Determinants and areas

1. a) Compute
$$\begin{vmatrix} 1 & 2 \\ 3 & 4 \end{vmatrix}$$
.

b) Compute
$$\begin{vmatrix} 1 & -2 \\ -3 & 4 \end{vmatrix}$$
.

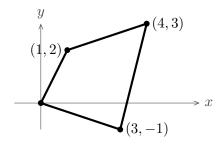
c) Compute
$$\begin{vmatrix} 3 & 4 \\ 1 & 2 \end{vmatrix}$$
.

Answer: a)
$$\begin{vmatrix} 1 & 2 \\ 3 & 4 \end{vmatrix} = 1 \cdot 4 - 2 \cdot 3 = -2.$$

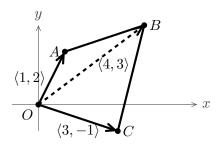
b)
$$\begin{vmatrix} 1 & -2 \\ -3 & 4 \end{vmatrix} = 1 \cdot 4 - (-2) \cdot (-3) = -2.$$

c)
$$\begin{vmatrix} 3 & 4 \\ 1 & 2 \end{vmatrix} = 3 \cdot 2 - 4 \cdot 1 = 2.$$

2. Find the area of the quadrilateral shown.



Answer:



We break the quadrilateral into two triangles. For convenience, on the figure, we have labeled the vertices \overrightarrow{OABC} and indicated the components of \overrightarrow{OA} , \overrightarrow{OB} and \overrightarrow{OC} .

Area
$$\triangle OAB = \frac{1}{2} \left| \det \begin{pmatrix} 1 & 2 \\ 4 & 3 \end{pmatrix} \right| = \frac{1}{2} |-5| = \frac{5}{2}.$$

Area
$$\triangle OBC = \frac{1}{2} \left| \det \begin{pmatrix} 4 & 3 \\ 3 & -1 \end{pmatrix} \right| = \frac{1}{2} |-13| = \frac{13}{2}.$$

Thus, area of quadrilateral $OABC = \frac{18}{2} = 9$.

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