Machine Learning Strategies in Cribbage

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Contents

1 Introduction

I just want to see if unicode characters will appear. Jag måste se om unicode-characterer funger. minä haluan katsoa kirjain öööö.

Generic introductory stuff giving a sentence or probably a paragraph about each of the sections covered.

1.1 Cribbage

Cribbage is a multi-phase card game, typically played between two opposing players. While variants exist for three or more players, this paper will focus on the two-player variant. The game presents an interesting research area because of its unique scoring methodology: each hand is counted in two various ways each round and the first player to reach as score of 121 points or more is declared the winner. Because of this atypical win condition, different strategies hold differing levels of importance throughout the game.

1.1.1 Rules of the Game

In order to be able to understand the crucial nature of the temporally dependent strategies, the rules and flow of a game of cribbage must be fully understood. While a complete set of tournament rules can be found at [ACC], what follows is an overview complete enough such that a novice player, following the scoring rules found in Appendix 6 could play a complete game, albeit likely not well.

The zeroth step taken once per game is to determine which player will be the dealer for the first round. The player who is not the dealer is called the pone. Each player cuts the deck once to get a single card. The player with the lower-valued card is the dealer; the other player is called the pone. From there, the usual round structure begins and proceeds in the following steps:

1. Each player is dealt 6 cards.

2. Each player selects 4 cards to keep for their own hand and 2 cards to toss into the crib.

3. A random card is cut from the remaining cards of the deck and placed face-up on top of the deck. If this cut card is a Jack of any suit, the dealer is awarded 2 points and pegs the points accordingly.

4. Starting with the pone, each player alternates playing a single card, keeping track of the total value of all card played so far, until all cards have been played, or neither player can play a card without exceeding a collective value of 31. In the latter case, the player last to play a card will be awarded points before the count is reset and play continues. If any of the combination of cards mentioned

in Appendix 6 is seen in the immediately preceding cards, the amount of points earned is immediately pegged on the board for the appropriate player. In cribbage terms, this is called *the play*.

5. After all cards have been played, the pone then counts his or her hand using the randomly cut card as a 5th card in hand before pegging these points on the board.

6. The dealer then proceeds to count his or her hand and peg the points in the same fashion, also considering the randomly cut card to be the 5th card in the hand.

7. The dealer then does the same for the crib.

8. The dealer and the pone swap roles and repeat from step 1.

If at any point a player achieves a score greater than or equal to 121, that player is immediately declared the winner and the game is over.

The win condition for this game can occur at any moment of the game, even beyond either player's control (see step 3). Because of this, it is crucial to play according to different strategies during different times of the game, where time can be defined by what score the player has, combined with what score their opponent has and which player is the dealer for that round. Typically, during early and middle-game play, the pone will attempt to maximize their own hand, while avoiding giving too much opportunity for the dealer to score points from the crib. However, in later play, this may no longer be a concern. For example, should the player be the pone and their score is 116 and the dealer has 117 points, due to the counting precedence, the player needs not concern themselves with what points the dealer will obtain through the crib if their own hand has at least 5 points guaranteed since the pone will count first and win. This only works, however, if the pone does not allow the dealer to score 4 points from *the play*. As can be seen, the player must balance multiple competing factors with varying emphasis over the course of the game.

2   Literature Review

Overview of the current literature surrounding this topic.

- Research done in cribbage

- Research done in related imperfect information games (e.g. poker)

- Overview on expert witness machine learning

- Any other topic that ends up getting used (Bayesian logic, statistics?)

2.1   Prior Cribbage Research

3   Data and Methods

Walk-through of how I went about researching the topic. (Maybe I should keep a diary or log or something so this isn't half made up at the end.) When all is said and done, include the final "output" graph in some easily viewable format (121-by-121 table of miniature bar graphs, RGB combination in each cell?).

