

Cancer Applications of Choropleth Maps, and the Potential of Cartograms and Alternative Map Displays

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Abstract

Cancer atlases communicate cancer statistics over geographic domains, typically with a choropleth map. They subdivide these domains into administrative regions such as countries, states, or suburbs. When communicating human-related statistics, the choropleth has a disadvantage in that it draws attention to sparsely populated rural areas to the neglect of small inner city areas. The smaller geographic areas are important to consider if they are densely populated. Alternative map displays, such as a cartogram or a hexagon tile map, can shift the attention of map users from the large rural areas by decreasing their size on the map display. This means alternative displays can be more effective at accurately communicating spatial patterns across spatial areas, by highlighting areas of interest. It is recommended that alternative displays are included in cancer atlases. In addition, with the ease of today's technology, user interaction with the displays is encouraged. Users should also be able to interactively display different statistics, such as incidence rate or relative incidence.

1 Introduction

Researchers, health authorities, governments, not-for-profits and the media are common communicators of cancer statistics. They often present statistics to the public as aggregated values for geopolitical areas. Presenting these statistics requires aggregating individual observations for the geographical units, especially for privacy protection, but also for political and policy purposes. Examples of typical geographical units include states, provinces, local government areas, and post/zip codes. It is easy to provide counts of the diagnoses or excess deaths within these areas. However, the amount of people living in each of the areas in a set of areas will be different. Calculating incidence rates involves dividing the count by the population for each area, for example, the rate per 100000 people. Counts and population datasets are collected routinely for public health reasons and may be made available to the general public as a service to the community.

To visualize and communicate geospatial cancer statistics over geographic domain, a choropleth map is the common display. Choropleth maps show polygons representing the geographic units, where each polygon is shaded with a color according to the area-specific values of the statistic being conveyed. Visualizing this data is helpful as geographic patterns of disease may be obscured when reported in a table [1]. Providing a visual representation of cancer outcomes allows identification of geographic patterns of the disease that can then be addressed with public health policy and actions. The spatial distribution of the disease incidence can be examined using a choropleth and may reveal a trend in longitude or latitude, or rural vs urban, or coastal vs inland, or even specific hot spots of the disease. One of the key challenges with mapping spatial patterns of disease is the design of visualizations [2]. It is important to consider the strengths and weaknesses of designs, as visualizing diseases on maps is often the first step in exploratory spatial data analysis and helps in the formulation of hypotheses. This paper considers the current visualization techniques to communicate statistics to the public and their applications to cancer statistics. Alternative approaches are also considered, and the limitations of the visualization methods, highlighting the

differences and historic use of these displays.

The paper is structured as follows. The next section describes the choropleth map, which is the common approach to disease maps and presents examples of atlases in use today. Section 3 discusses the limitations of the choropleth map. Section 4 describes alternative displays, including the cartogram, which is useful when the map has heterogeneously sized geographic units. Section 5 presents the limitations of the production and use of alternative displays. Disease maps are more useful when made interactive, Section 6 describes common options, along with a discussion of benefits and disadvantages.

2 Traditional approaches for cancer map displays

A choropleth map displays the geographical distribution of data over a set of spatial units by shading areas of a map [3]. Faithful rendering of the geography, when combined with an appropriate color scheme, can reveal spatial patterns among data values. Identifying and explaining spatial structures, patterns, and processes involve considering the individuals and organizing them into representable units of communities [1]. Early versions of choropleth maps used symbols or patterns instead of color. Choropleth maps can be used for displaying disease data [5], including cancer data [6]. In epidemiology, choropleth maps are often used as a tool to study the spatial distribution of cancer incidence and mortality.

Displaying familiar state boundaries can make a map easier to read [7] and allow viewers to infer the spatial relationships visually in the data using their mental model of the geography. The map users of disease displays may include researchers, the public, policymakers, and the media [6]. For these users, the familiarity of the geography is a worthy consideration when presenting results of spatial analysis.

2.1 Cancer atlases

A cancer atlas is a map, or collection of maps, representing cancer incidence and mortality for a country, or group of countries. Atlases are key to developing hypotheses regarding areas with unusually high rates, geographic correlations, work-related exposures, and high-risk diets [8]. The data collection methods across regions and the administrative control within regions lends itself to choropleth visualization. Cancer maps and atlases dating back to Haviland's maps in 1875, and early work in US cancer atlases appearing in 1971 [9]. The presentation of cancer statistics has increased with greater access to computational power and the availability of geographic information systems software [2].

Cancer maps are effective tools for communicating incidence, survival, and mortality to a wide range of audiences, including the public and others not trained in statistical analysis. These visualizations enable non-expert audiences to interpret the outputs of sophisticated statistical analysis. Cruickshank (1947) as cited by S. D. Walter [5], discusses using visuals as a ‘formal statistical assessment of the spatial pattern’. Overwhelmingly, choropleth maps are visualisation chosen to communicate cancer statistics to members of the public and other non-expert audiences.

