

# Controlling a Servo DC Motor using LEGO Mindstorms

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# What is a DC Servo Motor?

- A Motor is a device that converts *electrical energy* into *mechanical energy*.
- A *servomotor* allows for precise control of angular position using a *rotary encoder* for position feedback.
- Input: Voltage
- Output: Angular displacement of shaft

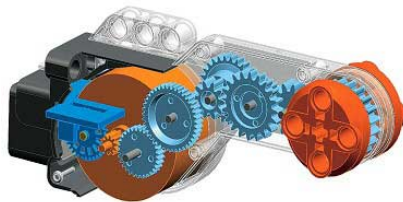
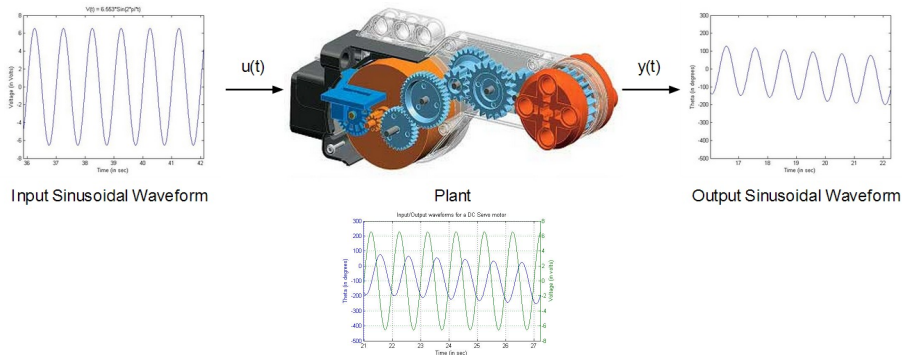


Figure : LEGO DC Servo Motor

<http://www.philohome.com/>

# What is a Linear System?



**Figure :** Block diagram showing Input/Output waveforms for a Servo Motor.

For a Linear system, a sinusoidal input produces a sinusoidal output which might be scaled and phase-shifted.

# Frequency Analysis using Simulink & Matlab

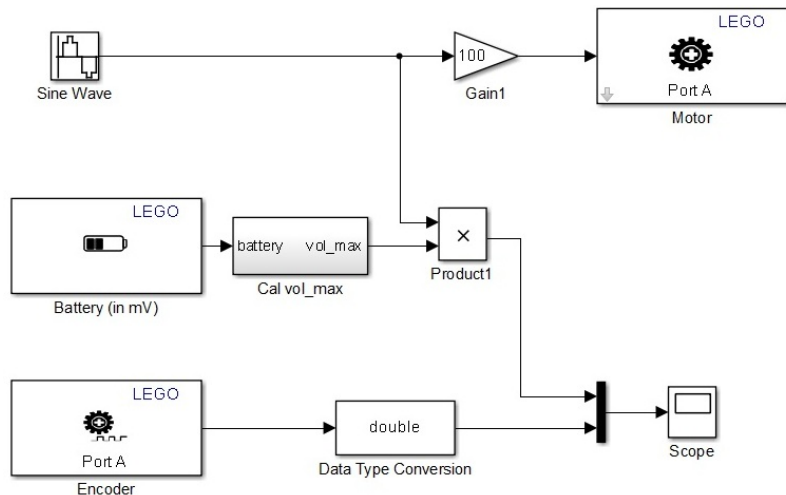


Figure : Block Diagram for observing frequency response of DC Servo Motor

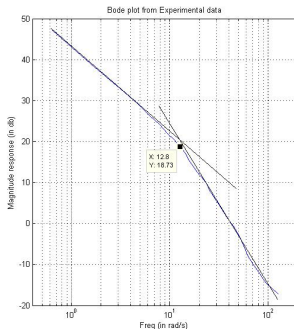
# Frequency response of Servo DC Motor

The Magnitude and phase difference is tabulated as shown in Table. The DC Servo does not respond beyond  $10\text{Hz}$  or  $62.8\text{rad/s}$ .

