

# HW8-Solutions

## Problem 1

Refer to Brand preference data, build a model with all independent variables (45 pts)

####a) Obtain the studentized deleted residuals and identify any outlying Y observations. Use the Bonferroni outlier test procedure with  $\alpha = .10$ . State the decision rule and conclusion. (5pts) ####b) Obtain the diagonal elements of the hat matrix, and provide an explanation for the pattern in these elements. (5pts) ####c) Are any of the observations outlying with regard to their X values according? (5pts) ####d) Management wishes to estimate the mean degree of brand liking for moisture content  $X_1 = 10$  and sweetness  $X_2 = 3$ . Construct a scatter plot of  $X_2$  against  $X_1$  and determine visually whether this prediction involves an extrapolation beyond the range of the data. Also, use (10.29) to determine whether an extrapolation is involved. Do your conclusions from the two methods agree? (5pts) ####e) The largest absolute studentized deleted residual is for case 14. Obtain the DFFITS, DFBETAS, and Cook's distance values for this case to assess the influence of this case. What do you conclude? (5pts) ####f) Calculate the average absolute percent difference in the fitted values with and without case 14. What does this measure indicate about the influence of case 14? (10pts) ####g) Calculate Cook's distance D; for each case and prepare an index plot. Are any cases influential according to this measure? (5pts) ####h) Find the two variance inflation factors. Why are they both equal to 1? (5pts)

a)

Solution: No outliers based on the bonferoni test.

```
library(knitr)
Brand.Preference <- read.csv("/cloud/project/Brand Preference.csv")
hw8.pr1<-lm(Y~X1+X2,data=Brand.Preference)
library(olsrr)
```

```
##
## Attaching package: 'olsrr'
```

```
## The following object is masked from 'package:datasets':
##
##      rivers
```

```
drst<-rstudent(hw8.pr1)
tb<-qt(1-0.1/(2*16),16-3-1)
sum(abs(drst)>abs(tb))
```

```
## [1] 0
```

b)

**Solution:** Max hat value is 0.2375 and the min is 0.1375. The avarega is 0.19. The compact range, no indication of outliers.

```
hii <- hatvalues(hw8.pr1)
hii
```

```
##      1      2      3      4      5      6      7      8      9     10     11
## 0.2375 0.2375 0.2375 0.2375 0.1375 0.1375 0.1375 0.1375 0.1375 0.1375 0.1375
##      12     13     14     15     16
## 0.1375 0.2375 0.2375 0.2375 0.2375
```

```
summary(hii)
```

```
##      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
## 0.1375 0.1375 0.1875 0.1875 0.2375 0.2375
```

c)

**Solution:** No outliers in direction of X, hat values are less than  $2 \cdot p/n$ .

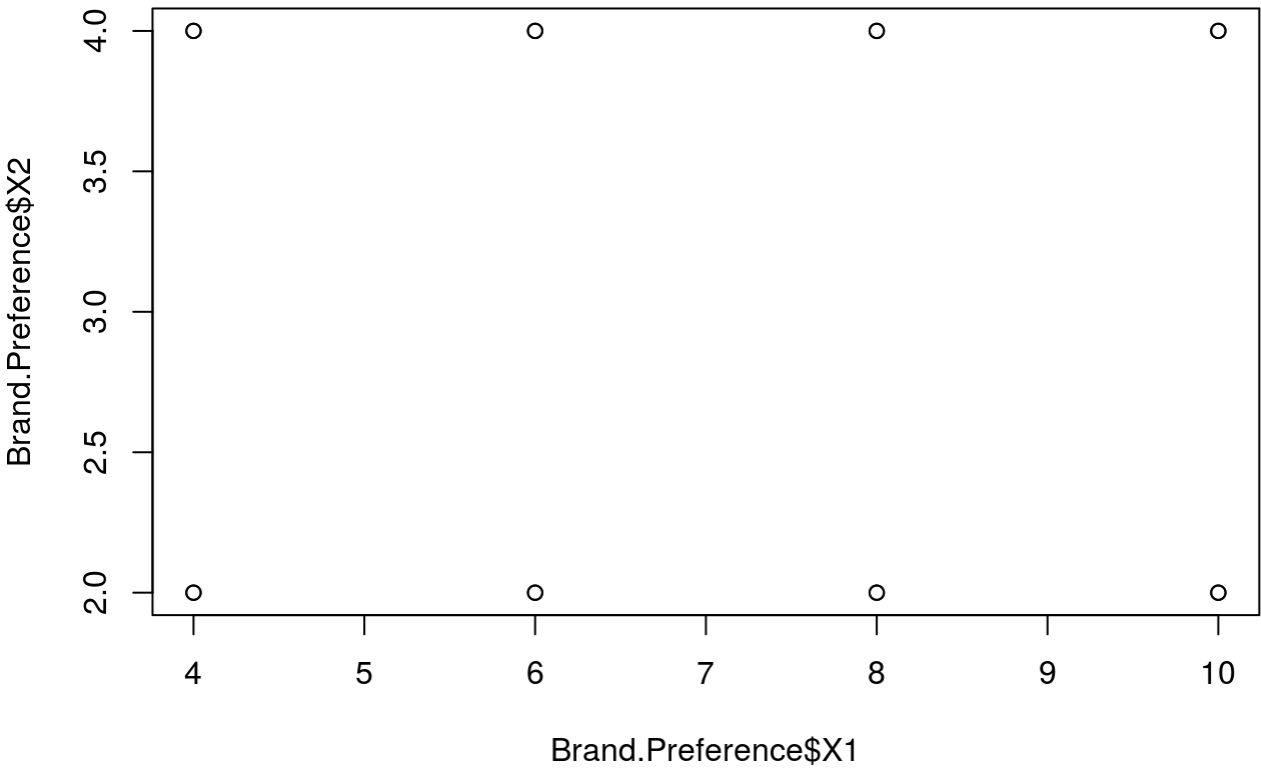
```
sum(hii > (2*3/16))
```

```
## [1] 0
```

d)

**Solution:** The hat value for the prediction is 0.175 which is within the hat values calculated at c (max= 0.2375 and min=0.1375). No extrapolation is required.

```
plot(Brand.Preference$X1, Brand.Preference$X2)
```



```
X<-model.matrix(hw8.pr1)
XXInv<-solve(t(X)%*%X)
Xhnew<-matrix(c(1,10,3),nrow=1,ncol=3)
Hatnew<-Xhnew%*%XXInv%*%t(Xhnew)
Hatnew
```

```
##      [,1]
## [1,] 0.175
```

e)

**Solution:** Case 14 has the max DFIITS, DFBETAS, and Cooks distance. Cooks distance is 2000 larger than the smallest cooks distance. Indicating influential point.

```
cd<-influence.measures(hw8.pr1)
cd
```

```
## Influence measures of
## lm(formula = Y ~ X1 + X2, data = Brand.Preference) :
##
##      dfb.1_ dfb.X1 dfb.X2 dffit cov.r cook.d hat inf
```

```
## 1 -0.02155 0.0157 0.0117 -0.0228 1.667 0.000188 0.238
## 2 0.00868 -0.0235 0.0175 0.0342 1.666 0.000422 0.237
## 3 -0.71785 0.5226 0.3895 -0.7593 1.084 0.180392 0.237
## 4 0.19619 -0.5324 0.3968 0.7735 1.068 0.186258 0.238
## 5 -0.11987 0.0442 0.0988 -0.1465 1.426 0.007666 0.138
## 6 0.02413 0.0800 -0.1790 -0.2655 1.322 0.024547 0.138
## 7 -0.25062 0.0924 0.2065 -0.3063 1.277 0.032297 0.138
## 8 -0.01832 -0.0607 0.1358 0.2015 1.384 0.014354 0.138
## 9 0.07315 0.0560 -0.1252 0.1857 1.397 0.012231 0.138
## 10 0.12431 -0.0728 -0.1627 -0.2413 1.347 0.020406 0.138
## 11 0.28674 0.2195 -0.4907 0.7279 0.708 0.149828 0.138
## 12 -0.20113 0.1177 0.2632 0.3904 1.171 0.050983 0.138
## 13 0.01467 -0.4378 0.3263 -0.6360 1.225 0.131821 0.237
## 14 0.83881 -0.8077 -0.6020 -1.1735 0.651 0.363412 0.237
## 15 -0.01917 0.5722 -0.4265 0.8314 1.002 0.210661 0.237
## 16 -0.09802 0.0944 0.0704 0.1371 1.643 0.006758 0.237
```

```
cd$infmat[14,6]/cd$infmat[,6]
```

```
##          1          2          3          4          5          6
## 1936.000000 860.444444 2.014568 1.951121 47.408648 14.804950
##          7          8          9         10         11         12
## 11.252151 25.317340 29.712712 17.809076 2.425527 7.128081
##         13         14         15         16
## 2.756853 1.000000 1.725106 53.777778
```

f)

