

### **CS109A Introduction to Data Science**

## Homework 6: Multilayer Feedforward Network - Dealing with Missing Data

Harvard University Fall 2018

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```
In [1]: #RUN THIS CELL
import requests
from IPython.core.display import HTML
styles = requests.get("https://raw.githubusercontent.com/Harvard-IACS/2018-0
HTML(styles)
```

Out[1]:

#### **INSTRUCTIONS**

- To submit your assignment follow the <u>instructions given in canvas</u> (<a href="https://canvas.harvard.edu/courses/42693/pages/homework-policies-and-submission-instructions">https://canvas.harvard.edu/courses/42693/pages/homework-policies-and-submission-instructions</a>).
- This homework can be submitted in pairs.
- If you submit individually but you have worked with someone, please include the name of your one partner below.

Names of person you have worked with goes here:

```
In [2]:
        %matplotlib inline
        import numpy as np
        import numpy.random as nd
        import pandas as pd
        import math
        import matplotlib.pyplot as plt
        import os
        import seaborn as sns
        sns.set(style="darkgrid")
        from sklearn.linear model import LogisticRegressionCV
        from sklearn.linear model import LinearRegression
        from sklearn.neighbors import KNeighborsRegressor
        from sklearn.model selection import cross val score
        from sklearn.metrics import accuracy_score
        from sklearn.metrics import confusion matrix
        from sklearn.preprocessing import Imputer
        from sklearn.preprocessing import StandardScaler
        from sklearn.metrics import mean squared error
        from sklearn.model selection import train test split
        from IPython.display import display
```

#### Overview

In this homework, you are free to explore different ways of solving the problems -within the restrictions of the questions. Your solutions should read like a report with figures to support your statements. Please include your code cells as usual but augment your solutions with written answers. We will also check for code readability and efficiency as we feel you have some experience now. In particular, for Q1, we expect you to write appropriate functions, such as your code can be generalized beyond the specified network architectures of his homework.

For this homework you may **not** use a machine learning library such as keras or tensorflow to build and fit the network. The objective is to build the network equations from scratch.

- Q1 explores approximating a function using a **Multilayer Feedforward Network** with one input layer, one hidden layer, and one output layer.
- Q2 deals with missing data in a medical dataset.

#### Question 1: Construct a feed forward neural network [50 pts]

In this part of the homework you are to construct three feed forward neural networks consisting of an input layer, one hidden layer with 1, 2 and 4 nodes respectively, and an output layer. The hidden layer uses the sigmoid as the activation function and use a linear output node. You should code the equations from scratch.

You are given three datasets containing (x, y) points where y = f(x):

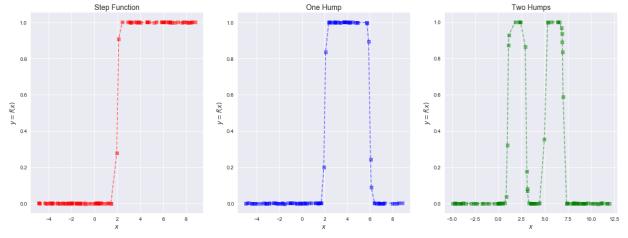
- In the first dataset, f(x) is a **single step** function (data in data/step df.csv),
- In the second dataset, f(x) is a **one hump** function (data in data/one hump df.csv),

- In the third dataset, f(x) is a **two equal humps** function (data in data/two\_hump\_df.csv).
- **1.1** Create a plot of each dataset and explore the structure of the data.
- **1.2** Give values to the weights **manually**, perform a forward pass using the data for the **single step** function and a hidden layer of **one** node, and plot the output from the network, in the same plot as the true *y* values. Adjust the weights (again manualy) until the plots match as closely as possible.
- **1.3** Do the same for the **one hump** function data, this time using a hidden layer consisting of **two** nodes.
- **1.4** Do the same for the **two hump** function data but this time increase the number of hidden nodes to **four**.
- **1.5** Choose the appropriate loss function and calculate and report the loss from all three cases. Derive the gradient of the output layer's weights for all three cases (step, one hump and two humps). Use the weights for the hidden layers you found in the previous question and perform gradient descent on the weights of this layer (output layer). What is the optimised weight value and loss you obtained? How many steps did you take to reach this value? What is the threshold value you used to stop?

#### **Answers**