Frequency(Hz)	Magnitude	Phase
0.10	227.70	-88.81
0.50	43.65	-97.98
1.00	20.38	-112.30
1.50	12.44	-121.47
2.00	8.64	-130.63
3.00	4.29	-143.81
4.00	2.57	-148.97
5.00	1.72	-159.28
6.00	1.20	-157.56
7.00	0.92	-157.56
8.00	0.72	-155.85
10.00	0.39	-169.53

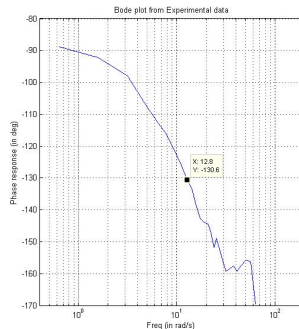
**Table :** Frequency response of the DC Servo Motor

# Bode Plot



**Figure :** Bode Plot from measured frequency response

From the bode plot, it is observed that the system has poles at  $s = 0$  and  $s = 13$ .



**Figure :** Bode Plot from measured frequency response

# Transfer Function model

The transfer function of the DC Servo motor is of the form:

$$H(s) = \frac{A}{s(s + \alpha)} \quad (1)$$

Fitting the model to the datapoint ( $12.8 \text{ rad/s}$ ,  $8.64 \text{ db}$ ,  $-130.63^\circ$ ), we get the transfer function of the motor to be:

$$H(s) = \frac{2018}{s(s + 13)} \quad (2)$$

This model can now be used to design a *PI-controller* for position control.



# PI Controller for position tracking

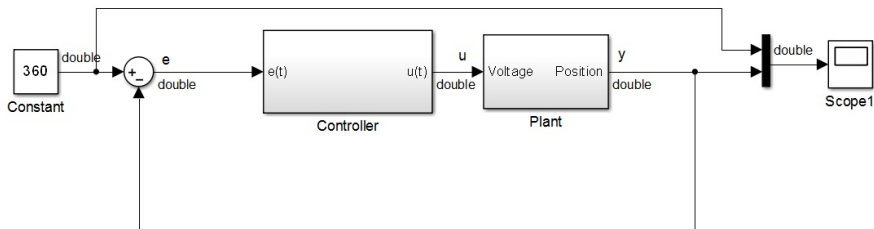


Figure : Simulink block diagram of PI Controller for position tracking

The  $k_p$  and  $k_i$  values are calculated using the experimentally determined Transfer function model.

# Calculation of Controller parameters

The transfer function model of the motor is,

$$P(s) = \frac{A}{s(s + \alpha)} \quad (3)$$

For PI Control,

$$C(s) = k_p + \frac{k_i}{s} = \frac{k_p s + k_i}{s} \quad (4)$$

The loop transfer function becomes,

$$L(s) = \frac{(k_p s + k_i)A}{s(s + \alpha)} \quad (5)$$

The characteristic polynomial is

$$(s^2 + 2\zeta\omega_0 s + \omega_0^2)(s + \beta\omega_0) = s^3 + s^2\alpha + Ak_p s + Ak_i \quad (6)$$

Taking  $\omega_0$  to be a free variable,

$$\omega_0 = \frac{\alpha}{\beta + 2\zeta} \quad k_p = \frac{(1 + 2\beta\zeta)\omega_0^2}{A} \quad k_i = \frac{\beta\omega_0^3}{A} \quad (7)$$

Substituting the values for  $A, \alpha$  and taking  $\beta = 1, \zeta = 1$  gives,

$$\boxed{k_p = 0.0279, k_i = 0.0403} \quad (8)$$

# Performance of PI Controller

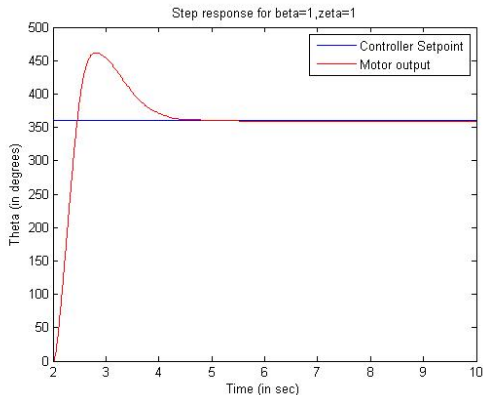


Figure : Step response of PI Controller

The system performance can be further improved by tuning the PI controller parameters.

# The End