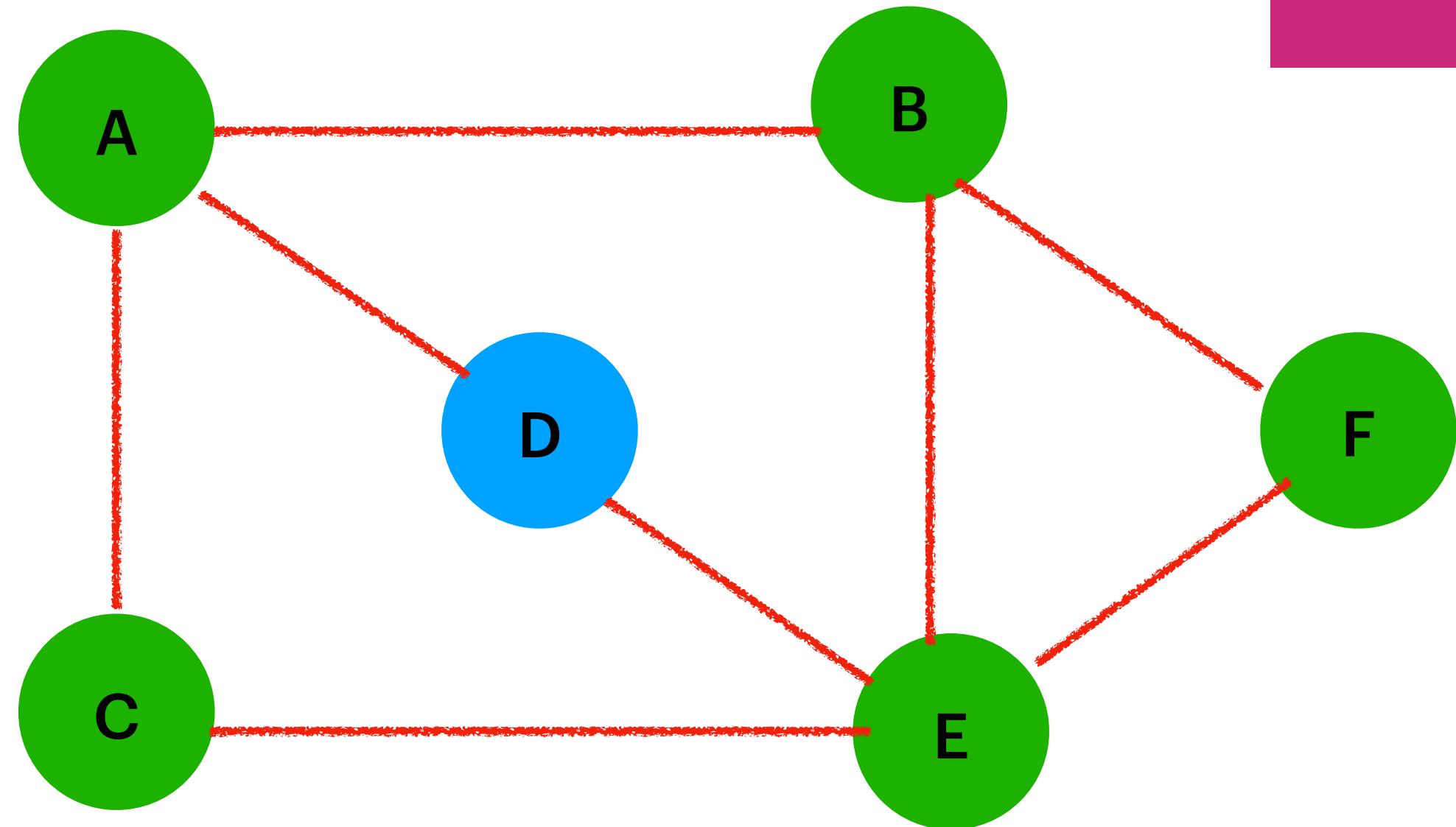


graph = [[1,2], [2,3], [3], []] n=4



Paths From 0 to 3

0 \rightarrow 1 \rightarrow 3 , 0 \rightarrow 2 \rightarrow 3 ,
0 \rightarrow 1 \rightarrow 2 \rightarrow 3

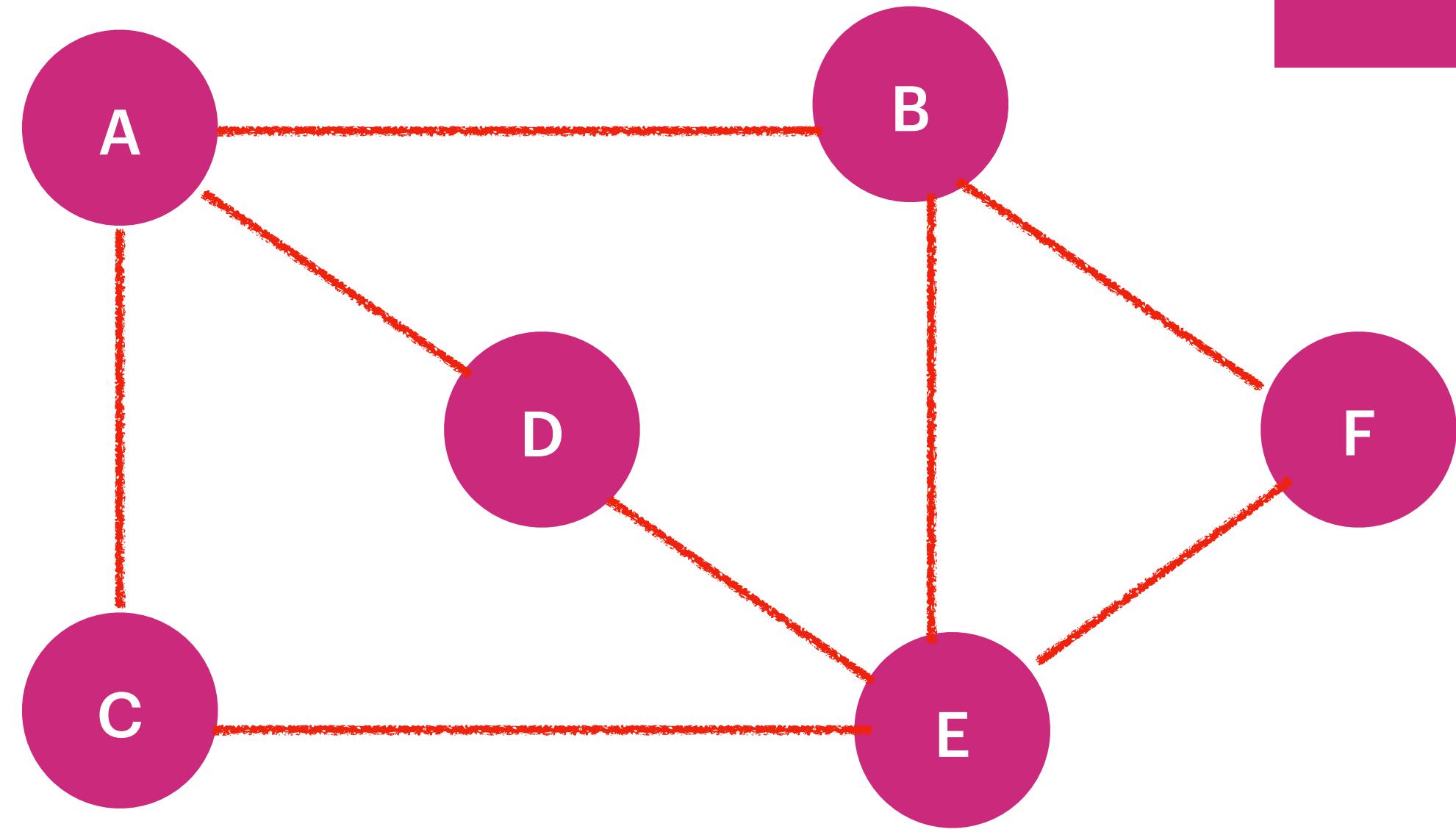


Print All the Paths From A \rightarrow F
DFS : $(V-1)!$
BFS : $(V-1)!$

BFS [
[A, B, F],
[A, C, E, F],
[A, D, E, F],
[A, B, E, F],
[A, C, E, B, F],
[A, D, E, B, F]
]

output : [[A,B,F], [A,B,E,F],[A,D,E,F],[A,D,E,B,F],[A,C,E,F],[A,C,E,B,F]]

ABF, ACEBF, ADEF, ABEF, ACEBF, ADEBF



BFS A->F [A, B, F]
 BFS B->D [B, A, D]
 BFS E->A [E, B, A]
 BFS C->B [C, A, B]
 BFS E->F [E, F]

Shortest Path between A & F :
 BFS : $O(V+E)$
 Output : [A,B,F]

A [C,D,B]
 Queue [AC,AD,AB] V[A]
 AC :
 Queue [AD,AB,ACA,ACE] V[A,C]
 AD:
 Queue [AB,ACA,ACE,ADA,ADE] : V[A,C,D]
 AB: V[A,C,D,B,E]
 Queue [ABF,ACE[C,B,F]]
 ABF -> F is Target Shortest Path

Clone Graph

Given a reference of a node in a connected undirected graph.

Return a deep copy (clone) of the graph.

Each node in the graph contains a value (int) and a list (List[Node]) of its neighbors.

```
class Node {  
    public int val;  
    public List<Node> neighbors;  
}
```

Input: adjList = [[2,4],[1,3],[2,4],[1,3]]

Output: [[2,4],[1,3],[2,4],[1,3]]

Explanation: There are 4 nodes in the graph.

1st node (val = 1)'s neighbors are 2nd node (val = 2) and 4th node (val = 4).

2nd node (val = 2)'s neighbors are 1st node (val = 1) and 3rd node (val = 3).

3rd node (val = 3)'s neighbors are 2nd node (val = 2) and 4th node (val = 4).

4th node (val = 4)'s neighbors are 1st node (val = 1) and 3rd node (val = 3).

Input: adjList = [[2],[1]]

Output: [[2],[1]]

Input: adjList = []

Output: []

Explanation: Note that the input contains one empty list. The graph consists of only one node with val = 1 and it does not have any neighbors.

Constraints:

The number of nodes in the graph is in the range [0, 100].

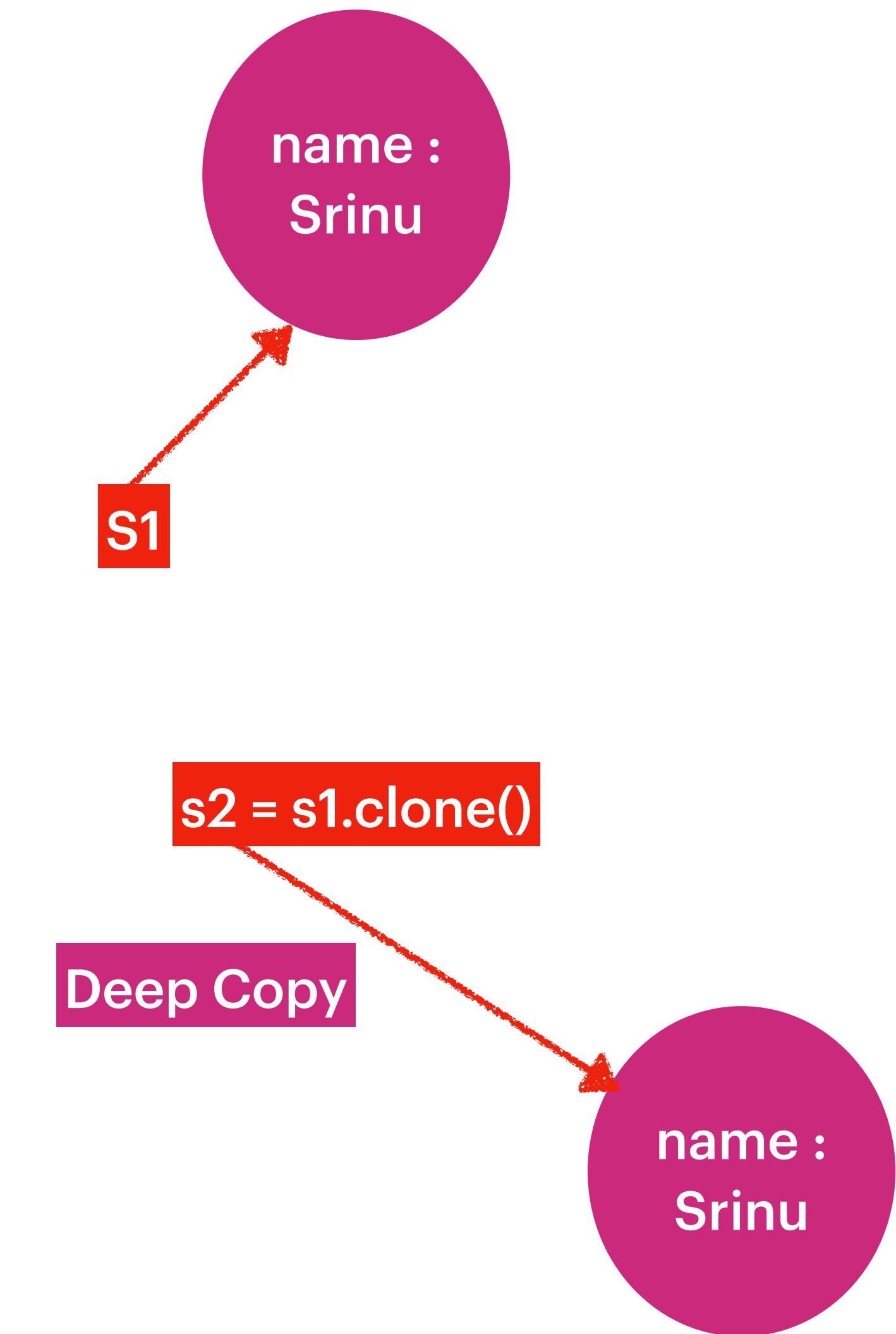
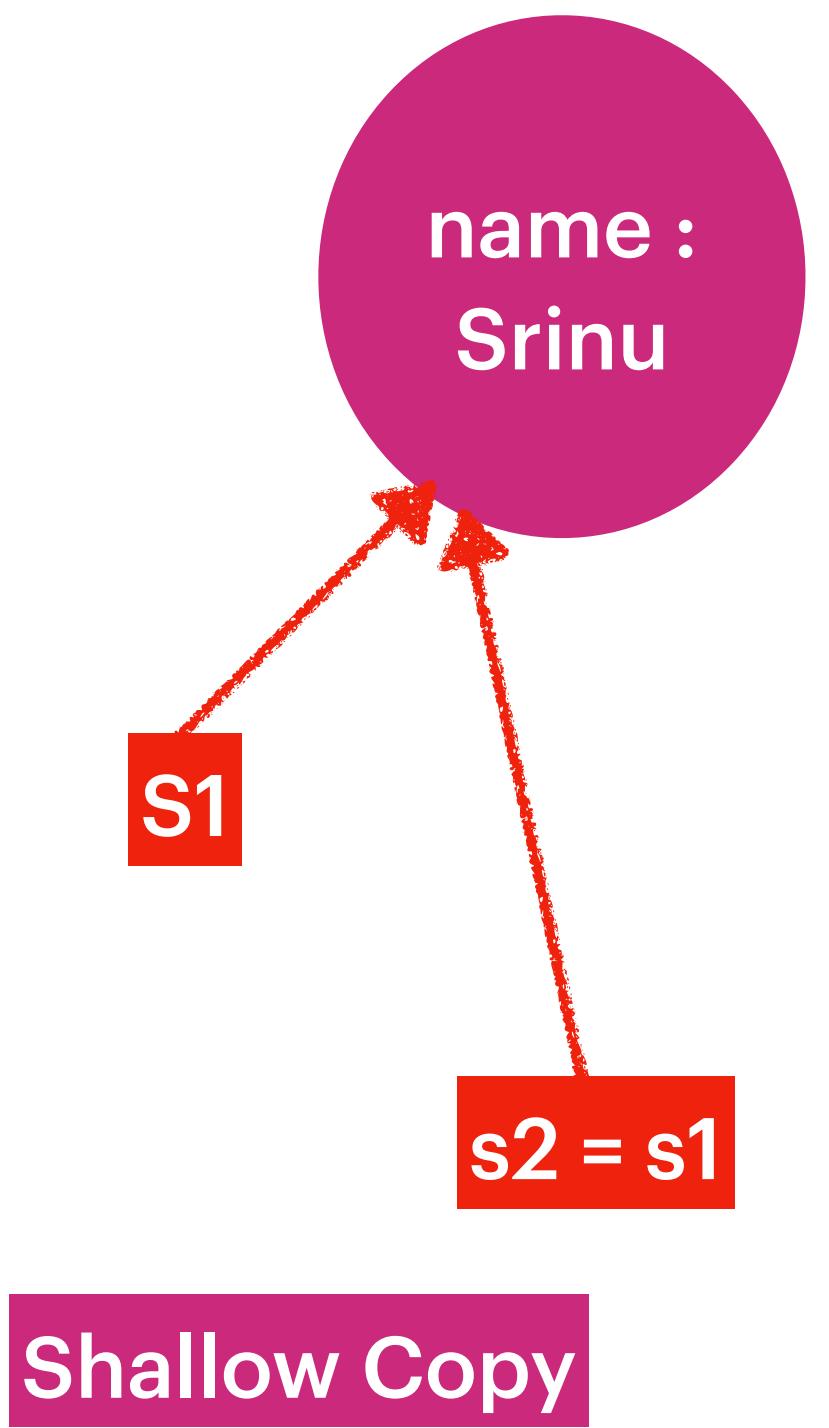
1 <= Node.val <= 100

Node.val is unique for each node.