```
In [3]: step_df = pd.read_csv('data/step_df.csv')
    one_hump_df = pd.read_csv('data/one_hump_df.csv')
    two_hump_df = pd.read_csv('data/two_hump_df.csv')

step_df = step_df.sort_values(by='x')
    one_hump_df = one_hump_df.sort_values(by='x')
    two_hump_df = two_hump_df.sort_values(by='x')
```

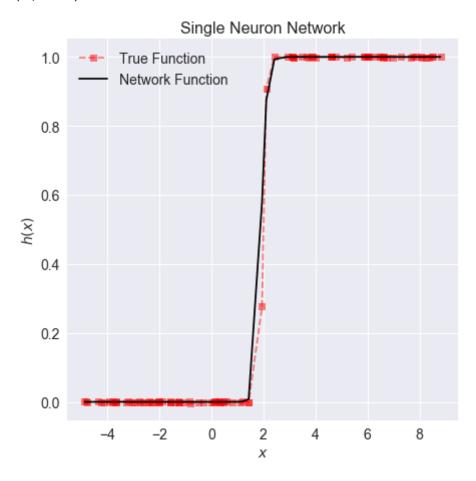


**Answer:** The graph for the Step Function looks like a sigmoid, which means we can model this by directly using the output from the activation function from the hidden layer. One Hump and Two Humps look like a combination of sigmoids and thus, will require two and four nodes respectively.

```
In [5]: # your code here
        def affine(w, x, b):
            z = w*x + b
            return(z)
        def activate(z):
            h = 1.0 / (1.0 + np.exp(-z))
            return(h)
        def yout(x, w, b, nodes, wout, bout):
            z = []
            for i in range(nodes):
                z.append(affine(w[i], x, b[i]))
            h = []
            for i in range(nodes):
                h.append(activate(z[i]))
            yout = bout
            for i in range(nodes):
                yout += wout[i]*h[i]
            return(yout, np.array(h))
        def plot_network(x, true_y, predicted_y, title):
            fig, ax = plt.subplots(1, 1, figsize=(7,7))
            ax.plot(x, true y, label=r'True Function', color='red', marker='s', ls=
            ax.plot(x, predicted_y, label=r'Network Function', color='k')
            ax.legend(loc='upper left', fontsize=14)
            ax.set xlabel(r'$x$', fontsize=14)
            ax.set_ylabel(r'$h(x)$', fontsize=14)
            ax.set title(title, fontsize=16)
            ax.tick params(labelsize = 14)
```

```
In [6]:
        x_step = step_df['x']
        w_step = np.array([9.9])
        b_step = np.array([-19])
        wout_step = np.array([1])
        bout_step = 0
        nodes_step = 1
        f step = step df['y']
        yout_step, hout_step = yout(x=x_step, w=w_step, b=b_step, nodes=nodes_step,
                                                wout=wout_step, bout=bout_step)
        # sanity check
        print(hout_step.shape)
        plot network(x step, f step, yout step, 'Single Neuron Network')
```

(1, 100)



**Answer:** Here we create functions affine, activate and yout that we can use for any number of nodes for given set of input x, hidden weights (w), hidden biases (b), output weights (wout), output biases (bout) and return the final output *Yhat*. Note that w, b and wout are arrays. After some trial and error we get above estimated function that closely matches out true repsonse.

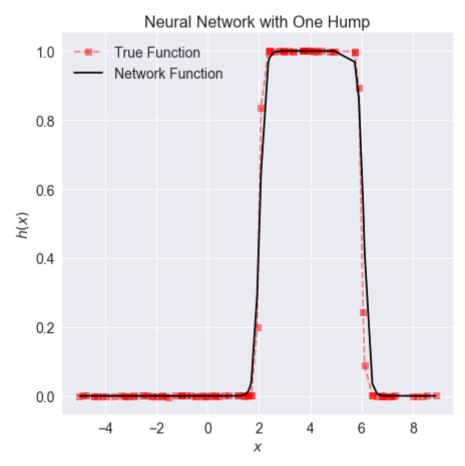
```
In [7]: # your code here
    x_one_hump = one_hump_df['x']
    w_one_hump = np.array([9.9, -9.7])
    b_one_hump = np.array([-20, 59])
    wout_one_hump = np.array([1, 1])
    bout_one_hump = -1
    nodes_one_hump = 2

    yout_one_hump, hout_one_hump = yout(x=x_one_hump, w=w_one_hump, b=b_one_hump, wout=wout_one_hump, bout=

