

**B.Tech DEGREE EXAMINATION, NOVEMBER 2023**

Fifth Semester

**18ECC204J - DIGITAL SIGNAL PROCESSING**

(For the candidates admitted during the academic year 2018-19 to 2021-22)

OPEN BOOK EXAMINATION

18ECC204J0

Note:

- Specific approved THREE text books (Printed or photocopy) recommended for the course.
- Handwritten class notes (certified by the faculty handling the course / Head of the Department).

Time: 3 Hours

Max. Marks: 100

Answer FIVE Questions  
(Question No. 3 is compulsory)

Marks BL CO

1. a. A digital communication link carries binary-coded words representing samples of an input signal

$$x_a(t) = 3\cos 600\pi t + 2\cos 1800\pi t$$

The link is operated at 10,000 bits/s, and each input sample is quantized into 1024 different voltage levels. What are the sampling frequency and the folding frequency? What is the Nyquist rate for the signal  $x_a(t)$ ? What are the frequencies in the resulting discrete-time signal  $x(n)$ ? [12 Marks]

12

3 1

- b. An analog electrocardiogram (ECG) signal contains useful frequencies up to 100 Hz. What is the Nyquist rate for this signal? Suppose we sample this signal at a rate of 250 samples/s, what is the highest frequency that can be represented uniquely at this sampling rate? [6 Marks]

6 3 1

- ii. Which of the following is the process of 'aliasing'?

1 1 1

(A) Peaks overlapping

(B) Phase overlapping

(C) Amplitude overlapping

(D) Spectral overlapping

- iii. The signal-to-quantization noise ratio in dB is represented as \_\_\_\_\_

1 1 1

(A)  $6.02 + 1.76b$ (B)  $1.76 + 6.02b$ (C)  $2.76 + 6.02b$ (D)  $3.76 + 6.02b$ 

12

2. a. Obtain the direct form I and direct form II realization for the following system [12 Marks]

18 3 2

$$y(n) = \frac{5}{8}y(n-1) - \frac{1}{16}y(n-2) + x(n) + \frac{3}{4}x(n-1) + \frac{1}{8}x(n-2)$$

- b. The DFT of a sequence  $x(n)$  that has  $N=2^m$  can be calculated using two algorithms. Algorithm A computes the DFT by direct evaluation and takes  $N^2$  seconds to run. Algorithm B implements DIT-FFT and takes  $5N \log_2 N$  seconds to run. What is the shortest sequence  $N$  such that Algorithm B runs faster than Algorithm A. [6 Marks]

6 3 2

- ii. If  $X(k)$  is the DFT of a sequence  $x(n)$  then DFT of real part of  $x(n)$  is \_\_\_\_\_

1 2 2

(A)  $(1/2)[X(k) + X^*(N-k)]$ (B)  $(1/2)[X(k) - X^*(N-k)]$ (C)  $X(k) + X^*(N-k)$ (D)  $X(k) - X^*(N-k)$ 

- iii. The bit reversed order of the given sequence  $\{1, 2, 3, 4, 4, 3, 2, 1\}$  is \_\_\_\_\_

1 2 2

(A)  $\{1, 3, 2, 4, 4, 2, 3, 1\}$ (B)  $\{1, 4, 3, 2, 2, 3, 4, 1\}$ (C)  $\{4, 3, 2, 1, 4, 3, 2, 1\}$ (D)  $\{4, 1, 2, 3, 3, 2, 1, 4\}$ 

12

3. a. Compute the 8-point DFT of the sequence  $x(n) = n+1$  for  $0 \leq n \leq 7$  by using the DIT-FFT algorithm. Defend that  $X(k)$  and  $X(N-k)$  are complex conjugates from the obtained DFT coefficients. [12 Marks]

18 4 2

- b. Perform the circular convolution of the two sequences  $x_1(n) = \{2, 1, 2, 1\}$  and  $x_2(n) = \{1, 2, 3, 4\}$  using the concentric circle method. [6 Marks]

6 4 2

- ii. Select the value of twiddle factor  $W_8^3$

1 1 2

(A) 1

(B)  $0.707 + j0.707$ (C)  $-0.707 - j0.707$ 

(D) -j

iii. If  $X(k)=[0, 3+j3, -j4, 3-j3, 0]$  is the DFT of a 8-point sequence, then  $X(5)=$

- (A) 0 (B)  $3+3j$   
(C)  $3-3j$  (D)  $4j$

1 2 2

4 i. a. Design FIR filter by truncating the given desired frequency response to 9 samples

a.i) 
$$H_d(e^{j\omega}) = \begin{cases} 1 & \text{for } |\omega| \leq \frac{\pi}{3} \text{ and } |\omega| \geq \frac{2\pi}{3} \\ 0 & \text{otherwise} \end{cases}$$

ii) Find the realizable transfer function. [12 Marks]

b. What are the desirable characteristics of a window? [6 Marks]

ii. The necessary and sufficient condition for linear phase characteristic in FIR filter is that the impulse response  $h(n)$  of the system should have the \_\_\_ property.

- (A) symmetric (B) anti-symmetric  
(C) linear (D) non-linear

iii. Which window function is also regarded as 'Raised-cosine window'?

- (A) Hamming window (B) Hanning window  
(C) Barlett window (D) Blackman window

5 i. Design a digital Butterworth filter satisfying the following constraints using bilinear transformation:

- 3 dB ripple in pass band  $0 \leq \omega \leq 0.2\pi$
- 25 dB attenuation in stop band  $0.45\pi \leq \omega \leq \pi$

ii. In bilinear transformation, the left-half of S-plane is mapped \_\_\_ in the z-domain

- (A) Entirely outside the unit circle (B) Partially outside the unit circle  
(C) Partially inside the unit circle (D) Entirely inside the unit circle

iii. Which of the following filters cannot be designed using the impulse invariance method?

- (A) Low pass (B) Band pass  
(C) Low and band pass (D) High pass

6 i. a. For the given analog transfer function, determine  $H(Z)$  of the digital filter using the impulse invariance method. Assume  $T=1$  sec. [12 Marks]

a.i) 
$$H(s) = \frac{4}{s^2 + 6s + 8}$$

ii) b. Compare digital and analog filters. [6 Marks]

ii. The poles of Chebyshev filter lie on

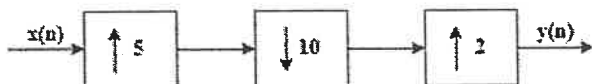
- (A) Unit circle (B) Ellipse  
(C) Parabola (D) Hyperbola

iii. What is the transfer function of Butterworth low pass filter of order 2?

- (A)  $1/(s^2 + \sqrt{2}s + 1)$  (B)  $1/(s^2 - \sqrt{2}s + 1)$   
(C)  $s^2 - \sqrt{2}s + 1$  (D)  $s^2 + \sqrt{2}s + 1$

7 i. a. Explain sampling rate conversion by a factor I/D. [12 Marks]

b. Develop an expression for  $y(n)$  as a function of  $x(n)$  for the given multirate system. [6 Marks]



ii. A two-channel subband coding filter bank is also called as \_\_\_

- (A) Quadrature-mirror filter bank (B) Analysis filter bank  
(C) Synthesis filter bank (D) Alias free filter bank

iii. If  $x[n] = [1, 5, 3, 2]$  then  $y[n] = x[n/2]$  will be

- (A)  $[1, 3]$  (B)  $[1, 0, 5, 0, 3, 0, 2, 0]$   
(C)  $[1, 5, 0, 0]$  (D)  $[1, 5, 3, 2, 0, 0, 0, 0]$