

## (Visible) Light Transport

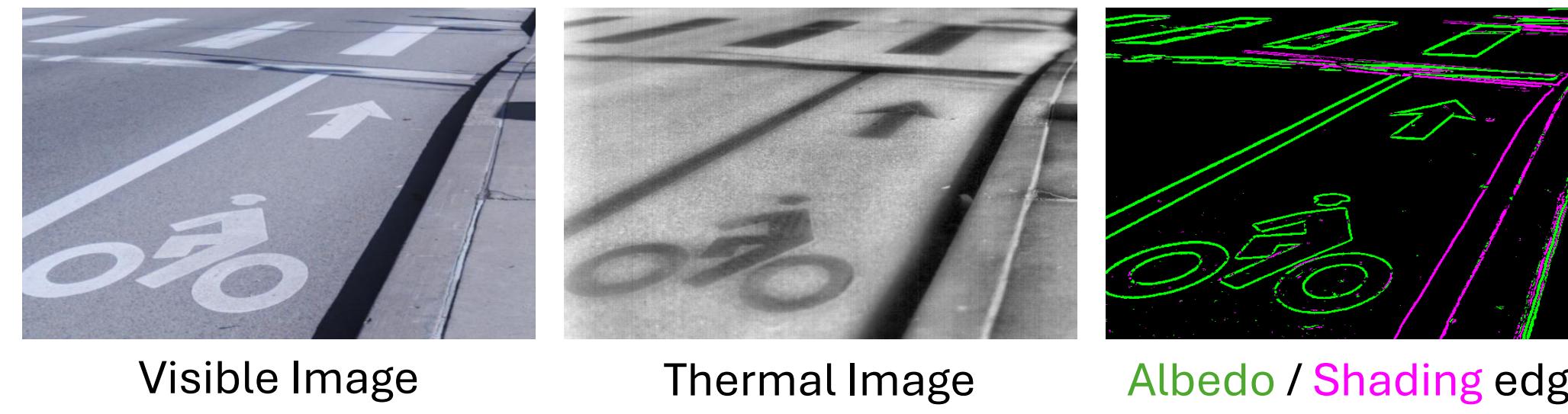
Mainstream Vision models:

Direct Illumination Scattering Media

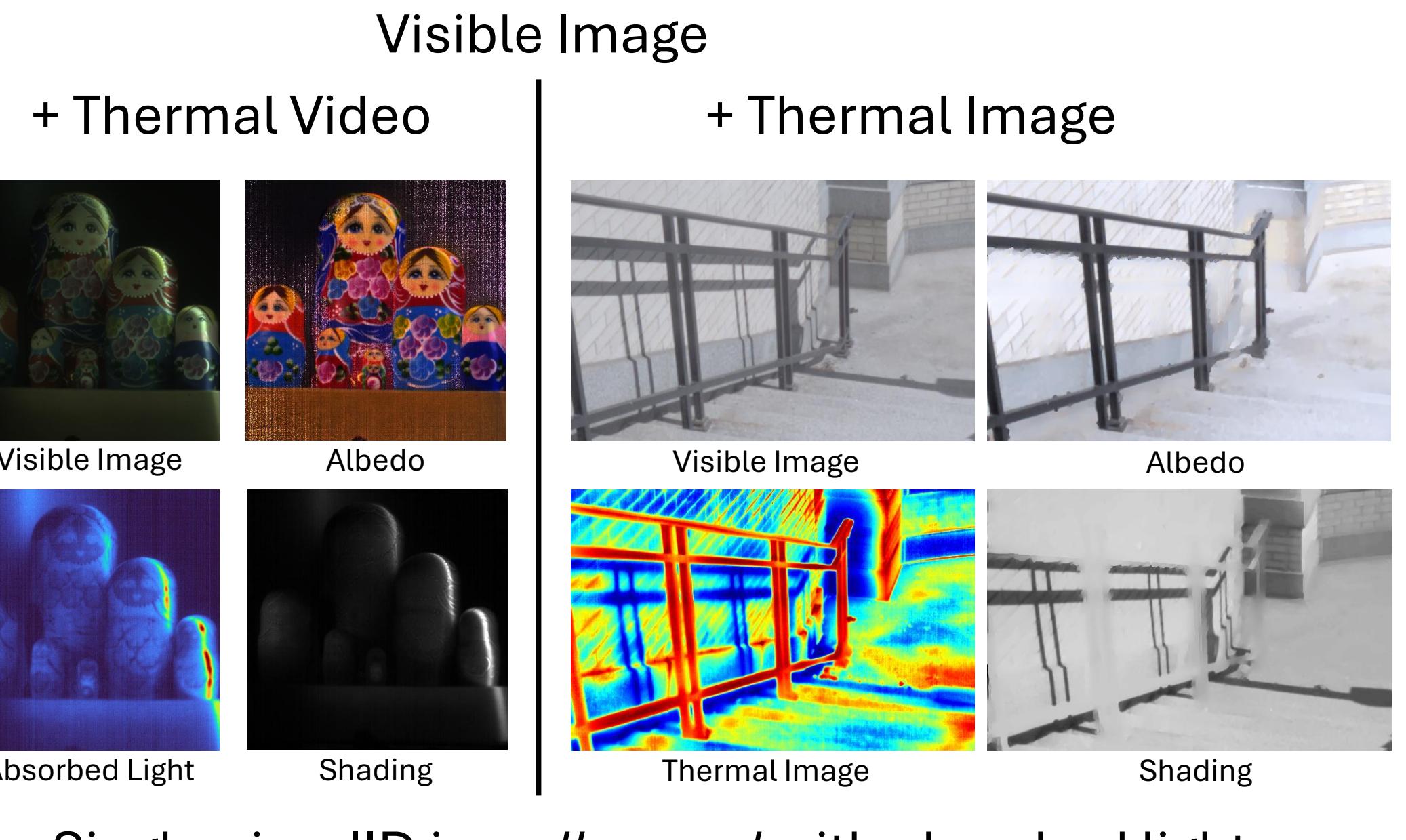
Global Illumination Absorbed Light

$$\text{VIS Intensity } I_v(\mathbf{x}) = \frac{\rho(\mathbf{x})}{\pi} \gamma \eta^*(\mathbf{x}) \xrightarrow[\text{camera gain}]{\text{scene irradiance}} S(\mathbf{x}) = (1 - \rho(\mathbf{x})) \eta^*(\mathbf{x}) \xrightarrow{\text{net absorbed energy}}$$