**Solution:** Predicted values are increased by %0.62.

```
p1<-hw8.prl$fitted.values[-c(14)]
t1<-lm(Y~X1+X2,data=Brand.Preference[-c(14),])
p2<-t1$fitted.values
cbind(Brand.Preference[-c(14),1],p1,p2)
```

```
##          p1          p2
## 1 64 64.10 63.45082
## 2 73 72.85 72.92213
## 3 61 64.10 63.45082
## 4 76 72.85 72.92213
## 5 72 72.95 72.73361
## 6 80 81.70 82.20492
## 7 71 72.95 72.73361
## 8 83 81.70 82.20492
## 9 83 81.80 82.01639
## 10 89 90.55 91.48770
## 11 86 81.80 82.01639
## 12 93 90.55 91.48770
## 13 88 90.65 91.29918
## 15 94 90.65 91.29918
```

```
## 16 100 99.40 100.77049
```

```
mean((abs(p1-p2)/p2)*100)
```

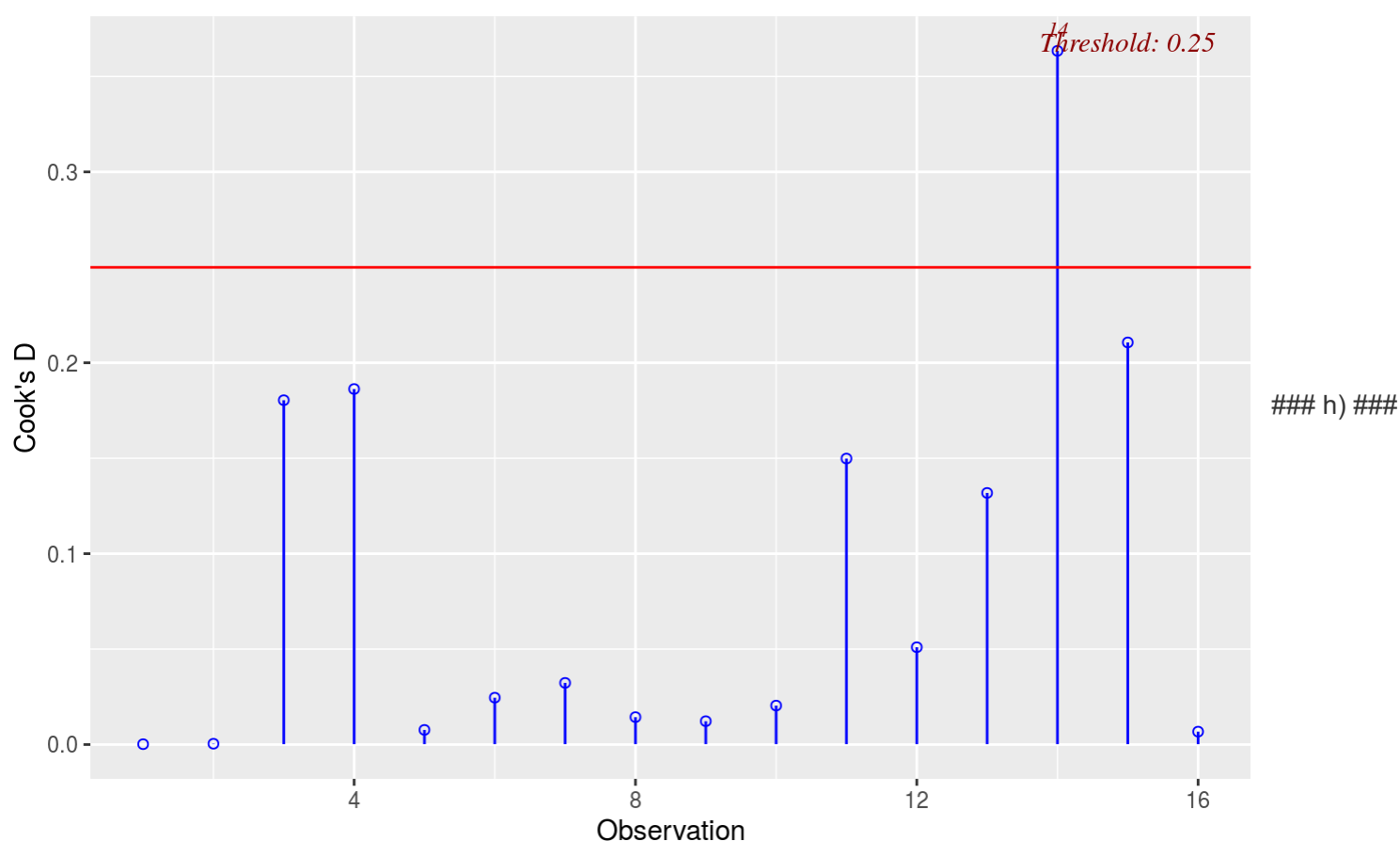
```
## [1] 0.6284827
```

g)

**Solution:** Case 14 is an influential point based on the plot.

```
ols_plot_cooks_d_chart(hw8.pr1)
```

Cook's D Chart



**Solution:** X1 and X2 are independent, therefore VIF=1.

```
library(faraway)
```

```
## Registered S3 methods overwritten by 'lme4':
##   method                                from
##   cooks.distance.influence.merMod      car
##   influence.merMod                     car
##   dfbeta.influence.merMod              car
##   dfbetas.influence.merMod             car
```

```
##
## Attaching package: 'faraway'
```

```
## The following object is masked from 'package:olsrr':
##
##      hsb
```

```
vif(hw8.pr1)
```

```
## X1 X2
##  1  1
```

```
cor(Brand.Preference)
```

```
##           Y           X1           X2
## Y  1.0000000  0.8923929  0.3945807
## X1 0.8923929  1.0000000  0.0000000
## X2 0.3945807  0.0000000  1.0000000
```

## Problem 2

Refer to the Lung pressure Data and Homework 7. The subset regression model containing first-order terms for  $X_1$  and  $X_2$  and the cross-product term  $X_1X_2$  is to be evaluated in detail. (35 pts)

##a) Obtain the residuals and plot them separately against  $Y$  and each of the three predictor variables. On the basis of these plots, should any further modification of the regression model be attempted? (5pts) ##b) Prepare a normal probability plot of the residuals. Also obtain the coefficient of correlation between the ordered residuals and their expected values under normality. Does the normality assumption appear to be reasonable here? (5pts) ##c) Obtain the variance inflation factors. Are there any indications that serious multicollinearity problems are present? Explain. (5pts) ##d) Obtain the studentized deleted residuals and identify outlying  $Y$  observations. Use the Bonferroni outlier test procedure with  $\alpha = .05$ . State the decision rule and conclusion. (5pts) ##e) Obtain the diagonal elements of the hat matrix. Are there any outlying  $X$  observations? Discuss. (5pts) ##f) Cases 3, 8, and 15 are moderately far outlying with respect to their  $X$  values, and case 7 is relatively far outlying with respect to its  $Y$  value. Obtain DFFITS, DFBETAS, and Cook's distance values for these cases to assess their influence. What do you conclude? (10pts)

a)

**Solution:** No pattern with residuals and  $X_3$ , indicating that  $X_3$  would not increase the power. There are couple of potential outliers in the data.