There are no repeated edges
and no self-loops in the graph.

The Graph is connected and all nodes can
be visited starting from the given node.

```
class cloneGraph {  
    public Node cloneGraph(Node node) {  
        }  
    }
```



Input: adjList = [[2,4],[1,3],[2,4],[1,3]]

Output: [[2,4],[1,3],[2,4],[1,3]]

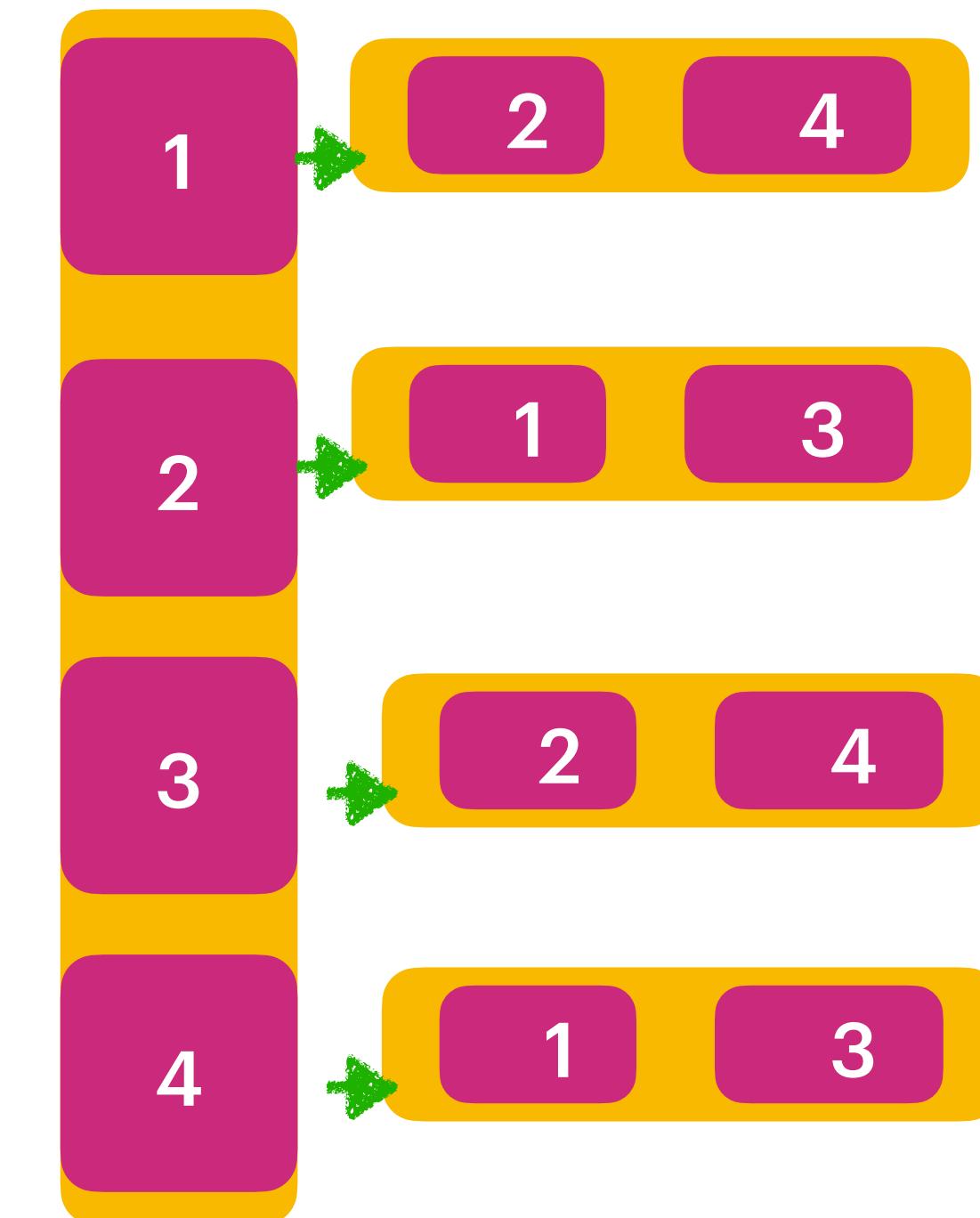
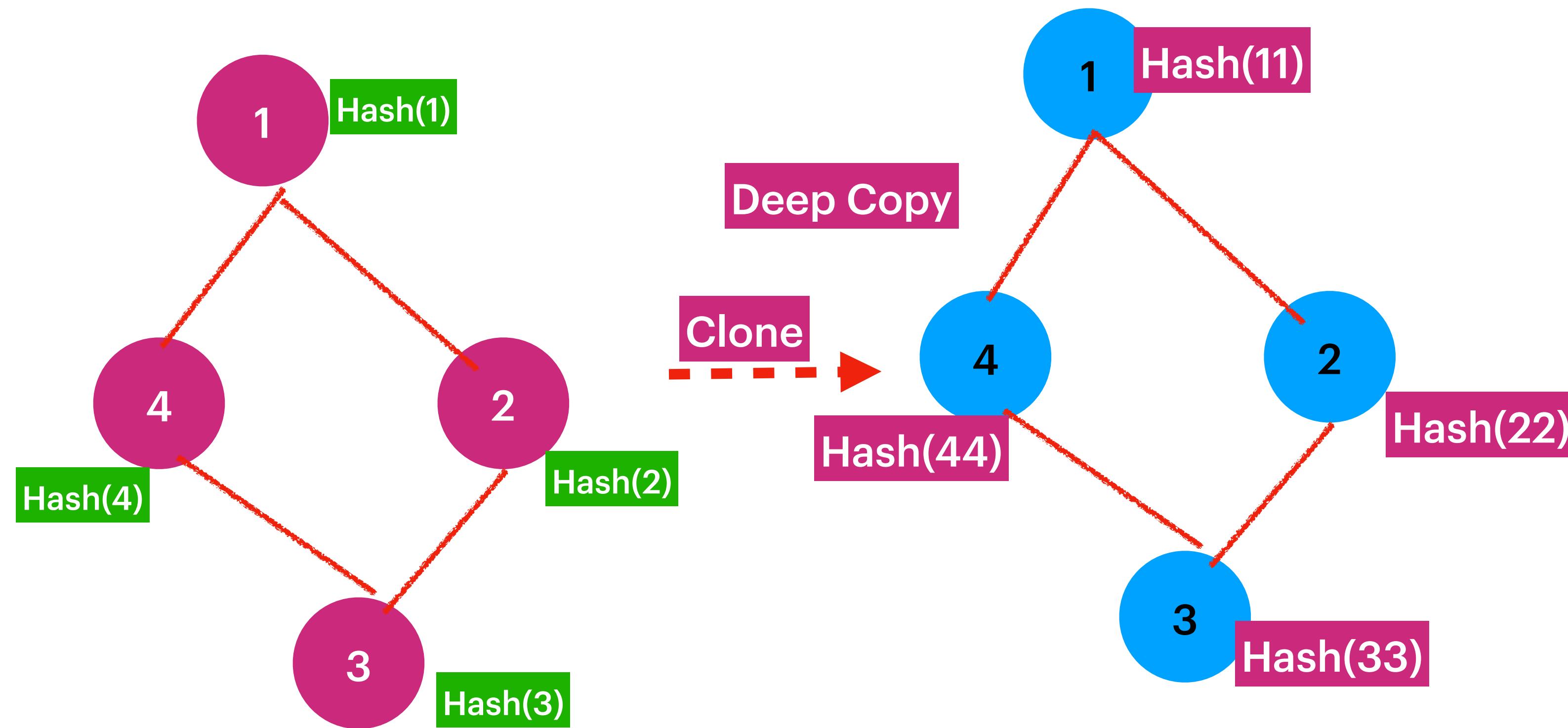
Explanation: There are 4 nodes in the graph.

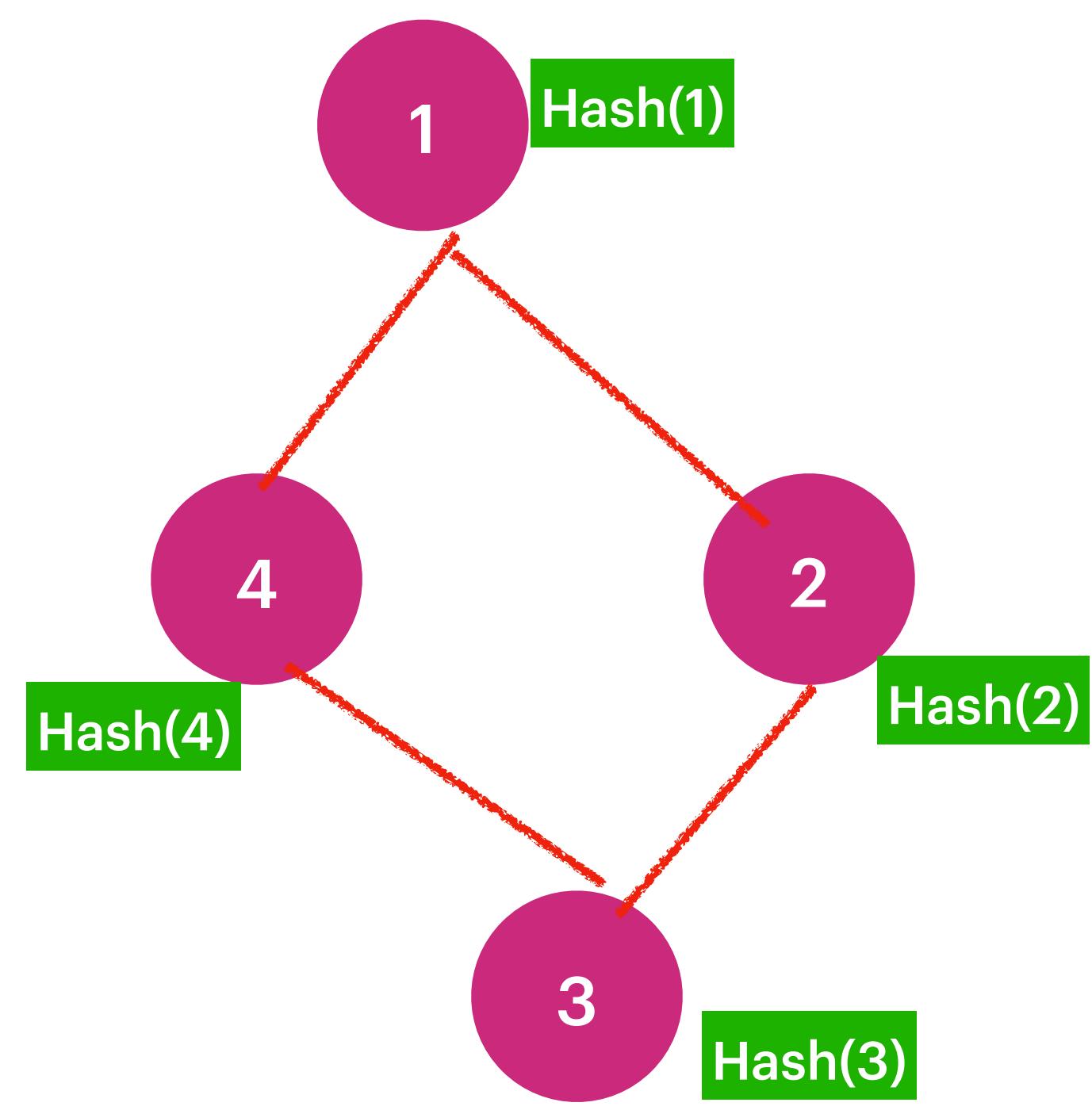
1st node (val = 1)'s neighbors are 2nd node (val = 2) and 4th node (val = 4).

2nd node (val = 2)'s neighbors are 1st node (val = 1) and 3rd node (val = 3).

3rd node (val = 3)'s neighbors are 2nd node (val = 2) and 4th node (val = 4).

