

The background of the slide features a complex network diagram. It consists of numerous nodes, represented by small spheres, connected by thin lines. The nodes are distributed across the frame, with a higher density on the right side. The spheres have a metallic, reflective appearance. The overall color scheme is a mix of light blue, white, and grey, with a subtle gradient. The network structure is intricate, showing many interconnected paths and clusters, typical of a multiplex network.

Complex Networks 2025

**Final Presentation**  
**Analysis of the**  
**European Air**  
**Transport Multiplex**  
**Network**

Authors:

**Marc Ballesteró Ribó**  
**Arnau Jutglar Puig**

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Task 2  
Complex Networks Analysis

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# Summary

**1**

**Network Description**

**2**

**Mesoscale Analysis:  
Communities**

**3**

**Dynamic Analysis:  
Random Walks and  
Synchronization**

**4**

**Multiplex Analysis**

# 1 Network Description

- We have been working with the **Air Transportation Multiplex Dataset**.
  - Airline routes among European airports, where each of the 37 edge types represents **routes** by a different airline.
  - **Undirected, unweighted, multiplex network**.

# 1 Network Description

- **Data Selection:**
  - **Lufthansa:** traditional, hub-and-spoke airline.
  - **Air France:** traditional, hub-and-spoke airline.
  - **Ryanair:** low-cost, point-to-point airline.
  - **+**
  - **Whole European Network:** collapse of all airlines network.

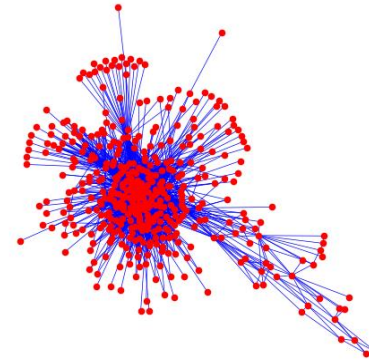
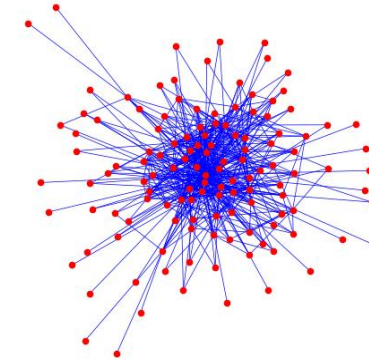
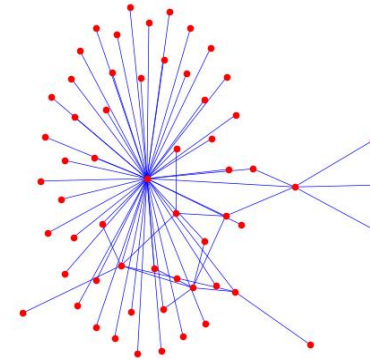
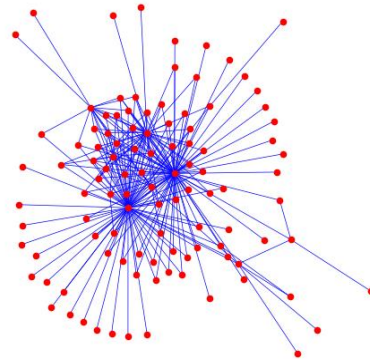
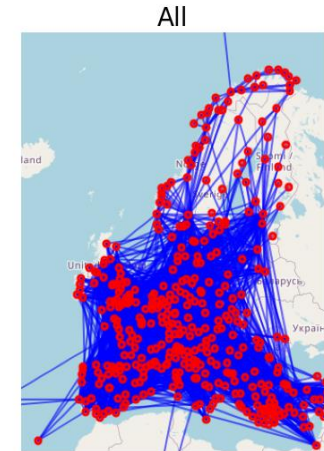
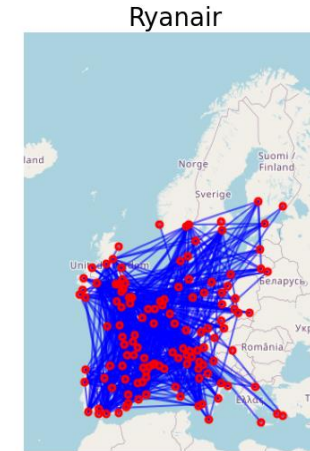
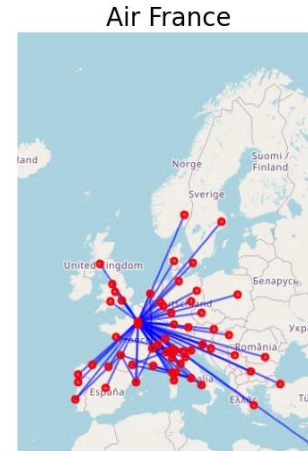
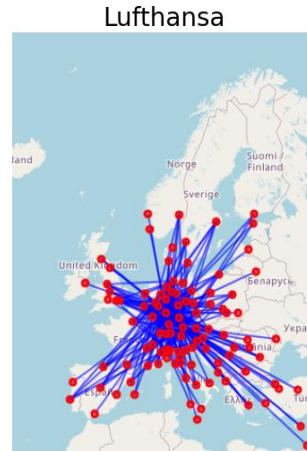