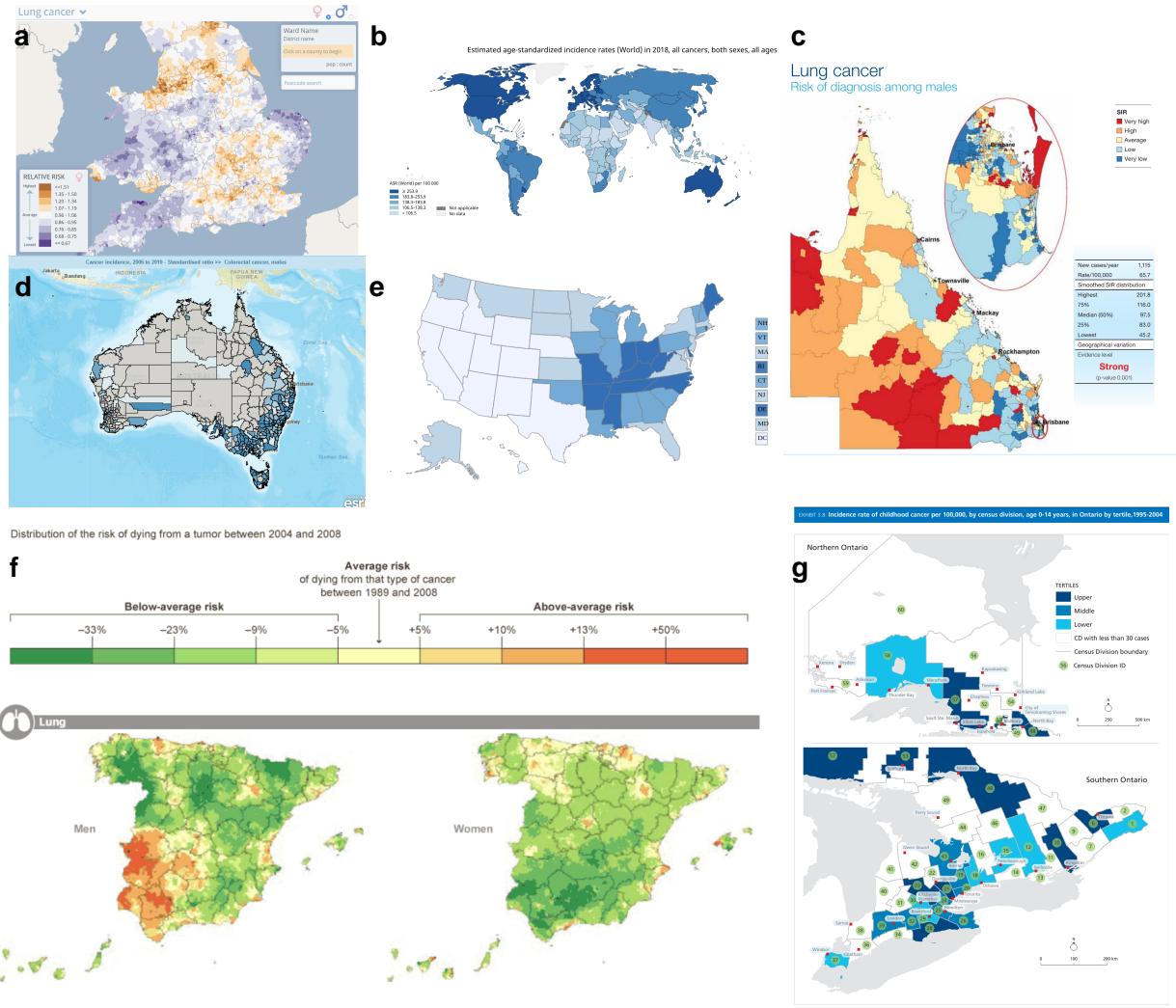


Figure 1: A selection of choropleth cancer maps from online atlases that are publicly available. Maps of various countries were chosen: United Kingdom, Australia, Spain, USA, Canada, and display several different colour palettes and legends. These atlases are described in Table 1.

Table 1: 1 A selection of choropleth cancer maps from online atlases.

Fig.	Atlas	Statistic	Data source
1a	The Environment and Health Atlas of England and Wales	relative risk for women developing lung cancer in England and Wales in 2010 [10]	Office for National Statistics (ONS) (England) and from the Welsh Cancer Intelligence and Surveillance Unit (WCISU)
1b	Globocan 2018: Estimated Cancer Incidence, Mortality and Prevalence Worldwide	age standardized incidence rates (per 100,000) for all invasive cancers for both men and women, aggregated at a national level for 2018 [11]	World Health Organization's International Agency for Research on Cancer.
1c	Atlas of Cancer in Queensland	the relative incidence ratio of lung cancer in males in the state of QLD within Australia based on data from 1998 to 2007, Queensland Cancer Council[12]	Queensland Cancer Registry
1d	Bowel Cancer Australia Atlas	the percentage of Australian males between 50 - 54 years of age diagnosed with bowel cancer in 2016 in Australia [13].	Bowel Cancer Australia
1e	United States Cancer Statistics: An Interactive Cancer Statistics Website	the incidence rate per 100,000, of all cancer types for men and women in the United States in 2016, aggregated at the state level [14].	<i>Centers for Disease Control and Prevention</i> , with data from state cancer registries.
1f	Map of Cancer Mortality Rates in Spain	side by side maps of relative risk of lung cancer for men vs women for 2004 to 2008 [15].	Map of cancer mortality rates in Spain
1g	Atlas of Childhood Cancer in Ontario	the incidence rate of childhood cancers per 100,000 (by census division) for children aged 0-14, in Ontario from 1995 to 2004 [16].	The Pediatric Oncology Group of Ontario Networked Information System

Epidemiologists and statisticians have developed the statistics used to communicate the burden of cancer over several decades. Table 2 summarizes the measures commonly presented in published cancer atlases. Mortality rates are commonly presented as relative rates of risk across the population and age-adjusted to correct for the higher prevalence of cancers in older populations. Stock developed the standardized mortality ratios through the 1930s, this is described by Howe [17].

Table 2: 2 Common measures for reporting cancer information.

Measure	Details
1. Count	Crude cancer counts
2. Rate per 100,000	Cancer incidence per 100,000 population
3. IR (Incidence Ratio)	$(IR)_i = \frac{(Incidence\ Rate)_i}{Average\ Incidence\ Rate},$ The cancer incidence rate in region i over the average cancer incidence rate for all of the regions
4. Age-Adjusted Rate per 100,000	Standardized by age structure or region
5. Age-Adjusted Relative Risk	Standardized by age structure in each region i
6. SIR (Standardized Incidence Ratio)	Incidence standardized by population at risk in each region i
7. Below or above Expected	An alternative expression of the SIR
8. RER (Relative Excess Risk)	$RER = \frac{(Cancer\ related\ mortality)_i}{Average\ cancer\ related\ mortality}$ Represents the estimate of cancer-related mortality within five years of diagnosis. Also referred to as ‘excess hazard ratio’

Roberts [18] identified 33 cancer atlases published between 2010 and 2018. Each of these online atlases uses choropleth maps. All except one of these were published by non-commercial organizations, including not-for-profits, government, research organizations, advocacy groups or government-funded partnerships. Figure 1 displays a subset of maps from these atlases, the selection varies in the geographies explored. Figure 1b shows Globocan 2018 [11] which explores Estimated Cancer Incidence, Mortality and Prevalence Worldwide using data sourced from cancer registries of each country. The Bowel Cancer Australia Atlas in Figure 1d presents an example of a cancer specific atlas, it shows the average Standardized Incidence Ratio of colorectal cancer for Australian males from 2006 to 2010 in Australia [13]. Like many of the atlases examined, there is a choice of gender displayed in the Bowel Cancer Atlas. An alternative approach used in the Map of Cancer Mortality Rates in Spain, Figure 1f shows side-by-side maps of the relative risk of lung cancer separately for men and women [15].