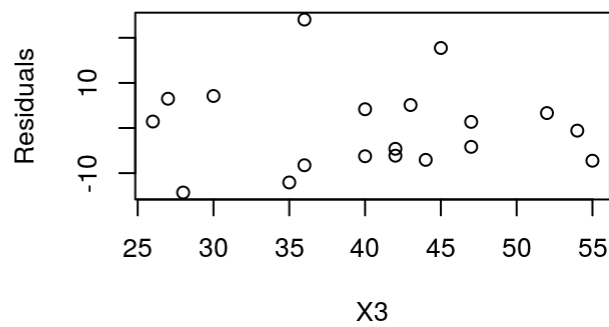
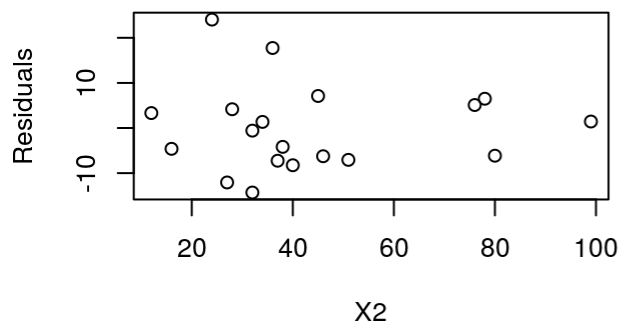
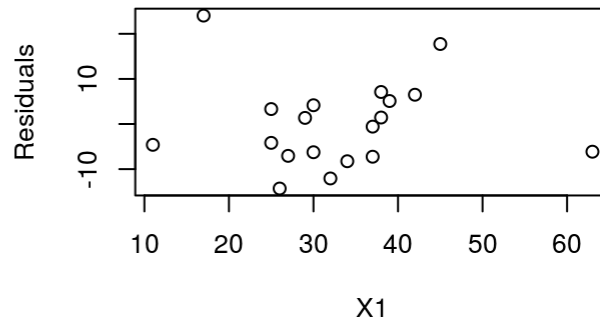
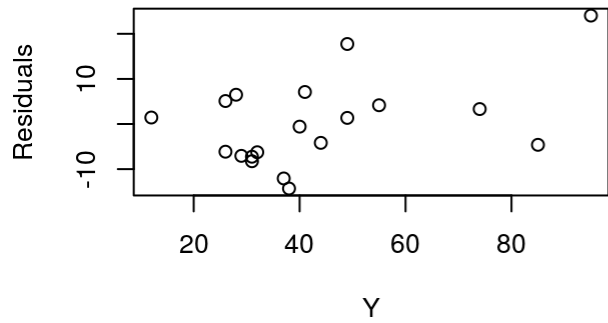
```
Lung.Pressure <- read.csv("/cloud/project/Lung Pressure.csv")
```

```
hw8.pr2<-lm(Y~X1+X2+I(X1*X2),data=Lung.Pressure)
summary(hw8.pr2)
```

```
##
## Call:
## lm(formula = Y ~ X1 + X2 + I(X1 * X2), data = Lung.Pressure)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -14.3075  -6.6602  -0.5824   4.6284  24.0398
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  134.399866   15.981599   8.410 4.63e-07 ***
## X1           -2.133022    0.522157  -4.085 0.000975 ***
## X2           -1.699330    0.363669  -4.673 0.000300 ***
## I(X1 * X2)    0.033347    0.009283   3.592 0.002667 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 10.58 on 15 degrees of freedom
## Multiple R-squared:  0.7922, Adjusted R-squared:  0.7507
## F-statistic: 19.06 on 3 and 15 DF,  p-value: 2.233e-05
```

```
par(mfrow=c(2,2))
plot(Lung.Pressure$Y,hw8.pr2$residuals,ylab="Residuals",xlab="Y")
plot(Lung.Pressure$X1,hw8.pr2$residuals,ylab="Residuals",xlab="X1")
plot(Lung.Pressure$X2,hw8.pr2$residuals,ylab="Residuals",xlab="X2")
plot(Lung.Pressure$X3,hw8.pr2$residuals,ylab="Residuals",xlab="X3")
```

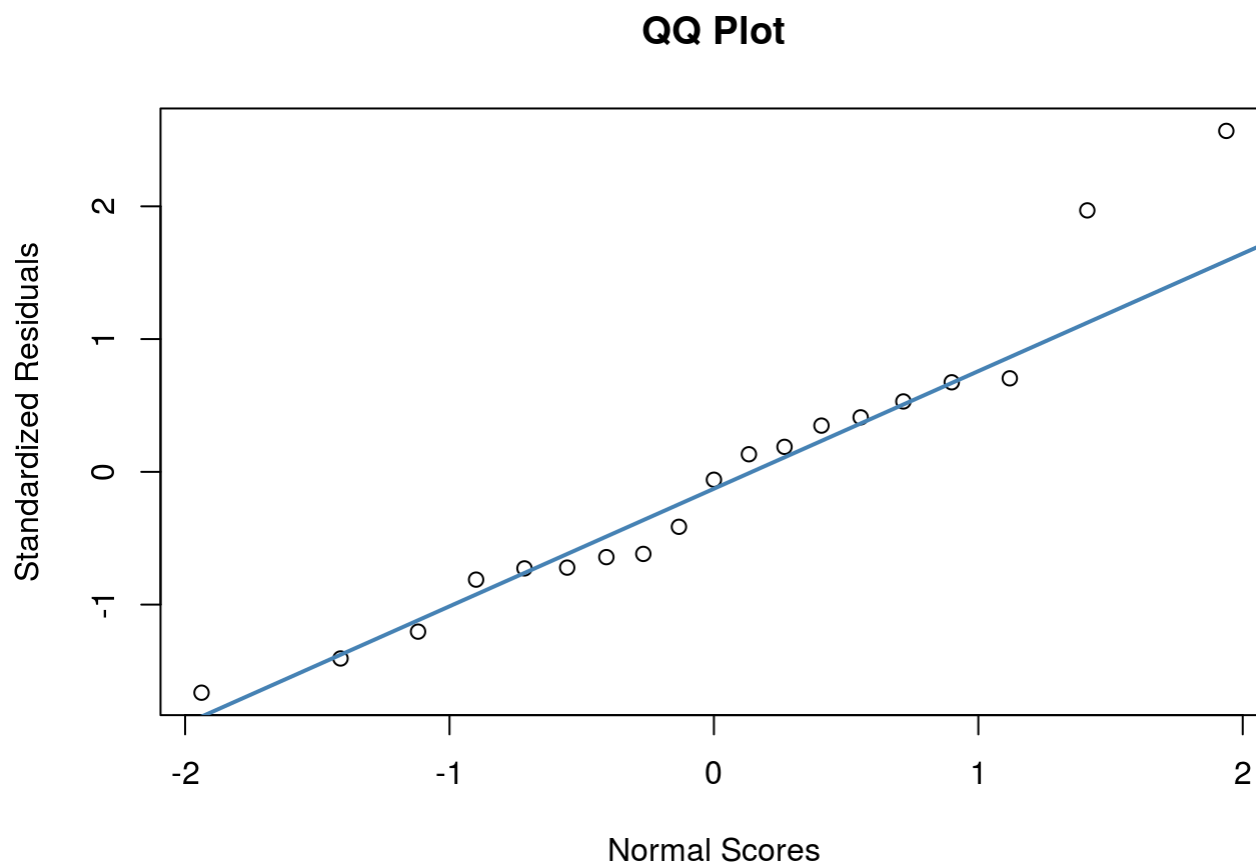
### b) ###



*Solution:* the correlation is 96%, and graph indicates that the assumption is reasoable.

```
stdei<- rstandard(hw8.pr2)
qqnorm(stdei,ylab="Standardized Residuals",xlab="Normal Scores", main="QQ Plot")
qqline(stdei,col = "steelblue", lwd = 2)
```





```
a2<-anova(hw8.pr2)
mse<-a2$`Mean Sq`[4]
ei<-hw8.pr2$residuals
ei.rank<-rank(ei)
z1<-(ei.rank-0.375)/(19+0.375)
exp.rank<-sqrt(mse)*qnorm(z1)
cor(exp.rank,ei)
```

```
## [1] 0.9606285
```

c)

**Solution:** Multicollinearity present  $VIF > 10$  for X2 and the interaction term.

```
library(faraway)
vif(hw8.pr2)
```

```
##           X1           X2 I (X1 * X2)
##  5.431477  11.639560  22.474469
```

d)

**Solution:** No outliers based on the bonforeni test. the largest deleted residual is observation 7, which larger than 3.

```
drst<-rstudent(hw8.pr2)
tb<-qt(1-0.05/(2*19),19-4-1)
sum(abs(drst)>abs(tb))
```

```
## [1] 0
```

e)