### Intrinsic Image Decomposition (IID)



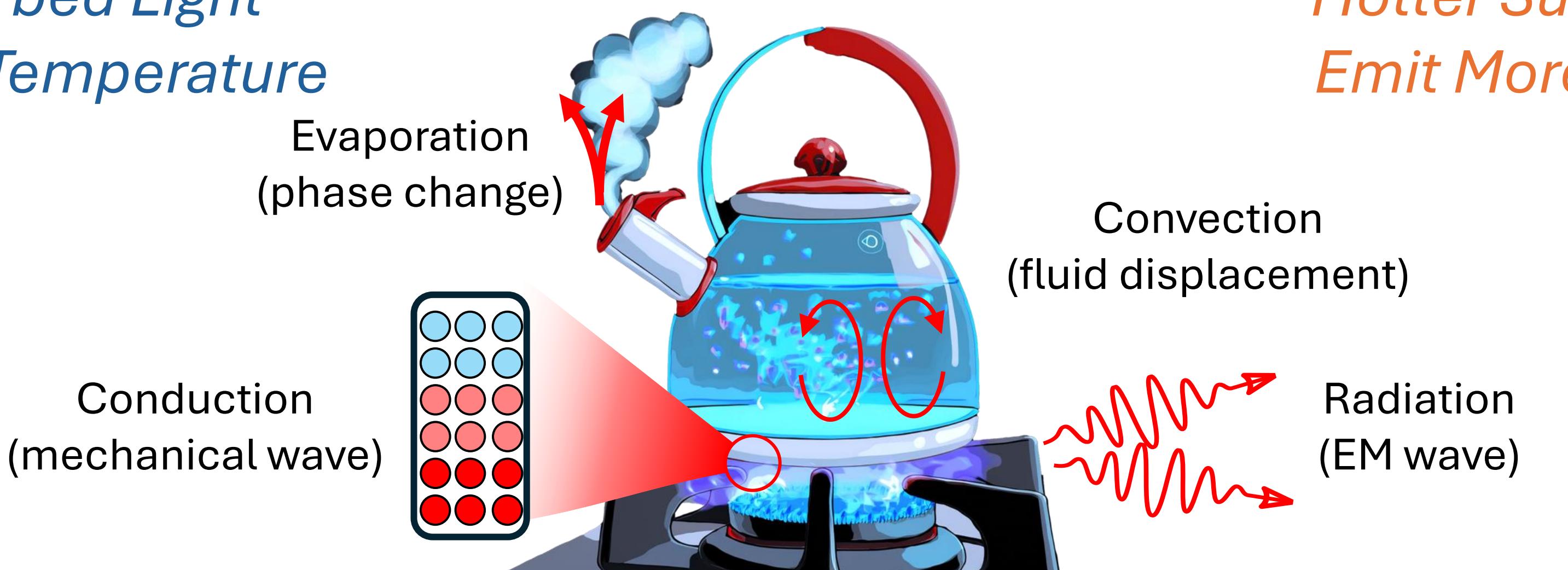
Brighter + Hotter = Receives More Heat  
 Brighter + Cooler = Reflects More Light



$$\text{Albedo } \rho(\mathbf{x}) = \frac{\pi I_v(\mathbf{x})}{\pi I_v(\mathbf{x}) + \zeta S(\mathbf{x})}$$