There are vast differences in the geographies considered by online atlases. Figure 1b shows global age-standardized incidence rates (per 100,000) for all invasive cancers for both men and women, aggregated at a national level for 2018. The United States Cancer Statistics [14] presented in Figure 1e contains the incidence rate per 100,000, of all cancer types for men and women in the United States in 2016, aggregated at the state level. The Environment and Health Atlas of England and Wales, Figure 1a shows the relative risk for women developing lung cancer in England and Wales in 2010 [10] at a neighborhood (small-area) scale. The Atlas of Cancer in Queensland, Figure 1c shows the relative incidence ratio of lung cancer in males for each Statistical Area at Level 2 [19] in the state of Queensland within Australia [12].

Age-specific atlases are less common, Figure 1g displays Atlas of Childhood Cancer in Ontario, this communicates the incidence rate of childhood cancers per 100,000 (by census division) for children aged 0-14, in Ontario from 1995 to 2004 [16]. This atlas communicates information regarding a small geographic region.

2.2 Additional considerations

Cancer atlases often display supplementary graphs and plots to add more information. Additional materials such as tables, graphs, and text explanations support understanding and inference derived from maps, ensuring the message communicated will be consistent across a range of viewers [6]. The many displays of statistical summaries, including dot plots, bar plots, box plots, cumulative distribution plots, scatter plots, and normal probability plots, can provide alternative views of the cancer statistics. These can also display supporting statistics such as error, confidence intervals, distributions, sample or population sizes, and standard deviation.

The statistics communicated in atlases are often used to describe differences between areas. This can occur at different levels of aggregation. Aggregation of global health statistics occurs within administrative and arbitrarily defined regions, such as those used by the World Health Organization and the United Nations [20]. World atlases can allow for displays of data aggregated into continents, countries, states, provinces and congressional districts [14]. Each population area will probably have a different number of people. Cancer atlases may also communicate the distribution of the population living in all areas in a table or histogram display [21]. Atlases can connect the population to the land available to them by communicating population density. Section 4 considers alternatives to choropleth that introduce population into the visualizations.

Map users can define the population further using the demographics of the individuals within each area. Demographics that can influence cancer rates include information regarding the age and sex distribution of the areas presented. Some digital atlases surveyed allow users to control the display to select subsets such as males, females or those aged over 65. Similarly, socioeconomic indicators, such as unemployment rates, poverty rates, remoteness, and education levels, can explain how the experience of cancer prevalence varies for various members of society. Few atlases provide this level of detail.

Introducing population and demographic information helps to interpret the rates in areas effectively, but there will still be uncertainty around the rates. To address this, a cancer atlases often communicates uncertainty about the value of a statistic. There are several potential sources of uncertainty: sampling error, errors arising from the disease reporting process (or data collection), and errors arising from the statistical modeling or simulation process. The most common measures used to represent uncertainty were credible or confidence intervals (CIs). Displaying the uncertainty associated with reported statistics is a vital feature of a cancer map, but it is difficult to display effectively. The map focuses on displaying the statistic and lacks additional space to represent the uncertainty. Providing an adjacent map or overlaying maps with symbols [22] are two approaches.

3 Limitations of choropleth displays

Australia presents an extreme case of an urban rural divide. The land mass occupied by urban electoral districts is only 10% of Australia, yet 90% of the population live in these urban areas [23].

Choropleth maps provide a familiar display, which shows data in a geographically recognisable way. A disadvantage is that the different population and geographical sizes of administrative areas can attract attention to the shades of the underpopulated but large areas [3]. Skowronnek also [4] discusses how choropleth maps suffer from area-size bias, as they give a ‘stronger visual weight’ to large administrative units. The administrative boundaries used to define regions may limit a choropleth display, as this display unfaithfully represents the disease distribution across the region

by obscuring small geographic areas. Sparsely populated rural areas are emphasized, whereas the areas representing inner city communities are very small. This is especially true for Australia.

Choropleth maps colour each geographic unit to allow map users to measure the value of the statistic [3]. Map users contrast the colours in neighbouring areas to understand the spatial distribution. Map creators must choose an effective colour scheme, but it is a difficult task [24]. The ColorBrewer system supports map creators in the decision making process, but this does not fully provide perceptual colour specifications. When communicating information using colour, a map creator should use a scheme that has a linear color gradient, with perceptually uniform color spaces to convey that equal steps in data align with equal steps in the colour scheme [25].

The use and colors of borders and backgrounds can also change the appearance of the colors representing the value of the statistics [24]. These supports are important, though, to allow a reference point to orient users to the geographic regions.

Inset maps like in Brisbane city in Figure 1c of the state of Queensland are commonly used to reduce distorted interpretations, but it is a bandaid remedy. For Australia, many, many inset maps would be needed.

c of the state of Queensland are commonly used to reduce distorted interpretations, but it is not always an appropriate solution. As this feature of population distributions continues to intensify, the need for cartograms as an alternative to a choropleth map should only increase. ->

4 Contemporary alternatives to choropleth maps

4.1 Cartograms

Choropleth maps imply uniformity of data across the geographic space but population densities are unlikely to be uniform [4]. Cartographers developed the cartogram to draw the attention to the population by transforming the map [26]. The resulting display can communicate the impact of the disease more accurately across the population, as recorded by the statistic, at the sacrifice of geographic accuracy.

When a map creator desires a uniform population density of the map base, the purposeful distortion of the map space is beneficial. The “population distribution is often extremely uneven in former British colonies” [23], and this makes the distortion necessary, [27] population will then become a uniformly distributed background for the statistic presented [28]. An area cartogram [29], or population-by-area cartogram [30] occurs after the distortion of the geographical shape according to population. Event cartograms change the area of regions on a map depending on the amount of disease-related events, but this does not consider the effects of land area and population [22].

Cartograms provide an alternative visualization method for statistical and geographical information. The key difference between a choropleth and a cartogram is the desirable augmentation of the size, shape, or distance of geographical areas [23]. Monmonier [31] suggests that map creators can use white lies to create useful displays by distorting the geometry and suppressing features. It is easy for the average person to disregard the impact of transformations used to create cartograms. One disadvantage of the conventional map is interpreting spatial patterns is difficult because of the sparsely populated rural areas being emphasized in a choropleth map, and the inner city areas are geographically small. The distortion of each area when making a cartogram is proportional to a value other than the actual earth size area [29]. The distortion in an area cartogram accounts for the population density, preventing it from obscuring the spatial patterns [30]. The spatial transformation

of map regions relative to the data emphasizes the data distribution instead of land size [32]. When visualizing population statistics, Dorling [23] considers this design ‘more socially just’, or honest [33], giving equitable representation and attention to all members of the population and reducing the visual impact of large areas with small populations [5]. Howe [17] suggests that ‘cancer occurs in people, not in geographical areas’ and that spatial socio-economic data, like cancer rates, are best presented on a cartogram for urban areas as the population map base avoids allocating ‘undue prominence’ to rural areas [27].