**Solution:** Indicating 3 outliers in X. Observations 3,8 and 15.

```
hii <- hatvalues(hw8.pr2)
hii
```

```
##          1          2          3          4          5          6          7
## 0.27569243 0.08336965 0.53886673 0.08482945 0.17565769 0.17374756 0.21775095
##          8          9         10         11         12         13         14
## 0.87827870 0.19254581 0.10171037 0.11155424 0.06796196 0.07530137 0.09294148
##          15         16         17         18         19
## 0.47982100 0.08967339 0.14443764 0.13905081 0.07680876
```

```
summary(hii)
```

```
##      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
## 0.06796 0.08725 0.13905 0.21053 0.20515 0.87828
```

```
sum(hii>(2*4/19))
```

```
## [1] 3
```

```
(hii>(2*4/19))
```

```
##          1          2          3          4          5          6          7          8          9         10         11         12         13
## FALSE FALSE  TRUE FALSE FALSE FALSE FALSE  TRUE FALSE FALSE FALSE FALSE FALSE
##          14         15         16         17         18         19
## FALSE  TRUE FALSE FALSE FALSE FALSE
```

f)

**Solution:** Case 8 has the largest cooks distance, it is an influential point. Cases 1 and 7 are outliers.

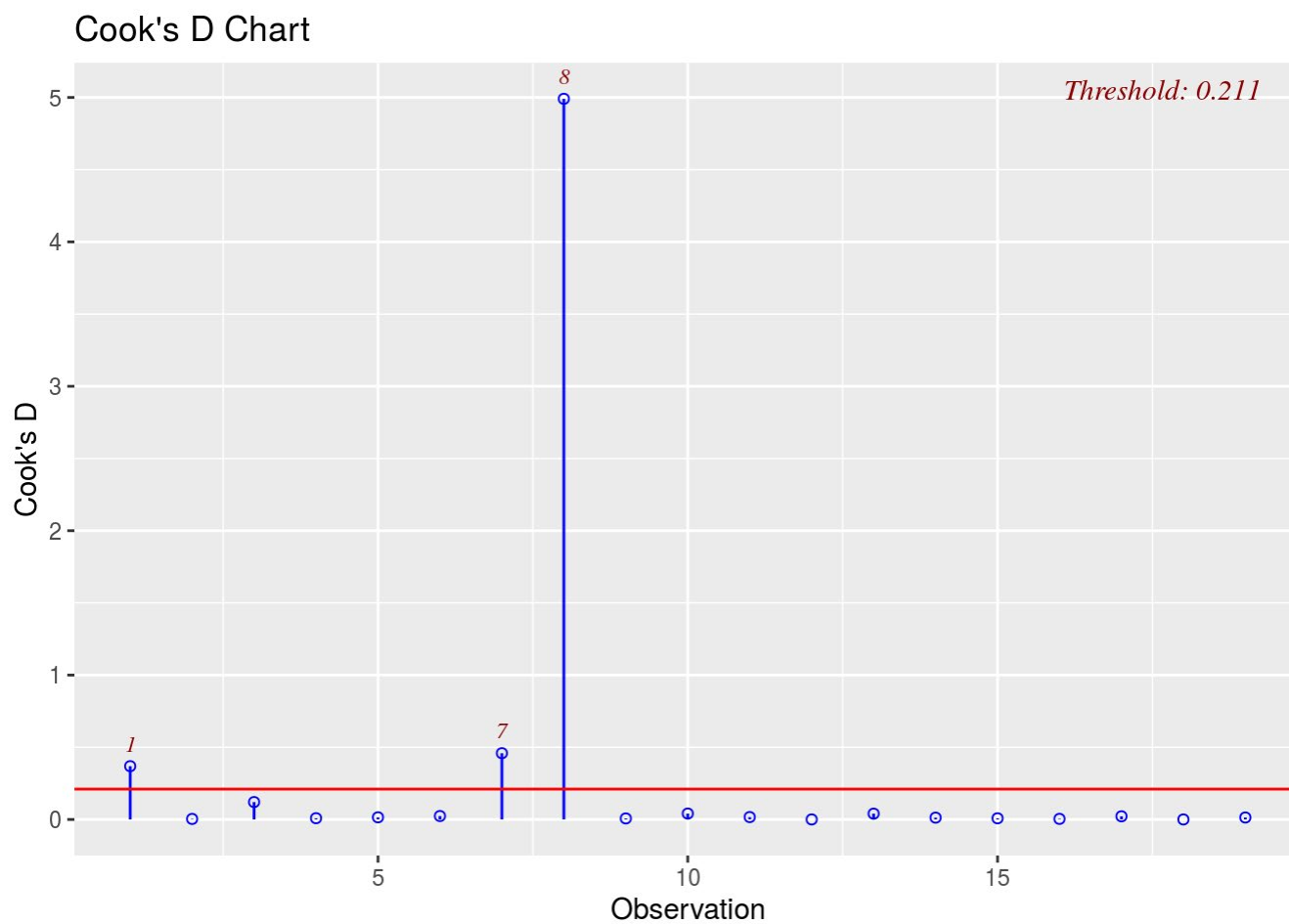
```
cd2<-influence.measures(hw8.pr2)
cd2
```

```
## Influence measures of
## lm(formula = Y ~ X1 + X2 + I(X1 * X2), data = Lung.Pressure) :
##
##      dfb.1_      dfb.X1      dfb.X2 dfb.I..X      dffit cov.r      cook.d      hat inf
## 1  -0.74721    1.086986    0.22392 -0.59551    1.3632 0.550 0.369041 0.2757  *
## 2   0.00722    0.030375   -0.00594 -0.02091    0.1203 1.374 0.003833 0.0834
## 3  -0.65194    0.591913    0.43337 -0.48191   -0.6802 2.556 0.120516 0.5389  *
## 4   0.04063   -0.040524   -0.10592  0.09287   -0.1842 1.299 0.008854 0.0848
## 5  -0.04872   -0.000561    0.10888 -0.04217    0.2387 1.482 0.014982 0.1757
## 6  -0.02764   -0.026282    0.07195  0.01040    0.3035 1.410 0.023920 0.1737
## 7   1.45413   -1.277609   -0.74152  0.84752    1.7486 0.166 0.458917 0.2178  *
## 8  -1.54691    1.186623    3.16227 -3.28579   -4.7798 4.790 4.990815 0.8783  *
## 9   0.10208   -0.046089   -0.10509  0.07011    0.1650 1.580 0.007236 0.1925
## 10  0.03588   -0.171698    0.00924  0.10165   -0.4116 0.977 0.040999 0.1017
## 11  0.10895   -0.171977   -0.06084  0.11835   -0.2534 1.285 0.016600 0.1116
## 12  0.00127    0.006001    0.00576 -0.00950    0.0346 1.407 0.000320 0.0680
## 13 -0.12604    0.051336   -0.01204  0.03230   -0.4159 0.810 0.040228 0.0753
## 14 -0.10749    0.144648    0.07972 -0.10974    0.2215 1.270 0.012712 0.0929
## 15 -0.01551   -0.035251    0.07715 -0.01570    0.1749 2.510 0.008170 0.4798  *
## 16 -0.02274    0.017421   -0.03719  0.02835   -0.1262 1.383 0.004218 0.0897
## 17  0.05185   -0.018569   -0.19203  0.14258   -0.2914 1.337 0.021956 0.1444
## 18  0.00912   -0.015709   -0.00358  0.00987   -0.0230 1.529 0.000142 0.1391
## 19  0.08055   -0.124148   -0.08285  0.11431   -0.2314 1.193 0.013708 0.0768
```