4th node (val = 4)'s neighbors are 1st node (val = 1) and 3rd node (val = 3).





```

CloneNode(1)  

4: 2  

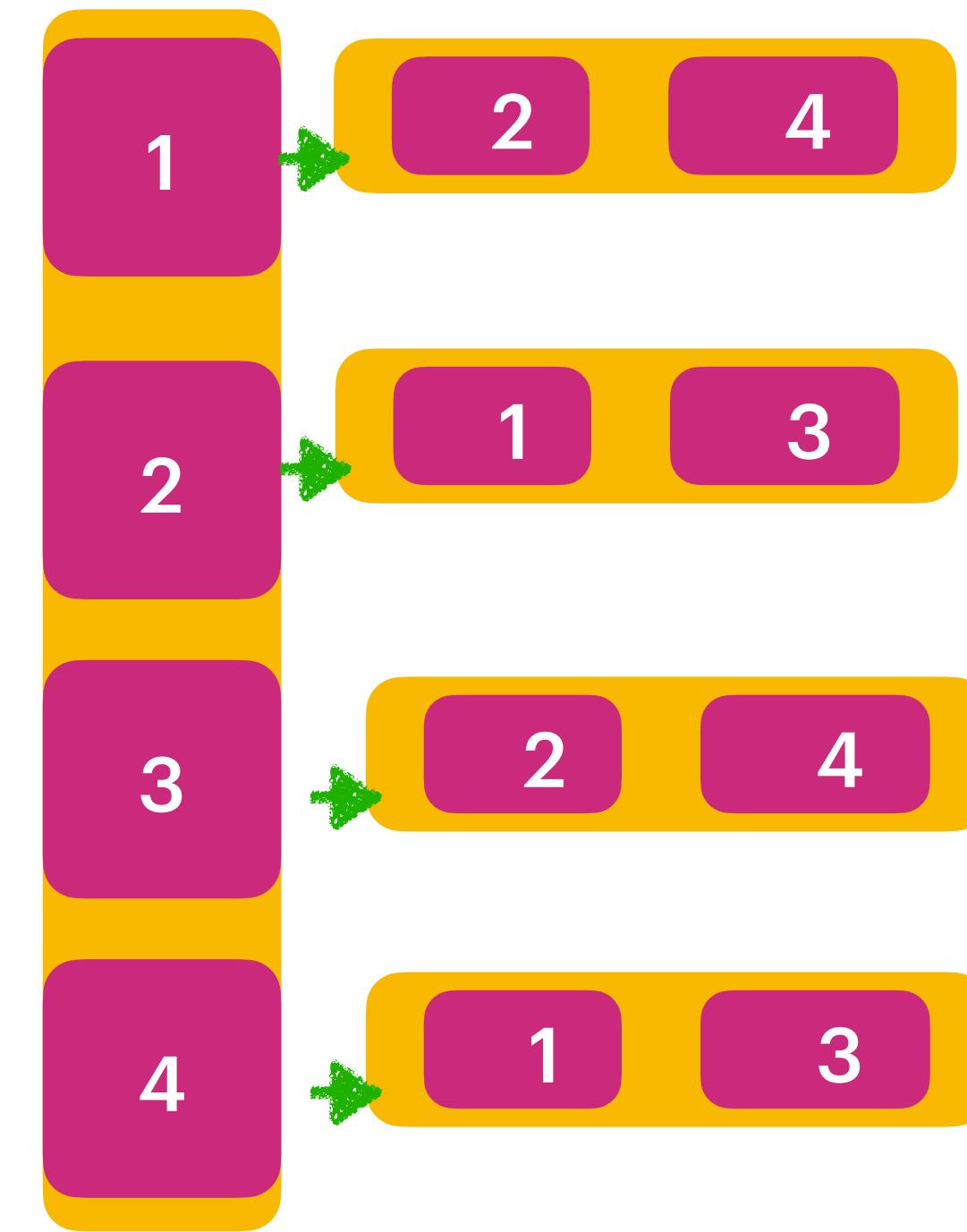
CloneNode(4) :  

1copyRefOfCloneNode(1) :  

3  

CloneNode(2) :

```



Construct N-ary Tree & Level Order Traversal

Given an n-ary tree, return the *level order* traversal of its nodes' values.

Nary-Tree input serialization is represented in their level order traversal, each group of children is separated by the null value (See examples).

Input: root = [1,null,3,2,4,null,5,6]
Output: [[1],[3,2,4],[5,6]]

Input: root = [1,null,2,3,4,5,null,null,6,7,null,8,null,9,10,null,null,11,null,12,null,13,null,null,14]
Output: [[1],[2,3,4,5],[6,7,8,9,10],[11,12,13],[14]]

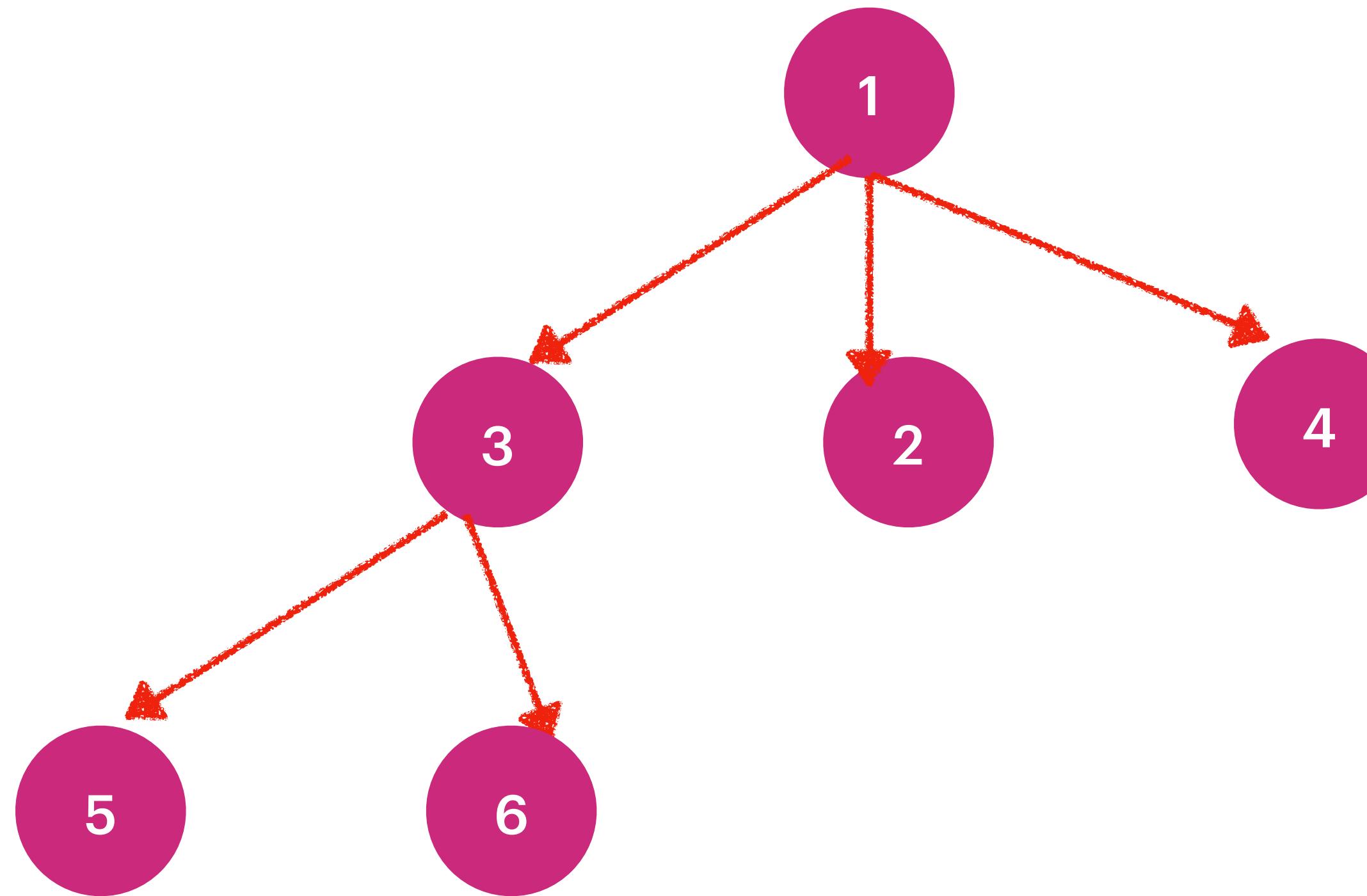
```
class Node {  
    public int val;  
    public List<Node> children;  
}
```

Constraints:
The height of the n-ary tree is less than or equal to 1000
The total number of nodes is between [0, 10⁴]

```
class Solution {  
public List<List<Integer>> levelOrder(Node root) {  
    }  
}
```

Input: root = [1,null,3,2,4,null,5,6]
Output: [[1],[3,2,4],[5,6]]

Construct N-ary Tree & Level Order Traversal



Output: [[1],[3,2,4],[5,6]]

Input: root = [1,null,2,3,4,5,null,null,6,7,null,8,null,9,10,null,null,11,null,12,null,13,null,null,14]

Output: [[1],[2,3,4,5],[6,7,8,9,10],[11,12,13],[14]]

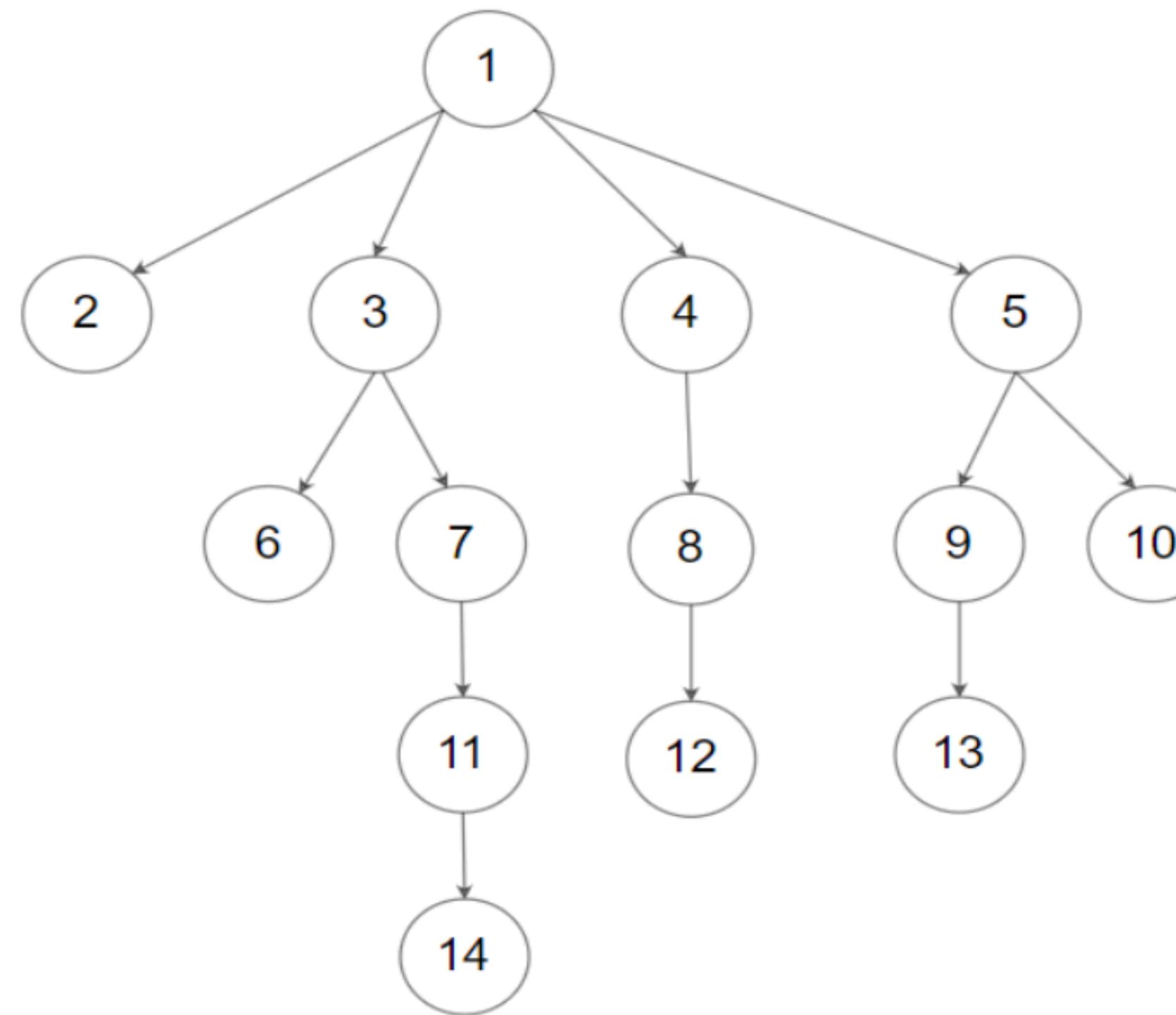
Queue[node[1])
L1 [1]
Queue : [2,3,4,5]

L2[2,3,4,5]
Queue[6,7,8,9,10]

L3[6,7,8,9,10]
Queue[11,12,13]

L4 :[11,12,13]
Queue: [14]

L5[14]
Queue:[]



Construct N-ary Tree & Level Order Traversal

Output: [[1],[2,3,4,5],[6,7,8,9,10],[11,12,13],[14]]

Walls and Gates

You are given an $m \times n$ grid rooms initialized with these three possible values.

-1 A wall or an obstacle.

0 A gate.

INF Infinity means an empty room.

We use the value $2^{31} - 1 = 2147483647$ to represent INF as you may assume that the distance to a gate is less than 2147483647.

Fill each empty room with the distance to its nearest gate.

If it is impossible to reach a gate, it should be filled with INF.

Input: rooms = [

[2147483647,-1,0,2147483647],

[2147483647,2147483647,2147483647,-1],

[2147483647,-1,2147483647,-1],

[0,-1,2147483647,2147483647]

]

Output: [

[3,-1,0,1],

[2,2,1,-1],

[1,-1,2,-1],

[0,-1,3,4]

]

Input: rooms = [[-1]]

Output: [[-1]]

$m == \text{rooms.length}$

$n == \text{rooms}[i].length$

$1 \leq m, n \leq 250$

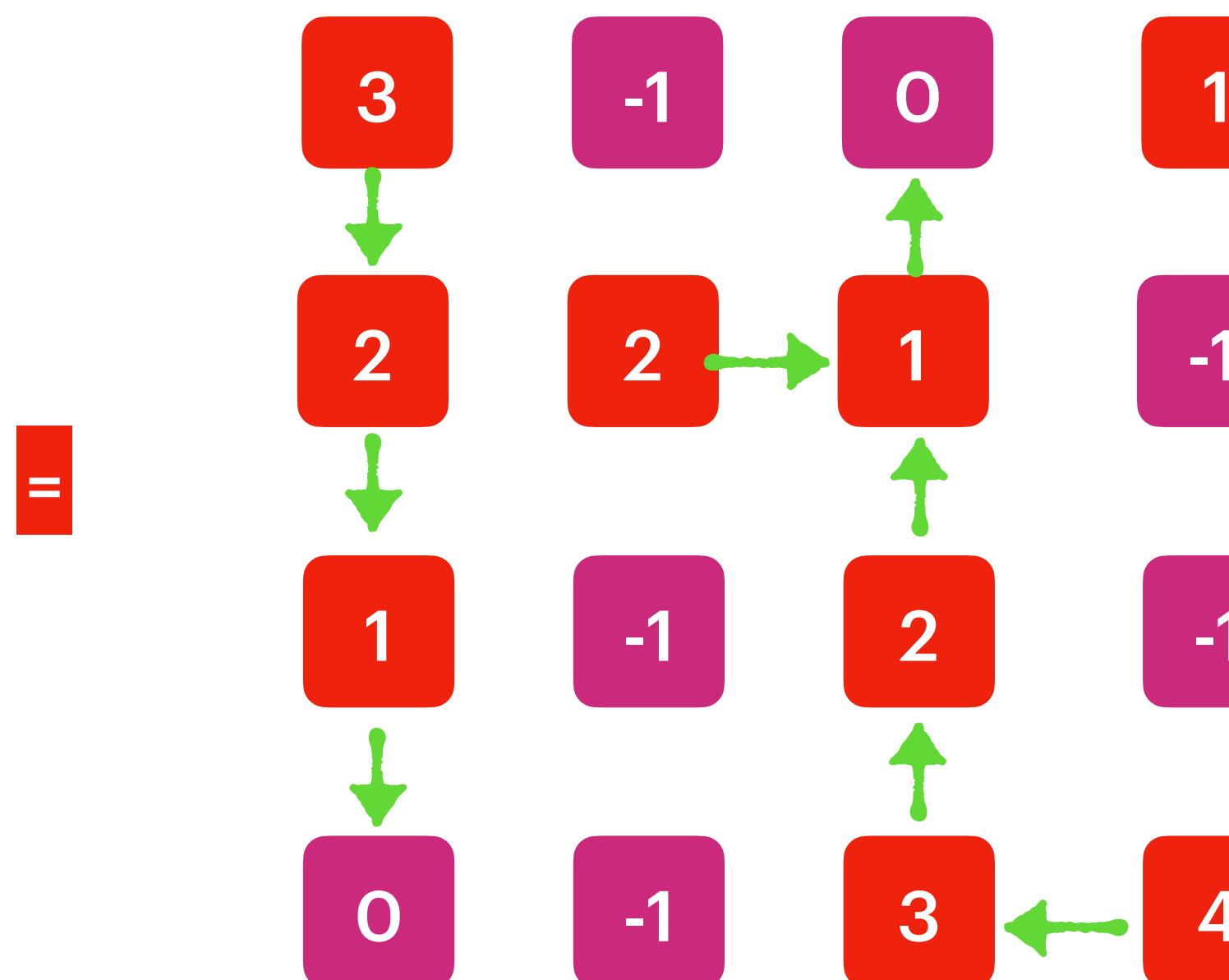
$\text{rooms}[i][j]$ is -1, 0, or $2^{31} - 1$.

```
[  
[E,-1,O,E],  
[E,E,E,-1],  
[E,-1,E,-1],  
[O,-1,E,E]  
]
```