$$\text{Shading } \eta(\mathbf{x}) = \pi I_v(\mathbf{x}) + \zeta S(\mathbf{x})$$

## Absorbed Light Raises Temperature



### Heat Transport (independent of $\lambda$ )

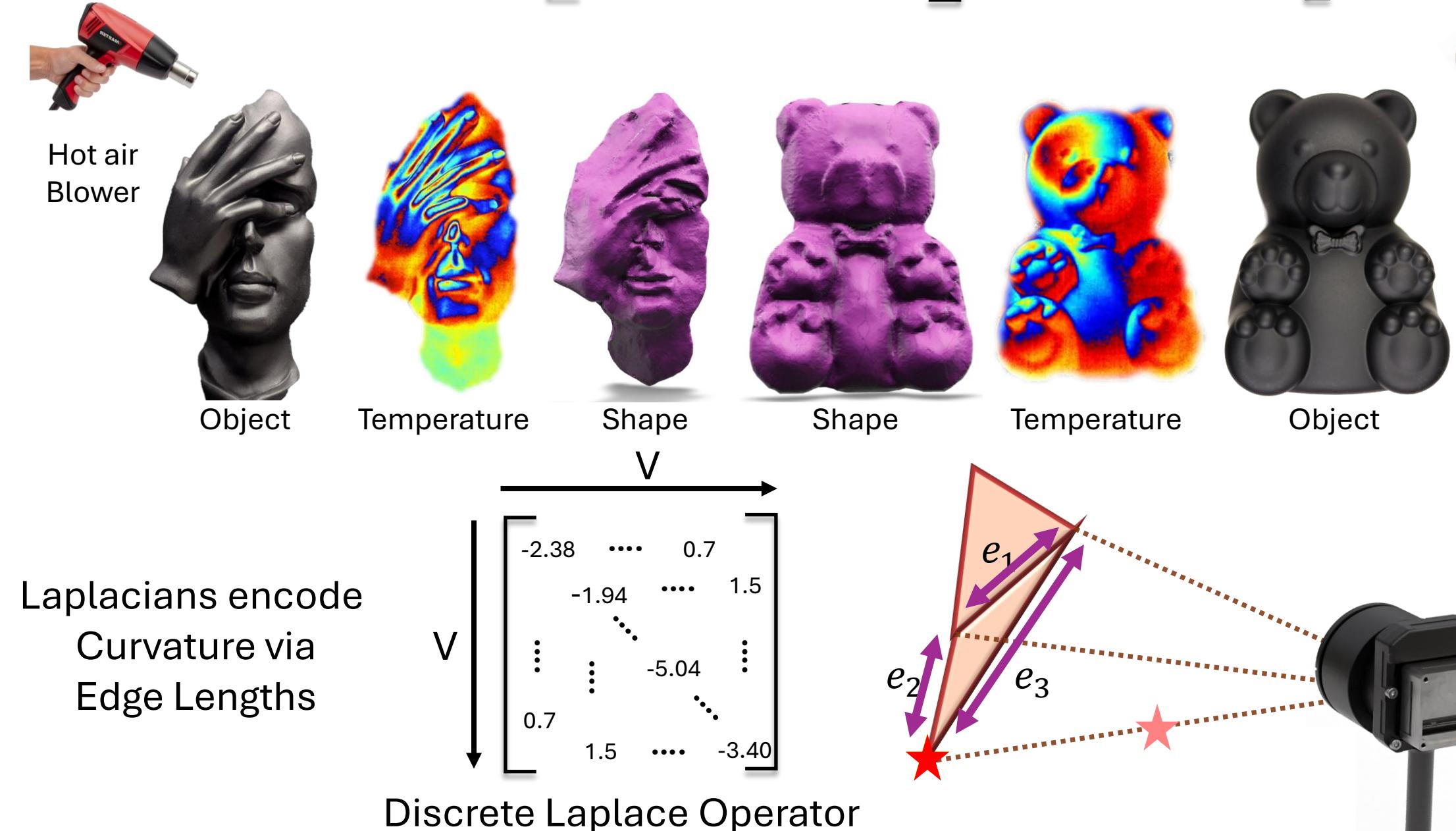
$$C_v \delta_z \frac{\partial T(\mathbf{x}, t)}{\partial t} = S(\mathbf{x}) + \sigma \epsilon (T_s^4 - T(\mathbf{x}, t)^4) + h_c (T_a - T(\mathbf{x}, t)) + \delta_z \kappa \Delta_x T(\mathbf{x}, t)$$

source intensity  
emissivity  
Stefan-Boltzmann constant  
heat capacity  
thickness  
surrounding temp.  
surface temperature  
convection coeff.  
air temp.  
thermal conductivity  
Laplace operator

### Shape from Heat Conduction

Thermal Video  
is a  
Linear System

$$\begin{bmatrix} \frac{T_1 - T_0}{dt} & \text{Known} & -T_1 & (T_1 - T_s) & 1 \\ \cdot & \text{Unknowns} & \cdot & \cdot & \cdot \\ \cdot & \cdot & \cdot & \cdot & \cdot \\ \frac{T_n - T_{n-1}}{dt} & \text{Known} & -T_n & (T_n - T_s) & 1 \end{bmatrix} \begin{bmatrix} \text{heat capacity} \\ \text{Laplace operator} \\ \text{convection coeff.} \\ \text{source intensity} \end{bmatrix} = \begin{bmatrix} 4\sigma\epsilon(T_s^4 - T_s^3 T_1) \\ \cdot \\ \cdot \\ 4\sigma\epsilon(T_s^4 - T_s^3 T_n) \end{bmatrix}$$



$$\text{Albedo } \rho(\mathbf{x}) = \frac{\pi I_v(\mathbf{x})}{\pi I_v(\mathbf{x}) + \zeta S(\mathbf{x})}$$

$$\text{Shading } \eta(\mathbf{x}) = \pi I_v(\mathbf{x}) + \zeta S(\mathbf{x})$$

## Hotter Surfaces Emit More Light

Thermal cameras measure temperature – Nope.