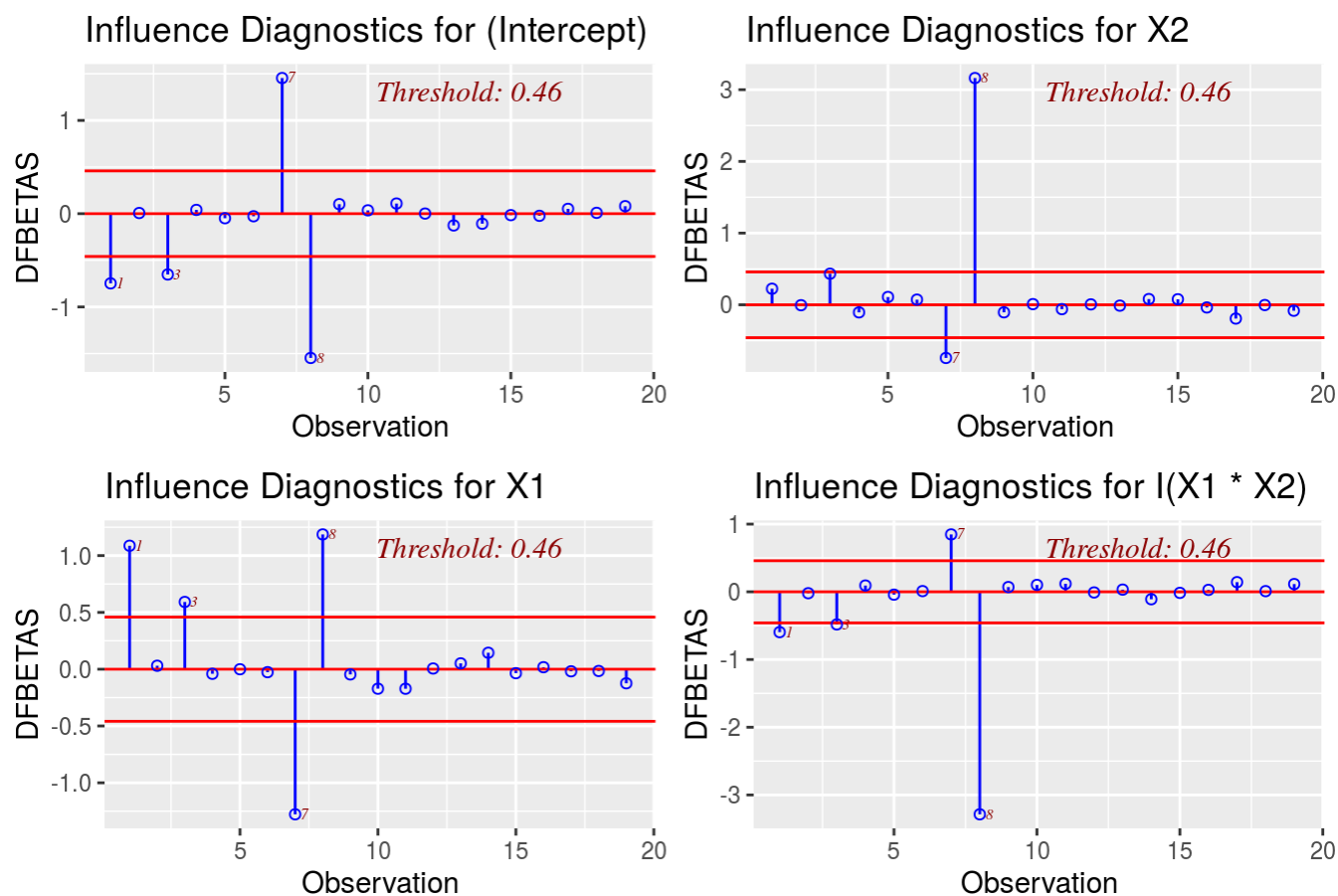
```
cd3<-cd2$infmat
cd3[c(3,7,8,15),]
```

```
##      dfb.1_      dfb.X1      dfb.X2      dfb.I(*X      dffit      cov.r
## 3  -0.6519371    0.59191342    0.43337176 -0.48191103 -0.6801824 2.5561254
## 7   1.4541305   -1.27760852   -0.74151968  0.84752328  1.7485509 0.1661137
## 8  -1.5469080    1.18662253    3.16226530 -3.28579003 -4.7797848 4.7895257
## 15 -0.0155059   -0.03525106    0.07714703 -0.01569977  0.1748573 2.5095274
##      cook.d      hat
## 3  0.120515509 0.5388667
## 7  0.458917058 0.2177509
## 8  4.990814979 0.8782787
## 15 0.008170411 0.4798210
```