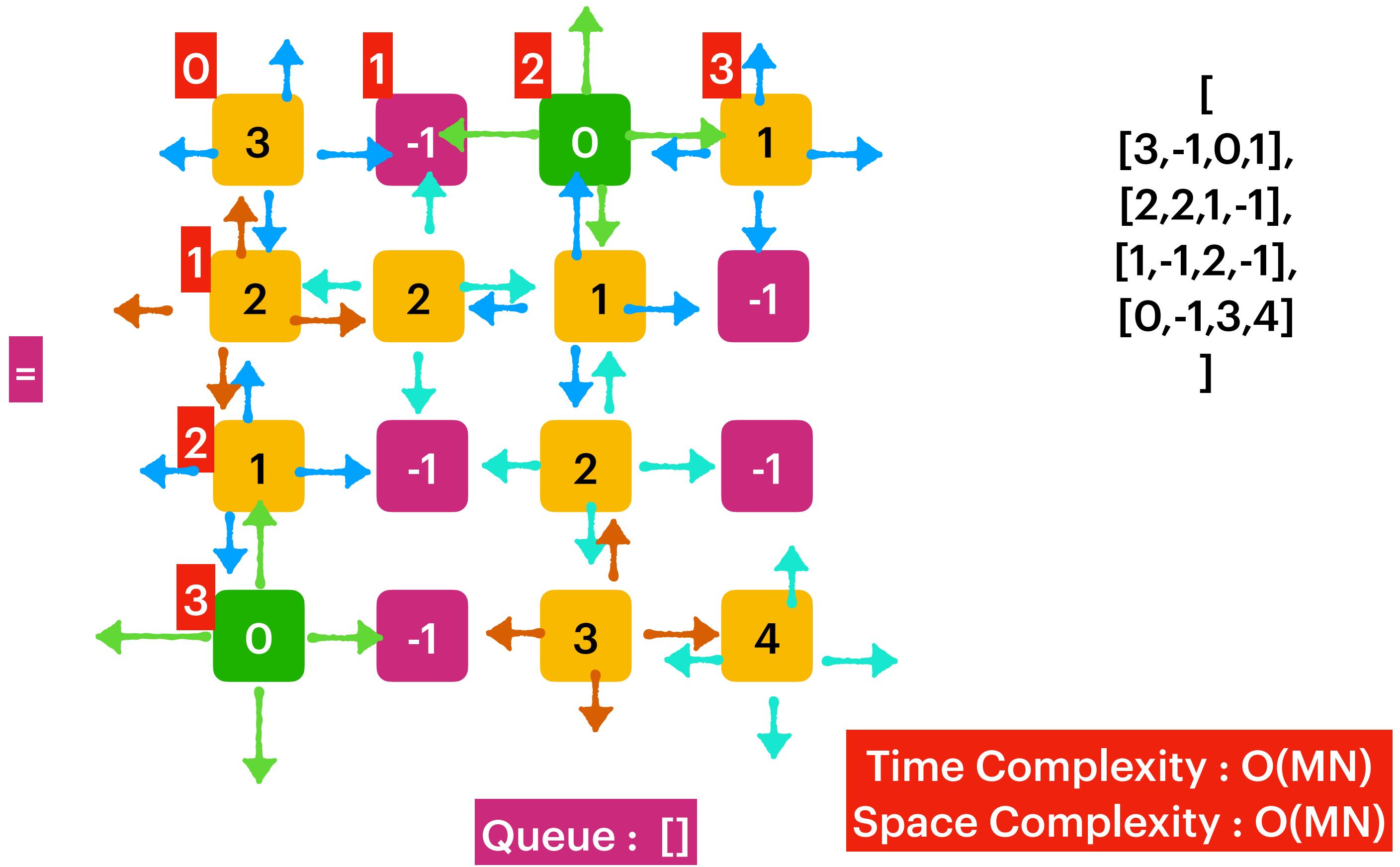
E = Integer.MAX_VALUE = Empty Room
-1 = Wall
0 = Gate

Fill the Empty Room with nearest possible distance

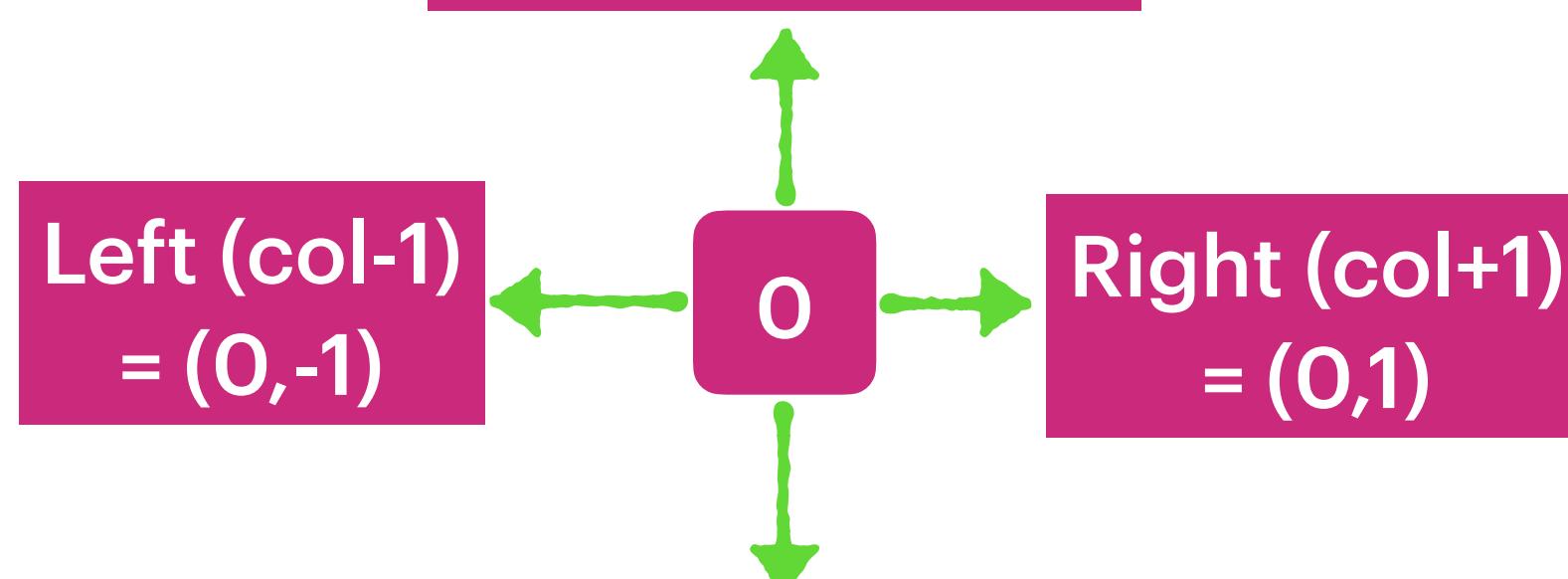
E	-1	0	E
E	E	E	-1
E	-1	E	-1
0	-1	E	E



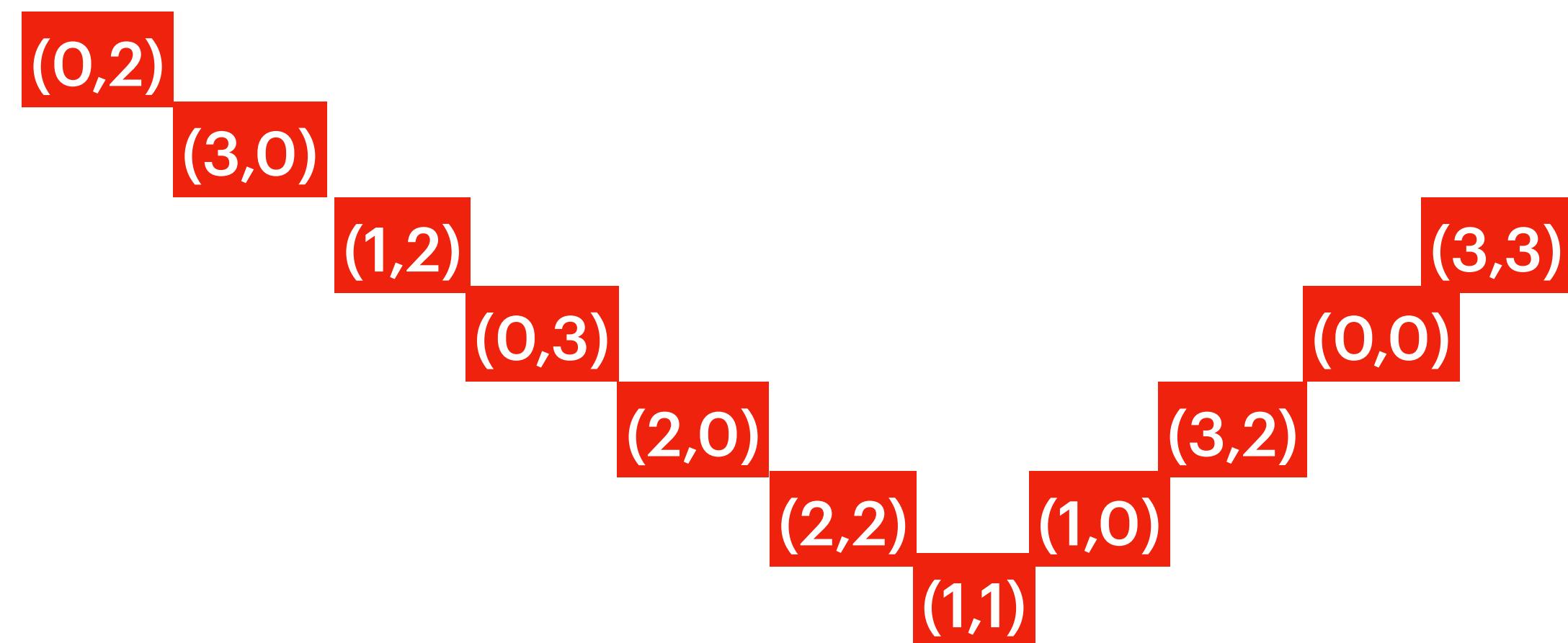
E	-1	0	E
E	E	E	-1
E	-1	E	-1
0	-1	E	E

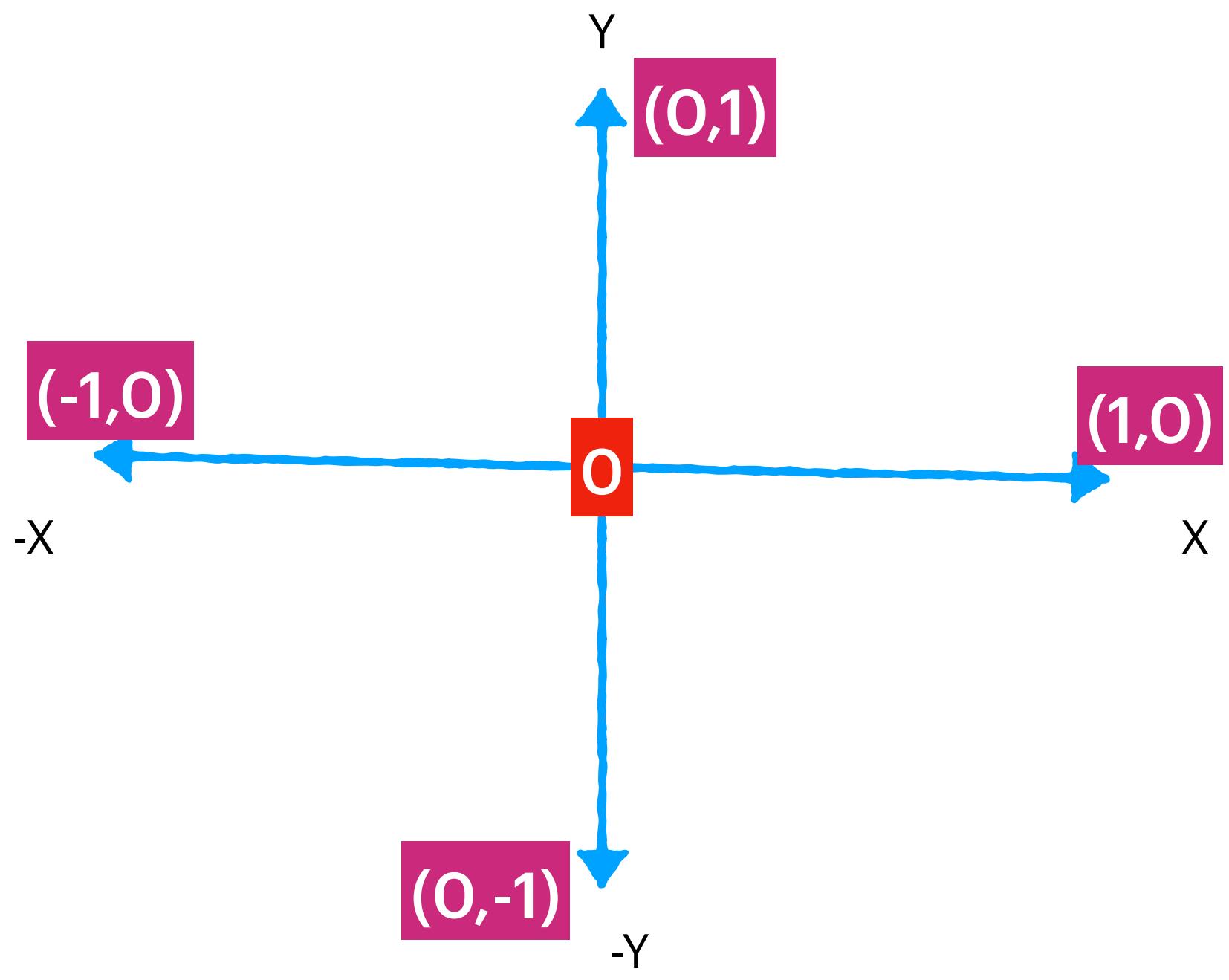


Up (row-1) = (-1,0)



Down (row+1) = (1,0)





01 Matrix

Given an $m \times n$ binary matrix mat , return the distance of the nearest 0 for each cell.
The distance between two adjacent cells is 1.

