Homework 2: EECE 5639 - Computer Vision

Sreejith Sreekumar: 001277209

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1 Question 1

1.1 Code

```
function gray_img = grayscale_generator(w,h)
    gray_img = im2double(128 * ones(w,'uint8'));
end
function sigma = estimate_noise(ImageArray, width, height, count)
    % calculation of E(i,j)
    E = double(zeros(height, width));
    %E = im2double(E)
    for k = 1:count
        for i = 1:width
            for j = 1:height
                E(i,j) = E(i,j) + double(ImageArray(k).Image(i,j));
        end
    \quad \text{end} \quad
    E = 1/count * E;
    % calculation of standard deviation of E(i,j) \\
    sum_sq_diff = 0
    for k = 1:count
        for i = 1:width
            for j = 1:height
                sum_sq_diff = sum_sq_diff + (E(i,j) - double(ImageArray(k).Image(i,j)))^2;
            end
        end
    end
    sigma = sqrt(((1/(count -1)) * sum_sq_diff))
```

```
end
count = 10;
width = 256;
height = 256;
% 10 grayscale images and store in a stucture
ImgArray(1:count) = struct('Image', [], 'Label', '');
for j = 1:count
  ImgArray(j).Image = grayscale_generator(width, height);
  ImgArray(j).Label = j;
end
% add additive zero-mean Gaussian noise to all those images
variance = (2*2)/(255*255)
for j = 1:count
    ImgArray(j).Image = imnoise(ImgArray(j).Image, 'gaussian', 0, variance);
end
noise = estimate_noise(ImgArray, width, height, count);
disp("Estimated noise in the images: " + noise)
1.2
     Results
variance =
   6.1515e-05
sum_sq_diff =
     0
sigma =
    2.0071
```

1.3 Comments

Estimated noise in the images: 2.0071

Grayscale images are generated and are stored in a structure arrray. The structure contains the content of the image as a matrix and a label (an integer). Zero mean gaussian noise with a varience of 2.0 is added to every image in the array.

Using the EST_NOISE procedure, the estimated gaussian noise in the image array is around 2.00

2 Question 2: Box Filter

2.1 Code

```
filterSize = 3;
for j = 1:count
    ImgArray(j).Image = imboxfilt(ImgArray(j).Image, filterSize);
end

% use the function implemented for question 1
noise = estimate_noise(ImgArray, width, height, count);
disp("Estimated noise in the images: " + noise)

2.2 Results
sum_sq_diff =
    0

sigma =
```

Estimated noise in the images: 0.67326

2.3 Comments

0.6733

Upon applying the 3 x 3 box filter, the noise reduces from 2.00 to 0.67

3 Question 3

3.1 Code: Generating the 2D gaussian filter mask

```
hsize = 7;
sigma = 1.4;
gaussian_filter = fspecial('gaussian',hsize,sigma)
```

3.2 Result

gaussian_filter =

0.0008	0.0030	0.0065	0.0084	0.0065	0.0030	0.0008
0.0030	0.0108	0.0232	0.0299	0.0232	0.0108	0.0030
0.0065	0.0232	0.0498	0.0643	0.0498	0.0232	0.0065
0.0084	0.0299	0.0643	0.0830	0.0643	0.0299	0.0084
0.0065	0.0232	0.0498	0.0643	0.0498	0.0232	0.0065
0.0030	0.0108	0.0232	0.0299	0.0232	0.0108	0.0030
0.0008	0.0030	0.0065	0.0084	0.0065	0.0030	0.0008

Separating into a horizontal and a vertical filter by the formula:

$$f(x,y) = (\frac{1}{\sqrt{K}}e^{-\frac{x^2}{2\sigma^2}})(\frac{1}{\sqrt{K}}e^{-\frac{y^2}{2\sigma^2}})$$

$$f(x,y) = (\frac{1}{\sqrt{K}}e^{-\frac{x^2}{3.28}})(\frac{1}{\sqrt{K}}e^{-\frac{y^2}{3.28}})$$

 $X = [0.0008 \ 0.0030 \ 0.0065 \ 0.0084 \ 0.0065 \ 0.0030 \ 0.0008] \ and \ Y = X^T$

Scaling this, we've:

$$X = \frac{1}{36} [1 \ 4 \ 8 \ 10 \ 8 \ 4 \ 1] \ and \ Y = X^T$$





Image for filterry

	R	Pz	B	Py	P5	R	
10 10	lo	10	10	40	40	40	40 40

Ignoring the borders and carrying out the computate for the rest of the pixels.