The creation of cartograms was historically in the hands of professional cartographers [34]. Early approaches by John Hunter and Jonathan Young (1968) and Durham’s wooden tile method, Skoda and Robertson’s (1972) steel ball-bearing approach and Tobler’s (1973) computer programs [23]. Howe [17] discusses the impact of electronic computer-assisted techniques. Geographical information systems allow map creators to produce cartograms and they use these systems depending on ‘the effectiveness, efficiency, and satisfaction of the map products’ [34].

There are many issues to consider when creating alternative map displays: the intended audience of the map, and its purpose are key points in cartogram use and creation as ‘there is no “best” cartogram or method of creating cartograms just as there is no “best” map’ (Monmonier and Schnell, 1988) [23]. Nusrat and Kobourov [35] provided a framework to investigate implementations of the many algorithms presented, and the “statistical accuracy, geographical accuracy, and topological accuracy”.

Table 3: 3 Maps used to present statistics for the United States of America. The colour of each state communicates the average age-adjusted rate of incidence for lung and bronchus for females and males in the United States 2012-2016.

Map display	Details
a. Contiguous	It has distorted each state’s shape according to the population of the state in 2015. The state of California has become much larger because of the large population density. This draws attention to the densely populated North-East region and detracts from the less populated Mid West.
b. Non-contiguous	It maintains the geographic shape of the states, but the size has altered according to the population of the state in 2015. The state of California has remained closer to its original size than its surrounding states. The North-East states have remained closer to their geographical size, for Massachusetts and Connecticut. This draws attention to the densely populated North-East region and the sparse Mid West.
c. Dorling	Circles are used to represent each state, but the population of the state determines the size in 2015. The North-East states remain closer to their neighbors and are slightly displaced from their geographic location. It highlights the sparsity of the population in the Mid West by the distance between the circles at the geographic centroids.

Map display	Details
d. Hexagon Tessellation	A hexagon of equal size represents each state. It is easy to contrast the neighboring states however the North-East regions have been displaced from their geographic location. It highlights the sparsity of the population in the Mid West by the light yellow color, the Age-Adjusted rate in Kentucky is the darkest and its neighbors are similar.

Figure 2 shows four different cartograms for the same data. The information in Table 3 summarizes what can be observed in the four types of cartograms.

4.1.1 Contiguous

A contiguous cartogram alters the choropleth according to a statistic and maintains connectivity of the map regions. Min Ouyang and Revesz [36] present three algorithms for creating value-by-area cartograms. They implement ‘map deformation’ to account for the value assigned to each area. Other methods include Tobler’s Pseudo-Cartogram Method, Dorling’s Cellular Automaton Method [23], Radial Expansion Method of Selvin et al., Rubber Sheet Method of Dougenik et al., Gusein-Zade and Tikunov’s Line Integral Method, Constraint-Based Method (Kocmoud and House) [32].

Figure 2 a shows a population contiguous cartogram of the United States. All states are visible and the shape of the United States overall is still recognizable. In contrast, Figure 3 a shows an Australian contiguous cartogram also based on population. The south east is completely distorted, areas with low population are still large very the map, as their initial area was used to determine the area allocated in the contiguous cartogram.

To be able to recognize the significant changes, a reader will usually have to know the initial geography to find the differences in the new cartogram layout [29]. Tobler’s Conformal mapping means to preserve angles locally so that the shapes of small areas on a traditional map and a cartogram would be similar. [32] presents this issue as conflicting tasks or aims, to adjust region sizes and retain region shapes.

4.1.2 Non-contiguous

Non-contiguous cartograms prioritize the shapes of the areas instead of connectivity. Each area stays in a similar position to its location on a choropleth map. Displaying the choropleth map base allows map users to make comparisons regarding the change in the area. The addition is the gap between areas, created as each area shrinks or grows according to the associated value of the statistic. Olson [29] discusses the creation of these maps and the significance of the empty areas left between the geographic boundaries and the new shape. It is the ‘difference from the original map that is the real message’ of these displays.

The distortion of region shapes on the contiguous cartogram presents an additional hurdle to visual recognition, and the non-contiguous cartogram eliminates this hurdle, and presents the meaningful empty-space property [37].