Input: mat = [
 [0,0,0],
 [0,1,0],
 [0,0,0]
]
Output: [
 [0,0,0],
 [0,1,0],
 [0,0,0]
]

Input: mat = [
 [0,0,0],
 [0,1,0],
 [1,1,1]
]
Output: [
 [0,0,0],
 [0,1,0],
 [1,2,1]
]

Constraints:
 $m == \text{mat.length}$
 $n == \text{mat[i].length}$
 $1 \leq m, n \leq 104$
 $1 \leq m * n \leq 104$
 $\text{mat}[i][j]$ is either 0 or 1.
There is at least one 0 in mat.

0	0	0
0	1	0
0	0	0

0	0	0
0	1	0
0	0	0

=

Input: mat = [
[0,0,0],
[0,1,0],
[0,0,0]
]
Output: [
[0,0,0],
[0,1,0],
[0,0,0]
]

0	0	0
0	1	0
1	1	1

Input: mat = [
[0,0,0],
[0,1,0],
[1,1,1]
]
Output: [
[0,0,0],
[0,1,0],
[0,0,0]
]

1 1 1

1 1 1

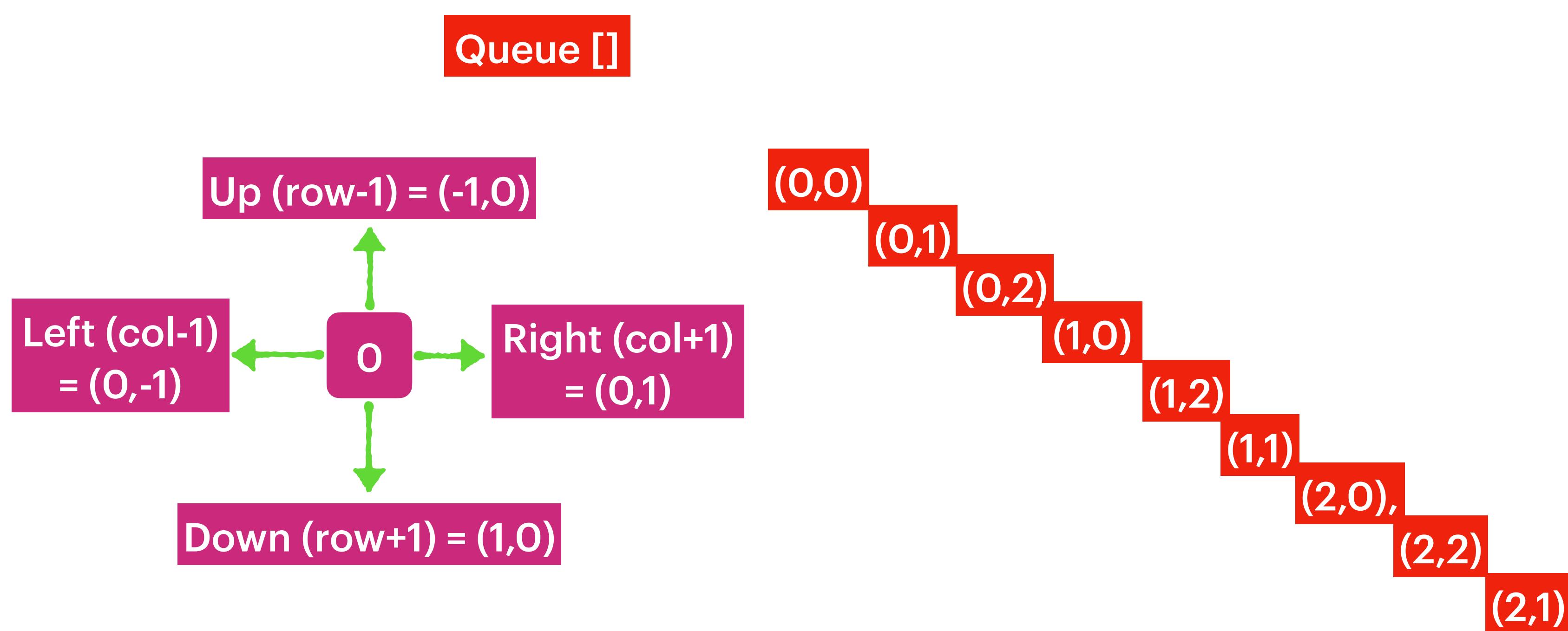
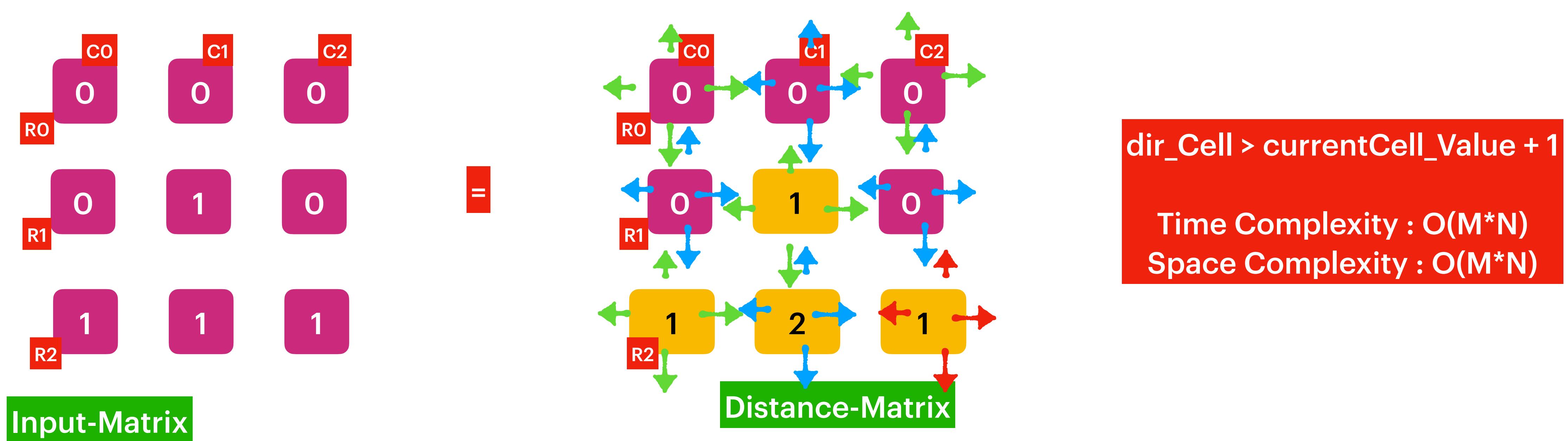
1 0 1

3 2 3

2 1 2

1 0 1

=



01 Matrix :: Level Order

Given an $m \times n$ binary matrix mat , return the distance of the nearest 0 for each cell.
The distance between two adjacent cells is 1.

Input: $\text{mat} = [$
 $[0,0,0],$
 $[0,1,0],$
 $[0,0,0]$
 $]$

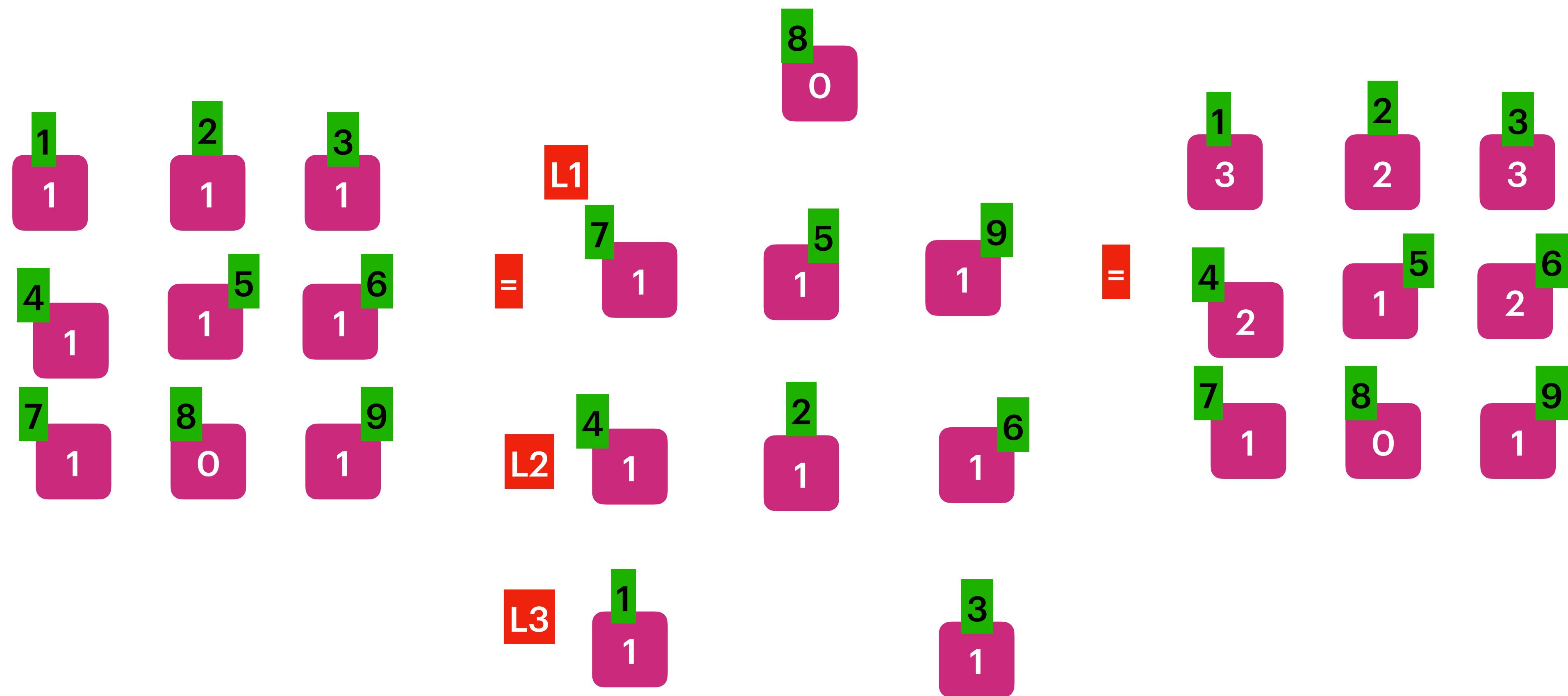
Output: [
 $[0,0,0],$
 $[0,1,0],$
 $[0,0,0]$
 $]$

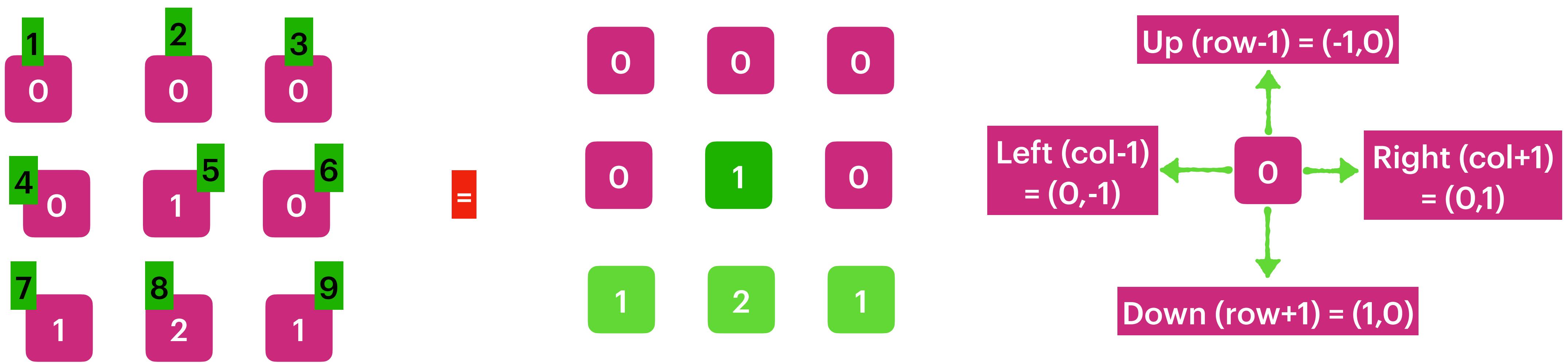
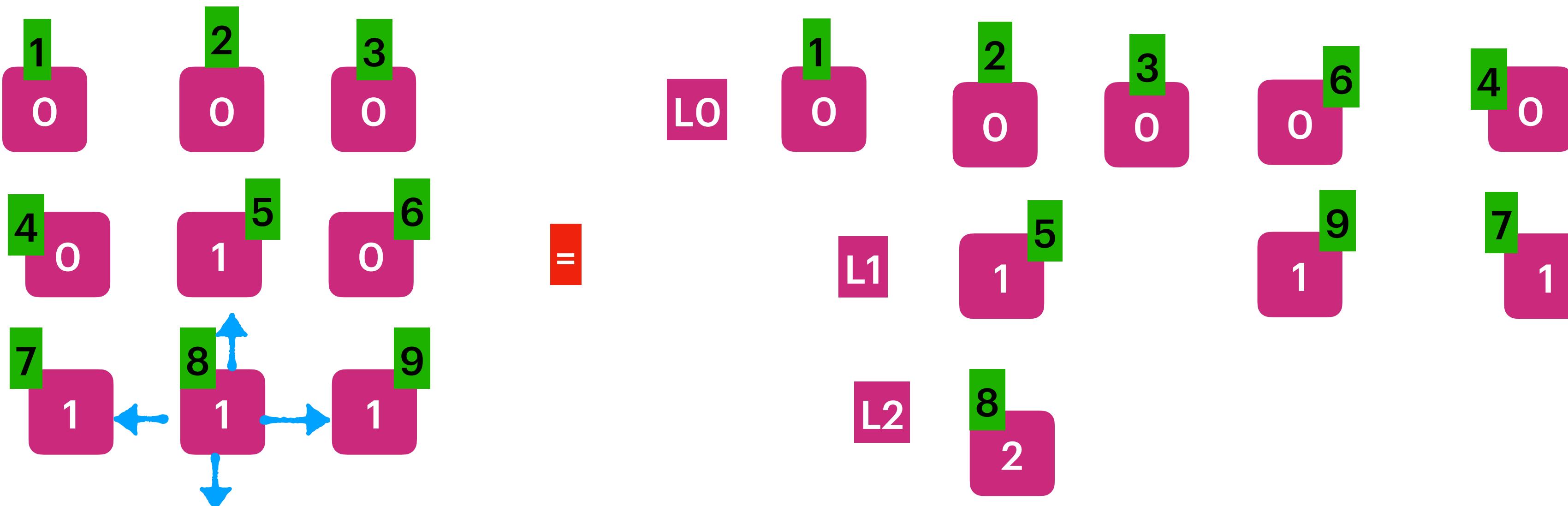
Input: $\text{mat} = [$
 $[0,0,0],$
 $[0,1,0],$
 $[1,1,1]$
 $]$

Output: [
 $[0,0,0],$
 $[0,1,0],$
 $[1,2,1]$
 $]$

Constraints:

- $m == \text{mat.length}$
- $n == \text{mat}[i].length$
- $1 \leq m, n \leq 104$
- $1 \leq m * n \leq 104$
- $\text{mat}[i][j]$ is either 0 or 1.
- There is at least one 0 in mat .