- Creation of framework

- Creation of "expert advisor"

- Training method for listener/combiner

- Initializations for training

3.1   Methods

3.1.1   Loss Function

A good loss function is critical to the proper training of a machine learning classifier. In classroom examples in which data can be mapped into a multidimensional space, this is typically accomplished by either a euclidean distance, or some other measure of how "wrong" the prediction is based on how much it varies from what is classified as "correct." In learning to predict using expert witnesses' testimony, this is measured in terms of *regret*. However, even though it is inevitable for the human player to think back on what could have been if he or she had chosen a different arrangement of cards to keep and throw, this is not a practically applicable loss function measure for the following reasons:

1. To evaluate how each hand "would" have done in any specific point in the game, a new "branching" game would have to be run through at that specific point. Basically, this means that a giant search tree would need to be made where the branches are randomly created using draws from the deck. Therefore the notion of "regret" is not easily practically computable.

2. It is difficult to determine what a better hand would have been in any case. For example, a hand that scored higher would not always be better. Furthermore, a hand that uses a higher score may not peg as well, etc. Therefore, it is difficult to be able to determine what is "correct" to calculate a distance from that.

Therefore, it may be useful instead to create a different system of punishment and reward rather than pure Loss. There are two possible routes I can think of at this junction.

1. Use the point spread between yourself and the opponent for the round.

   The problem with this strategy is that it depends on the opponent's performance as well as your own. In the case of our simulation, this is further problematic because the opponent's playing strategy and style is not known, which means this can't be rightfully evaluated.

2. In what position was the player left after playing with this hand.

   (a) Using intrinsic values for each playing state.

      This method relies upon previous knowledge of the game in order to set up position in which the player is at an advantage or disadvantage. While this may be acceptable for this small application, it should not be used in the general case.

   (b) Using a form of back-propagation.

      Each positions value will be computed based on the amount of times a player at that position ended up winning the game, and by how much. This would require the agent to be trained in reverse, so to speak. Early games could start at scores like 119 to 115 and compute which are likely to win, then make their way backwards to lower scores. Another option would be for each agent to keep track of its own path of scores and reward/punish all at the end, perhaps with different weights.

3.1.2 Strategies

A few basic behavioral strategies were coded for the agent to learn over the course of multiple simulated games. These represented most of the basic factors which a player will consider when making their decision as to which cards to keep. These included:

- `hand_max_min`: The hand(s) which has the maximum minimum possible score for the kept cards will be more highly desired. This is equivalent to choosing the hand with the largest guaranteed points.

- `hand_max_avg`: The hand(s) with the maximum average points over all possible cut cards will be the most highly desired. This strategy is useful for trying to maximize the expected score of one's own hand.

- `hand_max_med`: The hand(s) with the maximum median points possible to score will be the most highly desired. Similar to `hand_max_avg`, this strategy is useful when trying to maximize one's hand's expected score.

- `hand_max_poss`: The hand(s) with the maximum possible score will be the most highly desired. This strategy can be thought of as Hail Mary choice for the player trying to score as many points as possible, not taking into account its unlikelihood.

- `hand_min_avg_crib`: The hand(s) with the minimum average amount of points scored in the crib is the most highly desired. This strategy would be a very defensive strategy typically used by the pone to avoid giving points to the dealer.

- `hand_max_avg_both`: TODO: is this necessary, or will the weighting mechanism take care of this

- `pegging_max_avg_gained`: The hand(s) with the maximum average points gained through pegging is the most highly desired. This strategy would be useful for end-game play in a tight game. For instance, if both players are close to win, the dealer may choose to forego placing points into their hand and instead try to peg out since it is unlikely that they will get a chance to count their hand at all.

- `pegging_max_med_gained`: The hand(s) with the maximum median points scored during play will be the most highly desired. This strategy is similar to `pegging_max_avg_gained` in its use, but uses a slightly different internal measure for ranking.

- `pegging_min_avg_given`: The hand(s) with the minimum average points scored by the opposing player will be the most highly desired. This is a very defensive strategy also useful at the end of the game to prevent the opposing player from pegging out.

The above definitions refer to a hand's desirability. This can be thought of as an internal ranking of how likely a given strategy would be willing to choose a particular combination of cards. Because there are likely to be multiple possible combinations of cards which have the same desirability according to any given strategy, the implementation of the each strategy will point out all such possibilities.