## 1

# Network Description

- **Data Selection:**

- **Lufthansa:** hub-and-spoke.
- **Air France:** hub-and-spoke.
- **Ryanair:** point-to-point.
- **Whole European Network.**



In the plots, we can already see some interesting insights...



**Goal:** confirm them quantitatively

We have computed node communities for each of the networks using the following algorithms:

- **Greedy Modularity Maximization.**
- **Louvain Algorithm.**
- **Girvan-Newman Algorithm.**
  - Keep computing communities until a maximum of 15 is reached



We have simulated **random walks** on the network (1000 walkers, 10000 steps) and studied:

- Number of transits in each node.
  - Number of walkers at the end of the simulation in each node
- +
- Correlation of the previous parameters with centrality measures.



## Synchronization

Setting the scenario:

- Airports need to exchange information by opening a channel.
- They open it at every hour and can freely choose when (within such hour).
- The hour position is the phase.
- They have no internal tendency to change their phase. Their natural frequency is  $\omega = 0$ .
- They can't reach a straight global agreement.
- They update their phase by looking at their difference with their neighbors. Not just this but following a Kuramoto model.

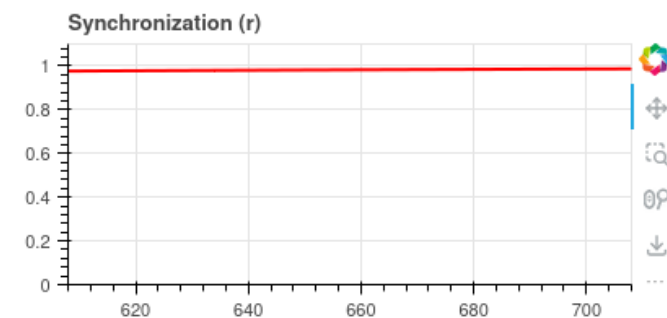
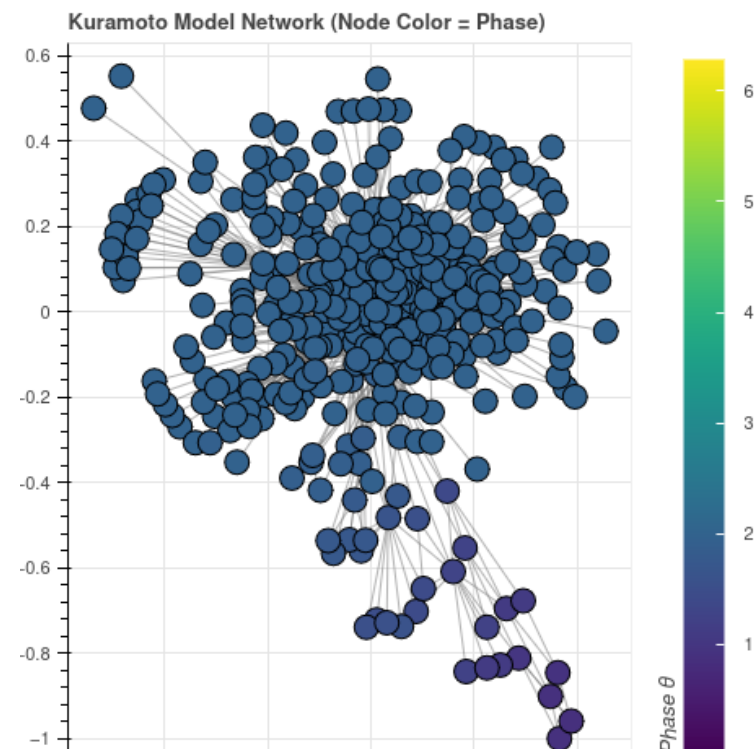
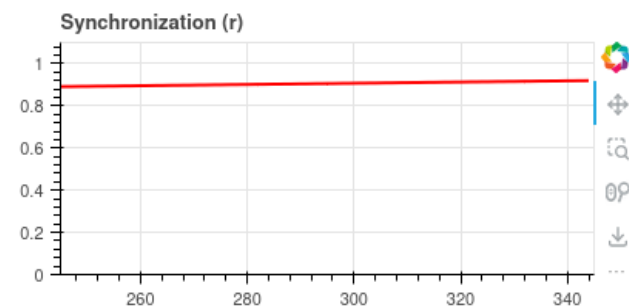
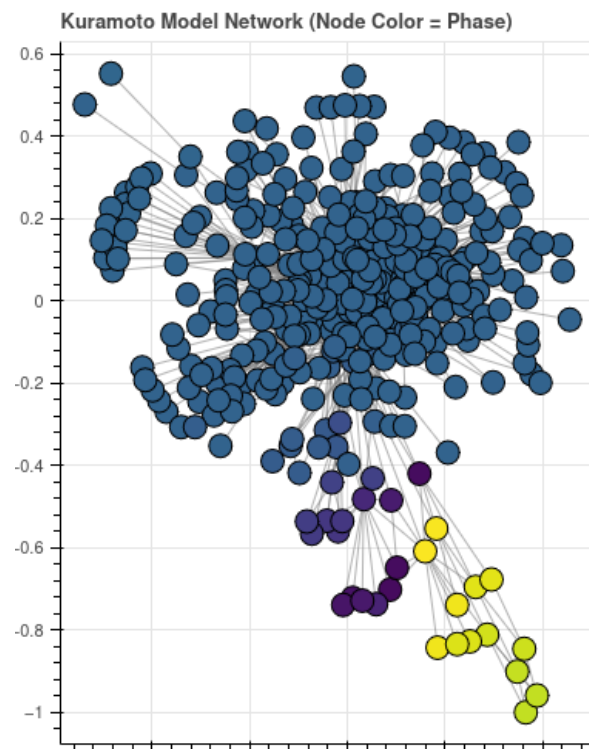
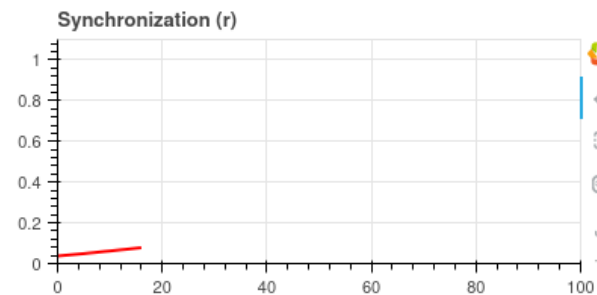
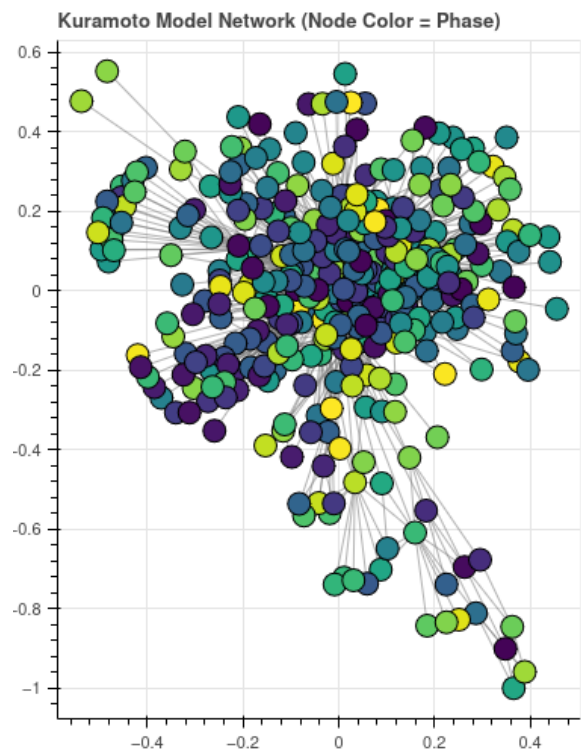
$$\dot{\theta}_i = K \sum_{j=1}^N A_{i,j} \sin(\theta_j - \theta_i)$$