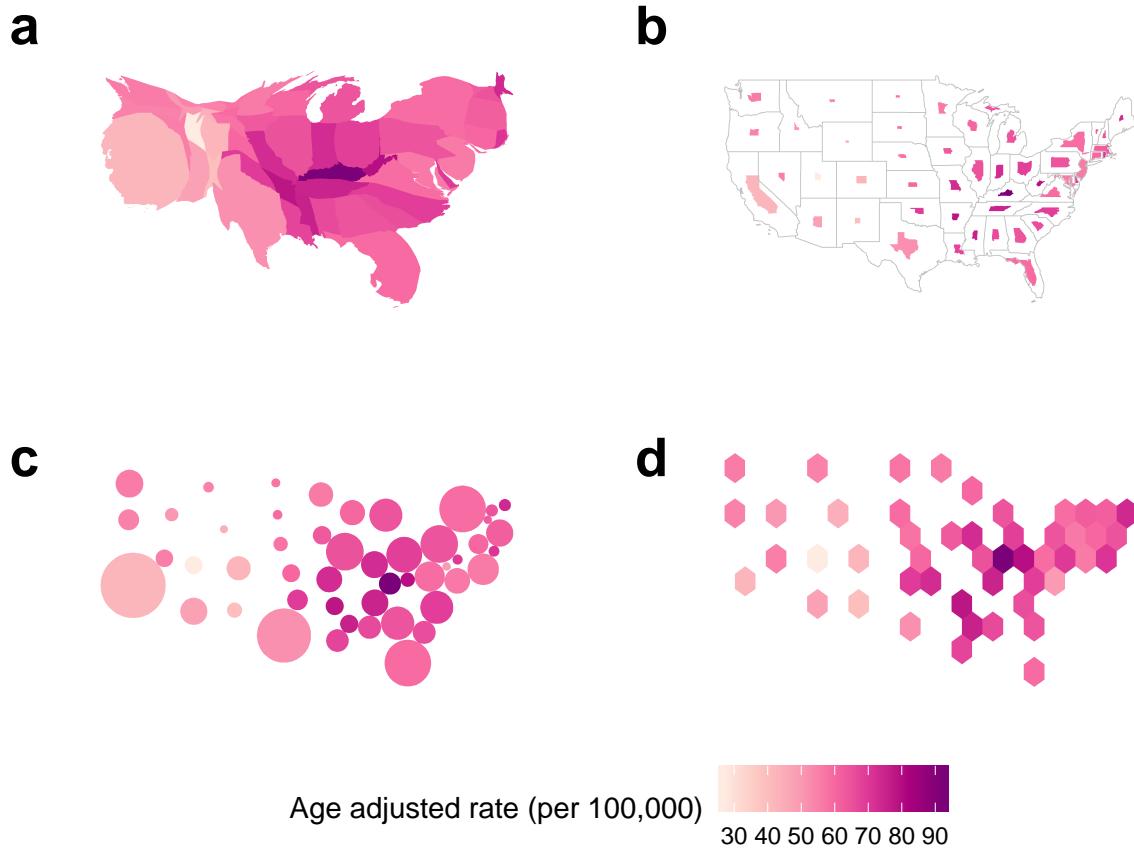


Figure 2: Common alternatives to maps, showing the same information for the United States of America: (a) contiguous cartogram, (b) non-contiguous, shape-preserved cartogram, (c) Dorling cartogram (non-contiguous), (d) hexagon tilemap (non-contiguous). Maps (a) - (c) are created by resizing and reshaping the states of the USA to match the 2015 population of the state. This provides a better sense of the extent of disease relative to the population in the country and can help ease losing information about physically small but population-dense states. Map creators give each state equal size and thus equal emphasis in (d) the hexagon tile map.

4.1.3 Dorling

Daniel Dorling presents an alternative display engineered to highlight the spatial distribution and neighborhood relationships without complex distortions of borders and boundaries. Daniel Dorling puts forward a simple question and his approach opposes preserving the intricate shape details [23]:

“If, for instance, it is desirable that areas on a map have boundaries which are as simple as possible, why not draw the areas as simple shapes in the first place?”

He acknowledged the sophistication of contiguous cartograms but critiqued their ‘very complex shapes,’ he answers this with his implementation of maps created using ‘the simplest of all shapes’. Circular cartograms use the same simple shapes for every region represented and resize the shapes according to the statistic represented or the population for a base map. This familiar shape may be more effective for understanding the spatial distribution than contiguous cartograms. Contiguous cartograms use a gravity model to apply distortions to create the ‘nonsense’ shapes that have ‘no meaning’ [33]. This method applies a gravity model to produce a compelling map, that avoids overlaps and keep spatial relationships with neighboring areas over many iterations. This implementation can work for up to ‘one hundred thousand’ areas.

Raisz laid the groundwork for this approach in the mid-1930s, and his rectangular cartograms provide dramatic comparisons and are especially useful for correcting misconceptions communicated by geographic maps. [38] quotes the official definition of Value-Area Cartograms, the simplistic displays which represent each area as a single rectangle, sized according to the value of the statistic. This rectangular display may sacrifice contiguity but allows for tiling where geographic neighbors placed in suitable relative positions also share borders [39]. Rectangular cartograms communicate bi-variate displays of the population by the size of each rectangular, and they use color to communicate a second variable [40].

4.2 Tile Map

A tile map provides a tessellated display of consistent shapes. A similar method to a rectangular cartogram, represents each geographic area using a square. The squares are tessellated to create a grid. This method has been used broadly in the media by FiveThirtyEight, Bloomberg Business, The Guardian, The Washington Post, The New York Times and NPR. Each area is represented by a square of the same dimensions, each tile is usually one unit of measurement, this could be geographic regions such as states or population-based that use a consistent measure of population for each tile. Regions with over four neighbors require some necessary displacement. The tile map uses color to represent a value of a statistic for each area. A similar method to a rectangular cartogram represents each geographic area using a square of the same dimensions. The squares tessellate to create a grid. There are online media sources using this method, these include NPR, FiveThirtyEight, The Wall Street Journal, The Washington Post. Tile maps may be difficult to create as they are best created manually, they require additional time and care as the number of geographic areas to include increases.

Cano and others [41] define the term ‘mosaic cartograms’ for hexagonal tile displays, where the number of tiles for each area or the color of them can communicate the statistic of regions. When using several tile per regions, map makers can adjust the complexity of the boundaries in the resulting display. They can also make a trade-off between boundary complexity and simplicity by the size of the tiles used.

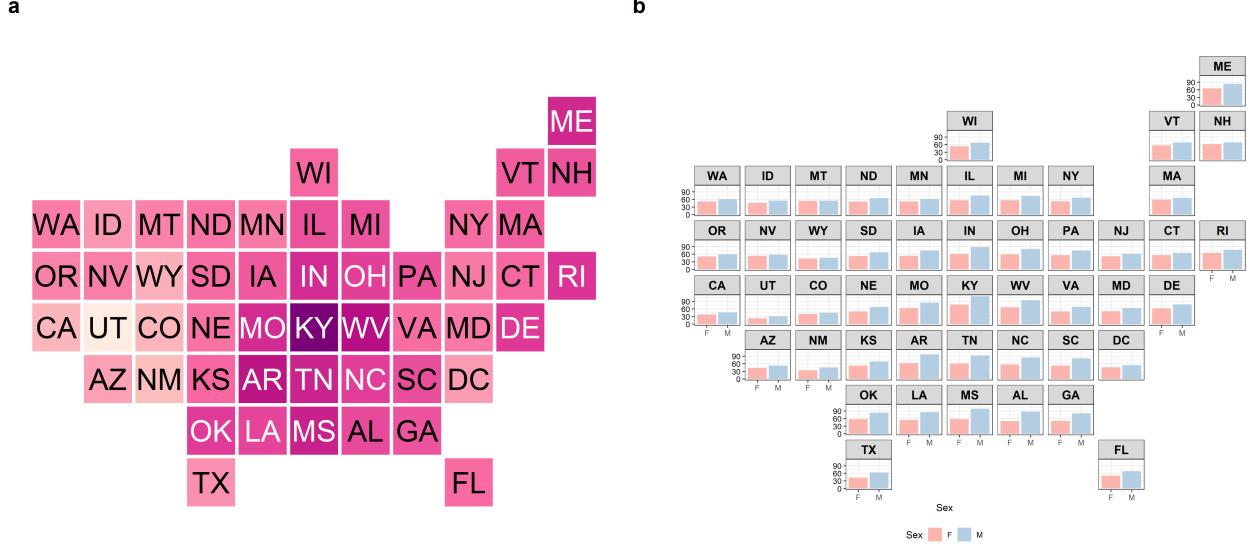


Figure 3: Two alternative displays, tile map (left) and geofaceted map (right), showing state age-adjusted rate of incidence for lung and bronchus in the USA. In the tile map, the layout approximates spatial location, with each state being an equal box filled with color representing cancer incidence. The geo-faceted map shows bar charts laid out in a grid approximating the spatial location of the state. The maps show age-adjusted rates for males and females. This display allows the presentation of multiple variables for each geographic area.