The choosing mechanism will then apply a different weight to each strategy's picks based on that strategy's weighting for the given score time. In this way, a hand that was highly recommended by strategies which are highly trusted will be more likely to be picked. Multiple recommendations from multiple strategies will also be combined together to further boost popular suggestions. After all recommendations have been accumulated, the option with the highest weight will be chosen by the agent for play in that round. In the event of a tie between two or more combinations of cards, the combination which was recommended by the

Because of the massive amount of possible combinations—many of which were unique due to the cards' position affecting the scoring outcome—the evaluation of some of these possibilities in which the crib was involved in real-time took a handful of seconds to evaluate during development. This was deemed much too slow as over the course of hundreds or thousands of simulated games, this delay would very quickly accumulate to performance-affecting delays. As a result, an alternative strategy of pre-computing the required knowledge and storing the values of interest into a database was implemented instead.

There are $\binom{52}{6}$ possible combinations of card which can be dealt to either player. Of these possibly dealt hands, there are then $\binom{6}{4} = 24$ possible combinations of cards that can be kept and "tossed" to the crib. For each of these 24 possible there are a further $(52 - 6) = 46$ possible cards that must be considered as possible cut cards for the kept hand. Additionally, for the thrown set of cards, there are $\binom{46}{2} = 1035$ possible combinations of cards which can be thrown by the opposing player into the crib as well as the $(46 - 2) = 44$ remaining possible cut cards. These cut cards must be considered separately in such a manner of evaluating $\binom{46}{2} \times 44 = 45540$ possibilities rather than simply looking at each of $\binom{46}{3} = 15180$ possibilities because whether or not the card is in the crib or not can affect the score.[1] Just as crucially, there are small differences in scoring the crib as opposed to scoring the player's own hand that mean that previous evaluations results are not reusable. This means that, altogether, there are

$$\binom{52}{6}\binom{6}{4}\left((46) + \left(\binom{46}{2} \times 44\right)\right) \approx 1.3921 \times 10^{13}$$

possible combinations of cards that need to be evaluated in total to fully understand the statistics of a cribbage game for each hand.

Although the majority of this project was coded in Python for its ease of use and speed of development, due to the performance-crucial, basic mathematical operations involved, the overheads of using a higher-level language was deemed too critical and this particular tool was developed in C instead. To put the performance gains into perspective, at its fastest, most parallelly processed state, the Python database populator was estimated to take approximately 4 months to simply list and evaluate all possible scores on a development machine, disregarding the file I/O operations required to write the results to the database. The same functionality, with the addition of file I/O, in the C program would take a relatively mere 14 days on that same machine. Thankfully, most of the framework for this rewrite had actually been developed previously as part of a mental exercise, so the loss in time for the rewrite was minimal.

While the combinations of chosen and tossed scores could be evaluated before any games had actually been played, the hands' usefulness during the pegging portion of the round needed to be evaluated in semi real-time. A single pegging agent was programmed with heuristics gained from a cribbage strategy book.[?] This agent was then played against a copy of itself with randomly allocated cards and the results of that round were recorded for each agent to provide an initial knowledge base. These results would then be queried by the agent during the choose phase of the game and contributed to at the end of the pegging phase.

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[1]TODO: example of right jack or something and point to rulebook

3.1.3 Training

4 Findings

What are the final results of the "experiment."

- Where did each initialization family end up going?

- Were they different or did the agent learn a "single" strategy in general?

- All this and more will be answered ... after the break!

5 Discussion

This is the difficult part. What does this part mean? And how does it differ from what I've already covered above in the Findings section.

6 Conclusion

Generic closing remarks and rephrasing of the original introduction again in parting. Because this is a thesis and likely fairly long, "In section X, we covered Y" is probably allowed and not tacky.

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Appendix 1. Cribbage Scoring Rules

A   During Play Round

B   During Counting phase

Appendix 2. somethigng else

Appendix 3. Will this work?