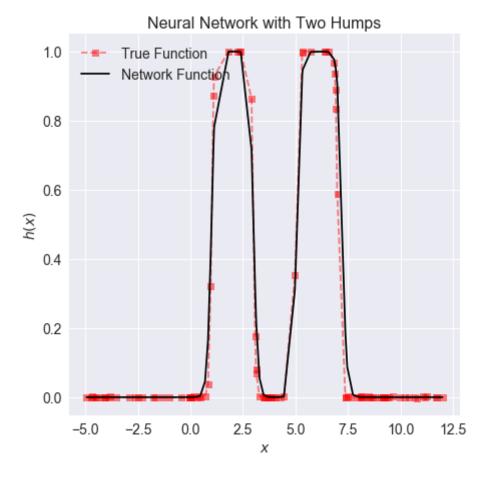
    # sanity check
    print(hout_one_hump.shape)

    f_one_hump = one_hump_df['y']

    plot_network(x_one_hump, f_one_hump, yout_one_hump, 'Neural Network with One
    (2, 100)
```



**Answer:** We use the same process to get estimated function for One Hump data set. Observe that the hidden weights are opposite in sign and almost same in magnitude for both the nodes. Biases are also have opposite signs but different magnitudes, depending on where we want to "place" the second node's output.



**Answer:** Here we get four nodes with similar weight magnitudes and opposite signs for two consecutive nodes.

```
In [9]: # your code here
    def CrossEntropy(yHat, y):
        eps = np.finfo(float).eps
        p = np.clip(yHat, eps, 1-eps)
        loss = -(y*np.log(p) + (1-y)*np.log(1-p))
        return(loss)
```

```
In [10]: # Step function
    error_step = CrossEntropy(yout_step, f_step)
    display(sum(error_step))

# One Hump
    error_one_hump = CrossEntropy(yout_one_hump, f_one_hump)
    display(sum(error_one_hump))

# Two Humps
    error_two_hump = CrossEntropy(yout_two_hump, f_two_hump)
    display(sum(error_two_hump))
```

- 1.010605439499416
- 3.0761116377755724
- 7.16530007770289

**Answer:** For calculating gradients of the output weights, we have to take the derivative of the loss function w.r.t. the output weights for each node. Since there is single output bias, bias gradient will always be a scalar irrespective of the number of nodes.

**Loss Function (Cross Entropy):** 

$$L = -[y_i * log p + (1 - y_i) * log(1 - p)]$$

where,

$$p = W_{out}.H_{out} + b_{out}$$

Derivative of the loss w.r.t. output layer weights:

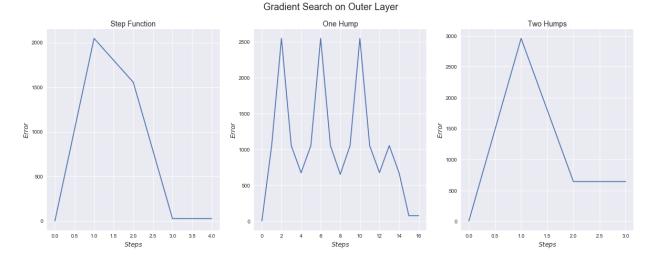
$$\frac{d_L}{d_{wout}} = -h_2 \left[ \frac{y_i}{p} - \frac{(1 - y_i)}{(1 - p)} \right]$$

Derivative of the loss w.r.t. output layer bias:

$$\frac{d_L}{d_{bout}} = -\left[\frac{y_i}{p} - \frac{1 - y_i}{p}\right]$$

```
In [11]: # functions for gradient descent
         def der weight(x, y, w, b, nodes, wout, bout):
             y_{out}, h = y_{out}(x, w, b, nodes, w_{out}, b_{out})
             eps = np.finfo(float).eps
             p = np.clip(y_out, eps, 1-eps)
             dL_{wout} = np.dot(h, (-(y/p)+(1-y)/(1-p)))
             return(dL_wout)
         def der_bias(yout, y):
             eps = np.finfo(float).eps
             p = np.clip(yout, eps, 1-eps)
             dL bout = np.sum(-(y/p)+(1-y)/(1-p))
             return(dL_bout)
         def gradient descent(x, y, w, b, nodes, wout, bout, thresh=0.00001, l=0.001)
             y_out, hout = yout(x=x, w=w, b=b, nodes=nodes, wout=wout, bout=bout)
             errors = [np.sum(CrossEntropy(y_out, y))]
             wout vals = [wout]
             bout_vals = [bout]
             for i in range(1, 1001):
                 y_out, hout = yout(x, w, b, nodes, wout, bout)
                  gradient_weight = der_weight(x, y, w, b, nodes, wout, bout)
                  gradient_bias = der_bias(yout=y_out, y=y)
                 wout_new = wout - l*gradient_weight
                 bout new = bout - l*gradient bias
                 yout new, hout new = yout(x, w, b, nodes, wout new, bout new)
                 error = np.sum(CrossEntropy(yout new, y))
                 errors.append(error)
                 wout vals.append(wout new)
                 bout vals.append(bout new)
                  if abs(error-errors[i-1])<thresh:</pre>
                      i=i
                      break
                 else:
                      wout = wout new
                      bout = bout new
             return(errors, wout vals[-1], bout vals[-1], i)
```