4.3 Geofacet

Hafen [42] formalizes the term geofaceting to describe a grid display, the arrangement of tiles to create a grid that mimics the geographic topology of the set of areas. Like tile maps, they can reuse the arrangement of the areas for other spatial distribution visualizations. Geofaceting has the functionality of facets, often used to replicate visualizations for each subset of the data. Here, the data subsets are geographic. A tile map communicates one value per region in a visualization, geofaceting is a more flexible visualization for communication as it increases the amount of information displayed. Virtually any plot display can be shown in the tile representing the areas, allowing displays of multiple variables or values per geographic entity. Creating a tile map or a geofacet both require manual creation of the grid, except for the grids that other have already contributed.

4.4 Multivariate displays

Pickle and others [43] present linked micro map plots to match geographic and statistical data visually, this serves as a solution to multi-dimensionality issues. An online atlas of US states uses this display. These maps group areas based on their value for one variable, and additional columns provide displays that contrast the areas in each group by other variables. The display juxtaposes choropleth maps and statistical plots; it shows one map per group of the key separating variable, in a row with each additional statistical plot. Linked micro maps predominantly use the choropleth map for displays of spatial relationships. These maps show spatial relationships by allotting spatial neighbors to the same group. It is one of several alternative displays that allow maps to become bivariate displays, commonly used to present both an estimate and the associated uncertainty.

Bivariate choropleth maps [44] blend color schemes to convey the intersection of categorized levels of an estimate and the associated uncertainty for each spatial area. Lucchesi and Wikle [44] also suggest map pixilation, it breaks each region into small pixels, and allocates values to the individual pixels to create texture. This reflects the uncertainty around the area’s estimate by randomly sampling from the confidence interval of the estimate of the area. Animating these displays involves resampling the pixels for each frame. Areas with uncertain values will flicker more dramatically than areas with more certain values.

5 Comparison and critique of alternative displays

5.1 Neither choropleth maps or cartograms perform well for Australia

Figure 3 shows four main types of cartograms displaying melanoma incidence on Statistical Areas at Level 3 [19] in Australia. The version of a contiguous cartogram (a) has expanded the highly populated areas while preserving the full shapes of rural areas. It has not fully resolved the population transformation of areas, and if it had accurately sized areas by population, the country would be unrecognizable. The shape-preserved cartogram is unreadable, and it has reduced all areas to tiny spots on the map. Zooming in on a high-resolution output shows it does preserve the areas. The Dorling cartogram and the hexagon tile map provide reasonable displays of the spatial distribution, despite having too much white-space in the outback areas.

5.2 Limitations of alternative displays

Cartograms provide the spatial distortion to more accurately convey the statistical distribution, focuses on the human impact of the disease. However, the transformation of contiguous cartograms often occurs at the expense of the shape of areas [32]. When the population density of the geographic units is highly dissonant with geographic density, the cartogram will lose all spatial context. Dorling [23] has a cartogram showing the 1966 general election results, which looked very little like the geographical shape of Australia.

Some mix of tiling, faceting or even micro maps, which allow some spatial continuity while also zooming into small areas, are good solutions for difficult geographies. Table 3 summarizes the key criteria for testing maps and alternative displays. Moore and Carpenter [1] and Bell et al. [6] provide suggestions and comments to help map creators best communicate their health data and spatial analysis.

Table 4: 3 Summary of features and constraints of common mapping methods used to display cancer statistics (Y=Yes, N=No, S=Sometimes).

	Choropleth	Contiguous	Non-contig	Dorling	tile maps	Geofacets
Spatial distortion	N	Y	Y	Y	Y	Y
Preserves neighbors	Y	Y	Y	S	S	S
Conceals small areas	Y	S	N	N	N	N
Uniform shape	N	N	N	Y	Y	Y
Univariate only	Y	Y	Y	S	S	N
Manual construction	N	N	N	N	Y	Y