## 3

# Dynamic Analysis: Synchronization

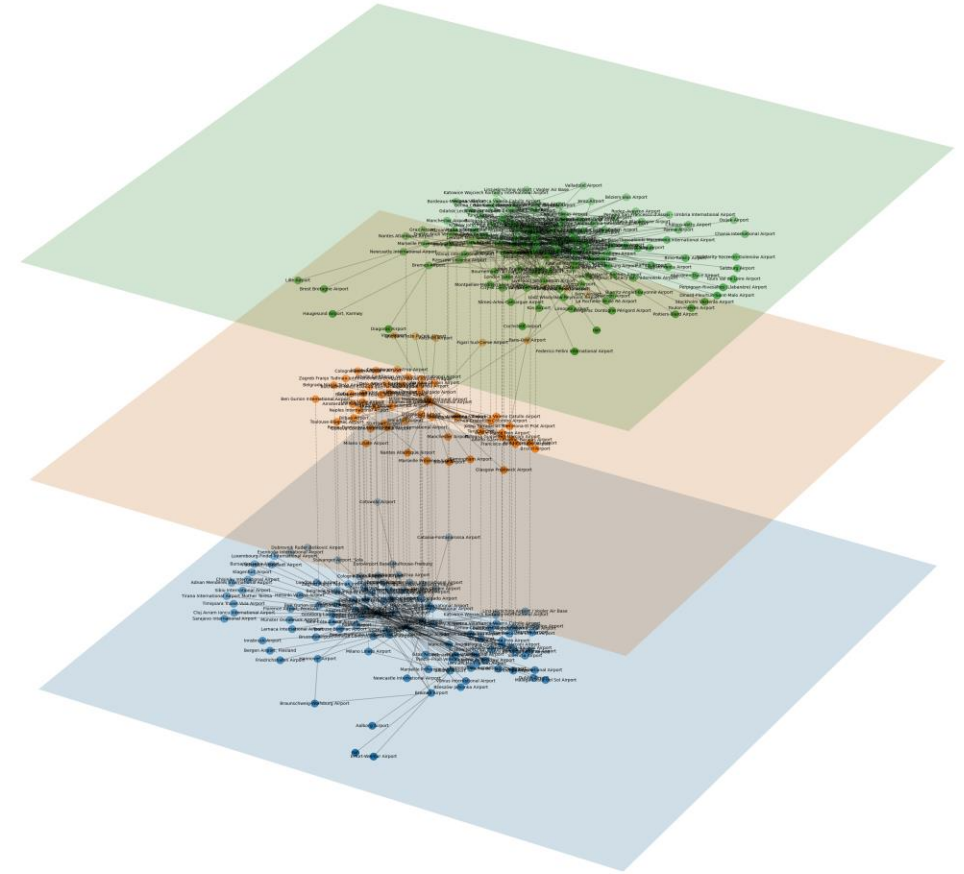


## **Multilayer network**

- The airlines network naturally follows a multilayer structure.
- Each layer is an airlines network.
- The layers can be connected by connecting the nodes corresponding to the same cities.
- This visualization can be useful to:
  - See which cities are operated by both companies.
  - See which paths can you take to travel from a city operated only by airline A to one operated only by airline B (if you want to avoid the hubs).

## Multilayer network

- The visualization is visually appealing.
- With so many nodes, it is difficult to interpret.



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Task 1

Microscale and Macroscale Analysis

**Thanks for  
your  
Attention!**

Authors:

Marc Ballesteró Ribó  
Arnau Jutglar Puig

Friday, March 25<sup>th</sup>, 2024

**Any questions?**

