

# **B.Tech/M.Tech(Integrated) DEGREE EXAMINATION, NOVEMBER 2023**

Third Semester

## **21MAB206T - NUMERICAL METHODS AND ANALYSIS**

*(For the candidates admitted during the academic year 2022-2023 onwards)*

**Note:**

- Part - A** should be answered in OMR sheet within first 40 minutes and OMR sheet should be handed over to hall invigilator at the end of 40<sup>th</sup> minute.
- Part - B** and **Part - C** should be answered in answer booklet.

**Time: 3 Hours**

**Max. Marks: 75**

**PART - A (20 × 1 = 20 Marks)**

Answer all Questions

**Marks BL CO**

- As soon as a new value of a variable is found by iteration, it is used immediately in the following equation. This method is called  
 (A) Gauss-Jordan Method (B) Gauss Seidal Method  
 (C) Gauss Jacobi Method (D) Gauss elimination Method  
 1 1 1
- In solving simultaneous equations by Gauss-Jordan Method, the co-efficient matrix is reduced to  
 (A) Diagonal Matrix (B) Null Matrix  
 (C) Square Matrix (D) Identity Matrix  
 1 1 1
- Newton Raphson method is also called  
 (A) Method of tangents (B) Method of chords  
 (C) Method of bisection (D) Method of False position  
 1 1 1
- The negative root of  $x^3 - 2x + 5 = 0$  approximately  
 (A) root lies between 0 and 1 (B) root lies between -1 and -2  
 (C) the root lies between -2 and -3 (D) root lies between 1 and 2  
 1 1 1
- What is  $\Delta^2 f(x)$ , if  $f(x) = x^2 - 3x + 1$ , taking  $h = 1$   
 (A)  $2x+1$  (B)  $2x$   
 (C) 2 (D) 0  
 1 1 2
- The operator  $E f(x)$  is equivalent to  
 (A)  $f(x+h)$  (B)  $f(x-h)$   
 (C)  $f(x-2h)$  (D)  $f(x+2h)$   
 1 1 2
- With usual notation,  $\delta E^{-\frac{1}{2}}$  is equal to  
 (A)  $\Delta$  (B)  $\nabla$   
 (C)  $E+1$  (D)  $\Delta+1$   
 1 1 2
- The missing term in the following table using finite difference technique is  

$x$	0	1	2	3	4
$f(x)$	1	3	9	-	81

 (A) 30 (B) 30.7  
 (C) 27.5 (D) 28.8

9. Newton's backward difference formula to get the first derivative of  $y(x)$  at any  $x$  is 1 1 3
- (A)  $\frac{dy}{dx} = \frac{1}{h} \left[ \nabla y_n + \left( \frac{2u+1}{2} \right) \nabla^2 y_n + \dots \right]$  (B)  $\frac{dy}{dx} = \frac{1}{h} \left[ \nabla y_n + \left( \frac{v+1}{2} \right) \nabla^2 y_n + \dots \right]$
- (C)  $\frac{dy}{dx} = \frac{1}{h} \left[ \Delta y_n + \left( \frac{2v+1}{2} \right) \Delta^2 y_n + \dots \right]$  (D)  $\frac{dy}{dx} = \frac{1}{h} \left[ \Delta y_0 + \left( \frac{2u-1}{2} \right) \Delta^2 y_0 + \dots \right]$
10. Simpson's three-eighth rule can be applied only when  $n$  is 1 1 3
- (A) Odd (B) Even  
(C) Prime (D) Multiple of 3
11. Trapezoidal rule is so called because it 1 1 3
- (A) Approximates the integral by the sum of  $n$  trapezoids (B) Finds the area of the trapezoid  
(C) Splits into  $n$  trapezoids (D) Gives approximate value
12. The error in Simpson's one-third rule is of order 1 1 3
- (A)  $h^2$  (B)  $h^4$   
(C)  $h^3$  (D)  $h^6$
13. Taylor's series method is 1 1 4
- (A) single-step method (B) Multi step method  
(C) Iterative method (D) Trial and error method
14. In Runge - Kutta method of fourth order,  $\Delta_1$  stands for 1 1 4
- (A)  $\frac{1}{6}(k_1 + k_2 + k_3 + k_4)$  (B)  $\frac{1}{6}(k_1 - 2k_2 + 2k_3 - k_4)$   
(C)  $\frac{1}{6}(2k_1 + k_2 + k_3 + 2k_4)$  (D)  $\frac{1}{6}(k_1 + 2k_2 + 2k_3 + k_4)$
15. Modified Euler's algorithm to find numerical solution of a first order differential equation for  $m = 0, 1, 2$ , is 1 1 4
- (A)  $y_{m+1} = y_m + h \left[ f \left( x_m + \frac{h}{2}, y_m + \frac{h}{2} f(x_m, y_m) \right) \right]$  (B)  $y_{m+1} = y_m + \frac{h}{2} [f(x_m, y_m) + f(x_m + h, y_m + hf(x_m, y_m))]$   
(C)  $y_{m+1} = y_m + hf(x_m, y_m)$  (D)  $y_{m+1} = y_m + \left[ f \left( x_m + \frac{h}{2}, y_m + \frac{h}{2} f(x_m, y_m) \right) \right]$
16. Given  $y' = x + y, y(0) = 1$ , then  $y(0.1)$  by Euler's method, taking  $h = 0.1$ , is 1 1 4
- (A) 1 (B) 0.2  
(C) 0.1 (D) 1.1
17. Bender-Schmidt recurrence equation is valid only if 1 1 5
- (A)  $k = \frac{h^2}{2}$  (B)  $k = \frac{ah^2}{2}$   
(C)  $k = \frac{2}{ah^2}$  (D)  $k = \frac{2}{h^2}$
18. The equation  $\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} = f(x, y)$  is also called 1 1 5
- (A) Laplace equation (B) Poisson's equation  
(C) One-dimensional heat equation (D) Two-dimensional heat equation