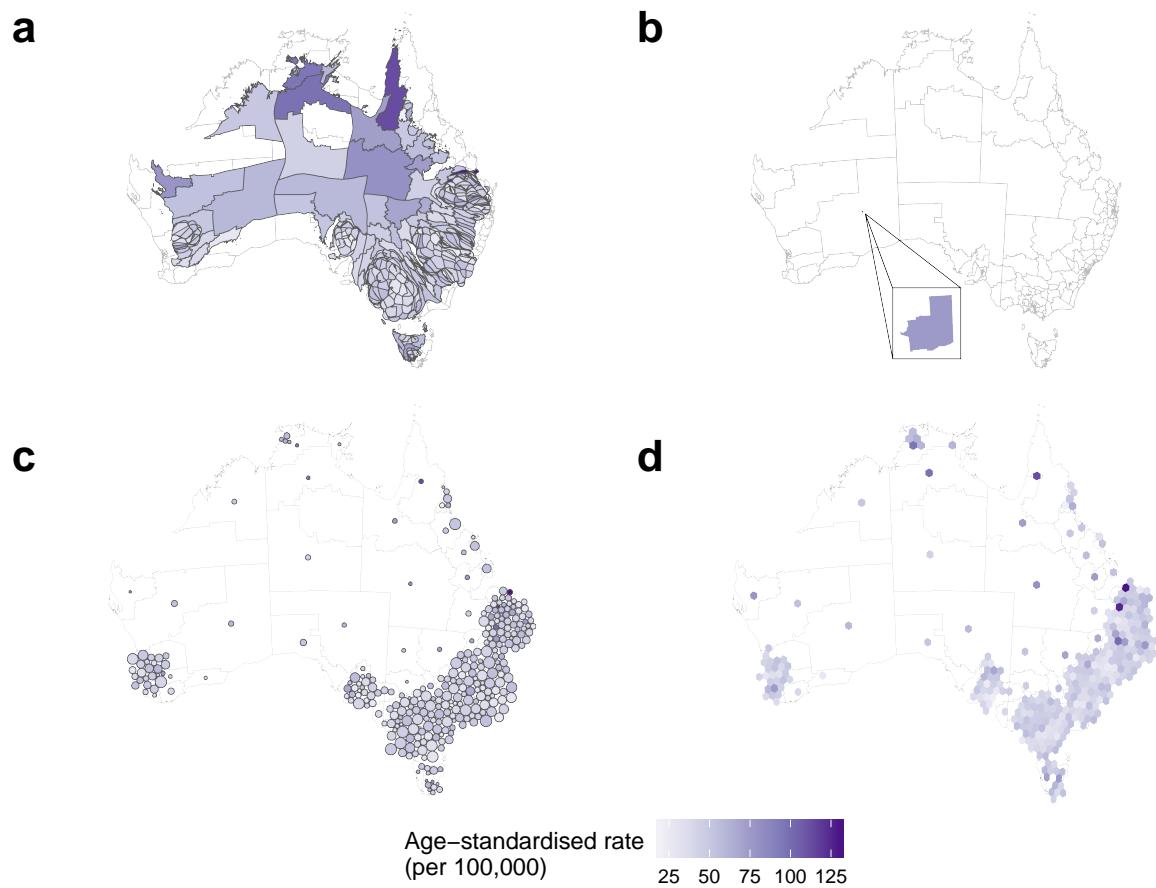


Figure 4: Cartograms showing melanoma incidence in Australia: (a) contiguous, partially population transformed, (b) non-contiguous shape preserved, (c) Dorling, (d) hexagon tile map. The contiguous cartogram has expanded the highly populated areas while preserving the full shapes of rural areas. If it accurately sized areas by population, the country would be unrecognizable. The shape-preserved is unreadable due to the small area sizes. The Dorling cartogram presents all areas but many are difficult to compare. The hexagon tile map provides a reasonable spatial distribution despite having isolated hexagons in the outback areas.

6 User interaction

One of the concerns of adding too much information to a map is the fear of cognitive overload [45] in which the user reaches an information threshold, beyond which will not be able to make sense of the information. It can be a juggling act for a diverse audience, with experts probably preferring more detail [46]. Interactivity is a design feature within modern mapping methods that can be used to incorporate additional information and complexity without overloading the user. Effective user-centred interactive actions produce rapid, incremental, and reversible changes to the display [47].

Monmonier [31] says that interactivity can be used to allow users to explore the map for more information and provides flexibility for the display. The user can toggle between different variables, map views or even multiple realizations of future scenarios [48]. This provides additional mechanisms for the users to digest the uncertainty of the available information [49]. When the needs of the audience are changeable and are also the priority, the map creator can allow interactivity for map users to explore a data set through dynamic interactions. This can allow inspection of the data from many views [51]. User interaction with maps helps to understand and interpret the spatial distribution of disease, to validate, explain or explore the presented statistics and their relationships to each other [52].

Interactivity enables supplementary information to be incorporated into online atlases without cluttering the display. Interactive design features, found in online cancer maps, include tool tips, drop-down menus, data selection, zooming, and panning allow users to explore the map as they want more information and allow flexibility in the display [31]. The use of these supports can be found in various online cancer maps [18].

Animation, in contrast to interactivity, usually involves pre-computing views and showing these in a sequence. An overview of animation in association with the R package `ggridge` [53], with some focus on maps, explaining transitions between frames in a linear, to provide a fixed narrative to passive users [54]. Animations are used to communicate a message by capturing and directing users' attention. It is most often employed to show changes over time. The controls for basic animation are usually placed outside of the plot space [54], the map image is updated/replaced as the animation progresses.

Weather maps are a thoroughly developed example of animation of spatial displays to communicate information to the general public [6]. The movement of a weather system will follow a forecasted path, all map users can follow the animated path of the weather system across the geography over a specified period.

The Australian Cancer Atlas [55] provides tours that change the display to draw users' attention to areas on the map that are relevant to the story. This implementation of animation gives users tools to plan their exploration.

6.1 Under-utilized techniques

Figure 7 shows two examples of more sophisticated interactive maps. The Spanish Cancer map (left) contains a linked display between a choropleth map and time series plots of cancer change. In linked plots, changing values in one display will trigger changes of corresponding elements in another display. Here, the temporal change in the choropleth map can be played out as an animation. Mousing over the time series plots will highlight the line for a particular region. The Canadian