```
In [25]:
         errors grad step, w grad step, b grad step, i step = gradient descent(x=x st
                                                                                 bout=k
         errors grad one, w grad one, b grad one, i one = gradient descent(x=x one h
                                                                             b=b one hu
                                                                             wout=wout
         errors grad two, w grad two, b grad two, i two = gradient descent(x=x two h
                                                                             b=b two hi
                                                                             wout=wout
         print('Wout for Step: %s' %w grad step)
         print('Wout for One Hump: %s' %w_grad_one)
         print('Wout for Two Hump: %s' %w grad two)
         print(b grad step)
         print(b grad one)
         print(b_grad_two)
         fig, ax = plt.subplots(1, 3, figsize=(20,7))
         ax[0].plot(range(i step+1), errors grad step)
         ax[0].set_xlabel(r'$Steps$', fontsize=12)
         ax[0].set_ylabel(r'$Error$', fontsize=12)
         ax[0].set_title('Step Function', fontsize=14)
         ax[1].plot(range(i_one+1), errors_grad_one)
         ax[1].set xlabel(r'$Steps$', fontsize=12)
         ax[1].set ylabel(r'$Error$', fontsize=12)
         ax[1].set title('One Hump', fontsize=14)
         ax[2].plot(range(i two+1), errors grad two)
         ax[2].set xlabel(r'$Steps$', fontsize=12)
         ax[2].set ylabel(r'$Error$', fontsize=12)
         ax[2].set title('Two Humps', fontsize=14)
         fig.suptitle('Gradient Search on Outer Layer', y=0.98, fontsize = 18)
         Wout for Step: [1.88852171e+14]
         Wout for One Hump: [3.30994060e+14 1.57031116e+14]
         Wout for Two Hump: [-1.46938059e+14 -1.20798938e+14 -1.07092700e+14 -1.43
         068467e+141
         -65066801491440.9
         -365158304750451.0
         -288935616425653.1
Out[25]: Text(0.5,0.98, 'Gradient Search on Outer Layer')
```



The gradient descend function follows below steps:

- 1. Find the change in weights and bias using the forward feed functions.
- 2. Calculate the new weights and bias from 1
- 3. Estimate the new y values using the new weights and bias from 2
- 4. Find the loss using cross entropy of the new estimated y from 3
- 5. Validate against the threshold and update the variables

The plots show that the errors go up and down and they eventually reach a minimum error and plateaus. For step function and one hump, the errors are reduced to near 0 at the end, but two humps has an end error of 650. The peak errors for these three functions are between 2000 to 3000.

For the output layer, the most optimized weight values are below for each dataset:

- Wout for Step: [1.88852171e+14]
- Wout for One Hump: [3.30994060e+14 1.57031116e+14]
- Wout for Two Hump: [-1.46938059e+14 -1.20798938e+14 -1.07092700e+14 -1.43068467e+14]

The number of steps it takes each dataset to reach the optimized weight values are below:

Step Function: 3 StepsOne Hump: 15 StepsTwo Humps: 2 steps

The threshold value we used to stop the gradient\_descent function is 0.00001.

#### Question 2: Working with missing data. [50 pts]

In this exercise we are going to use the **Pima Indians onset of diabetes** dataset found in <code>pima-indians-diabetes.csv</code>. This dataset describes patient medical record data for Pima Indians and whether they had an onset of diabetes within five years. It is a binary classification problem (onset of diabetes as 1 or not as 0). The input variables that describe each patient are numerical and have varying scales. The list below shows the eight attributes plus the target variable for the dataset:

- Number of times pregnant.
- Plasma glucose concentration a 2 hours in an oral glucose tolerance test.
- Diastolic blood pressure (mm Hg).

- Triceps skin fold thickness (mm).
- 2-Hour serum insulin (mu U/ml).
- · Body mass index.
- · Diabetes pedigree function.
- · Age (years).
- Outcome (1 for early onset of diabetes within five years, 0 for not), target class.
- **2.1**. Load the dataset into a pandas dataframe named <code>pima\_df</code> . Clean the data by looking at the various features and making sure that their values make sense. Look for missing data including disguised missing data. The problem of disguised missing data arises when missing data values are not explicitly represented as such, but are coded with values that can be misinterpreted as valid data. Comment on your findings.
- **2.2** Split the dataset into a 75-25 train-test split (use random\_state=9001). Fit a logistic regression classifier to the training set and report the accuracy of the classifier on the test set. You should use  $L_2$  regularization in logistic regression, with the regularization parameter tuned using cross-validation (LogisticRegressionCV). Report the overall classification rate.
- **2.3** Restart with a fresh copy of the whole dataset and impute the missing data via mean imputation. Split the data 75-25 (use random\_state=9001) and fit a regularized logistic regression model. Report the overall classification rate.
- **2.4** Again restart with a fresh copy of the whole dataset and impute the missing data via a model-based imputation method. Once again split the data 75-25 (same random\_state=9001) and fit a regularized logistic regression model. Report the overall classification rate.
- **2.5** Compare the results in the 3 previous parts of this problem. Prepare a paragraph (5-6 sentences) discussing the results, the computational complexity of the methods, and explain why you get the results that you see.
- **2.6** This question does not have one answer and requires some experimentation. Check which coefficients changed the most between the model in 2.1-2.2 and the models in 2.3 and 2.4. Are they the coefficients you expected to change given the imputation you performed? If not explain why (supporting your explanation using the data is always a good idea).

#### **Answers**