Rotting Oranges

You are given an $m \times n$ grid where each cell can have one of three values:

- 0 representing an empty cell,
- 1 representing a fresh orange, or
- 2 representing a rotten orange.

Every minute, any fresh orange that is 4-directionally adjacent to a rotten orange becomes rotten.

Return the minimum number of minutes that must elapse until no cell has a fresh orange.
If this is impossible, return -1.

Input: grid = [[2,1,1],[1,1,0],[0,1,1]]
Output: 4

Input: grid = [[2,1,1],[0,1,1],[1,0,1]]
Output: -1

Explanation: The orange in the bottom left corner
(row 2, column 0) is never rotten,
because rotting only happens 4-directionally.

Input: grid = [[1]]
Output: -1

Explanation: Since the orange can never rotate.

Input: grid = [[0,0,0,0,0]]
Output: 0

Explanation: Since there are no oranges to rotate.

Input: grid = [[0]]
Output: 0

Explanation: Since there are already
no fresh oranges at minute 0,
the answer is just 0.

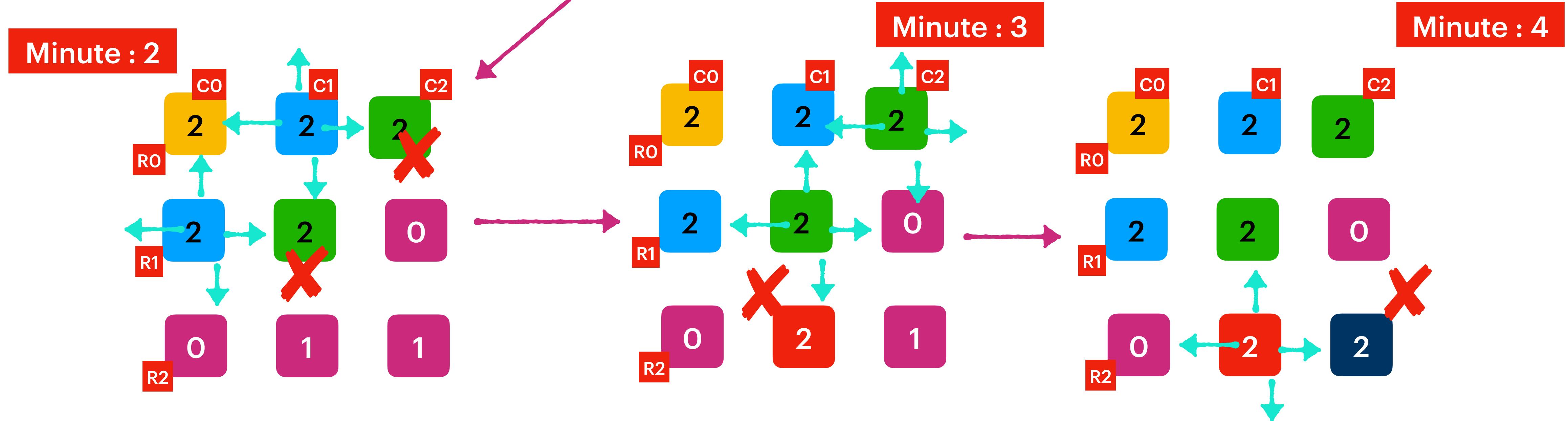
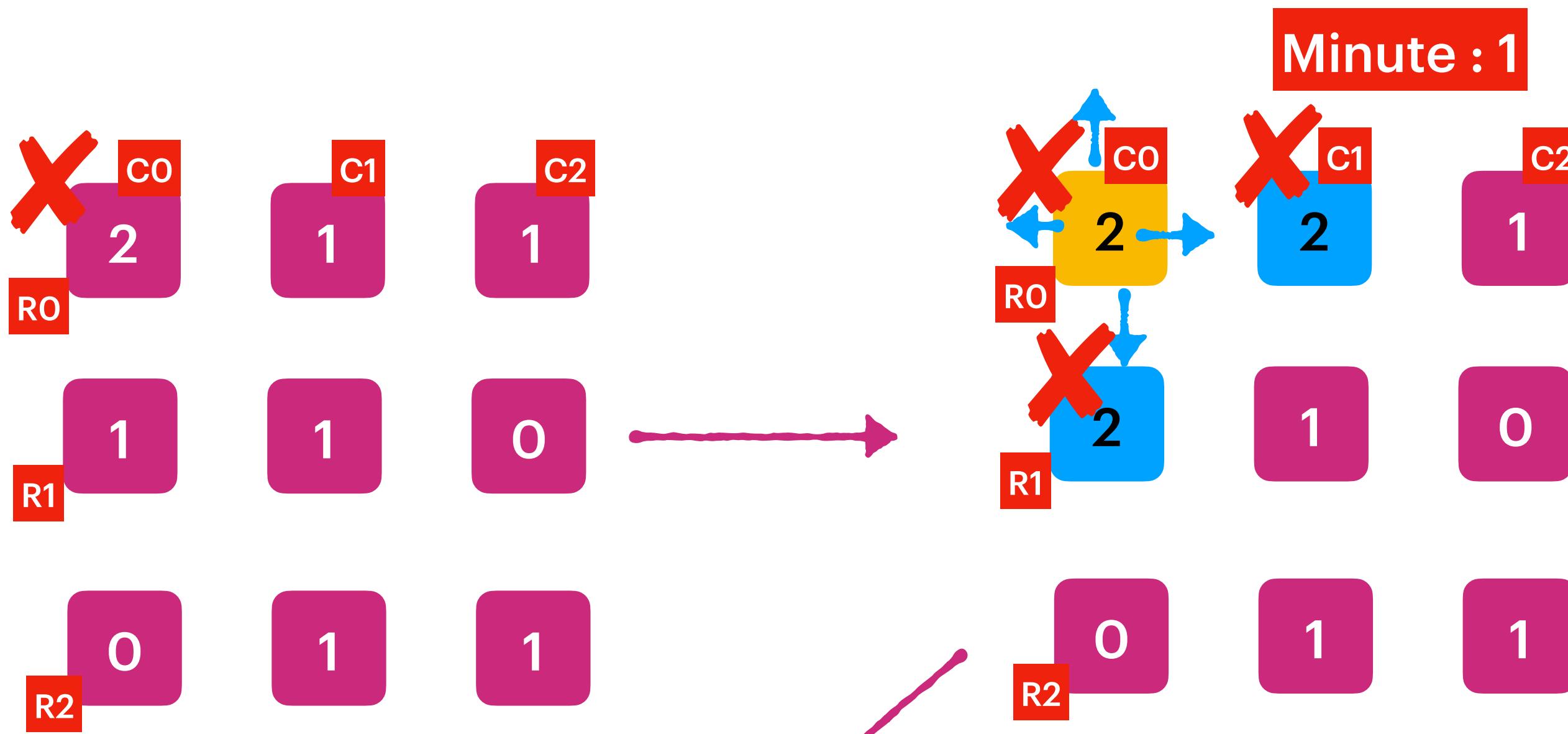
Constraints:

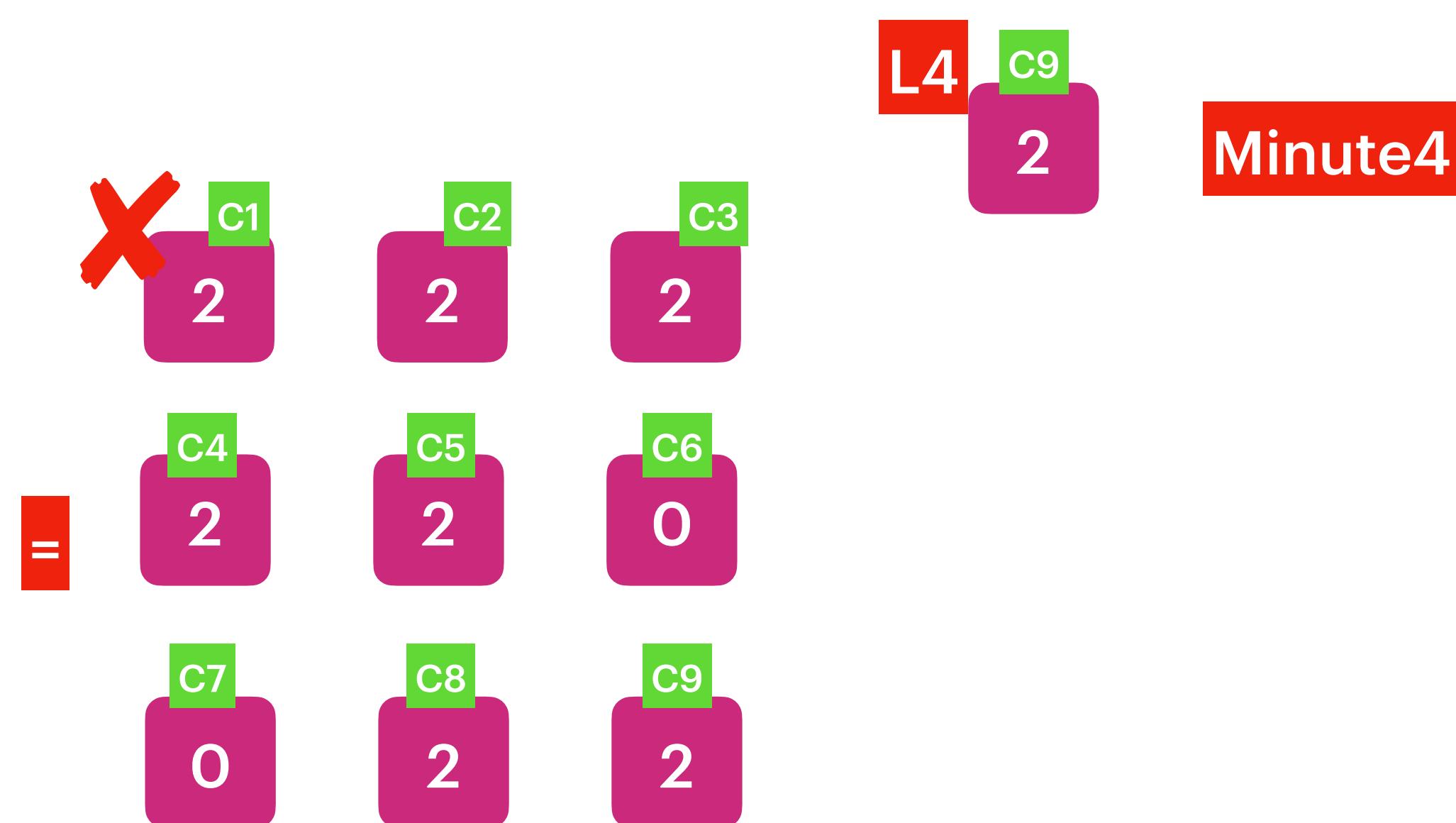
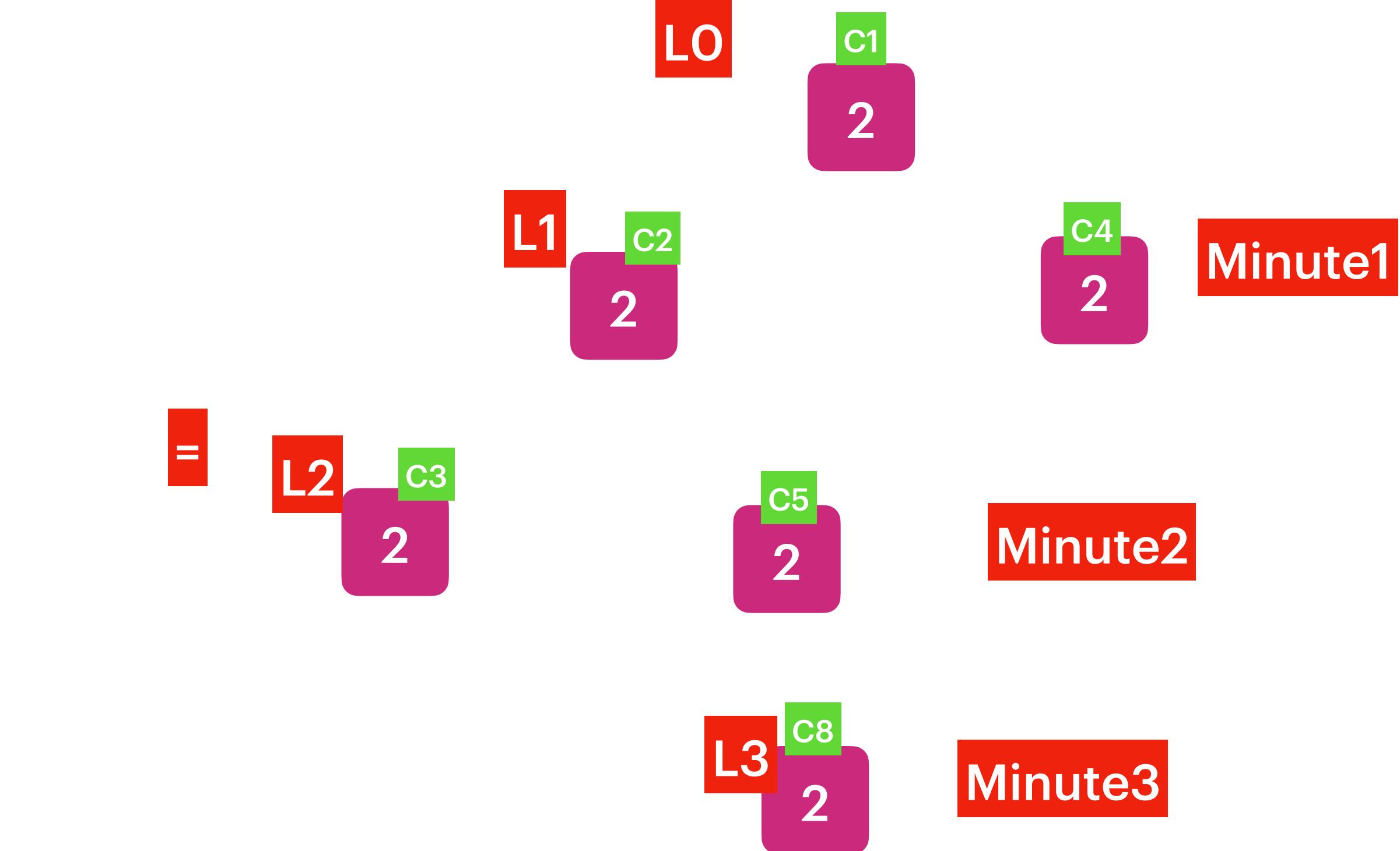
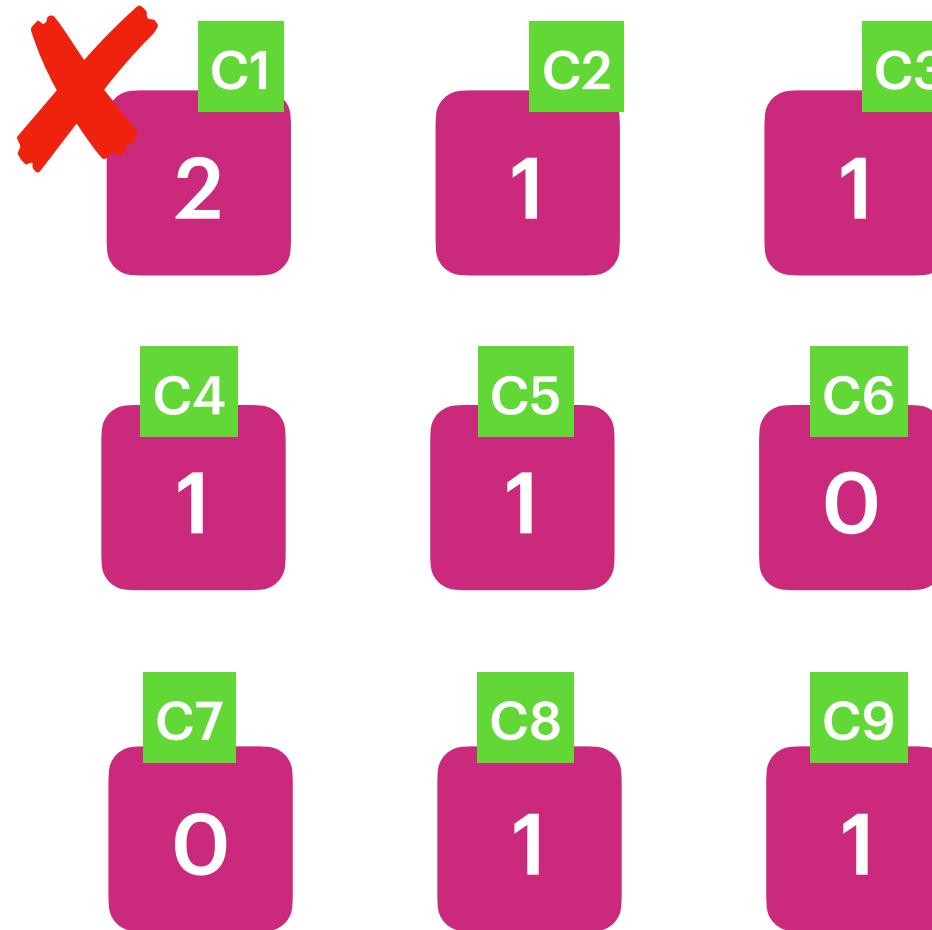
$m == \text{grid.length}$
 $n == \text{grid[i].length}$
 $1 \leq m, n \leq 10$
 grid[i][j] is 0, 1, or 2.