19. The error in the diagonal five point formula is \_\_\_\_\_ times the error in the standard five point formula  
 (A) 1 (B) 2  
 (C) 3 (D) 4
20. Bender-Schmidt scheme converges for  
 (A)  $\lambda = 1$  (B)  $\lambda = \frac{1}{2}$   
 (C)  $\lambda = 3$  (D)  $\lambda = \frac{3}{2}$

**PART - B (5 × 8 = 40 Marks)**

**Marks BL CO**

Answer all Questions

21. (a) Find a positive real root of  $x e^x = 2$  by using the method of false position, correct to 3 decimal places  
 (OR)

- (b) Solve the system of equations by Gauss Elimination method

$$2x + y + 4z = 12$$

$$8x - 3y + 2z = 20$$

$$4x - 11y - z = 33$$

22. (a) Use Lagrange's formula to fit a polynomial to the data and hence find  $y$  ( $x=1$ ).  
 $x:$  -1 0 2 3  
 $y:$  -8 3 1 12

(OR)

- (b) Find the age corresponding to the annuity value of 13.6 given the table

Age (x)	30	35	40	45	50
Annuity value (y)	15.9	14.9	14.1	13.3	12.5

23. (a) Find the value of  $\sec 31^\circ$  from the following data

$\theta$ (in degrees)	31	32	33	34
$\tan \theta$	0.6008	0.6249	0.6494	0.6745

(OR)

- (b) Evaluate  $\int_4^{5.2} \log_e x \, dx$  using trapezoidal rule and Simpson's rule taking  $h=0.2$

24. (a) Solve  $\frac{dy}{dx} = x^2 - y$  given  $y(0) = 1$ , and get  $y(0.1)$ ,  $y(0.2)$  by Taylor series method.

(OR)

- (b) Using Improved Euler's method solve  $\frac{dy}{dx} = y + e^x$   $y(0)=0$ , for  $x=0.2, 0.4$ .

25. (a) Using Crank-Nicholson's scheme  
 Solve  $u_{xx} = 16u_t$ ,  $0 < x < 1$ ,  $t > 0$ , given  $u(x, 0) = 0$ ,  $u(0, t) = 0$ ,  $u(1, t) = 100t$   
 Compute  $u$  for one step in  $t$  direction taking  $h = \frac{1}{4}$ .

(OR)

- (b) Using Schmid's process solve  $u_{xx} = 2u_t$ , with the conditions  $u(x, 0) = \frac{1}{4}x(15 - x)$  for  $0 \leq x \leq 12$ ;  $u(0, t) = 0$ ;  $u(12, t) = 9$  for  $0 < t < 12$  take  $h=3=k$ .

**PART - C (1 × 15 = 15 Marks)**

Answer any 1 Questions

**Marks BL CO**

26. Apply the fourth order Runge Kutta method to find  $y(0.2)$  given that  $y' = y + xy^2$ ,  $y(0)=1$ , by taking  $h=0.1$  correct to four decimal places. 15 3 4
27. By Iteration method, solve the Laplace equation  $u_{xx} + u_{yy} = 0$ , over the square region, satisfying the boundary conditions.  
 $u(0, y) = 0, 0 \leq y \leq 3$   
 $u(3, y) = 9 + y, 0 \leq y \leq 3$   
 $u(x, 0) = 3x, 0 \leq x \leq 3$   
 $u(x, 3) = 4x, 0 \leq x \leq 3$   
Find the values correct to 3 decimal places 15 3 5

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