```
In [13]: # your code here
    pima_df = pd.read_csv('data\pima-indians-diabetes.csv')
    display(pima_df.describe())
    display(pima_df.head(5))
    display(pima_df.dtypes)
    pima_df.isnull().sum()
```

Print_drvibnarr()*5am()													
	Pregnan	cies	G	lucose	BloodPr	essure	SkinThi	ckness	In	sulin	ВМІ	Diabetes	sPe
count	764.000	0000	764.000000		764.000000		764.000000		764.000000		764.000000		
mean	3.853	3.853403		922775	69.111257		20.537958		80.070681		31.998429		
std	3.374327		32.039835		19.403339		15.970234		115.431087		7.899591		
min	0.000	0000	0.	000000	0.000000		0.	0.000000		0000	0.000000		
25%	1.000000		99.000000		62.000000		0.000000		0.000000		27.300000		
50%	3.000000		117.000000		72.000000		23.000000		34.000000		32.000000		
75%	6.000000		141.000000		80.000000		32.000000		128.250000		36.600000		
max	17.000	17.000000		199.000000		122.000000		99.000000		0000	67.100000		
Pre	anancies	Glu	icose	Blood	Pressure	SkinTl	nickness	Insulin	RMI	Diah	etesPedigree	Function	Αç
0	6	<u> </u>	148	<u> </u>	72		35	0		Diab		0.627	
	1		85		66		29	0				0.351	(
1													
2	8		183		64		0	0				0.672	(
3	1		89		66		23	94	28.1			0.167	2
4	0		137		40		35	168	43.1			2.288	(
Pregnancies				i	nt64								
Glucose					nt64								
BloodPressure			int64										
SkinThickness			int64										
Insulin				nt64 at64									
BMI DiabotogRodigrooFungtion					at64								
DiabetesPedigreeFunction Age					nt64								
Outcome					ject								
dtype: object													
Pregnancies				0									
Glucose				0									
BloodPressure				0									
SkinThickness				0									
Insulin BMI				0 0									
DiabetesPedigreeFunction				-									
Age				0									
Outcome				0									
dtype: int64													

Out[13]:

```
In [14]: # Cleaning the "Outcome" values
    display(pima_df.Outcome.unique())
    pima_df.Outcome = pima_df.Outcome.replace(to_replace={'1':1, '0':0, '0\\':0, pima_df.Outcome = pima_df.Outcome.astype('category')
    pima_df.Outcome.unique()
    array(['1', '0', '0\\', '1\\', '0}'], dtype=object)