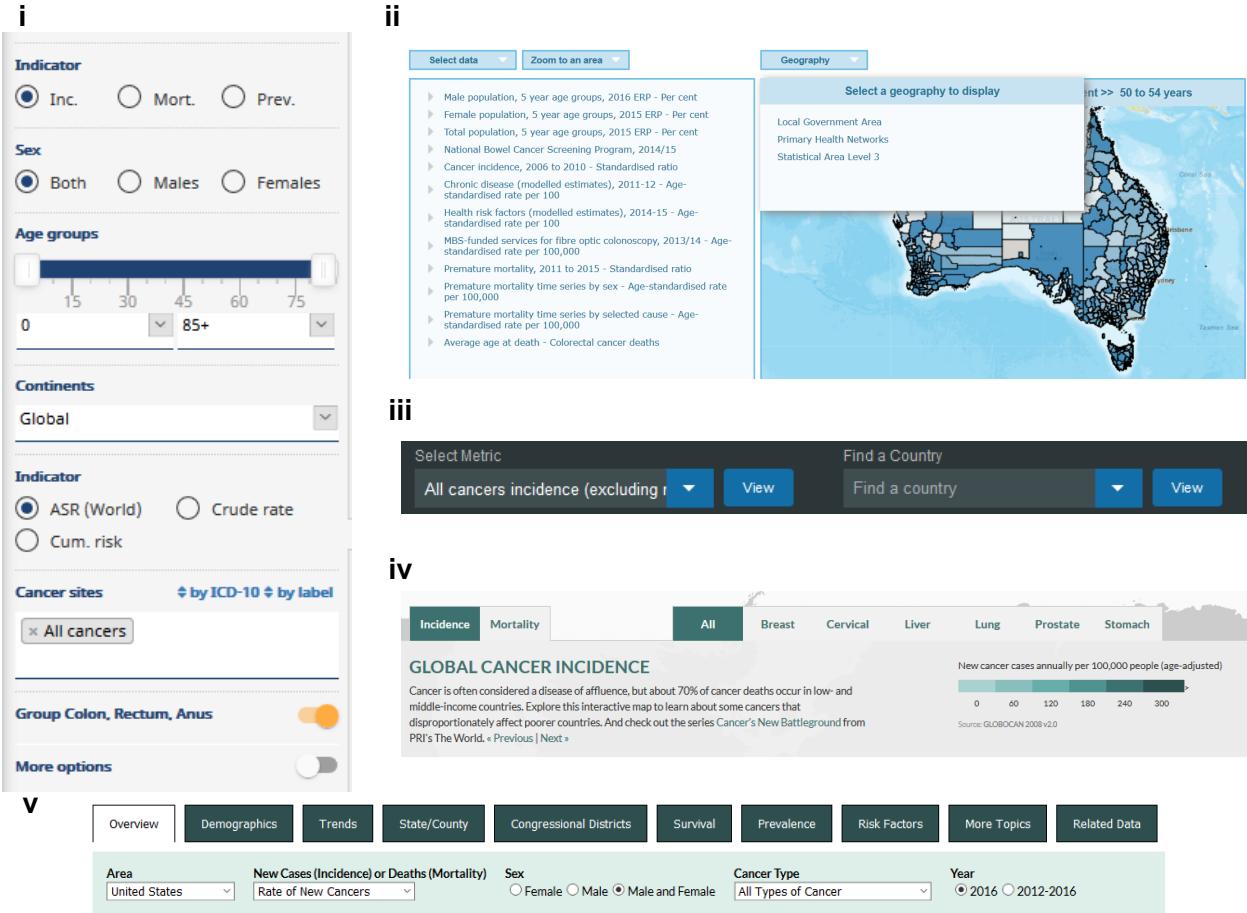


Figure 5: Interactive controls of displays in publicly available choropleth cancer maps: (i) GUI controls for statistic, sex, age groups, continents, and cancer types for Globocan 2018: Cancer Today, (ii) Menus for variable selection and zooming on Bowel Cancer Australia Atlas, (iii) Menus for choosing variables and countries in The Cancer Atlas, (iv) Tabs for different indicators and cancer types in Global Cancer Map, (v) Menus and toggles for variable and subset selection in United States Cancer Statistics: Data Visualizations.

Breast Cancer Mortality map (right) has a magnifying glass that allows the user to zoom into small areas. It is easy to control and shows precise details in small areas.

7 Conclusions

This paper provides an overview of mapping practices as commonly used for cancer atlases and recommends new approaches, such as cartograms and hexagon tile maps that should be adopted going forward. The conventional approach is the choropleth map, and it is widely used. The choropleth map suffers when there are small geographic units, as occurs in Australia where the population is concentrated on the coast, the information about the burden of cancer on those communities can be hidden. Making an inset can clarify congested regions but this breaks the viewers' attention as they shift focus from the map to the inset, and if there are many congested areas, many insets would be needed. The map alternatives implement tradeoffs between the familiar

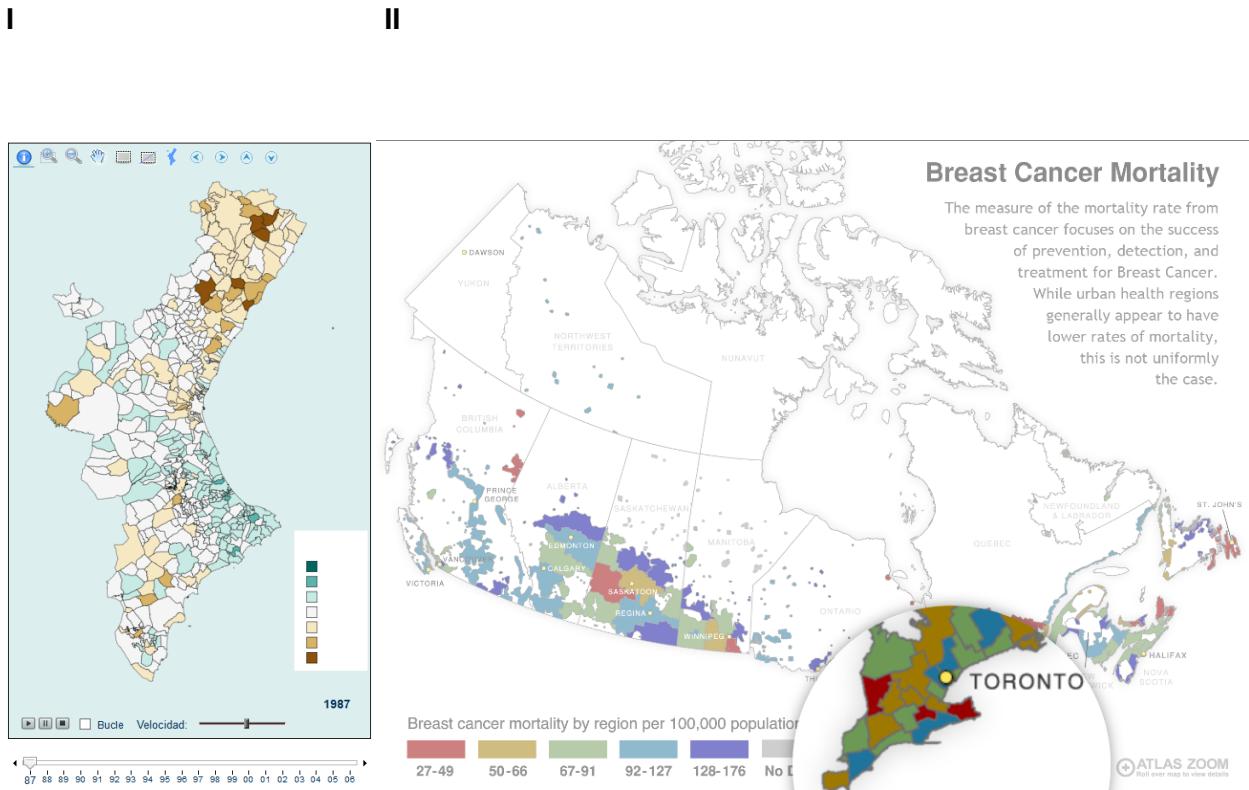


Figure 6: Two examples of advanced interactivity (and animation) in publicly available choropleth cancer maps: a. Linked maps and time-series line plots, with temporal animation in Map of Cancer Mortality Rates in Spain, b. A highly responsive magnifying glass on a map of Breast Cancer Mortality in Canada.

shapes, and the importance of the geographic areas in the context of the areas. Given the population or a cancer statistic for each area, the geographic size or shape will change. Alternative displays allow the spatial distribution of cancer data to be digested by map users.

Many statistics are commonly used in cancer displays. The most basic is the incidence rate. It is common to see relative rates which measure how far a region is above or below the average. The purpose of using a relative rate is, perhaps the desire to pinpoint the areas that need attention because they have higher than expected rates. A region might be much higher than average, but it may not be close to a health concern, because all regions have a low incidence. Supplementary materials can allow map users to recognise when this occurs.

Interaction with maps is an important component of public atlases, and is easy to add with today's technology. The purpose is to provide access to more information than is possible to display in a single map, without overwhelming the viewer. Too many choices can similarly overwhelm a viewer, and thus decisions do need to be made about content to provide for accurate and comprehensive communication of information. Similarly, providing ways for users to interact with the display encourages engagement, and creative, efficient, elegant, interactive tools elicit curiosity about the data.

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Files to reproduce the paper, and code to reproduce the plots, are available at <https://github.com/srkobakian/review>.

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