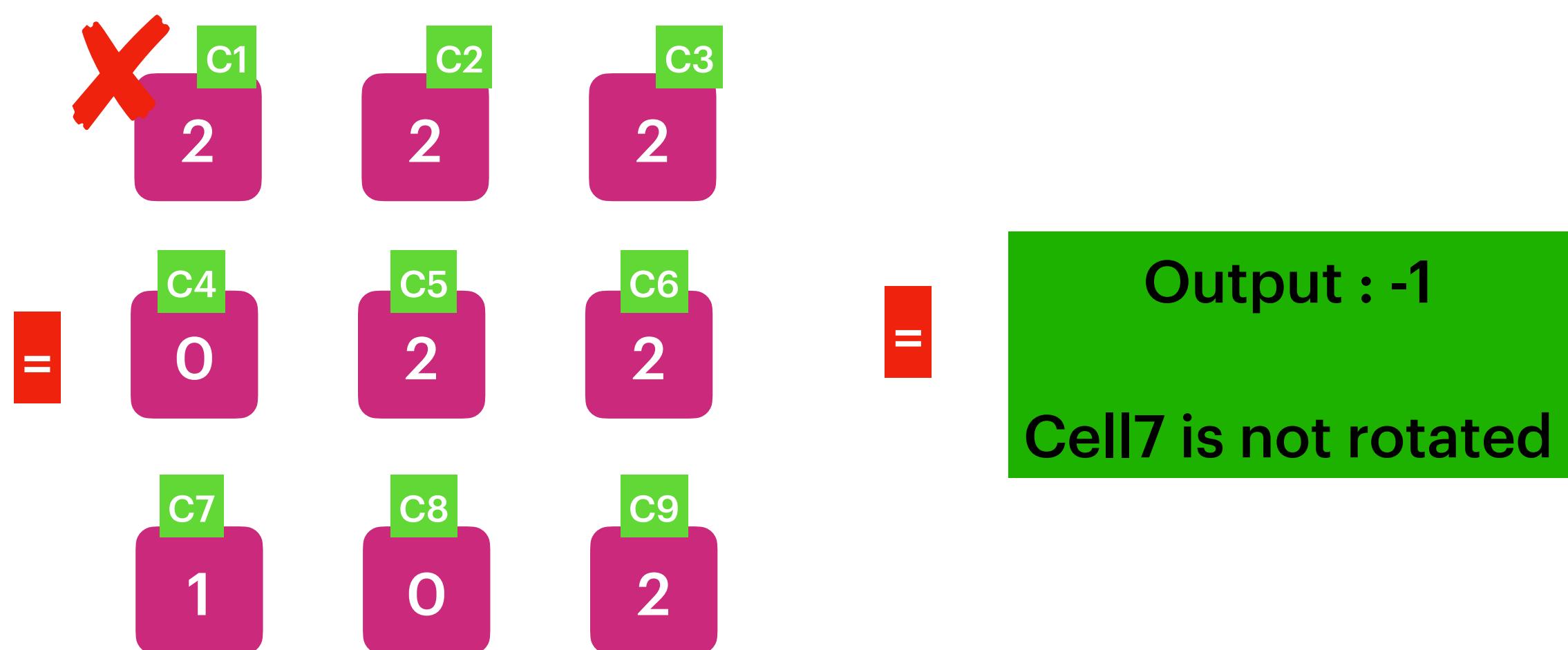
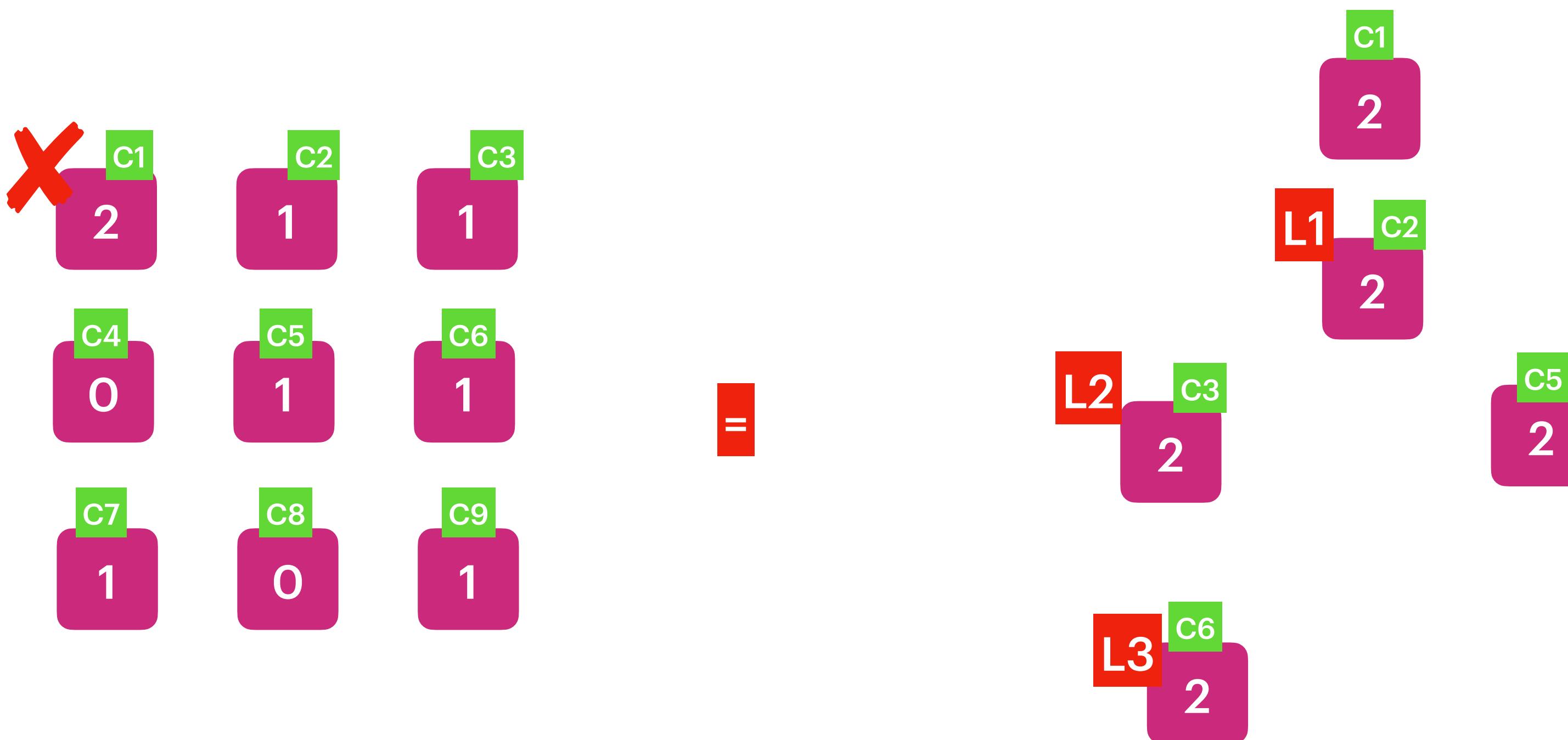
Input: grid = [[0,2]]
Output: 0

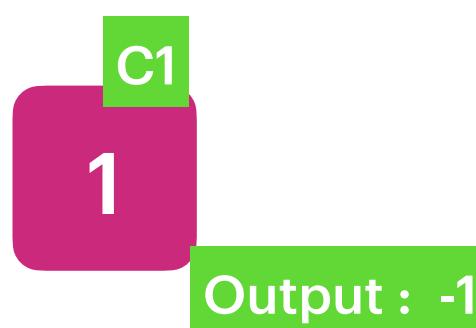
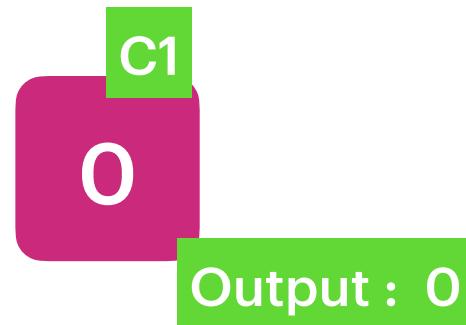
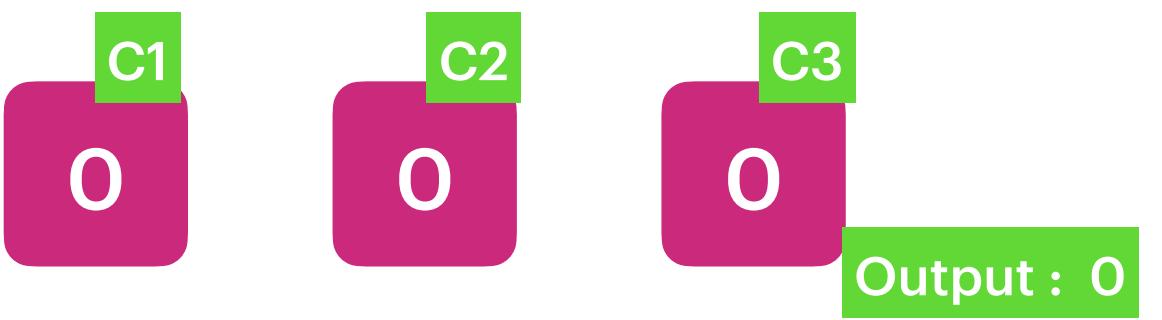
Explanation: Since there are already
no fresh oranges at minute 0,
the answer is just 0.

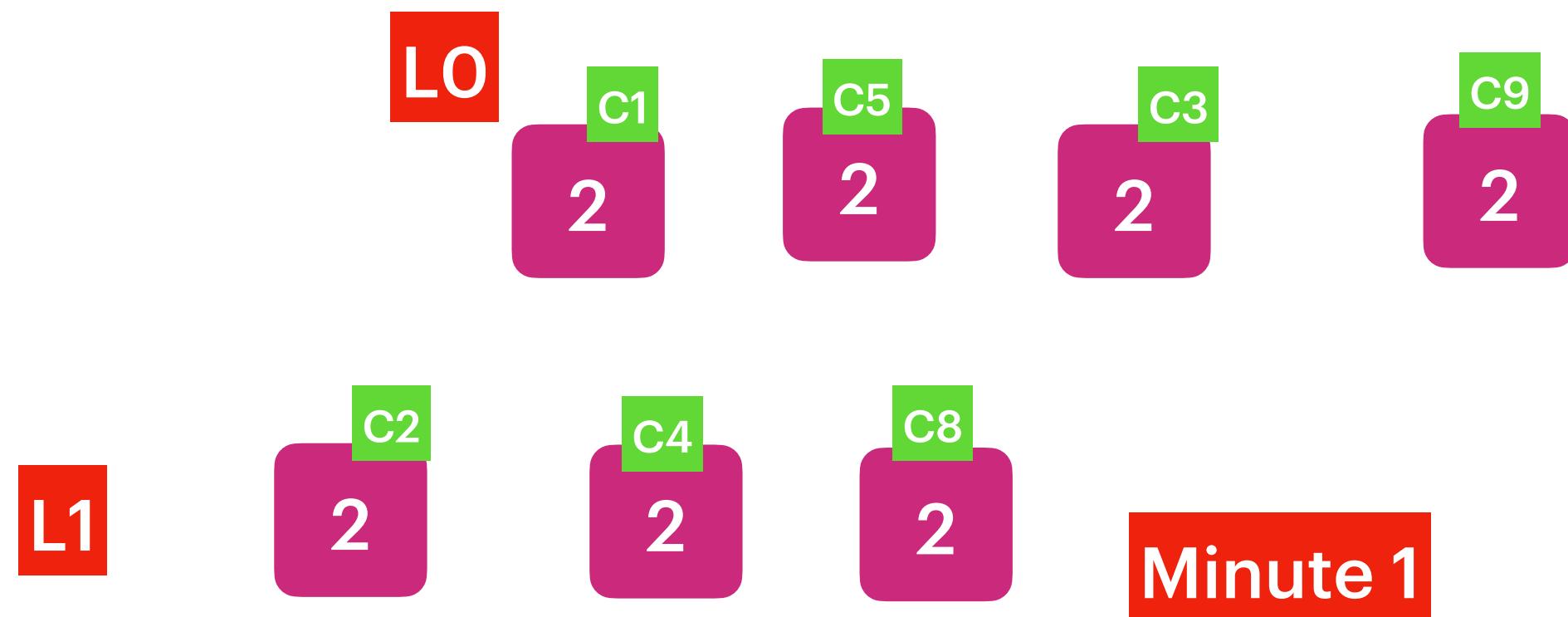
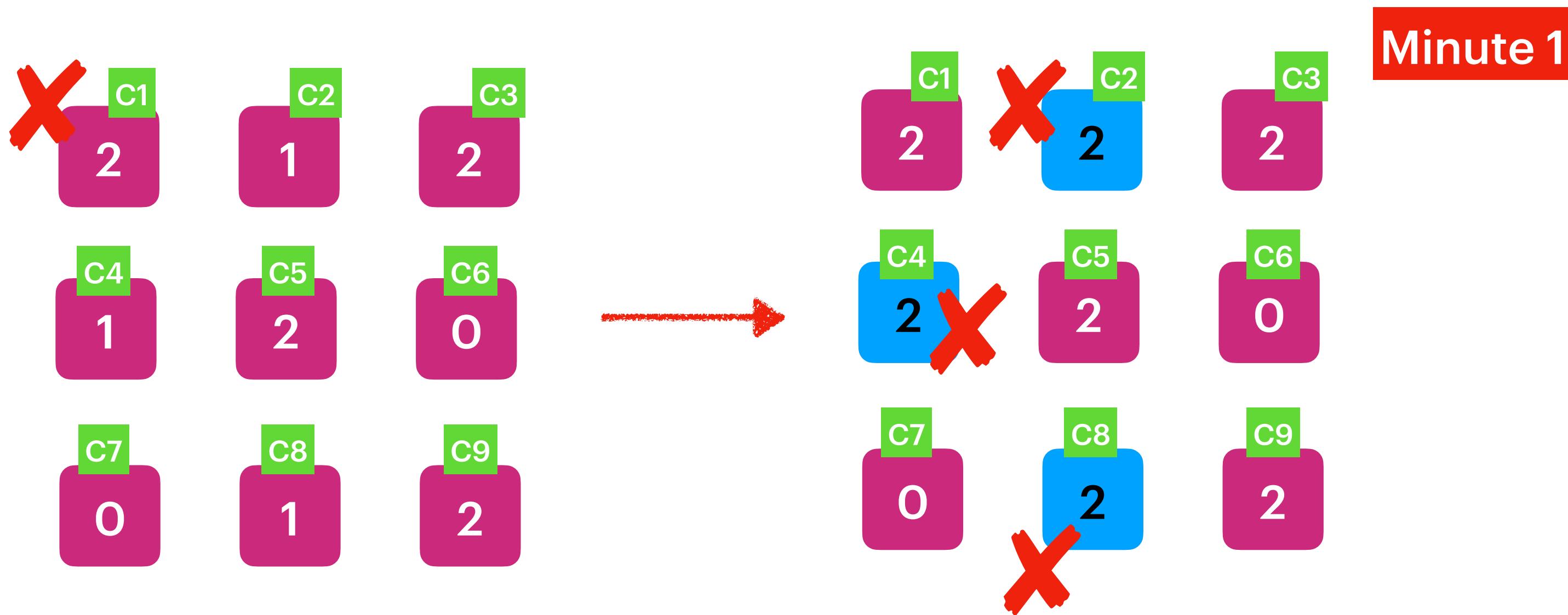
```
[  
[2,1,1],  
[1,1,0],  
[0,1,1]  
]
```