Out[14]: [1, 0]
    Categories (2, int64): [1, 0]
```

```
In [15]: # functions for future preprocessing
         def scale(fit df, trans df, na col):
              df_scaled = trans_df.copy()
              for i in fit_df.columns:
                  if i in na col:
                      fit_df_notna = fit_df[[i]].loc[fit_df[i]!=0]
                      scaler = StandardScaler().fit(fit_df_notna)
                      df scaled.loc[df scaled[i]!=0, i] = scaler.transform(df scaled[[
                      df_scaled.loc[df_scaled[i]==0, i] = [np.nan]*len(df_scaled.loc[df_scaled.loc]
                  else:
                      scaler = StandardScaler().fit(fit df[[i]])
                      df_scaled[i] = scaler.transform(df_scaled[[i]])
              return(df_scaled)
         def Xy(df, response: str='Outcome'):
              practice_df = df.copy()
              y = practice df[response]
              X = practice_df.drop(columns=response)
              return(y, X)
         def impute na(df impute, na col, method):
              df = df_impute.copy()
              for i in na_col:
                  df.loc[df[i]==0, i] = [np.nan]*len(df.loc[df[i]==0, i])
              if method == 'none':
                  df=df impute
              elif method == 'mean':
                  for i in list(df[na col].columns):
                      df.loc[df[i].isnull(), i] = df[i].dropna().mean()
              elif method in ['knn', 'lm']:
                  predictors = list(set(na col)^set(df impute.columns))
                  for i in list(df[na col].columns):
                      X pred = df.loc[df[i].isnull(), predictors]
                      y = df.loc[-df[i].isnull(), i]
                      X = df.loc[~df[i].isnull(), predictors]
                      X \text{ scaled} = \text{scale}(X, X, \text{na col} = [])
                      if method == 'knn':
                          knn = KNeighborsRegressor(15).fit(X scaled, y)
                          df.loc[df[i].isnull(), i] = knn.predict(X pred)
                      elif method == 'lm':
                          lm = LinearRegression().fit(X scaled, y)
                          df.loc[df[i].isnull(), i] = lm.predict(X pred)
                      predictors.append(i)
              return(df)
         def get_design_mat(df, na_col, impute_method='none', response: list=['Outcor
              # impute values using 'impute method'
              df impute = impute na(df, na col=na col, method=impute method)
              train df, test df = train test split(df impute, test size=0.25, random s
              # Get X, y
              y_train, X_train = Xy(train_df)
              y test, X test = Xy(test df)
```

```
# Scale
X_train_scaled = scale(X_train, X_train, na_col)
X_test_scaled = scale(X_train, X_test, na_col)

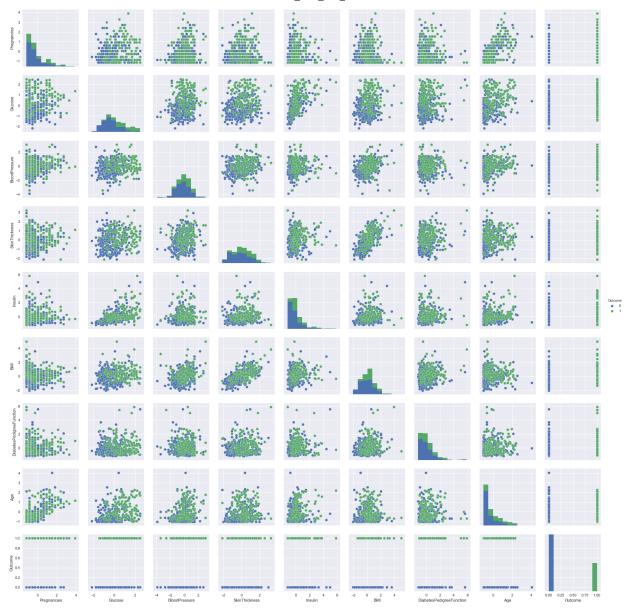
return(X_train_scaled, y_train, X_test_scaled, y_test)
```

```
In [16]: # Data Exploration
    na_col = ['Glucose', 'BMI', 'BloodPressure', 'SkinThickness', 'Insulin']
    pred_impute = []
    response = ['Outcome']
    pima_scaled=pima_df.copy()
    scale_cols = list(pima_scaled.drop(columns=response).columns)
    pima_scaled[scale_cols] = scale(pima_df[scale_cols], pima_df[scale_cols], na
    # number of na's in each column
    display(pima_scaled.isnull().sum())