$$P_2 = 10 + 10 + 10 + 10 + 40 = \frac{80}{5} = 16$$

$$\beta_3 = \frac{30+40+40}{5} = \frac{110}{5} = 22$$

$$P4 = 10 + 10 + 40 + 40 + 40 = \frac{140}{5} = 28$$

$$\frac{1}{6} = \frac{40+40+40+40+40}{5} = \frac{200}{5} = 40$$

Averaging filter
$$\bigcirc$$

$$P_1 \quad P_2 \quad P_3 \quad P_4 \quad P_5 \quad P_6$$

$$| 10 | 10 \quad | 70 \quad | 10 \quad | 40 \quad |$$

 $10+20+\frac{160}{10}+80+40=\frac{310}{10}=31$

$$P_6 = 40 + 80 + 160 + 80 + 40 = \frac{400}{10} = 40$$

The second titler is much more expensive in computational cost compared the first filter, since it involves more anthmetic operations.

Varience Companion

Filter 1:

Varience =
$$\frac{6^2}{mn} = \frac{6^2}{5\pi i} = \frac{6^2}{5}$$
 — ①

Filter 2:

Let X_1, X_2, X_3, X_4, X_5 be 5 pixels which hold noise values n_1, n_2, n_3, n_4, n_5

$$0 = \frac{1}{10} \left[x_1 + n_1 + 2(x_2 + n_2) + 4(x_3 + n_3) + 2(x_4 + n_4) + (x_5 + n_5) \right]$$

$$= E \left[\left[\frac{1}{10} (n_1 + 2n_2 + 4n_3 + 2n_4 + n_5) \right]^2 \right]$$

$$= \frac{1}{100} \left[E \eta_1^2 + 4 E \eta_2^2 + 16 E \eta_3^2 + 4 E \eta_4^2 + E \eta_5^2 \right]$$

Now
$$E(x)^2 = [E(x)]^2 + D(x)$$
,
 $E(n_1^2) = (E(n_2))^2 + D(n_1) = \sigma^2$
 $A = (n_2^2) = (2E(n_2))^2 + D(n_2) = 4\sigma^2$

$$E(n_3^2) = E(n_3)^2 + D(n_3) = 166^2$$

$$E(n_4^2) = E(n_3^2 + D(n_3) = 46^2$$

$$E(n_5^2) = E(n_5^2) + D(n_5) = 6^2$$

Now, Varience =
$$\frac{(1+4+16+4+1)}{100}$$
 6^2 = $\frac{13.6^2}{50}$ = $\frac{1}{2}$

Comparing the values (1) and (2), we can see that the second filter ($\frac{1}{1}$ = 4 2 1]) causes more varience compared to the first ($\frac{1}{5}$ [11111])

(5) Consider that the pixel inder consideration is to the right of the step we could have four possible cares

		χı	X 2
220000	50	6	0
	50	0	100
	50	100	0
	50	166	100

Pixel under consideration

Operation: [-1 2 -1]

Possible pixel values after the application of this filter

Care I : -50 + 0 -100 = -150

Care III: -50+200+0= 150

Care TE: -50+200-100 = 50

Now, P(Salti) = 0.7 and P(Pepper) = 0.3

P (pixel value = -50) = .3x.3 = 0.09

P(Pixel value = -150) = 0.3 x 0.7 = 0.21

P (Pixel value = 150) = 0.7 × 0.3 = 0.21

P(Pixel value = 50) = 0.7 x 0.7 = 0.49

Equation of the image I(e,j) = |e-j|

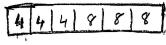
							2	£
0	1	2	3	4	5	6	7	A CONTRACTOR OF STREET
ı	0	l	2	3	4	5	6	PARCELLE PROPERTY.
2	1	0		2	3	4	5	CALIFORNIA AND AND ADDRESS OF THE PARTY OF T
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Applying the 3x3 median filter we have: (and copying the borders)

0	١	2	3	4	5	6	7
1	1	1	2	3	4	5	6
2	1	1	1	2	3	4	5
3	2	1			2	3	4
4	3	2	1	1		2	3
5	4	3	2	1	1	1	2
6	5	4	3	2	1	1	1
7	6	5	4	3	2	1	0

$$(7)$$
 1D step profile fi) = $\begin{cases} 4 & i \in [0,3] \\ 8 & i \in [4,7] \end{cases}$

(i) Median filter with n=3, and copying the border:



(11) Averaging mask \frac{1}{4}[121]

$$P_1 = \frac{2x_1+1x_1}{4} = 3$$
 $P_2 = \frac{4+8+4}{4} = 4$

$$P_3 = 4 + 8 + 4 = 4$$
 $P_4 = 4 + 16 + 8 = 7$

$$P_6 = \frac{8+16+8}{4} = 8$$
 $P_6 = \frac{8+16+8}{4} = 8$

The median fitter does not change the pixels, in this case whereas the averaging mark smoothers it.