Number of Islands

Given an $m \times n$ 2D binary grid grid which represents a map of '1's (land) and '0's (water), return the number of islands.

An island is surrounded by water and is formed by connecting adjacent lands horizontally or vertically.

You may assume all four edges of the grid are all surrounded by water.

Input: grid =
["1","1","1","1","0"],
["1","1","0","1","0"],
["1","1","0","0","0"],
["0","0","0","0","0"]
]
Output: 1

Input: grid =
["1","1","0","0","0"],
["1","1","0","0","0"],
["0","0","1","0","0"],
["0","0","0","1","1"]
Output: 3

$m == \text{grid.length}$
 $n == \text{grid[i].length}$
 $1 \leq m, n \leq 300$
 $\text{grid}[i][j]$ is '0' or '1'!

0	0	0	0	0	0
---	---	---	---	---	---

0	0	0	0	0	0
---	---	---	---	---	---

0	0	0	0	0	0
---	---	---	---	---	---

islandsCount : 0

0	0	0	0	0	0
---	---	---	---	---	---

0	0	0	1	0	0
---	---	---	---	---	---

islandsCount : 1

0	0	0	0	0	0
---	---	---	---	---	---

0	0	1	0	0	0
---	---	---	---	---	---

0	0	0	1	0	0
---	---	---	---	---	---

islandsCount : 3

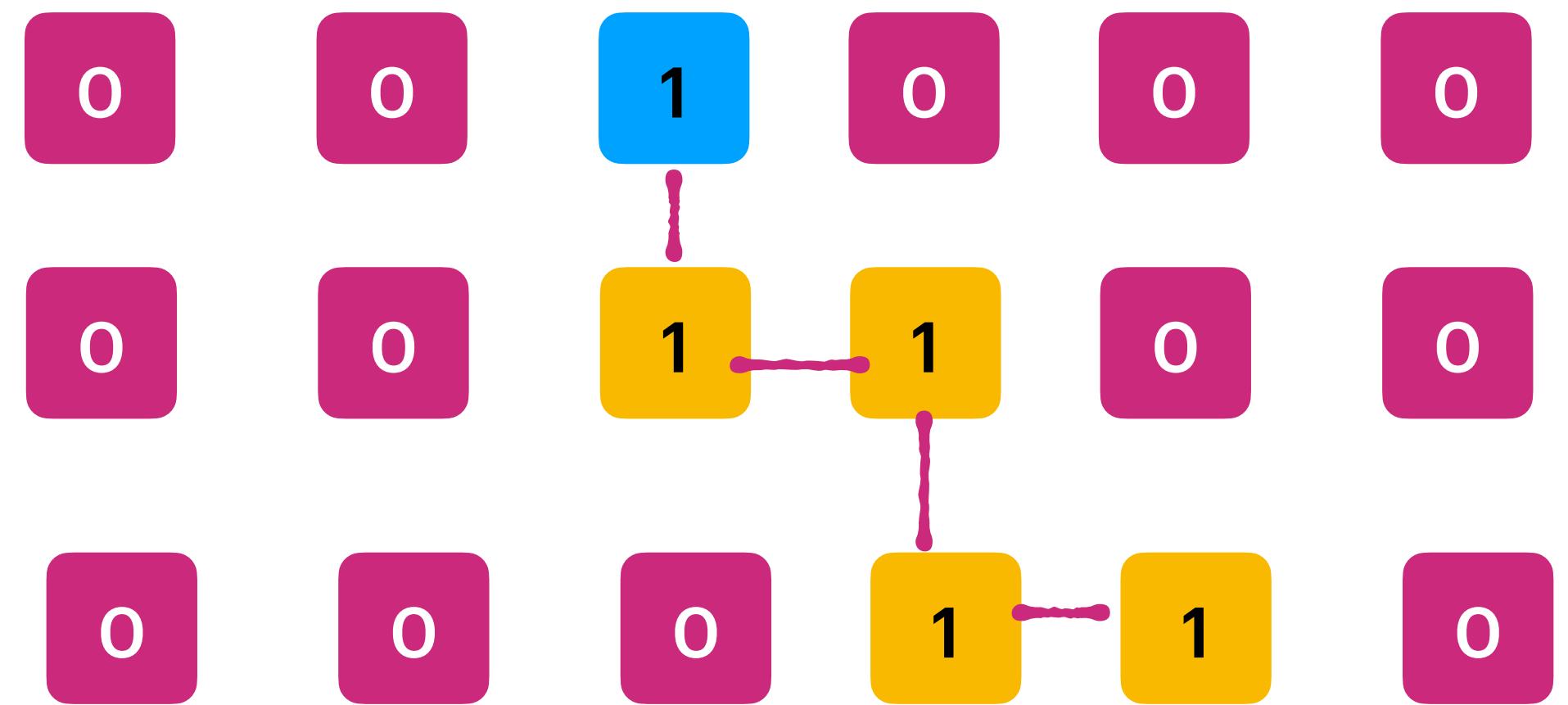
0	0	0	0	1	0
---	---	---	---	---	---

0	0	1	0	0	0
---	---	---	---	---	---

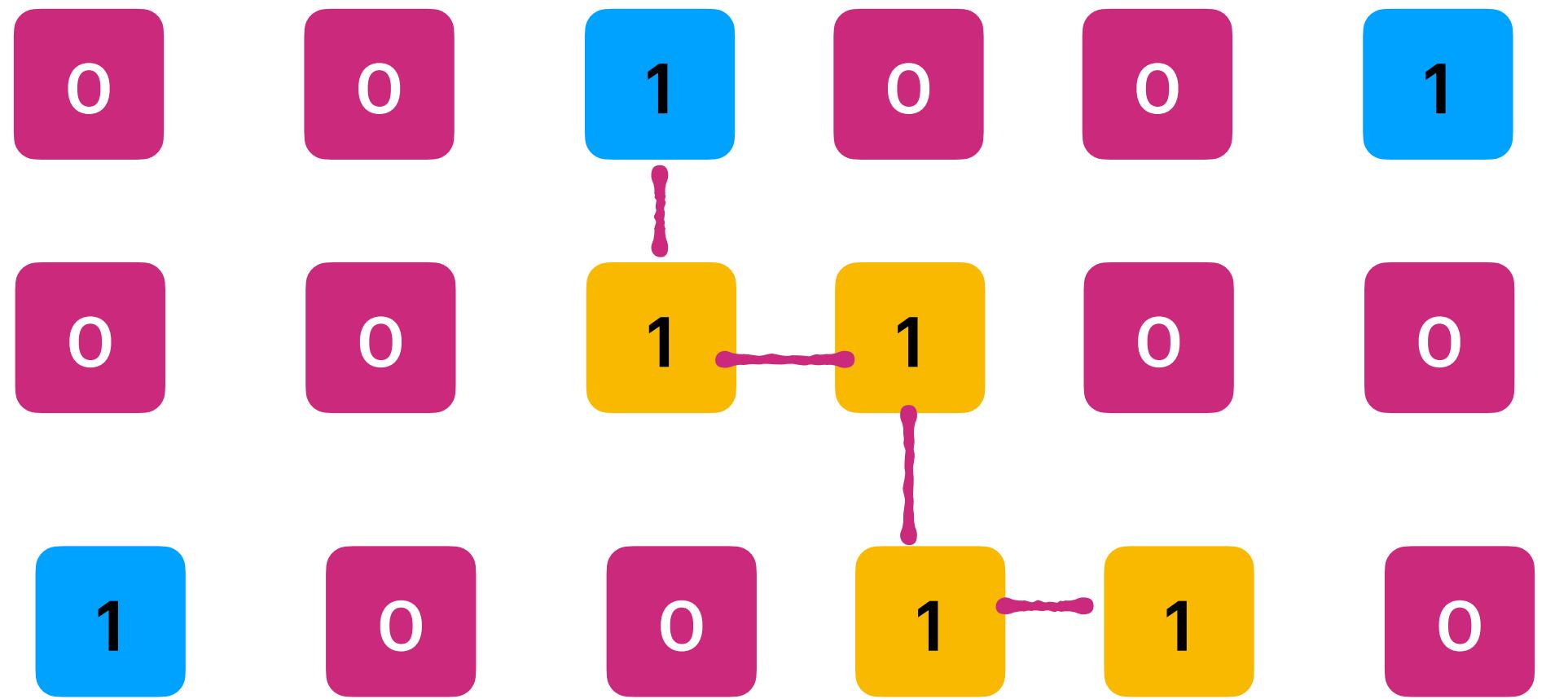
0	0	1	0	0	0
---	---	---	---	---	---

islandsCount : 2

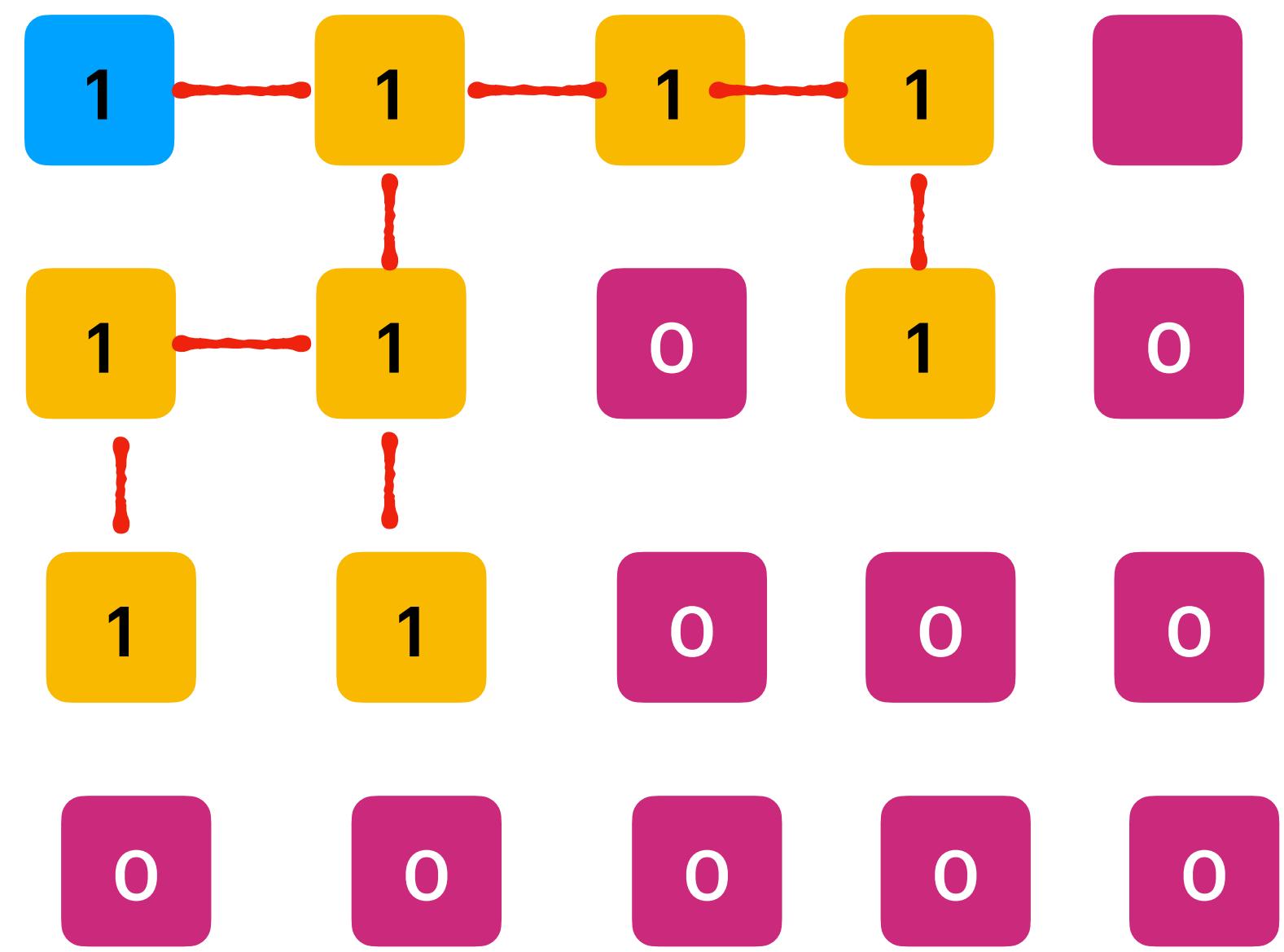
0	0	0	0	1	0
---	---	---	---	---	---



islandsCount : 1



islandsCount : 3



islandsCount : 1

0	0	1	0	0	0
0	0	1	1	0	0
0	0	0	0	1	0

Total Islands : 2

```

for ( r : Row )
{
    for(r : Col)
    {
        if(cell[r][c] == 1)
            bfs[r,c];
        islandCount+
    }
}

```

0	0	1	0	0	0
0	0	0	0	0	0
0	0	0	0	1	0

Step1

BFS/
DFS

0	0	0	0	0	0
0	0	0	0	0	0
0	0	0	0	1	0

islandCount = 1

0	0	1	0	0	0
0	0	0	0	0	0
0	0	0	0	1	0

Step2

islandCount = 2