# pairplot
    pima_scaled = pima_scaled.dropna()
    sns.pairplot(pima_scaled, hue='Outcome')
```

```
Pregnancies
                                0
                                5
Glucose
                               35
BloodPressure
SkinThickness
                              226
Insulin
                              371
BMI
                               11
DiabetesPedigreeFunction
                                0
Age
                                0
Outcome
                                0
dtype: int64
```

Out[16]: <seaborn.axisgrid.PairGrid at 0x1b82f5ab38>



#### **Answer:**

- 1. We notice that the predictors Glucose, BMI, BloodPressure, SkinThickness and Insulin have a minimum value of 0, but based on some research online we find that they cannot never be 0. Hence we identify this set as the columns that contain disguised missing values.
- 2. Next, we notice that our response Outcome is an object in the dataset instead of being an integer or binary. So we do a groupby() on it to investigate further and find that it has bad data. We replace values that contain '0' as 0 and '1' as 1.
- 3. Then we write functions that go into <code>get\_design\_mats()</code>, where we will scale, get X and Y matrices, identify and impute missing values, and create train and test sets.
- 4. Notice that we get maximum number of missing values in the columns SkinThickness (226 NA's) and Insulin (371 NA's). Also notice in the pairplot() above that SkinThickness shows clear correlation to BMI and Insulin shows correlation Glucose. The observations in this point are important when we do model-based imputation in 2.4. We will explain our function impute na there.

print('Test accuracy score when NAs are dropped: %s'%accuracy score(y test\_c

2.2

In [17]: # get scaled matrices

```
X_train_scaled, y_train, X_test_scaled, y_test = get_design_mat(pima_df, na
In [18]: # drop na
    X_train_dropna = X_train_scaled.dropna()
    y_train_dropna = y_train[X_train_dropna.index]
    X_test_dropna = X_test_scaled.dropna()
    y_test_dropna = y_test[X_test_dropna.index]
    logcv_sc = LogisticRegressionCV(cv=5, penalty='12').fit(X_train_dropna, y_train_t('Train_accuracy_score_when_NAs_are_dropped: %s'%accuracy_score(y_train_accuracy_score(y_train_accuracy_score_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_are_var_
```

Train accuracy score when NAs are dropped: 0.8
Test accuracy score when NAs are dropped: 0.7326732673267327

coef = {'Drop NAs': logcv sc.coef [0]}

2.3

# In [19]: # your code here X\_train\_mean, y\_train, X\_test\_mean, y\_test = get\_design\_mat(pima\_df, na\_col= logcv\_avg = LogisticRegressionCV(cv=5, penalty='l2').fit(X\_train\_mean, y\_tra print('Train accuracy score when NAs are imputed with mean: %s'%accuracy\_sco print('Test accuracy score when NAs are imputed with mean: %s'%accuracy\_score coef['Impute NAs - Mean'] = logcv\_avg.coef\_[0]

Train accuracy score when NAs are imputed with mean: 0.7713787085514834 Test accuracy score when NAs are imputed with mean: 0.7801047120418848

2.4