### Heat-to-Light



## (Thermal) Light Transport

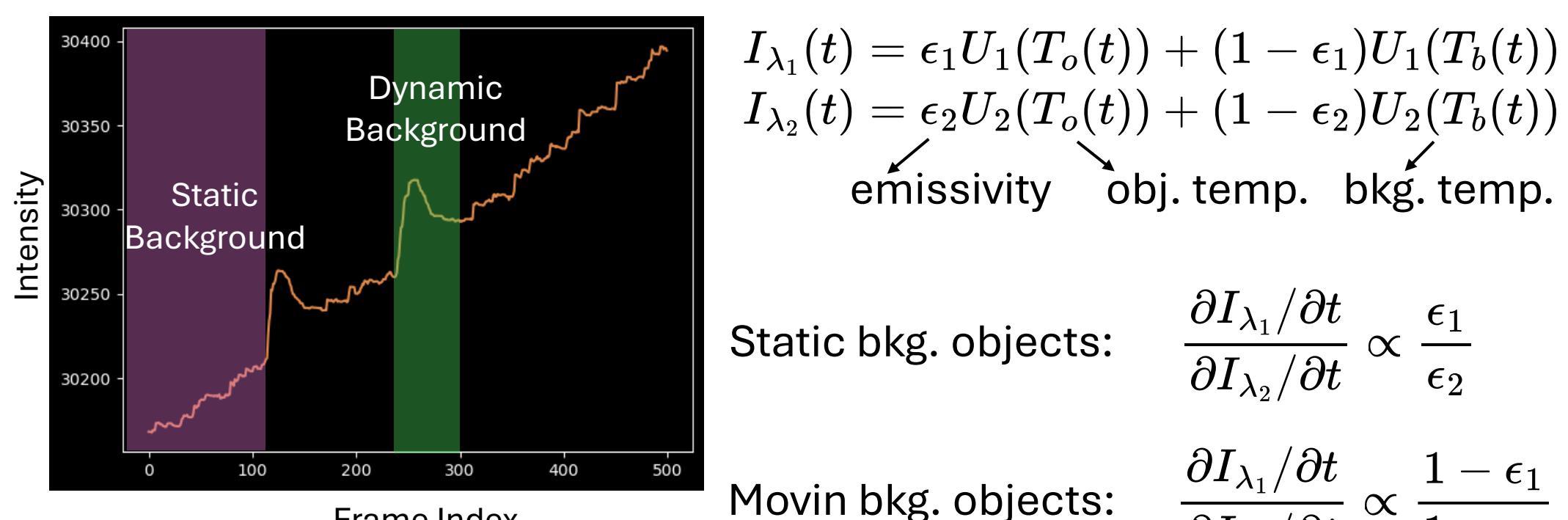
Thermal cameras measure radiance – Yes!

$$\text{LWIR Intensity } I_l(\mathbf{x}, t_n) = \epsilon U(T(\mathbf{x}, t_n)) + U_s$$

emissivity  
temperature  
sur. radiance  
camera response

### Reflection-Emission Separation

Accurate Temperature requires Accurate Emissivity



$$I_{\lambda_1}(t) = \epsilon_1 U_1(T_o(t)) + (1 - \epsilon_1) U_1(T_b(t))$$

$$I_{\lambda_2}(t) = \epsilon_2 U_2(T_o(t)) + (1 - \epsilon_2) U_2(T_b(t))$$

$$\text{Static bkg. objects: } \frac{\partial I_{\lambda_1}/\partial t}{\partial I_{\lambda_2}/\partial t} \propto \frac{\epsilon_1}{\epsilon_2}$$

$$\text{Movin bkg. objects: } \frac{\partial I_{\lambda_1}/\partial t}{\partial I_{\lambda_2}/\partial t} \propto \frac{1 - \epsilon_1}{1 - \epsilon_2}$$

### Shape from Laplacian and Shading

Laplacians have Local Binary Ambiguity  $\cap$  Shading has Per-pixel Cone Ambiguity = Two Global Solutions