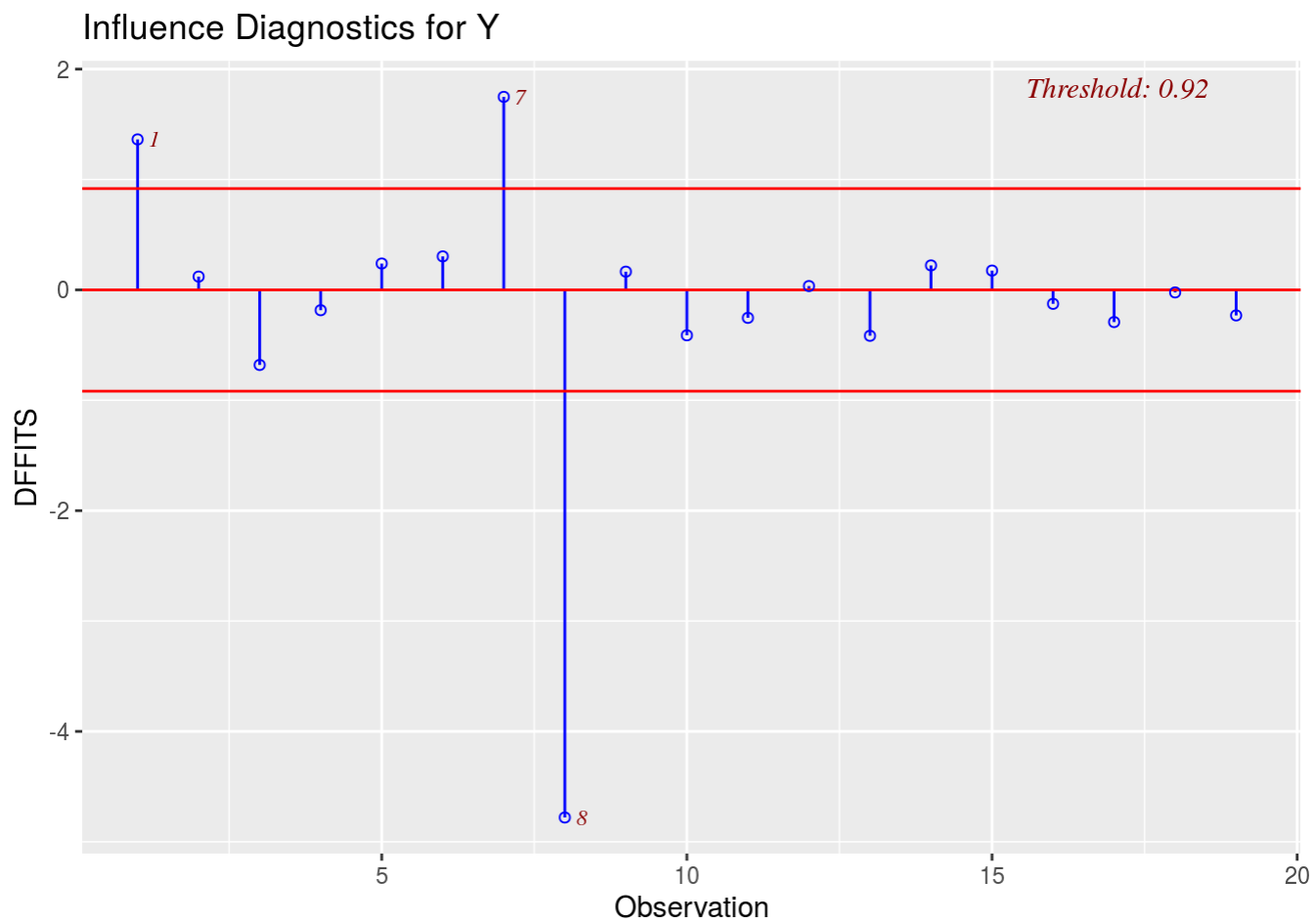
```
ols_plot_cooksd_chart(hw8.pr2)
```



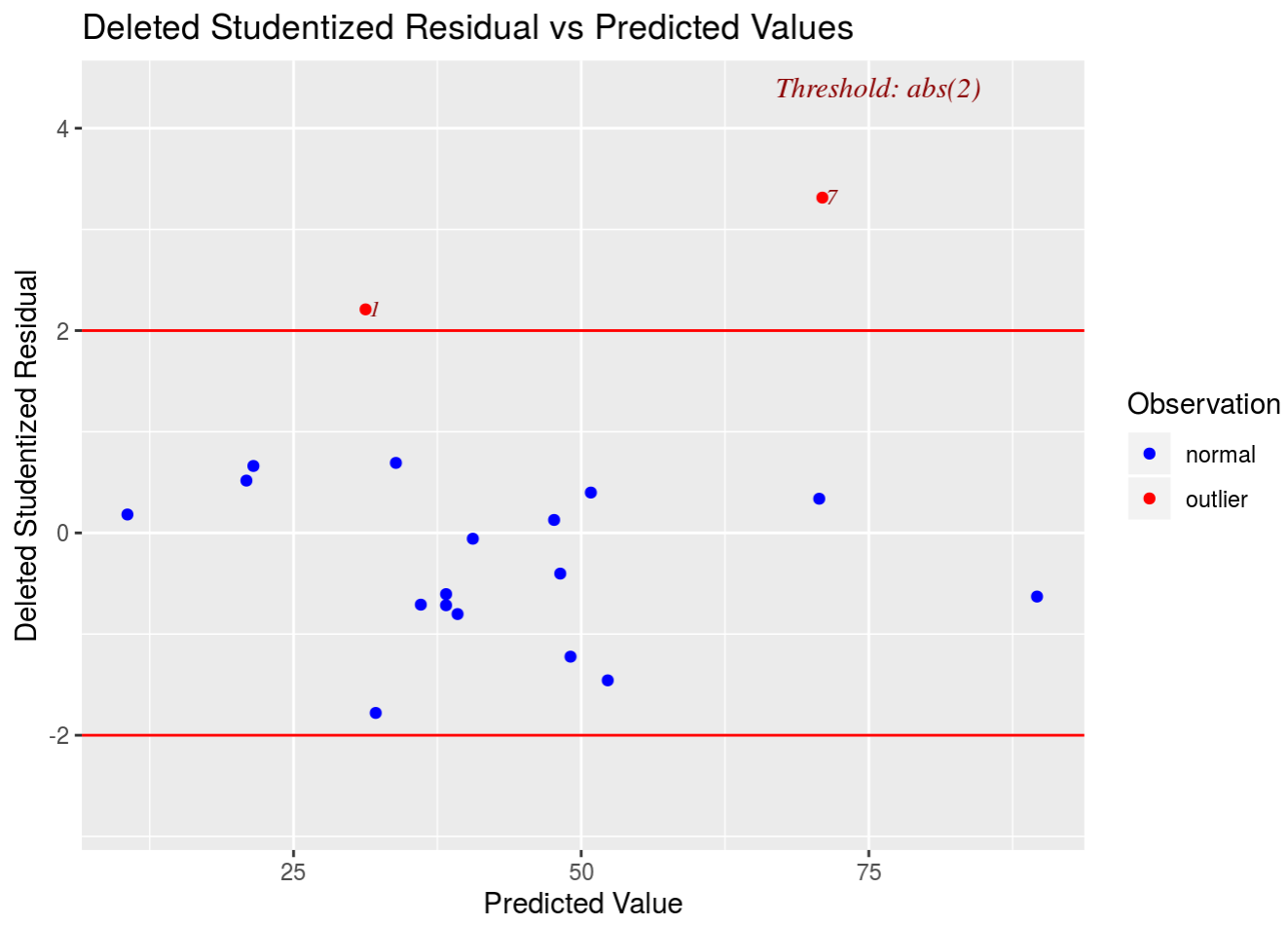
```
ols_plot_dfbetas(hw8.pr2)
```



```
ols_plot_dffits(hw8.pr2)
```



```
ols_plot_resid_stud_fit(hw8.pr2)
```



## Problem 3

Refer to the Prostate Cancer data set in Appendix C.6 and Homework 7. For the best subset model developed in Homework 7, perform appropriate diagnostic checks to evaluate outliers and assess their influence. Do any serious multicollinearity problems exist here? (20pts)

**Solution:** The model is significant with 41% Rsquare. There outlier observations 47,95,96 and 97. The observation 97 is also an influential point. The regression model assumptions are not hold for normality and nonconstant variances based on the graphs.

```
Prostate.Cancer <- read.csv("/cloud/project/Prostate Cancer.csv")
hw8.pr3<-lm(PSA.level~Cancer.volume+Capsular.penetration,data=Prostate.Cancer)
summary(hw8.pr3)
```

```
##
## Call:
## lm(formula = PSA.level ~ Cancer.volume + Capsular.penetration,
##     data = Prostate.Cancer)
##
```

```
## Residuals:
##      Min       1Q   Median       3Q      Max
## -60.346  -8.324  -1.205    4.159  183.843
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)      1.3276     4.2861   0.310   0.757
## Cancer.volume      2.4139     0.5655   4.269 4.69e-05 ***
## Capsular.penetration 2.4533     1.1779   2.083   0.040 *
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 31.48 on 94 degrees of freedom
## Multiple R-squared:  0.4165, Adjusted R-squared:  0.4041
## F-statistic: 33.55 on 2 and 94 DF,  p-value: 1.01e-11
```

```
influence.measures(hw8.pr3)
```

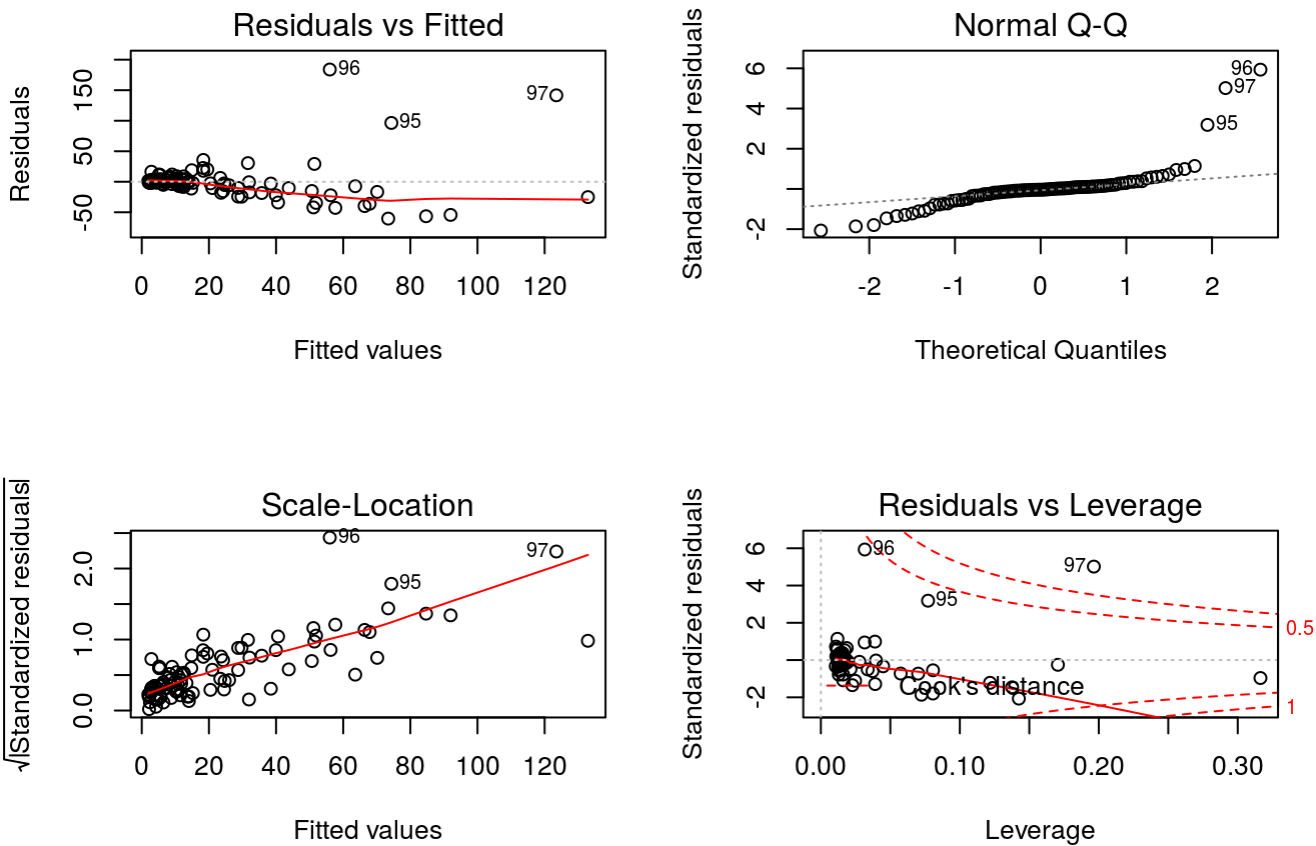
```
## Influence measures of
##      lm(formula = PSA.level ~ Cancer.volume + Capsular.penetration,      data = Prostate.Cance
## r) :
##
##      dfb.1_  dfb.Cnc.  dfb.Cps.      dffit cov.r   cook.d    hat inf
## 1  -8.55e-03  3.75e-03  2.53e-04 -8.57e-03 1.051 2.47e-05 0.0173
## 2  -5.86e-03  2.69e-03  6.77e-05 -5.87e-03 1.051 1.16e-05 0.0177
## 3  -8.09e-03  3.51e-03  2.71e-04 -8.12e-03 1.051 2.22e-05 0.0172
## 4  -5.16e-03  2.40e-03  2.54e-05 -5.17e-03 1.051 8.99e-06 0.0178
## 5  -1.88e-02  4.72e-03  3.72e-03 -1.95e-02 1.047 1.28e-04 0.0148
## 6  -5.23e-05  2.40e-05  4.96e-07 -5.23e-05 1.051 9.22e-10 0.0177
## 7  -1.59e-02  4.05e-03  3.12e-03 -1.65e-02 1.048 9.21e-05 0.0149
## 8  -1.44e-02  3.86e-03  2.65e-03 -1.49e-02 1.048 7.50e-05 0.0150
## 9   1.80e-03 -8.08e-04 -3.56e-05  1.80e-03 1.051 1.09e-06 0.0175
## 10 -5.93e-03  2.14e-03  5.89e-04 -6.00e-03 1.049 1.21e-05 0.0160
## 11 -3.47e-03  1.24e-03  3.58e-04 -3.51e-03 1.049 4.16e-06 0.0160
## 12  6.92e-03 -3.25e-03 -6.92e-06  6.93e-03 1.051 1.62e-05 0.0179
## 13 -3.30e-02 -2.91e-03  1.38e-02 -4.00e-02 1.041 5.38e-04 0.0125
## 14 -2.51e-02 -2.95e-03  1.34e-02 -3.07e-02 1.045 3.18e-04 0.0141
## 15 -2.38e-02  5.38e-03  3.19e-03 -2.52e-02 1.044 2.13e-04 0.0127
## 16 -2.52e-02 -4.35e-03  1.47e-02 -3.19e-02 1.045 3.42e-04 0.0142
## 17  3.75e-04 -2.00e-04  4.43e-05  3.77e-04 1.051 4.78e-08 0.0173
## 18 -3.87e-02 -5.66e-02  5.13e-02 -9.89e-02 1.029 3.28e-03 0.0160
## 19  8.65e-03 -3.78e-03 -2.65e-04  8.67e-03 1.051 2.53e-05 0.0173
## 20  2.96e-03 -1.09e-03 -2.79e-04  3.00e-03 1.049 3.02e-06 0.0161
## 21 -1.31e-02  1.31e-03  4.41e-03 -1.44e-02 1.047 7.03e-05 0.0141
## 22 -5.47e-02  2.09e-02 -3.91e-02 -8.93e-02 1.026 2.67e-03 0.0129
## 23  1.15e-02 -5.02e-03 -3.66e-04  1.16e-02 1.050 4.50e-05 0.0172
## 24 -5.00e-02  2.63e-02 -2.96e-02 -6.64e-02 1.035 1.48e-03 0.0131
## 25  2.95e-03 -9.84e-04 -3.67e-04  3.00e-03 1.049 3.04e-06 0.0157
## 26 -1.81e-02 -1.67e-03  9.20e-03 -2.18e-02 1.046 1.61e-04 0.0141
## 27 -1.56e-03  6.31e-04  1.06e-05 -1.57e-03 1.048 8.35e-07 0.0151
## 28  1.35e-02 -5.75e-03 -5.44e-04  1.35e-02 1.050 6.18e-05 0.0171
## 29 -1.57e-02  6.16e-03 -1.01e-03 -1.61e-02 1.046 8.78e-05 0.0133
```



##	30	-4.53e-02	-1.63e-03	-5.88e-02	-1.39e-01	1.010	6.44e-03	0.0160	
##	31	4.66e-03	-2.06e-03	1.22e-04	4.69e-03	1.049	7.40e-06	0.0157	
##	32	1.31e-02	-4.79e-03	-1.23e-03	1.32e-02	1.049	5.89e-05	0.0161	
##	33	-8.49e-03	2.36e-04	3.40e-03	-9.65e-03	1.047	3.14e-05	0.0140	
##	34	1.54e-02	-5.98e-03	-1.15e-03	1.55e-02	1.049	8.12e-05	0.0164	
##	35	1.21e-02	-5.81e-03	7.18e-04	1.21e-02	1.050	4.96e-05	0.0164	
##	36	-7.23e-03	6.51e-05	3.02e-03	-8.29e-03	1.047	2.32e-05	0.0140	
##	37	-5.28e-02	6.59e-02	-7.55e-02	-9.34e-02	1.060	2.93e-03	0.0337	
##	38	1.48e-02	-4.74e-03	-2.02e-03	1.51e-02	1.048	7.70e-05	0.0155	
##	39	-1.94e-02	-3.80e-02	-8.01e-02	-2.06e-01	0.996	1.41e-02	0.0227	
##	40	3.70e-03	-1.57e-03	2.30e-04	3.77e-03	1.047	4.78e-06	0.0142	
##	41	1.60e-02	-4.55e-03	-2.67e-03	1.64e-02	1.048	9.08e-05	0.0151	
##	42	-4.55e-03	-3.84e-04	2.28e-03	-5.48e-03	1.047	1.01e-05	0.0140	
##	43	1.18e-02	-5.10e-03	5.08e-04	1.19e-02	1.048	4.78e-05	0.0149	
##	44	-2.83e-02	6.70e-03	-4.66e-03	-3.41e-02	1.040	3.92e-04	0.0107	
##	45	-3.75e-03	1.80e-04	1.07e-03	-4.25e-03	1.045	6.10e-06	0.0122	
##	46	-3.48e-03	-1.05e-03	2.43e-03	-4.73e-03	1.048	7.53e-06	0.0147	
##	47	-2.67e-02	3.70e-01	-7.90e-01	-8.59e-01	1.047	2.37e-01	0.1425	*
##	48	8.47e-03	-2.12e-03	-9.59e-04	8.88e-03	1.046	2.65e-05	0.0129	
##	49	-5.14e-03	-2.17e-03	4.15e-03	-7.49e-03	1.048	1.89e-05	0.0153	
##	50	9.27e-03	-1.60e-03	-1.94e-03	9.94e-03	1.046	3.33e-05	0.0130	
##	51	2.03e-02	-2.61e-03	-6.29e-03	2.21e-02	1.046	1.64e-04	0.0142	
##	52	1.61e-03	4.86e-04	-1.12e-03	2.19e-03	1.048	1.61e-06	0.0147	
##	53	2.61e-02	-1.39e-02	4.64e-03	2.67e-02	1.047	2.39e-04	0.0156	
##	54	-3.61e-02	1.50e-02	-3.23e-02	-6.59e-02	1.037	1.46e-03	0.0140	
##	55	1.14e-01	-5.57e-01	4.56e-01	-5.88e-01	1.117	1.14e-01	0.1376	*
##	56	1.76e-02	-5.96e-04	-6.94e-03	1.99e-02	1.046	1.34e-04	0.0140	
##	57	1.66e-02	-9.15e-03	4.65e-03	1.75e-02	1.047	1.04e-04	0.0145	
##	58	4.36e-02	-1.40e-02	-5.94e-03	4.45e-02	1.045	6.66e-04	0.0155	
##	59	4.32e-02	-1.31e-02	-6.53e-03	4.43e-02	1.044	6.60e-04	0.0153	
##	60	2.94e-02	-4.17e-03	-8.75e-03	3.18e-02	1.045	3.40e-04	0.0142	
##	61	4.69e-02	-1.50e-02	-6.39e-03	4.78e-02	1.044	7.70e-04	0.0155	
##	62	-4.61e-02	6.66e-02	-9.93e-02	-1.17e-01	1.060	4.59e-03	0.0372	
##	63	3.79e-03	-1.11e-01	2.20e-02	-1.77e-01	1.017	1.04e-02	0.0246	
##	64	-5.60e-02	1.08e-01	-1.61e-01	-1.78e-01	1.077	1.06e-02	0.0574	
##	65	-5.59e-03	-6.37e-03	8.14e-03	-1.19e-02	1.053	4.79e-05	0.0196	
##	66	1.47e-02	-1.05e-03	-3.91e-03	1.65e-02	1.045	9.20e-05	0.0122	
##	67	-2.35e-02	9.49e-03	-1.61e-02	-3.68e-02	1.042	4.56e-04	0.0128	
##	68	-9.81e-03	-1.35e-02	1.48e-02	-2.35e-02	1.051	1.86e-04	0.0182	
##	69	6.90e-02	-2.96e-02	-2.56e-03	6.92e-02	1.041	1.61e-03	0.0171	
##	70	3.14e-02	-5.88e-03	-6.14e-03	3.34e-02	1.043	3.76e-04	0.0131	
##	71	-1.51e-02	9.03e-03	-1.16e-02	-2.20e-02	1.047	1.63e-04	0.0144	
##	72	4.10e-02	-3.89e-03	-1.39e-02	4.52e-02	1.043	6.87e-04	0.0141	
##	73	3.04e-02	-1.12e-02	2.26e-03	3.18e-02	1.043	3.40e-04	0.0126	
##	74	-7.30e-03	3.41e-03	-4.09e-03	-9.87e-03	1.045	3.28e-05	0.0126	
##	75	4.88e-02	-1.56e-01	-7.64e-03	-2.61e-01	1.019	2.25e-02	0.0391	
##	76	1.18e-01	-1.10e-01	-2.67e-01	-5.27e-01	0.994	9.02e-02	0.0724	
##	77	1.43e-02	4.78e-03	-5.64e-03	2.12e-02	1.043	1.51e-04	0.0111	
##	78	-5.72e-04	-3.94e-03	3.81e-03	-4.90e-03	1.075	8.09e-06	0.0397	
##	79	-2.79e-02	2.03e-01	-4.19e-01	-4.56e-01	1.121	6.90e-02	0.1217	*
##	80	2.11e-03	-6.31e-02	4.91e-02	-7.24e-02	1.077	1.77e-03	0.0448	
##	81	5.96e-02	-1.31e-02	-2.67e-03	6.49e-02	1.033	1.41e-03	0.0115	
##	82	-2.66e-02	8.51e-02	-1.77e-01	-1.99e-01	1.092	1.33e-02	0.0700	
##	83	-1.58e-03	-1.25e-02	9.59e-03	-1.59e-02	1.062	8.49e-05	0.0277	

##	84	-5.46e-03	-2.22e-02	-1.80e-02	-7.14e-02	1.047	1.71e-03	0.0213	
##	85	5.49e-02	-2.31e-02	1.60e-02	6.26e-02	1.034	1.32e-03	0.0119	
##	86	1.83e-01	-2.90e-01	-9.53e-02	-5.39e-01	1.011	9.46e-02	0.0807	*
##	87	4.48e-02	4.41e-02	-5.89e-02	8.85e-02	1.038	2.63e-03	0.0186	
##	88	6.30e-02	-8.52e-04	-1.20e-02	7.56e-02	1.027	1.91e-03	0.0109	
##	89	1.04e-03	4.15e-02	-1.34e-01	-1.63e-01	1.112	8.87e-03	0.0807	*
##	90	1.10e-01	-4.64e-02	3.22e-02	1.26e-01	1.002	5.25e-03	0.0119	
##	91	2.61e-02	-1.10e-01	8.87e-02	-1.15e-01	1.242	4.47e-03	0.1706	*
##	92	2.46e-02	1.59e-01	-1.55e-01	1.99e-01	1.041	1.32e-02	0.0389	
##	93	-1.11e-02	1.34e-01	-6.49e-02	1.70e-01	1.036	9.64e-03	0.0315	
##	94	3.06e-01	-6.12e-01	2.76e-01	-6.56e-01	1.466	1.44e-01	0.3163	*
##	95	-6.07e-02	-1.44e-01	7.42e-01	9.70e-01	0.794	2.83e-01	0.0771	*
##	96	-1.40e-01	9.79e-01	-3.08e-01	1.35e+00	0.261	3.83e-01	0.0316	*
##	97	-8.76e-01	2.51e-01	1.84e+00	2.88e+00	0.505	2.05e+00	0.1964	*

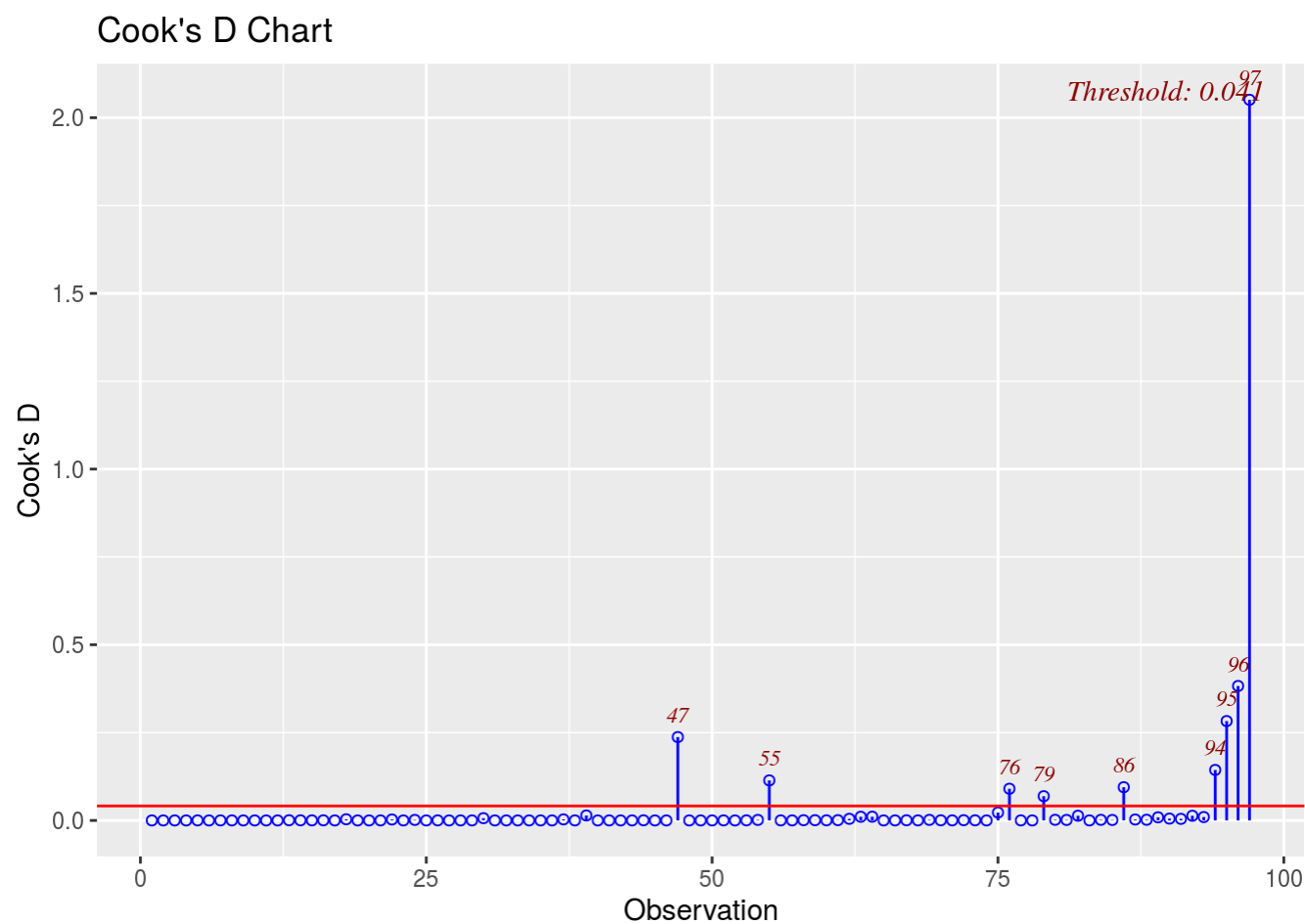
```
par(mfrow=c(2,2))
plot(hw8.pr3)
```



```
vif(hw8.pr3)
```

##	Cancer.volume	Capsular.penetration
##	1.923468	1.923468

```
ols_plot_cooksd_chart(hw8.pr3)
```



```
ols_plot_resid_stud_fit(hw8.pr3)
```