```
In [20]: # your code here
# Missing values imputed using KNeighborsRegressor()
X_train_knn, y_train, X_test_knn, y_test = get_design_mat(pima_df, na_col=nalogcv_knn = LogisticRegressionCV(cv=5, penalty='12').fit(X_train_knn, y_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_tr
```

Train accuracy score when NAs are imputed with KNeighborsRegressor(): 0.7 661431064572426

Test accuracy score when NAs are imputed with KNeighborsRegressor(): 0.77 4869109947644

In [21]: # Missing values imputes using LinearRegression()
X\_train\_lm, y\_train, X\_test\_lm, y\_test = get\_design\_mat(pima\_df, na\_col=na\_cologcv\_lm = LogisticRegressionCV(cv=5, penalty='12').fit(X\_train\_lm, y\_train)
print('Train accuracy score when NAs are imputed with LinearRegression(): %s
print('Test accuracy score when NAs are imputed with LinearRegression(): %s
coef['Impute NAs - Linear Model'] = logcv lm.coef [0]

Train accuracy score when NAs are imputed with LinearRegression(): 0.7643 979057591623

Test accuracy score when NAs are imputed with LinearRegression(): 0.79057 59162303665

#### Answer:

• impute\_na(): The function imputes NA's based on the method passed as an argument. Specifically for model-based methods (knn and lm) it starts with first variable in na\_cols (list of variables that contain NA's, passed as an argument) and uses all the other columns that are not in this list to predict NA's. We keep adding each element in na\_cols to our set of predictors as we go on imputing NA's.

#### 2.5

Answer: We have accuracy, corresponding to the method of imputation, in the descending order as: lm, mean, knn and drop NA's. lm does the best job as we have the two variables SkinThickness and Insulin that have maximum NA's to be linearly correlated with BMI and Glucose respectively - so we predict maximum missing values with highest accuracy with this method. Its interesting to see that mean does a slightly better job than knn - this is probably because of multi-collinearity. When we impute all the missing values for SkinThickness and Insulin with mean, our model thinks they are not important and other predictors (BMI and Glucose, as these are correlated to them) explain the variance instead. Dropping all observations with NA's is the most ineffective way as we lose useful information that could improve our results.

In order to include as much information as possible to impute missing values, we make our list na\_cols (that is passed to the function impute\_na()) in the ascending order of the number of NA's so the variables with least NA's are imputed first and are used as predictors for imputing those with most NA's - so we predict the missing values of the variables with maximum number of NA's as accurately as possible with the available information.

In [22]: pd.

pd.DataFrame(coef, index=X\_train\_scaled.columns)

Out[22]:

	Drop NAs	Impute NAs - Mean	Impute NAs - kNN	Impute NAs - Linear Model
Pregnancies	0.229560	0.412841	0.312723	0.378936
Glucose	0.734882	1.101539	0.828271	1.082110
BloodPressure	0.047397	-0.130239	-0.039781	0.105592
SkinThickness	0.135909	-0.016152	0.114843	-0.013337
Insulin	0.046651	-0.092583	0.048541	0.019272
ВМІ	0.314231	0.674449	0.470917	0.304163
DiabetesPedigreeFunction	0.221479	0.262457	0.222390	0.310531
Age	0.343882	0.150346	0.142781	0.118701

Answer: Note that the variables that show highest change in their coefficients (Pregnancies, Age, BMI, Glucose) are the variables that have no or very few missing values. Which means that - A. we do lose out on valuable information when we drop all NA's and B. That the variables with highest missing values (SkinThickness and Insulin) are being regularized and replaced by variables correlated to them. Note that linear model imputation gives us coefficients closer to the ones with dropped NA's than any other model. Let's try to increase our regularization strength and see what we get.

logcv sc = LogisticRegressionCV(Cs=5, cv=5, penalty='12').fit(X\_train\_dropna In [23]: print('Train accuracy score when NAs are dropped: %s'%accuracy score(y train print('Test accuracy score when NAs are dropped: %s'%accuracy score(y test\_c coef5 = {'Drop NAs': logcv\_sc.coef\_[0]} logcv\_avg = LogisticRegressionCV(Cs=5, cv=5, penalty='12').fit(X\_train\_mean, print('Train accuracy score when NAs are imputed with mean: %s'%accuracy sco print('Test accuracy score when NAs are imputed with mean: %s'%accuracy score coef5['Impute NAs - Mean'] = logcv\_avg.coef\_[0] logcv knn = LogisticRegressionCV(Cs=5, cv=5, penalty='12').fit(X train knn, print('Train accuracy score when NAs are imputed with KNeighborsRegressor(): print('Test accuracy score when NAs are imputed with KNeighborsRegressor(): coef5['Impute NAs - kNN'] = logcv knn.coef [0] logcv lm = LogisticRegressionCV(Cs=5, cv=5, penalty='12').fit(X train lm, y print('Train accuracy score when NAs are imputed with LinearRegression(): %s print('Test accuracy score when NAs are imputed with LinearRegression(): %s' coef5['Impute NAs - Linear Model'] = logcv\_lm.coef\_[0]

Train accuracy score when NAs are dropped: 0.803448275862069
Test accuracy score when NAs are dropped: 0.7524752475247525
Train accuracy score when NAs are imputed with mean: 0.7713787085514834
Test accuracy score when NAs are imputed with KNeighborsRegressor(): 0.7
Train accuracy score when NAs are imputed with KNeighborsRegressor(): 0.7
713787085514834
Test accuracy score when NAs are imputed with KNeighborsRegressor(): 0.78
53403141361257
Train accuracy score when NAs are imputed with LinearRegression(): 0.7643
979057591623
Test accuracy score when NAs are imputed with LinearRegression(): 0.79057

In [24]: pd.DataFrame(coef5, index=X train scaled.columns)

#### Out[24]:

	Drop NAs	Impute NAs - Mean	Impute NAs - kNN	Impute NAs - Linear Model
Pregnancies	0.244598	0.428384	0.422887	0.390673
Glucose	1.254742	1.142494	1.094012	1.114568
BloodPressure	-0.049552	-0.143579	-0.113211	0.108129
SkinThickness	0.045572	-0.029456	0.068624	-0.013340
Insulin	-0.241585	-0.109817	-0.025156	0.016736
ВМІ	0.611585	0.703629	0.632550	0.308367
DiabetesPedigreeFunction	0.328791	0.269282	0.266481	0.317155
Age	0.569583	0.148776	0.135216	0.112601

Answer: We get the same accuracy for Impute NAs - Linear Model as before, while the accuracy for Impute NAs - kNN is slightly increased and is now the same as Impute NAs - Mean. Also note how SkinThickness and Insulin are almost completely regularized in Impute NAs - Linear Model.

59162303665

In [ ]: